Efficient Identity Based Ring Signature

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Abstract. Identity-based (ID-based) cryptosystems eliminate the need of validity checking of the certificates and the need of registering for a certificate before getting the public key. These two features are desirable especially for the efficiency and the real spontaneity of ring signature, where a user can anonymously sign a message on behalf of a group of spontaneously conscripted users including the actual signer.

To the best of authors' knowledge, the number of pairing computations of all existing ID-based ring signature schemes from bilinear pairings grows linearly with the group size, which made the efficiency of ID-based schemes over traditional schemes questionable.

In this paper, we construct an efficient ID-based ring signature which only needs two pairing computations for any group size. The proposed scheme is proven to be existential unforgeable against adaptive chosen message-and-identity attack under the random oracle model, using the forking lemma for generic ring signature schemes.

 $\textbf{Key words:} \ \textbf{Identity-based signature, ring signature, bilinear pairings, efficiency, real spontaneity, anonymity}$

1 Introduction

Ring signature is a group-oriented signature with privacy concerns: any user can anonymously signs a message on behalf of a group of spontaneously conscripted users including the actual signer. Any verifier can be convinced that the message has been signed by one of the member in this group, but the actual signer remains unknown. However, the theory of ring signature faced two problems when it comes to reality.

In traditional public key infrastructure (PKI), the public key is usually a "random" string that is unrelated to the identity of the user, so there is a need for a trusted-by-all certificate authority (CA) to assure the relationship between the cryptographic keys and the user. Therefore, any verifier of a signature must obtain a copy of user's certificate and check the validity of the certificate before checking the validity of the signature. In ring signature, not only the verifier must verify all the public keys of the group. The signer must do so as well or his/her anonymity is penalized (consider the extreme case that all certificates used are indeed invalid except the signer's one). The communication and the validation of a large number of public keys greatly affect the efficiency of the scheme. Moreover, real spontaneity is not always possible for ring signature under traditional PKI. Any signer can spontaneously conscript users who have already registered for a certificate.

Identity-based (ID-based) ring signature solved these problems: the public key of each user can be easily and publicly computed from a string corresponding his/her identity (for

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example, an email address). This property avoids the necessity of certificates, and associates an implicit public key to each person over the world.

Unfortunately, the theory of ID-based ring signature also faced obstacle in real application. ID-based ring signature schemes are usually derived from bilinear pairings, a powerful but computationally expensive cryptographic primitive. The important properties of bilinear pairings and associated intractable problems are recalled in Section 3.

From the review in the next section, we know that the number of pairing computations of all existing ID-based ring signature from bilinear pairings grows linearly with the group size, which made the efficiency of ID-based schemes over traditional schemes questionable. It is fair to say devising an ID-based ring signature using sublinear numbers of pairing computation remains an open question.

In this paper, we close this open problem. An efficient ID-based ring signature is constructed in Section 5, which only takes two pairing computations for any group size, and the generation of the signature involves no pairing computations at all. The proposed scheme is proven to be existential unforgeable against adaptive chosen message-and-identity attack under the random oracle model. The framework and the security notion of ID-based ring signature are discussed in Section 4.

2 Related Work

ID-based ring signature was introduced in [17] and a more efficient version was proposed in [12]. Small inconsistencies in [17] and [12] were fixed by [1], together with a new proxy ring signature scheme from the delegation function due to [?]. Another ring signature with formally proven security was proposed in [10], where ID-based ring signature from anonymous subsets was also considered. The scheme in [10] supports parallel pairing operations, which is not possible in schemes like [1, 12, 17].

Threshold ring signature is the t-out-of-n threshold version of ring signature, where t or more entities can jointly generate a valid signature but t-1 or fewer entities cannot. These schemes are applied in pervasive computing applications and mobile ad-hoc networks, where ad-hoc groups are very common. The first ID-based threshold ring signature was proposed in [7]. It supports robustness and trusted authority compatibility. The scheme's time and space complexity are up to the state-of-the-art of existing pairing-based ring signature and threshold ring signature, if not better than. Actually, the scheme in [7] was the most efficient (in terms of number of pairing operations required) ID-based ring signature scheme (when t=1).

Taken into account the total computational costs for signature generation and verification, existing solutions [1, 7, 10, 12, 17] need a number of pairing computations ranging from n + 1 to 4n - 1 where n is the group size of the ring signature. Since pairing computation is usually the most expensive one among others in ID-based cryptosystems, this linear dependence with the group size is undesirable.

We remark that there are non-ID-based ring signature from bilinear pairings, for examples, [2, 15, 16, 18,?].

Indeed, the real spontaneity of ID-based ring signature also relies on the assumption that the trusted authority (the private key generator) will not reveal any information about who has requested for his/her private key and who has not. In [9], an secure and anonymous ID-based key issuing protocol was proposed such that any eavesdropper cannot learn what is the

identity associated with the private key being issued even though the key is not transmitted via a secure channel.

Ring signature scheme can be used to derive other primitives as well. It had been utilized to construct non-interactive deniable ring authentication [13], perfect concurrent signature [14] and multi-designated verifiers signature [5, 11].

3 Bilinear Pairings and Related Complexity Assumptions

Before presenting our results, we review the definitions of bilinear pairing and related complexity assumptions.

Bilinear pairing is an important primitive for many cryptographic schemes [1–18,?]. Here, we describe some of its key properties.

Let $(\mathbb{G}_1, +)$ and (\mathbb{G}_2, \cdot) be two cyclic groups of prime order q. The bilinear pairing is given as $\hat{e} : \mathbb{G}_1 \times \mathbb{G}_1 \to \mathbb{G}_2$, which satisfies the following properties:

- 1. Bilinearity: For all $P,Q,R\in\mathbb{G}_1$, $\hat{e}(P+Q,R)=\hat{e}(P,R)\hat{e}(Q,R)$, and $\hat{e}(P,Q+R)=\hat{e}(P,Q)\hat{e}(P,R)$.
- 2. Non-degeneracy: There exists $P, Q \in \mathbb{G}_1$ such that $\hat{e}(P, Q) \neq 1$.
- 3. Computability: There exists an efficient algorithm to compute $\hat{e}(P,Q) \ \forall P,Q \in \mathbb{G}_1$.

Definition 1. Given a generator P of a group \mathbb{G} and a 3-tuple (aP, bP, cP), the Decisional Diffie-Hellman problem (DDHP) is to decide whether c = ab.

Definition 2. Given a generator P of a group \mathbb{G} , (P, aP, bP, cP) is defined as a valid Diffie-Hellman tuple if c = ab.

Definition 3. Given a generator P of a group \mathbb{G} and a 2-tuple (aP, bP), the Computational Diffie-Hellman problem (CDHP) is to compute abP.

Definition 4. If \mathbb{G} is a group such that DDHP can be solved in polynomial time but no probabilistic algorithm can solve CDHP with non-negligible advantage within polynomial time, then we call \mathbb{G} a Gap Diffie-Hellman (GDH) group.

We assume the existence of a bilinear map $\hat{e}: \mathbb{G}_1 \times \mathbb{G}_1 \to \mathbb{G}_2$ that one can solve Decisional Diffie-Hellman Problem in polynomial time.

4 Ring Signature

4.1 Framework of ID-Based Ring Signature

An ID-based ring signature scheme consists of four algorithms: Setup, KeyGen, Sign, and Verify.

- Setup: On an unary string input 1^k where k is a security parameter, it produces the common public parameters params, which include a description of a finite signature space and a description of a finite message space.
- KeyGen: On an input of signer's identity $ID \in \{0,1\}^*$, it outputs the signer's secret signing key S_{ID} . (The corresponding public verification key Q_{ID} can be computed easily by everyone.)

- Sign: On input of a message m, a group of n users' identities $\{ID_i\}$, where $1 \leq i \leq n$, and the secret keys of one members $\{S_{ID_s}\}$, where $1 \leq s \leq n$; it outputs an ID-based ring signature σ on the message m.
- Verify: On a ring signature σ , a message m and the group of signers' identities $\{ID_i\}$ as the input, it outputs \top for "true" or \bot for "false", depending on whether σ is a valid signature signed by a certain member in the group $\{ID_i\}$ on a message m.

These algorithms must satisfy the standard consistency constraint of ID-based ring signature scheme, i.e. if $\sigma = \text{Sign}(m, \{ID_i\}, S_{ID_s})$, we must have $\text{Verify}(\sigma, \{ID_i\}, m) = \top$.

For an ID-based ring signature scheme to be considered as secure, we need to consider its unforgeability and signer ambiguity.

4.2 Unforgeability of ID-Based Ring Signature

The following EUF-IDRS-CMIA2 game played between a challenger \mathcal{C} and an adversary \mathcal{A} formally defines the existential unforgeability of ID-based ring signature under adaptive chosen-message-and-identity attack.

EUF-IDRS-CMIA2 Game:

Setup: The challenger C takes a security parameter k and runs the Setup to generate common public parameters params and also the master secret key s. C sends params to A.

Attack: The adversary A can perform a polynomially bounded number of queries in an adaptive manner (that is, each query may depend on the responses to the previous queries). The types of queries allowed are described below.

- Hash functions queries: \mathcal{A} can ask for the values of the hash functions (e.g. $H(\cdot)$ and $H_0(\cdot)$ in our proposed scheme) for any input.
- KeyGen: \mathcal{A} chooses an identity ID. \mathcal{C} computes $\mathsf{Extract}(ID) = S_{ID}$ and sends the result to \mathcal{A} .
- Sign: \mathcal{A} chooses a group of n users' identities $\{ID_i\}$ where $1 \leq i \leq n$, and any message m. \mathcal{C} outputs an ID-based ring signature σ .

Forgery: The adversary \mathcal{A} outputs an ID-based ring signature σ and a group of n users' identities $\{ID_i\}$ where $1 \leq i \leq n$. The only restriction is that $(m, \{ID_i\})$ does not appear in the set of previous Sign queries and each of the secret keys in $\{S_{ID_{i_i}}\}$ is never returned by any KeyGen query. i.e. no private keys in $\{S_{ID_{i_i}}\}$ is known. It wins the game if $\mathsf{Verify}(\sigma, \{ID_i\})$ is equal to \top . The advantage of \mathcal{A} is defined as the probability that it wins.

Definition 5. An ID-based ring signature scheme is said to have the existential unforgeability against adaptive chosen-message-and-identity attacks property (EUF-IDRS-CMIA2 secure) if no adversary has a non-negligible advantage in the EUF-IDRS-CMIA2 game.

4.3 Signer Ambiguity of ID-Based Ring Signature

Definition 6. An ID-based ring signature scheme is said to have the unconditional signer ambiguity if for any group of n users' identities $\{ID_i\}$ where $1 \le i \le n$, any message m and any signature σ , where $\sigma = \text{Sign}(m, \{ID_i\})$; any verifier \mathcal{A} even with unbounded computing resources, cannot identify the actual signer with probability better than a random guess. That is, \mathcal{A} can only output the actual signer indexed by s with probability no better than $\frac{1}{n}$.

5 Efficient ID-based Ring Signature

The design of the proposed scheme to be presented in this section is inspired by the "attack" in [4], where the problem of ID-based batch verification was investigated. They showed that existing ID-based signature schemes prior to their work cannot support batch verifications of multiple signatures by showing attacks on aggregate verification mechanisms. The failure of aggregate verification indeed comes from the gap between the possibility of using only a single private key to sign n messages and the desired requirement of using at least n private keys to sign n messages. In this section, the failure is converted into a useful result: an efficient ID-based ring signature scheme with a constant number of pairing computations.

5.1 Construction

Define $\mathbb{G}_1, \mathbb{G}_2$, and $\hat{e}(\cdot, \cdot)$ as in the Section 3 where \mathbb{G}_1 is a GDH group. $H(\cdot)$ and $H_0(\cdot)$ are two cryptographic hash functions where $H: \{0,1\}^* \to \mathbb{G}_1$ and $H_0: \{0,1\}^* \to \mathbb{Z}_q^*$.

Setup: TA randomly chooses $x \in_R \mathbb{Z}_q^*$, keeps it as the master secret key and computes the corresponding public key $P_{pub} = xP$. The system parameters are:

$$params = \{\mathbb{G}_1, \mathbb{G}_2, \hat{e}(\cdot, \cdot), q, P, P_{pub}, H(\cdot), H_0(\cdot)\}.$$

KeyGen: The signer with identity $ID \in \{0,1\}^*$ submits ID to TA. TA sets the signer's public key Q_{ID} to be $H(ID) \in \mathbb{G}_1$, computes the signer's private signing key S_{ID} by $S_{ID} = xQ_{ID}$. Then TA sends the private signing key to the signer via a secure channel, or using the protocol proposed in [9].

Sign: Let $L = \{ID_1, ID_2, \dots, ID_n\}$ be the set of all identities of the n users, the actual signer, indexed by s (i.e. his/her public key is $Q_{ID_s} = H(ID_s)$) carries out the following steps to give an ID-based ring signature on behalf of the group L.

- 1. Choose $r_i \in_R \mathbb{Z}_q^*$, compute $U_i = r_i Q_{ID_i}$ and $h_i = H_0(m||L||U_i) \ \forall i \in \{1, 2, \cdots, n\} \setminus \{s\}$.
- 2. Choose $r'_s \in_R \mathbb{Z}_q^*$, compute $U_s = r'_s Q_{ID_s} \sum_{i \neq s} \{(r_h + h_i)Q_{ID_i}\}$.
- 3. Compute $h_s = H_0(m||L||U_s)$ and $V = (h_s + r'_s)S_{ID_s}$.
- 4. Output the signature for m and L as $\sigma = \{\bigcup_{i=1}^n \{U_i\}, V\}$.

Verify: A verifier can check the validity of a signature $\sigma = \{\bigcup_{i=1}^n \{U_i\}, V\}$ for the message m and a set of identities L as follows.

- 1. Compute $h_i = H_0(m||L||U_i) \ \forall i \in \{1, 2, \dots, n\}.$
- 2. Checking whether $\hat{e}(P_{pub}, \sum_{i=1}^{n} (U_i + h_i Q_{ID_i})) = \hat{e}(P, V)$.
- 3. Accept the signature if it is true, reject otherwise.

5.2 Consistency

The consistency of our scheme can be easily verified by the following equations.

$$\hat{e}(P_{pub}, \sum_{i=1}^{n} (U_i + h_i Q_i)) = \hat{e}(P_{pub}, U_s + h_s Q_{ID_s} + \sum_{i \neq s} (U_i + h_i Q_{ID_i}))$$

$$= \hat{e}(P_{pub}, h_s Q_{ID_s} + r'_s Q_{ID_s} - \sum_{i \neq s} \{(r_i + h_i) Q_{ID_i}\} + \sum_{i \neq s} (U_i + h_i Q_{ID_i}))$$

$$= \hat{e}(P_{pub}, h_s Q_{ID_s} + r'_s Q_{ID_s} - \sum_{i \neq s} (U_i + h_i Q_{ID_i}) + \sum_{i \neq s} (U_i + h_i Q_{ID_i}))$$

$$= \hat{e}(P_{pub}, h_s Q_{ID_s} + r'_s Q_{ID_s})$$

$$= \hat{e}(xP, (h_s + r'_s) Q_{ID_s})$$

$$= \hat{e}(P, (h_s + r'_s) S_{ID_s})$$

$$= \hat{e}(P, (h_s + r'_s) S_{ID_s})$$

5.3 Efficiency

We consider the costly operations which include point addition on \mathbb{G}_1 (\mathbb{G}_1 Add), point scalar multiplication on \mathbb{G}_1 (\mathbb{G}_1 Mul), multiplication in \mathbb{G}_2 or \mathbb{Z}_q ($\mathbb{G}_2/\mathbb{Z}_q$ Mul), hashing into the group (Hash) and pairing operation (Pairing). We use the MapToPoint hash operation in BLS short signature scheme [3]. Before our proposal, the scheme that requires the least number of pairing operations is [7] (named S-IDTRS). Table 1 shows a summary of the efficiency of our proposed scheme (named S-IDRS). Taken into account the total cost of signature generation and verification, we can see that our proposed scheme is the only schemes using a constant number of pairing operations, with comparable requirements in other operations.

	Efficiency				
Schemes	G_1 Add	G_1 Mul	G_2/Z_q Mul	Hash	Pairing
Zhang-Kim [17]	1	2n	2n-1	2n	4n-1
Lin-Wu [12]	2n-1	2n	3n	0	2n+1
Herranz-Sáez [10]	3n-1	2n	0	0	n+3
Awasthi-Lai [1]	2n-1	2n+1	2n-1	0	4n-1
S-IDTRS [7]	2n	4n	n-1	0	n+1
Proposed S-IDRS	3n-2	3n	0	0	2

Table 1. Efficiency of existing ID-based ring signature from bilinear pairings

Considering the signature size, we share the same order of space complexities as all other schemes we considered [1, 7, 10, 12, 17], we are not sacrificing the signature size for lowering time complexity.

5.4 Existential Unforgeability and Signer Ambiguity

The security of our proposed scheme is summarized in the following two theorems.

Theorem 1 In the random oracle model (the hash functions are modeled as random oracles), if there is an algorithm \mathcal{A} that can win the EUF-IDRS-CMIA2 game in polynomial time, then CDHP can be solved with non-negligible probability in polynomial time.

Proof. Suppose the challenger \mathcal{C} receives a random instance (P, aP, bP) of the CDHP and has to compute the value of abP. \mathcal{C} will run \mathcal{A} as a subroutine and act as \mathcal{A} 's challenger in the EUF-IDRS-CMIA2 game. During the game, \mathcal{A} will consult \mathcal{C} for answers to the random oracles H and H_0 . Roughly speaking, these answers are randomly generated, but to maintain the consistency and to avoid collision, \mathcal{C} keeps three lists to store the answers used. We assume \mathcal{A} will ask for H(ID) before ID is used in any other queries.

 \mathcal{C} gives \mathcal{A} the system parameters with $P_{pub} = bP$. Note that b is unknown to \mathcal{C} . This value simulates the master key value for the TA in the game.

H requests: We embed part of the challenge aP in the answer of many H queries. When \mathcal{A} asks queries on the hash value of identity ID, \mathcal{C} picks $y_i \in_R \mathbb{Z}_q^*$ and repeats the process until y_i is not in the list L_1 . C then flips a coin $W \in \{0,1\}$ that yields 0 with probability ζ and 1 with probability $1-\zeta$. (ζ will be determined later.) If W=0 then the hash value H(ID) is defined as y_iP ; else if W=1 then returns $H(ID)=y_i(aP)$. In either case, \mathcal{C} stores (ID, y_i, W) in the list L.

Note that when W=0, the associated private key is $y_i(bP)$ which \mathcal{C} knows how to compute. But when W=1, since both a and b are unknown to \mathcal{C} , a KeyGen request on this identity will make \mathcal{C} fails.

 H_0 requests: When \mathcal{A} asks queries on these hash values, \mathcal{C} checks the corresponding list L_2 . If an entry for the query is found, the same answer will be given to A; otherwise, a randomly generated value will be used as an answer to A, the query and the answer will then be stored in the list.

Sign requests: A chooses a group of n users' identities $L = \{ID_i\}$ where $1 \le i \le n$, and any message m. On input of (L, m), \mathcal{C} outputs an ID-based ring signature σ as follows.

- 1. Choose an index $s \in \{1, 2, \dots, n\}$.

- 2. Choose $r_i \in_R \mathbb{Z}_q^*$, compute $U_i = r_i Q_{ID_i}$ and $h_i = H_0(m||L||U_i) \ \forall i \in \{1, 2, \cdots, n\} \setminus \{s\}$. 3. Choose $h_s' \in_R \mathbb{Z}_q^*$ and $z \in_R \mathbb{Z}_q^*$, compute $U_s = zP h_s' Q_{ID_s} \sum_{i \neq s} \{(r_h + h_i)Q_{ID_i}\}$. 4. Store the relationship $h_s = H_0(m||L||U_s)$ to the list L_2 and compute V = z(bP), repeat Step 3 in case collision occurs.
- 5. Output the signature for m and L as $\sigma = \{\bigcup_{i=1}^n \{U_i\}, V\}$.

Finally, \mathcal{A} outputs a forged signature $\sigma = \{\cup_{i=1}^n \{U_i\}, V\}$ that is signed by a certain member in the group $\{ID_i\}$ where $Q_{ID_i} = H(ID_i) = y_i(aP) \forall i \in \{1, 2, \dots, n\}$, i.e. \mathcal{A} has not requested for any one of the private keys of members in the group. It follows from the forking lemma for generic ring signature schemes [10] that if \mathcal{A} is a sufficiently efficient forger in the above interaction, then we can construct a Las Vegas machine \mathcal{A}' that outputs two signed messages $\sigma = \{\bigcup_{i=1}^n \{U_i\}, V\}$ and $\sigma' = \{\bigcup_{i=1}^n \{U_i\}, V'\}$. Suppose $h_i = H_0(m||L||U_i)$ and $h'_i = H_0(m||L||U_i)$ for all $i \in \{1, 2, \dots, n\}$, we have $h_i = h'_i$ for all $i \in \{1, 2, \dots, n\} \setminus s$.

Given the machine \mathcal{A}' derived from \mathcal{A} , we can solve the CDHP by computing abP = $(h_s - h'_s)^{-1}(V - V').$

Theorem 2 Our ID-based ring signature scheme satisfies the unconditional signer ambiguity property.

Proof. Since $\cup_{i\neq s} \{r_i\}$ and also r'_s are randomly generated, hence $\cup_{i=1}^n \{U_i\}$ are also uniformly distributed.

It remains to consider whether $V=(h_s+r'_s)S_{ID_s}$ leaks information about the actual signer. Since h_s is publicly computable, we focus on the value of $V-h_sS_{ID_s}=r'_sS_{ID_s}$. Obviously, $r'_sS_{ID_s}$ is related to U_s . Any one can compute the value of $r'_sQ_{ID_s}$ by $U_s+\sum_{i\neq s}(U_i+h_iQ_{ID_i})$. Together with the fact that the bilinearity can relate $r'_sS_{ID_s}$ and $r'_sQ_{ID_s}$ by checking whether $\hat{e}(r'_sQ_{ID_s},P)=\hat{e}(r'_sS_{ID_s},P_{pub})$, one may be tempted to see if ID_j is the actual signer by checking whether the following equality holds.

$$\hat{e}(U_j + \sum_{i \neq j} (U_i + h_i Q_{ID_i}), P_{pub}) = \hat{e}(V, P) / \hat{e}(h_j Q_{ID_j}, P_{pub})$$

However, we claim that this method is of no use, as the above equality not only holds when j = s, but also $\forall j \in \{1, 2, \dots, n\} \setminus \{s\}$. i.e. the signature is symmetric.

$$\begin{split} \hat{e}(U_{j} + \sum_{i \neq j} (U_{i} + h_{i}Q_{ID_{i}}), P_{pub}) &= \hat{e}(\sum U_{i} + \sum_{i \neq j} h_{i}Q_{ID_{i}}, P_{pub}) \\ &= \hat{e}(\sum_{i \neq s} U_{i} + U_{s} + \sum_{i \neq j} h_{i}Q_{ID_{i}}, P_{pub}) \\ &= \hat{e}(\sum_{i \neq s} U_{i} + r'_{s}Q_{ID_{s}} - \sum_{i \neq s} \left\{ (r_{h} + h_{i})Q_{ID_{i}} \right\} + \sum_{i \neq j} h_{i}Q_{ID_{i}}, P_{pub}) \\ &= \hat{e}(\sum_{i \neq s} U_{i} + r'_{s}Q_{ID_{s}} - \sum_{i \neq s} (U_{i} + h_{i}Q_{ID_{i}}) + \sum_{i \neq j} h_{i}Q_{ID_{i}}, P_{pub}) \\ &= \hat{e}(r'_{s}Q_{ID_{s}} - \sum_{i \neq s} h_{i}Q_{ID_{i}} + \sum_{i \neq j} h_{i}Q_{ID_{i}}, P_{pub}) \\ &= \hat{e}(r'_{s}Q_{ID_{s}} + h_{s}Q_{ID_{s}} - h_{j}Q_{ID_{j}}, P_{pub}) \\ &= \hat{e}(r'_{s}Q_{ID_{s}} + h_{s}Q_{ID_{s}} - h_{j}Q_{ID_{j}}, xP) \\ &= \hat{e}(V - h_{j}S_{ID_{s}}, P) \\ &= \hat{e}(V - h_{j}S_{ID_{j}}, P) \\ &= \hat{e}(V, P)/\hat{e}(h_{j}Q_{ID_{j}}, xP) \\ &= \hat{e}(V, P)/\hat{e}(h_{j}Q_{ID_{j}}, xP) \\ &= \hat{e}(V, P)/\hat{e}(h_{j}Q_{ID_{j}}, P_{pub}) \end{split}$$

To conclude, for any fixed message m and fixed set of identities L, the distribution of $\{\bigcup_{i=1}^n \{U_i\}, V\}$ are independent and uniformly distributed no matter who is the actual signer. So we conclude that even an adversary with all the private keys corresponding to the set of identities L and unbounded computing resources has no advantage in identifying any one of the participating signers over random guessing.

6 Conclusion

For ring signature scheme to be practical, we need to eliminate the need of validity checking of the certificates and the need of registering for a certificate before getting the public key. ID-based solutions can provide these two features. Nonetheless, existing proposals of ID-based ring signature are computationally inefficient, since the number of pairing computations grows linearly with the group size. This paper closes the open problem of devising an ID-based ring

signature using sublinear numbers of pairing computation. We construct an efficient ID-based ring signature which only needs two pairing computations for any group size. The proposed scheme is proven to be existential unforgeable against adaptive chosen message-and-identity attack under the random oracle model, using the forking lemma for generic ring signature schemes. Future research directions include making a constant-size ID-based ring signature scheme or making the ring signature scheme works in a hierarchical setting [8].

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