## VMPC one-way function

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#### Abstract

The VMPC function is a combination of two basic operations: permutation composition and integer addition. The function resulting from this combination shows to have very high resistance to inverting. Computational effort of about $2^{260}$ operations is estimated to be required to invert the VMPC function. The value of the function can be computed with 3 elementary computer processor instructions per byte. An open question is whether the function's simplicity raises a realistic chance that the lower bound on the complexity of inverting it might be proved.


## 1. Introduction

VMPC is an abbreviation of Variably Modified Permutation Composition.
The VMPC function is a combination of triple permutation composition and integer addition. It differs from a simple triple permutation composition with one integer addition operation performed on some of the elements of the permutation. The consequence of this addition operation is corruption of cycle structure of the transformed permutation - the fundamental source of the function's resistance to inverting.

The VMPC function has a simple formal definition and the value of the function can be computed with 3 one-clock-cycle instructions of an Intel 80486 and newer or compatible processor per byte.

Inverting the function is estimated to require an average computational effort of about $2^{260}$ operations. This effort can be significantly extended at only linear cost.

Adding one more one-cycle instruction to the implementation of the function increases its resistance to inverting to an average level of about $2^{420}$ operations. Adding another onecycle instruction raises it to about $2^{550}$ operations and adding yet another one-cycle instruction produces a function requiring an average computational effort of about $2^{660}$ operations to be inverted.

The simplicity of the VMPC function could raise a question whether it might be possible to prove the lower bound on the complexity of inverting it. This currently is an open problem and a possible subject of future research.

The more detailed explanation of why the VMPC function it hard to invert is to be found in section 6.

## 2. Definition of the VMPC function

## Notation:

$\mathrm{n}, \mathrm{P}, \mathrm{Q}: \mathrm{P}$ and $\mathrm{Q}: \mathrm{n}$-element permutations. For simplicity of further implementations P and Q are one-to-one mappings $\mathrm{A} \rightarrow \mathrm{A}$, where $\mathrm{A}=\{0,1, \ldots, \mathrm{n}-1\}$
k : Level of the function; $\mathrm{k}<\mathrm{n}$

+ : addition modulo $n$


## Definition:

A k-level VMPC function, referred to as $\mathrm{VMPC}_{\mathrm{k}}$, is such transformation of $P$ into Q , where

$$
\mathbf{Q}[\mathbf{x}]=\mathbf{P}\left[\mathbf{P}_{\mathbf{k}}\left[\mathbf{P}_{\mathbf{k}-1}\left[\ldots\left[\mathbf{P}_{1}[\mathbf{P}[\mathrm{x}]]\right] \ldots\right]\right],\right.
$$

$x \in\{0,1, \ldots, n-1\}$,
$P_{i}$ is an n-element permutation such that $P_{i}[x]=f_{i}(P[x])$, where $f_{i}$ is any function such that $\mathrm{P}_{\mathrm{i}}[\mathrm{x}] \neq \mathrm{P}[\mathrm{x}] \neq \mathrm{P}_{\mathrm{j}}[\mathrm{x}]$ for $\mathrm{i} \in\{1 \ldots \mathrm{k}\}, \mathrm{j} \in\{1 \ldots \mathrm{k}\} /\{\mathrm{i}\}$.

For simplicity of further implementations $f_{i}$ is assumed to be $f_{i}(x)=x+i$

## Example:

$\mathrm{Q}=\mathrm{VMPC}_{1}(\mathrm{P})$ is such transformation of P into Q , where:
$\mathrm{Q}[\mathrm{x}]=\mathrm{P}\left[\mathrm{P}_{1}[\mathrm{P}[\mathrm{x}]]\right]$,
$P_{1}[x]=P[x]+1$.

Table 1. Definitions of 1,2,3 and 4-level VMPC function

| Function | Definition |
| :--- | :--- |
| $\mathrm{VMPC}_{1}$ | $\mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]$ |
| $\mathrm{VMPC}_{2}$ | $\mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]$ |
| $\mathrm{VMPC}_{3}$ | $\mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]+3]$ |
| $\mathrm{VMPC}_{4}$ | $\mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]+3]+4]$ |

## 3. The 3-instruction implementation of the VMPC function

Implementation of a 1-level VMPC function, where $\mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]$, for 256 -element permutations P and Q in assembly language is described.

## Assume that :

- Pa is a 257 -byte array indexed by numbers from 0 to 256 , the P permutation is stored in the array at indexes from 0 to $255(\mathrm{~Pa}[0 \ldots 255]=\mathrm{P})$ and that $\mathrm{Pa}[256]=\mathrm{Pa}[0]$.
- the EAX 32-bit register stores value zero. ("AL" denotes 8 least significant bits of EAX)
- the EDX 32-bit register stores an address, where the Pa array is stored in memory
- the ECX 32-bit register specifies which element of the Q permutation to compute


## Execute:

Table 2. Implementation of 1-level VMPC function

| Instruction | Decription |
| :--- | :--- |
| MOV AL, [EDX] + ECX | Store ECX-th element of P in AL |
| MOV AL, $[E D X]+$ EAX | Store AL-th element of P in AL |
| MOV AL, $[E D X]+$ EAX + 1 | Store (AL+1)-th element of P in AL |

The 3 MOV instructions in Table 2 store the ECX-th element of permutation Q , where $\mathrm{Q}=\mathrm{VMPC}_{1}(\mathrm{P})$, in the AL (and EAX ) register.

## 4. Example values of the VMPC function

Values of the 1,2,3 and 4-level VMPC function of an example 10-element permutation P are shown in Table 3.

Table 3. Example values of the VMPC function for 10-element permutations

| Index | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P | 2 | 0 | 4 | 3 | 6 | 9 | 7 | 8 | 5 | 1 |
| $\mathrm{Q}_{1}=\mathrm{VMPC}_{1}(\mathrm{P})$ | 9 | 3 | 8 | 6 | 5 | 4 | 1 | 7 | 2 | 0 |
| $\mathrm{Q}_{2}=\mathrm{VMPC}_{2}(\mathrm{P})$ | 0 | 9 | 2 | 5 | 8 | 7 | 3 | 1 | 6 | 4 |
| $\mathrm{Q}_{3}=\mathrm{VMPC}_{3}(\mathrm{P})$ | 3 | 4 | 9 | 5 | 0 | 2 | 7 | 6 | 1 | 8 |
| $\mathrm{Q}_{4}=\mathrm{VMPC}_{4}(\mathrm{P})$ | 8 | 5 | 3 | 1 | 6 | 7 | 0 | 2 | 9 | 4 |

## 5. Complexities of computing / inverting the VMPC function

Efforts required to compute and to invert the 1,2,3 and 4-level VMPC function for 256element permutations are shown in Table 4:

Table 4. Complexities of computing / inverting the VMPC function for 256-element permutations

| Function | VMPC $_{1}$ | $\mathrm{VMPC}_{2}$ | $\mathrm{VMPC}_{3}$ | $\mathrm{VMPC}_{4}$ |
| :--- | :---: | :---: | :---: | :---: |
| Number of MOV instructions required to compute <br> one byte of the value of the function | 3 | 4 | 5 | 6 |
| Estimated average number of computational <br> operations required to invert the function | $2^{260}$ | $2^{420}$ | $2^{550}$ | $2^{660}$ |

## 6. Difficulty of inverting the VMPC function

n-element permutation P has to be recovered given information from n -element permutation, Q , where $\mathrm{Q}=\mathrm{VMPC}_{\mathrm{k}}(\mathrm{P})(\mathrm{e} . \mathrm{g} . \mathrm{n}=256, \mathrm{k}=1: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1])$.

By definition each element of Q is formed by $\mathrm{k}+2$ (e.g. 3), usually different, elements of P . One element of Q (e.g. $\mathrm{Q}[33]=25$ ) can be formed by many possible configurations of P elements (e.g. $\mathrm{P}[33]=10, \mathrm{P}[10]=20, \mathrm{P}[21]=25$ or $\mathrm{P}[33]=1, \mathrm{P}[1]=4, \mathrm{P}[5]=25$, etc.).

It cannot be said which of the configurations is more probable. One of the configurations has to be picked (usually $\mathrm{k}+1$ (e.g. 2) elements of P have to be guessed) and the choice must be verified using all those other Q elements, which use at least one of the P elements from the picked configuration.

Each element of P is usually used to form $\mathrm{k}+2$ (e.g. 3) different elements of Q . As a result, usually $(\mathrm{k}+2)^{*}(\mathrm{k}+1)$ (e.g. 6) new elements of Q need to be inverted (all $\mathrm{k}+2$ elements of P used to form each of those Q elements need to be revealed) to verify the P elements from the picked configuration.

This would not be difficult for a simple (e.g. triple) permutation composition, where the cycle structure of P is retained by Q (some cycles are only shortened).

In Variably Modified Permutation Composition however the cycle structure of P is corrupted by the addition operation(s) and cannot be easily recovered from Q .

Due to that it is usually impossible to find two different elements of Q , which use at least $\mathrm{k}+1$ (e.g. 2) exactly the same elements of P . (This can be done easily for a simple permutation composition)

In fact only such element of Q can usually be found, name it $\mathrm{Q}[\mathrm{r}]$, which uses only one of the $\mathrm{k}+2$ (e.g. 3) elements of P , used to form another Q element. This forces the k remaining (e.g. 1) elements of P , used to form $\mathrm{Q}[\mathrm{r}]$, to be guessed to make the verification of the initial pick possible.

However at each new guessed element of P , there usually occur $\mathrm{k}+1$ (e.g. 2) new elements of $Q$ which use this element of $P$ and which need to be inverted to verify the guess.

The algorithm falls into a loop, where at every step usually $k$ (e.g. 1) new elements of $P$ need to be guessed to verify the previously guessed elements. It quickly occurs that the $\mathrm{k}+2$ (e.g. 3) elements of P picked at the beginning of the process indirectly depend on all n (e.g. 256) elements of Q .

The described scenario is the case usually and it is sometimes possible to benefit from coincidences (where for example it is possible to find two elements of Q , which use more than one (e.g. 2) exactly the same $P$ elements (e.g. $\mathrm{Q}[2]=3$ : $\mathrm{P}[2]=4, \mathrm{P}[4]=8, \mathrm{P}[9]=3$ and $\mathrm{Q}[5]=8: \mathrm{P}[5]=9, \mathrm{P}[9]=3, \mathrm{P}[4]=8)$ ).

The actual algorithm of inverting VMPC was optimized to benefit from the possible coincidences. The average number of P elements which need to be guessed - for $\mathrm{n}=256$ has been reduced to only about 34 for 1-level VMPC function, to about 57 for 2-level VMPC, to about 77 for 3-level VMPC and to about 92 for 4 -level VMPC function.

Searching through the possible states of these P elements takes on average about $2^{260}$ steps for 1-level VMPC function (not $2^{268,7}$ ), about $2^{420}$ for 2-level VMPC, about $2^{550}$ for 3-level VMPC and about $2^{660}$ steps for 4-level VMPC function.

## 7. Algorithm of inverting the VMPC function

The fastest method of inverting the VMPC function found derives $n$-element permutation P which produces a given $\mathrm{Q}=\mathrm{VMPC}_{\mathrm{k}}(\mathrm{P})$ permutation, according to the following algorithm:

## Notation:

$P_{t}: n$-element table, the searched permutation will be stored in

Argument, Value; Base, Parameter of an element of $P_{t}$ :
For an element $\mathrm{P}_{\mathrm{t}}[\mathrm{x}]=\mathrm{y}: \mathrm{x}$ is termed the argument and y the value.
The base is either the argument or the value; the parameter is the corresponding the value or the argument.

Example: for an element $\mathrm{P}_{\mathrm{t}}[3]=5$ : If value 5 is the base, argument 3 is the parameter.
1.1) Reveal one element of $P_{t}$ by assuming $P_{t}[x]=y$; where $x$ and $y$ are any values within range $x \in\{0,1, \ldots, n-1\}, y \in\{0,1, \ldots, n-1\}$
1.2) Choose at random whether $x$ is the base and $y$ the parameter or $y$ the base and $x$ the parameter of the element $P_{t}[x]=y$. Denote $P_{t}[x]=y$ as the current element of $P_{t}$.
2) Reveal all possible elements of $P_{t}$ by running the deducing process (see section 7.1)
3) If $n$ elements of $P_{t}$ have been revealed with no contradiction in step 2:

Terminate the algorithm and output $P_{t}$
4) If fewer than $n$ elements of $P_{t}$ have been revealed with no contradiction in step 2:
4.1) Reveal a new element of $P_{t}$ by running the selecting process (see section 7.2). Denote the revealed element as the current element of $\mathrm{P}_{\mathrm{t}}$.
4.2) Save the parameter of the current element of $P_{t}$
4.3) Go to step 2
5) If a contradiction occurred in step 2 :
5.1) Remove all elements of $P_{t}$ revealed in step 2 when the current element of $P_{t}$ had been revealed
5.2) Increment modulo $n$ the parameter of the current element of $\mathrm{P}_{\mathrm{t}}$
5.3) If the parameter of the current element of $\mathrm{P}_{\mathrm{t}}$ has returned to the value saved in step 4.2:
5.3.1) Remove the current element of $\mathrm{P}_{\mathrm{t}}$
5.3.2) Denote the element, which had been the current element of $P_{t}$ directly before the element removed in step 5.3.1 became the current one, as the current element of $\mathrm{P}_{\mathrm{t}}$
5.3.3) Go to step 5.1
6) Go to step 2

### 7.1. The deducing process

The deducing process reveals all possible elements of $\mathrm{P}_{\mathrm{t}}$, given Q and given the already revealed elements of $\mathrm{P}_{\mathrm{t}}$ according to the following algorithm:

Notation: as in section 7, with:
C,A : temporary variables
Word $x$ of Statement $y$ :
Statement y : A set of all elements of $\mathrm{P}_{\mathrm{t}}$ used to calculate $\mathrm{Q}[\mathrm{y}]$
Word x : x-th consecutive element of $\mathrm{P}_{\mathrm{t}}$ used to calculate $\mathrm{Q}[\mathrm{y}]$ :
Example for $\mathrm{VMPC}_{2}: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]$ :
Assume $\mathrm{P}_{\mathrm{t}}[2]=3, \mathrm{P}_{\mathrm{t}}[3]=5, \mathrm{P}_{\mathrm{t}}[6]=2, \mathrm{P}_{\mathrm{t}}[4]=7$, which produces $\mathrm{Q}[2]=7$.
The elements $P_{t}[2]=3, P_{t}[3]=5, P_{t}[6]=2, P_{t}[4]=7$ form statement 2 .
The element $P_{t}[2]=3$ is word 1 of statement $2 ; P_{t}[3]=5$ is word 2 of statement 2, etc.
1.1) Set $C$ to 0
1.2) Set A to 0
2) If the element $P_{t}[A]$ is revealed:
2.1) If the element $P_{t}[A]$ and $k$ other revealed elements of $P_{t}$ fit a general pattern of $k+1$ words of any statement : Deduce the remaining word of that statement (see example 7.1.1)
2.2) If the deduced word is not a revealed element of $P_{t}$ :
2.2.1) Reveal the deduced word as an element of $\mathrm{P}_{\mathrm{t}}$

### 2.2.2) Set C to 1

2.3) If the deduced word contradicts any of the already revealed elements of $P_{t}$ :

Output a contradiction and terminate the deducing algorithm (see example 7.1.2)
3.1) Increment $A$
3.2) If A is lower than n : Go to step 2
3.3) If C is equal 1 : Go to step 1.1

## Example 7.1.1)

For $\mathrm{VMPC}_{2}: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]$ :

Assume that $Q[0]=9$ and that the following elements of $P_{t}$ are revealed:
$P_{t}[0]=1, \quad P_{t}[1]=3, \quad P_{t}[8]=9$

Word 3 of statement 0 can be deduced as $P_{t}{ }^{‘}[4]=6\left(P_{t}{ }^{`}[3+1]=8-2\right)$

## Example 7.1.2)

For $\mathrm{VMPC}_{2}: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]$ :

Assume that $\mathrm{Q}[7]=2$ and that the following elements of $\mathrm{P}_{\mathrm{t}}$ are revealed:

$$
\mathrm{P}_{\mathrm{t}}[1]=8, \quad \mathrm{P}_{\mathrm{t}}[9]=3, \quad \mathrm{P}_{\mathrm{t}}[5]=2 \text { and } \mathrm{P}_{\mathrm{t}}[6]=1
$$

Word 1 of statement 7, deduced as $P_{t}{ }^{‘}[7]=1$, contradicts the already revealed element $\mathrm{P}_{\mathrm{t}}[6]=1$.

### 7.2. The selecting process

The selecting process selects such new element of $P_{t}$ to be revealed which maximizes the number of elements of $\mathrm{P}_{\mathrm{t}}$ possible to deduce in further steps of the inverting algorithm.

The selecting process outputs a selected base and a randomly chosen parameter of a new element of $\mathrm{P}_{\mathrm{t}}$.

Notation: as in section 7.1, with:
G,R,X,Y : temporary variables
$\mathrm{Ta}, \mathrm{Tv}$ : temporary tables

Weight : table of numbers:

Weight $[1 ; 2 ; 3 ; 4]=(2 ; 5 ; 9 ; 14) ;$ Example $:$ Weight $[3]=9$
1.1) Set Ta and Tv to 0
1.2) Set $G$ to 0
1.3) Set $R$ to 1
2) Count the number of revealed elements of $P_{t}$ which fit the general pattern of words of a statement in which an unrevealed element of $P_{t}$ with argument $G$ would be word $R$. Increment $\mathrm{Ta}[\mathrm{G}]$ by Weight of this number (see example 7.2.1)
3) Count the number of revealed elements of $P_{t}$ which fit the general pattern of words of a statement in which an unrevealed element of $P_{t}$ with value $G$ would be word $R$.
Increment $\mathrm{Tv}[\mathrm{G}]$ by Weight of this number
4.1) Increment $R$
4.2) If $R$ is lower than $k+2$ : Go to step 2
4.3) Increment $G$
4.4) If G is lower than n : Go to step 1.3
5.1) Pick any index of Ta or Tv for which the number stored in any of the tables Ta or Tv is maximal (see example 7.2.2)
5.2) If the index picked in step 5.1 is an index of Ta:
5.2.1) Store this index in variable $X$
5.2.2) Generate a random number Y within range $\mathrm{Y} \in\{0,1, \ldots, \mathrm{n}-1\}$, such that an element of $P_{t}$ with value $Y$ is not revealed
5.2.3) Output $\mathrm{P}_{\mathrm{t}}{ }^{\prime}[\mathrm{X}]=\mathrm{Y}$, where X is the base and Y is the parameter
5.3) If the index picked in step 5.1 is an index of Tv:
5.3.1) Store this index in variable Y
5.3.2) Generate a random number $X$ within range $X \in\{0,1, \ldots, n-1\}$, such that an element of $P_{t}$ with argument $X$ is not revealed
5.3.3) Outputs $\mathrm{P}_{\mathrm{t}}^{\prime}[\mathrm{X}]=\mathrm{Y}$, where Y is the base and X is the parameter

## Example 7.2.1)

For $\mathrm{VMPC}_{2}: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]$ :
Assume that $G=8 ; R=2 ; Q[6]=1$ and that the following elements of $P_{t}$ are revealed: $\mathrm{P}_{\mathrm{t}}[6]=8, \mathrm{P}_{\mathrm{t}}[5]=1$

There are two revealed elements of $P_{t}$ which fit the general pattern of words of a statement in which $\mathrm{P}_{\mathrm{t}}[8]$ would be word $2: \mathrm{P}_{\mathrm{t}}[6]=8, \mathrm{P}_{\mathrm{t}}[5]=1$ :

$$
\begin{array}{llll}
\text { word 1 } & \text { word 2 } & \text { word 3 } & \text { word 4 } \\
P_{t}[6]=8, & P_{t}[8]=?, & P_{t}[?]=?, & P_{t}[5]=1
\end{array}
$$

$$
\mathrm{Ta}[8]=\mathrm{Ta}[8]+\text { Weight }[2]=\mathrm{Ta}[8]+5
$$

## Example 7.2.2)

Assume $\mathrm{Ta}=(0,5,2,7,5,7)$ and $\mathrm{Tv}=(2,7,0,0,5,2)$
The maximal number stored in any of the tables is 7: $\mathrm{Ta}[3]=\mathrm{Ta}[5]=\mathrm{Tv}[1]=7$
Pick any of: index 3 of Ta, index 5 of Ta or index 1 of Tv

## 8. Example complexities of inverting the VMPC function

Complexity of inverting the VMPC function has been approximated as an average number of times the deducing process in step 2 of the inverting algorithm described in section 7 has to be run until permutation $\mathrm{P}_{\mathrm{t}}$ satisfies $\mathrm{Q}=\mathrm{VMPC}_{\mathrm{k}}\left(\mathrm{P}_{\mathrm{t}}\right)$

Complexities of inverting the VMPC function of the following levels have been approximated:

$$
\begin{aligned}
& \mathrm{VMPC}_{1}: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1] \\
& \mathrm{VMPC}_{2}: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2] \\
& \mathrm{VMPC}_{3}: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]+3] \\
& \mathrm{VMPC}_{4}: \mathrm{Q}[\mathrm{x}]=\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{P}[\mathrm{x}]]+1]+2]+3]+4]
\end{aligned}
$$

Table 5. Example complexities of inverting the VMPC function

| Function | $\mathbf{V M P C}_{\mathbf{1}}$ | $\mathbf{V M P C}_{\mathbf{2}}$ | $\mathbf{V M P C}_{\mathbf{3}}$ | $\mathbf{V M P C}_{\mathbf{4}}$ |
| :--- | :---: | :---: | :---: | :---: |
| $\mathbf{n}$ | $2^{4,1}$ | $2^{5,5}$ | $2^{6,1}$ | $2^{6,9}$ |
| $\mathbf{6}$ | $2^{7,1}$ | $2^{9,7}$ | $2^{11,5}$ | $2^{13,0}$ |
| $\mathbf{1 0}$ | $2^{11,5}$ | $2^{16,6}$ | $2^{20,4}$ | $2^{23,3}$ |
| $\mathbf{1 6}$ | $2^{24}$ | $2^{37}$ | $2^{47}$ | $2^{54}$ |
| $\mathbf{3 2}$ | $2^{53}$ | $2^{84}$ | $2^{108}$ | $2^{127}$ |
| $\mathbf{6 4}$ | $2^{117}$ | $2^{190}$ | $2^{245}$ | $2^{292}$ |
| $\mathbf{1 2 8}$ | $2^{260}$ | $2^{420}$ | $2^{550}$ | $2^{660}$ |
| $\mathbf{2 5 6}$ |  |  |  |  |

## 9. Conclusions

An idea of a simple one-way function has been presented. The VMPC function's resistance to inverting is strictly related to the addition operation(s) performed at some step(s) of the composition. Their role can be clearly illustrated by comparing the process of inverting a simple permutation composition with inverting the Variably Modified Permutation Composition.

It is an open problem whether the simplicity of the VMPC function helps make a hypothetical attempt to prove the lower bound on the complexity of inverting the function worth undertaking.

