

# Towards Security Two-part ID-based Authenticated Key Agreement Protocols

Songping Li<sup>1</sup>, Jin Li<sup>2</sup> and Maozhi Xu<sup>1</sup>

<sup>1</sup>School of Mathematical Sciences, Peking University, Beijing, 100871 P. R.China

<sup>1</sup>{lsp,mzxu}@pku.edu.cn

<sup>2</sup>Huawei Technologies Co., Shenzhen, 518129 P. R.China

<sup>2</sup>jingle@huawei.com

**Abstract.** In this paper we find that Xie's ID-2-AKP (ID-based two-party authenticated key agreement protocol) modified from McCullagh-Barreto which is proposed in CT-RSA 2005 doesn't provide protection against KCI attack likewise, and finally utilize the modular arithmetic, first proposed in MQV and also used in Kim, to get a modified new ID-2-AKP. We also give another ID-2-AKP utilizing the operation, which is always nominated addition, in the finite field to give another modified version. The two protocols are in possession of all the desired security attributes. We also compare our new protocols with others in terms of computational cost and security properties.

**Keywords.** key management, authenticated protocol, ID-based, Key Compromise Impersonation

## 1 Introduction

Authenticated key establishment protocols are designed to provide two or more specified entities communicating over an open network with a shared secret key that may subsequently be used to achieve some cryptographic goal such as confidentiality or data integrity. There are two fundamental types of key establishment protocols [7]: key transport and key agreement. Key agreement protocols are more reliable because both entities contribute information that is used to derive the shared secret key.

A key agreement protocol is desired to have these fundamental security goals: implicit key authentication and explicit key authentication [8,9]. A key agreement protocol which provides implicit key authentication to both participating entities is called an authenticated key agreement protocol (AKP), while one providing explicit key authentication to both participating entities is called an authenticated key agreement with key conformation protocol (AKCP).

As it has been proved to be difficult to deploy a public key infrastructure (PKI) system. Thus it is preferred to design easy to deploy authenticated key agreement systems. Identity based key agreement system is such an example. An AKP is called identity-based if in the protocol, users use an identity based asymmetric key pair instead of a traditional public/private key pair for authentication and determination of the established key.

In addition to implicit key authentication and key confirmation, a number of desirable security attributes of AK and AKC protocols have been identified. Typically the importance of supplying these attributes will depend on the application.

1. **Known-key security.** Each run of a key agreement between A and B should produce a unique secret key : such keys are called session keys. A protocol should still achieve its goal in the face of an adversary who has learned some other session keys.

2. **Forward secrecy.** If long-term private keys of one or more entities are compromised, the secrecy of previous session keys established by honest entities is not affected.

3. **Key-compromise impersonation resistant attribute.** Suppose A's long-term private key is disclosed. Clearly an adversary that knows this value can now impersonate A, since it is precisely this value that identifies A. However, it may be desirable in some circumstances that this loss does not enable the adversary to impersonate other entities to A.

4. **Unknown key-share attribute.** Entity B cannot be coerced into sharing a key with entity A without B's knowledge, i.e., when B believes the key is shared with some entity  $C \neq A$ , and A (correctly) believes the key is shared with B.

5. **Key Control.** Neither entity should be able to force the session key to be a pre-selected value. That is, the session key is determined by all the entities and no one can influence the generation of the session key.

Since the basic Diffie-Hellman key agreement scheme that provides the first practical solution to the key distribution problem, numerous protocols have been proposed. But many of these protocols were subsequently found to be flawed. For example, it is known that Unified Model, MTI/C0 and MQV protocol are vulnerable to key-compromise impersonation attack, small subgroup attack, and unknown key-share attack, respectively [10]. At Asiacrypt'96, Just and Vaudenay [11] proposed a 2-AKP whose elliptic curve version was subsequently proposed by Song and Kim [12] At Indocrypt'00. But in 2002, Kim [8] pointed that Just-Vaudenay protocol didn't provide protection against KCI attack, and finally present a modified version that can provide.

Based on Weil and Tate pairing techniques, several practical ID-AKPs, e.g., Smart [13], Chen-Kudla [14], Scott [15], Shim [16], and McCullagh-Barreto [6] etc., have been proposed. However, none of these protocols is secure (see,[17]). Recently, Xie [5] proposed an ID-AKP which is modified from McCullagh-Barreto[6] and asserted it can resistant KCI attack. Wang[18] also presented a new security ID-AKP not long ago.

The remainder of the paper is organized as follows. Section 2 introduces Technical Backgrounds. In section 3, we briefly explain Kim's protocol and show how they can resist KCI attack in deed. In section 4, we give a KCI attack to Xie's modified protocol after review McCullagh-Barreto's protocol and Xie's modification. In section 5, we present two new ID-2-AKPs that are in possession of all the desired security attributes. In section 6, we compare our new protocols with others in terms of computational cost and security properties. The concluding remark will be followed in section 7.

## 2 Technical Backgrounds

### 2.1 Bilinear Pairing

In this section, we shall briefly describe the properties of the bilinear pairings. The bilinear parings include Weil pairing and Tate pairing in elliptic curve cryptography, as the MOV attack using Weil pairing and the FR attack using Tate pairing reduce the discrete logarithm problem on some

elliptic curves to the discrete logarithm problem in a finite field [25,26]. Recently, the bilinear pairings have been used in construction of the identity-based cryptography.

We let  $G_1$  be a cyclic additive group generated by  $P$ , whose order is a prime  $q$ , and  $G_2$  be a cyclic multiplicative group of the same order  $q$ . We assume that the discrete logarithm problem (DLP) in both  $G_1$  and  $G_2$  are hard. We let  $\hat{e} : G_1 \times G_1 \rightarrow G_2$  be a pairing which satisfies the following properties:

1. Bilinear

$$\hat{e}(P_1 + P_2, Q) = \hat{e}(P_1, Q) \hat{e}(P_2, Q)$$

$$\hat{e}(P, Q_1 + Q_2) = \hat{e}(P, Q_1) \hat{e}(P, Q_2)$$

2. Non-degenerate

$$\text{if } P \text{ is a generator of } G_1, \text{ then } \hat{e}(P, P) \neq 1.$$

3. Computability

There is an efficient algorithm to compute  $\hat{e}(P, Q)$  for all  $P, Q \in G_1$  in polynomial-time.

The non-degeneracy does not hold for the standard Weil pairing  $e(P, Q)$ , but it does hold for the modified Weil pairing  $\hat{e}(P, Q)$ . We note that the Weil and Tate pairings associated with supersingular elliptic curves or abelian varieties can be modified to create such bilinear maps. We may refer to [19,27] for more details.

## 2.2 Diffie-Hellman Assumptions

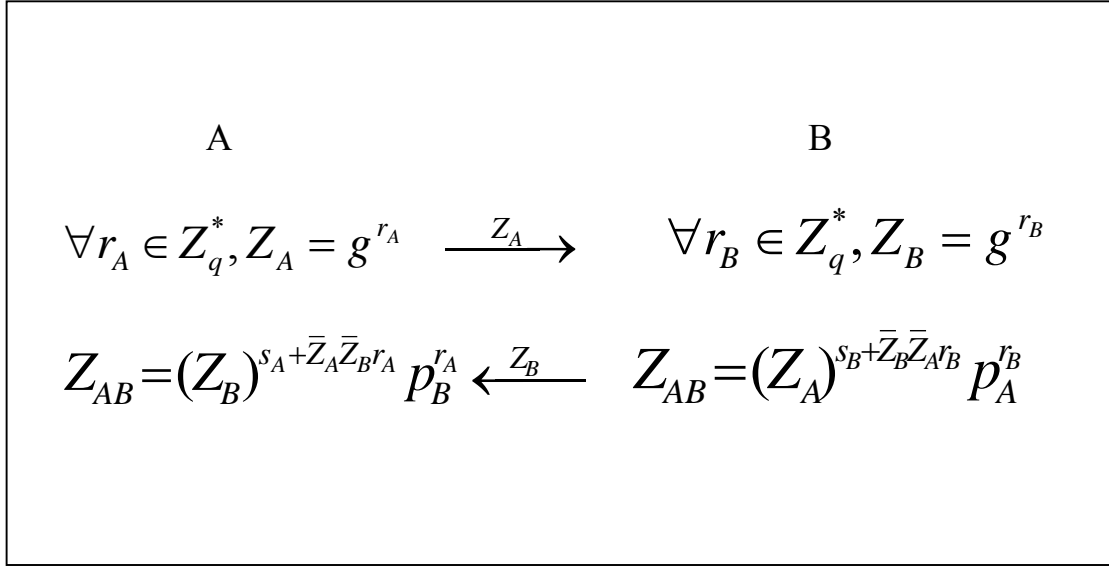
With the group  $G_1$  described in Section 2.1, there are the following problems in elliptic curve cryptography:

- Discrete Logarithm (DL) Problem: Given  $P, Q \in G_1$ , find an integer  $n$  such that  $P = nQ$  whenever such integer exists.
- Computational Diffie-Hellman (CDH) Problem: Given a triple  $(P, aP, bP) \in G_1$  for  $a, b \in \mathbb{Z}_q$ , find the element  $abP$ .
- Decision Diffie-Hellman (DDH) Problem: Given a quadruple  $(P, aP, bP, cP) \in G_1$  for  $a, b, c \in \mathbb{Z}_q$ , decide whether  $c = ab \pmod q$  or not.
- Gap Diffie-Hellman (GDH) Problem: A class of problems where the CDH problem is hard but DDH problem is easy.

## 3 Kim's Protocol

In 2002, Kim[8] proposed a modified version of the Just-Vaudenay protocol[11] to resist the KCI attack. We will briefly explain Kim's protocol as follows. Let  $p$  is an 1024 bits prime,  $q$  is an 160 bits prime divisor of  $p-1$  and  $G$  is a  $q$  order subgroup of  $\mathbb{Z}_p^*$ . Kim utilizes the following notation proposed in the MQV protocol: If  $X \in [1, p-1]$  then  $\bar{X} = (X \pmod{2^{80}}) + 2^{80}$ . Note that  $\bar{X} \pmod q \neq 0$ . In the protocol, two principals  $A$  and  $B$  agree publicly on an element  $g$  in a multiplicative group  $G$  and their private keys are  $s_A$  and  $s_B$  respectively and public keys are

$p_A = g^{s_A}$  and  $p_B = g^{s_B}$  correspondingly. They select random values  $r_A$  and  $r_B$ ,



**Figure 1: Kim's Protocol**

respectively, in the range between 1 and  $q$ . A calculates  $Z_A = g^{r_A}$  and B calculates  $Z_B = g^{r_B}$  and they exchange these values as shown in Figure 1. The shared secret is

$$Z_{AB} = g^{r_B s_A + \bar{Z}_A \bar{Z}_B r_A r_B + r_A s_B}.$$

Shim believes that an adversary C cannot implement the KCI attack since she cannot determine the value  $\bar{Z}_B$  in advance. We can prove that as follows:

In fact, C wants to counteract  $p_B^{r_A}$  which is indispensable in the calculation of  $Z_{AB} = g^{r_B s_A + \bar{Z}_A \bar{Z}_B r_A r_B + r_A s_B}$ . So he should get  $Z_B$  to s.t.

$$Z_B = g^{r_C} p_B^{\frac{-1}{\bar{Z}_A \bar{Z}_B}} = g^{r_C} (M)^{-1/\bar{Z}_B} \quad (r_C \text{ is a random value selected by C, } M = p_B^{1/\bar{Z}_A}).$$

We know that  $M$  is a positive constant, so C should get  $Z_B$  by the solution of discrete equation  $Z_B (M)^{1/\bar{Z}_B} = g^{r_C}$ .  $\forall r_C \in Z_q^*$ , let  $\bar{Z}_B = Z_B + k \cdot 2^{80}$  ( $k$  is a

positive integer), and then we want to solve the equation  $Z_B (M)^{1/\bar{Z}_B} = g^{r_C}$  in turn with variable  $k$ . In other words, we want to get a solution of the discrete transcendental equation

$$xa^{\frac{1}{x+c}} = b \quad (a > 0, a, b, \text{ and } c \text{ are constants}) \text{ which we denote as } \alpha.$$

Actually we have known that it is a difficult problem to get the analytic solution of the transcendental equation yet. We know neither whether it has a solution nor the number of solutions up to the present. There are only several approximate solutions to the transcendental equation, such as iterative method and dichotomy etc. . So it is naturally hard to get the solution  $\alpha$  of the discrete transcendental equation in big prime field. It seems at least as hard as discrete logarithm problem in big prime field. So Kim's protocol provides protection against KCI attack for sure. The protocol also has other attributes, such as Known Key-Security, Perfect-Forward-Secrecy etc. .

#### 4 McCullagh-Barreto's Protocol and Xie's Modified Version

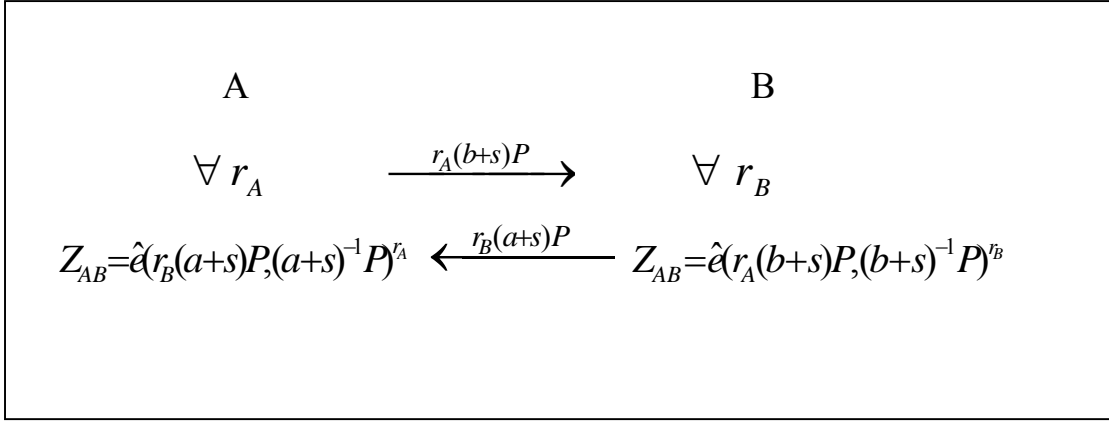
Resently, McCullagh and Barreto[6] proposed a ID-2-AKP in CT-RSA 2005. But later Xie[4] pointed out McCullagh-Barreto's protocol proposed in [6] didn't provide protection against KCI attack and proposed a new ID-2-AKP[5] modified from that and asserted it can resistant KCI attack. But we find the modification is unsuccessful.

First we briefly explain McCullagh-Barreto's protocol. McCullagh-Barreto's protocol like all other ID-AKPs has three algorithms: **Setup**, **Extract** and **Key agreement**.

**Setup:** The KGC (Key Generation Centre) is responsible for the creation and secure distribution of users private keys.  $G_1$  and  $G_2$  are two groups, both of prime order  $q$ , suitable bilinear map  $\hat{e} : G_1 \times G_1 \rightarrow G_2$  (which can be modified from Tate pairing or Weil Pairing in elliptic curve, see, [19,20]).  $P$  is a generator element of  $G_1$ .  $H$  is an one-way hash fountion as  $H : \{0, 1\}^* \rightarrow Z_q^*$ . The KGC randomly generates a master secret  $s \in_R Z_q^*$ , and calculates a master public key  $sP$ . The parameters and master public key are distributed to the users of the system through a secure authenticated channel. The system public parameters is  $\langle E, q, G_1, G_2, P, sP, \hat{e}, H \rangle$ .

**Extract:** The identities of the two principles, A and B, are  $ID_A$  and  $ID_B$  respectively. Let  $a = H(ID_A)$  and  $b = H(ID_B)$ . A's public key is  $P_A = (a + s)P$ , which can be computed as  $aP + sP$ . The KGC computes Alice's private key as  $S_A = (a + s)^{-1}P$  and then sends it to A through a secret channel. The same is to B and so the public key and the private key of B are  $P_B = (b + s)P$  and  $S_B = (b + s)^{-1}P$  respectively.

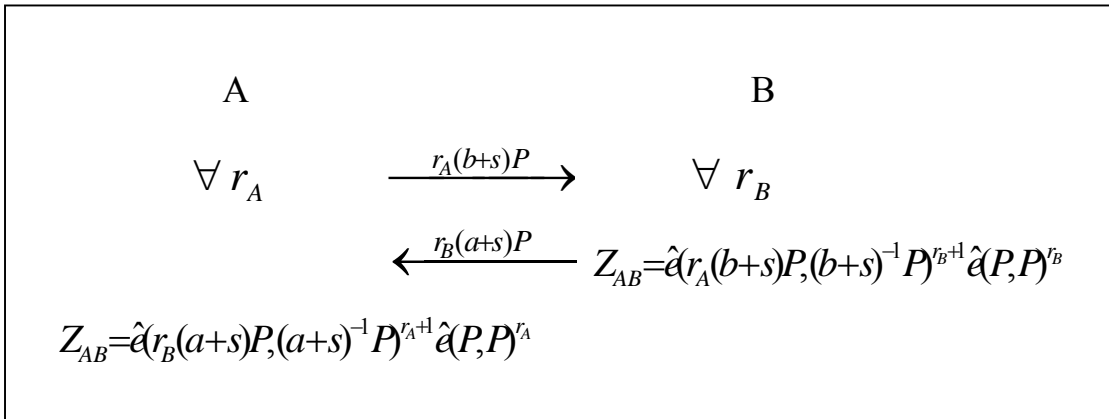
**Key Agreement:** Assume that A and B have private keys issued by the same KGC. The key agreement is shown in Figure 2, and the shared secret is  $Z_{AB} = \hat{e}(P, P)^{r_A r_B}$ .



**Figure 2: McCullagh-Barreto's Protocol**

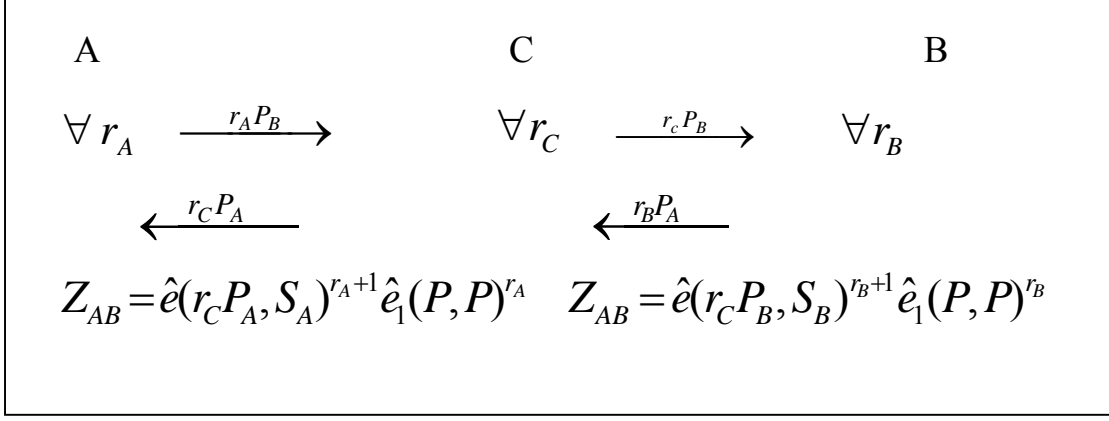
But later Xie[4] pointed out that McCullagh-Barreto's protocol was vulnerable to KCI attack: the adversary C can send  $r_B(b+s)P$  to A and then get the shared secret by calculating  $Z_{AB} = \hat{e}(r_A(b+s)P, (a+s)^{-1}P)^{r_B}$ . McCullagh and Barreto's modified version to resist Xie's KCI attack is to change the expression of the shared secret calculation to  $Z_{AB} = \hat{e}(P, P)^{r_A+r_B}$ . But we know, it does not provide Perfect Forward Secrecy property. Because the adversary C can get the previous session keys by calculating  $Z_{AB} = \hat{e}(r_A(b+s)P, (b+s)^{-1}P)\hat{e}(r_B(a+s)P, (a+s)^{-1}P)$ .

Xie then gave a modified version to McCullagh-Barreto's protocol. His protocol only changes the expression of the shared secret calculation likewise. The algorithms of Setup and Extract are the same as McCullagh-Barreto's. In the Key Agreement, the shared secret is  $Z_{AB} = \hat{e}(P, P)^{r_A r_B + r_A + r_B}$ , as is shown in Figure 3.



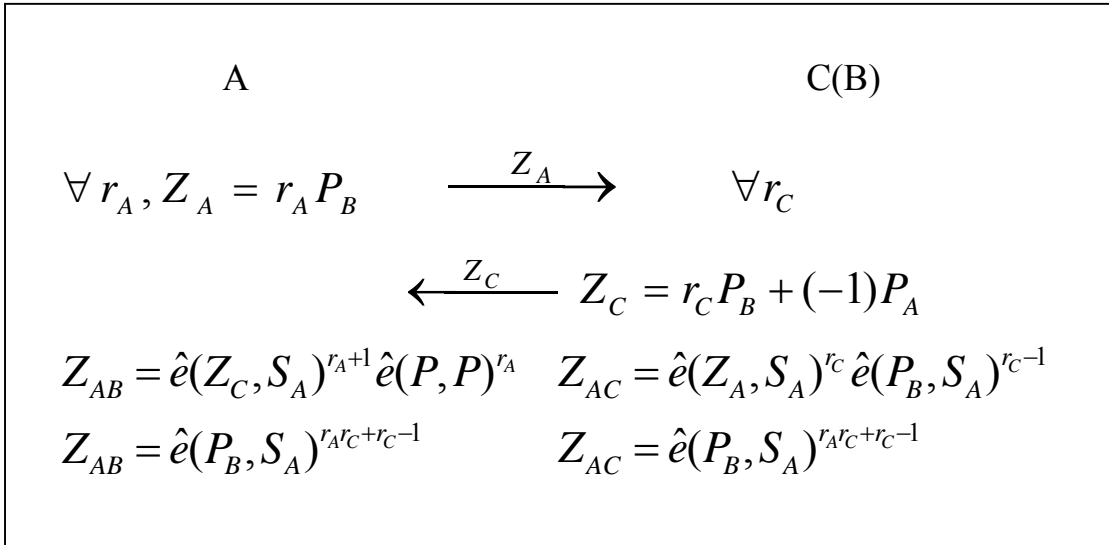
**Figure 3: Xie's Protocol**

But we find the modification is unsuccessful because it is vulnerable to the KCI attack yet. Actually the protocol has a leak of -1. when the adversary C let  $r_C = -1$ , he can succeed in man-in-middle attack which is shown in Figure 4 and gets the shared secret  $Z_{AB} = \hat{e}(P, P)^{-1}$ .



**Figure 4: man-in-middle attack to Xie's Protocol**

Although A and B can reject the random value -1 from the other side to prevent it, the leak is intrinsic as long as the shared secret is calculate by  $Z_{AB} = \hat{e}(r_C P_A, S_A)^{r_A+1} \hat{e}_1(P, P)^{r_A}$ . We can utilize the leak of -1 to carry out KCI attack, as is shown in Figure 5. After the attack, the adversary C can impersonate B to share secret  $Z_{AC} = \hat{e}(P_B, S_A)^{r_A r_C + r_C - 1}$  with A while A believes he has shared the secret with B.



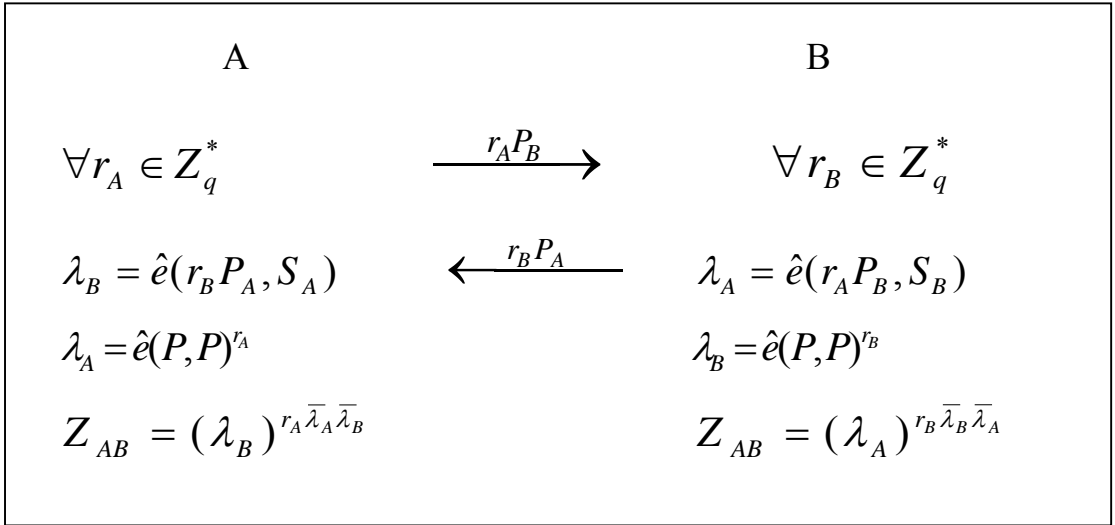
**Figure 5: KCI attack to Xie's Protocol**

## 5 Two New ID-2-AKPs

### 5.1 ID-2-AKP I

Inspired on Kim's protocol in section 3, here we give a modified version of McCullagh , Barreto and Xie's ID-2-AKPs [5, 6] with the help of the notation first proposed in the MQV protocol: If  $X \in [1, p-1]$  then  $\bar{X} = (X \bmod 2^{80}) + 2^{80}$ . Our modified protocol can prevent from the KCI attack and has less computational cost than Wang's in [18].

The algorithms of Setup and Extract are the same as McCullagh , Barreto and Xie's , except the additions of the notation  $\bar{X}$  and a system public parameter  $\hat{e}(P, P)$ . The main modification is in the Key Agreement as is shown in Figure 6. The final shared secret is  $Z_{AB} = \hat{e}(P, P)^{r_A r_B \bar{\lambda}_A \bar{\lambda}_B}$  ( where  $\lambda_A = \hat{e}(P, P)^{r_A}$ ,  $\lambda_B = \hat{e}(P, P)^{r_B}$  ). The adversary C couldn't construct message to make KCI attack like Kim's protocol in section 2. Because C have no knowledge of either  $r_A$  or  $r_B$  and he couldn't get  $\lambda_A = \hat{e}(P, P)^{r_A} = \hat{e}(r_A P_B, S_B)$  which is indispensable in the calculation of  $Z_{AB}$ .



**Figure 6: A New ID-2-AKP (ID-2-AKP I)**

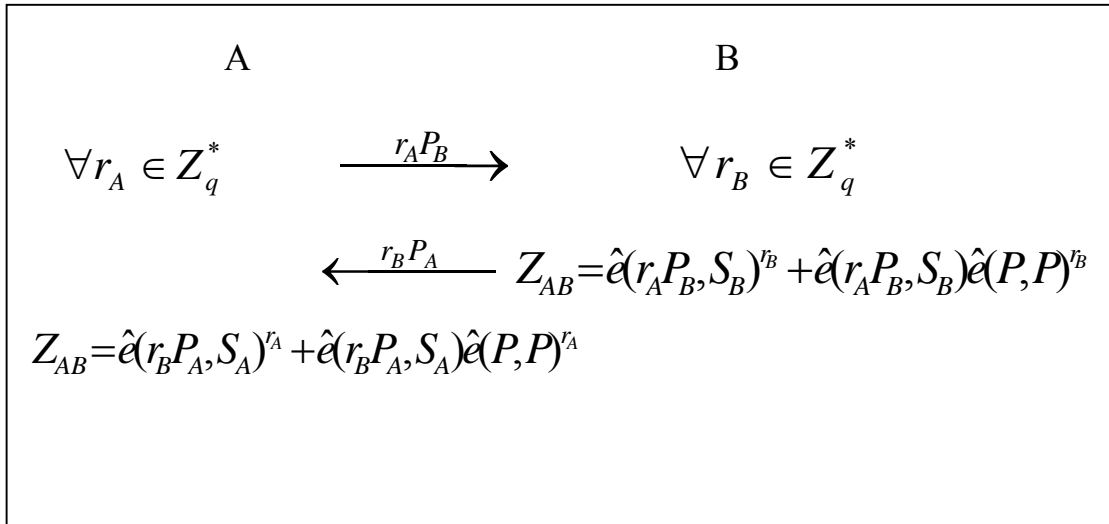
Our modified protocol also provides other security properties as is provided in McCullagh, Barreto and Xie's, such as Known Key Security, Perfect Forward-Secrecy etc. . That is similar to the explanationsto be described in section 5.2.



## 5.2 ID-2-AKP II

With the help of the addition operation in the finite field, we will give another modified version. The algorithms of Setup and Extract are similar to McCullagh , Barreto and Xie's , except the + operation and a system public parameter  $\hat{e}(P, P)$ . Let p is an 1024 bits prime, q is an 160 bits prime divisor of p-1,  $G_1$  is a q order subgroup of  $Z_p^*$  and  $G_2$  is a q order subgroup of the multiplicative group  $F_p^*$  of finite field  $F_p$  (that is,  $G_2$  is a subfield of  $F_p$ ). The + operation is the addition operation in finite field  $F_p$ .

The remainder modification is in the Key Agreement as is shown in Figure 7. The final shared secret is  $Z_{AB} = \hat{e}(P, P)^{r_A r_B} + \hat{e}(P, P)^{r_A} \hat{e}(P, P)^{r_B}$ . As the calculations is in finite field, so we know entity A and entity B share the same value above. We also know the value of the shared secret is in finite field  $F_p$  but not only in  $G_2$ . In order to avoid the particular value 0 which is the zero in finite field  $F_p$ , we select  $G_2$  such that  $\forall g \in G_2, -g \notin G_2$  ( $-g$  is negative element of  $g$  in  $F_p$ ). But it seems that it is very hard to find the desired  $G_2$  and validate it for sure. But we can settle the matter by checking the shared key  $Z_{AB}$  and redoing a new key agreement after drawing it away while  $Z_{AB} = 0$ .



**Figure 7: Another ID-2-AKP ( ID-2-AKP II)**

Now we explain our protocol providing the desirable security attributes:

1. **Known-key security.** Each run of the key agreement between A and B produces a unique session key due to the random numbers  $r_A$  and  $r_B$ , and there are no ways to get some session key from other session keys.

2. **Forward secrecy.** Even if all the long-term private keys of A and B are compromised, it is hard to get  $\hat{e}(P, P)^{r_A r_B}$  for the adversary that is indispensable in the calculation of  $Z_{AB}$ . This can be concluded by the assumptions in section 2.2. So the previous session keys are not affected.

3. **Key-compromise impersonation resistant attribute.** Suppose A's long-term private key is disclosed, the adversary C couldn't construct message to make KCI attack like Figure 4. Because C have no knowledge of either  $r_A$  or  $S_B$  and he couldn't kill  $\hat{e}(P, P)^{r_A}$  which is indispensable in the calculation of  $Z_{AB}$ .

4. **Unknown key-share attribute.** As we know, the unknown key-share attack usually utilizes the method of tampering the public-key certificates. In ID-based key agreement since the public-keys are the identities and the public-key certificates are discarded, so unknown key-share attack is hard to be carried into execution and the security attribute of Unknown Key-Share resistant is naturally owned by all ID-based protocols.

5. **Key Control.** Neither entity should be able to force the session key to be a pre-selected value for they offer the random numbers  $r_A$  and  $r_B$  each other.

Our new ID-2-AKPs inherits other merits from McCullagh-Barreto. For example, it can be used Between Members of Distinct Domains as the shared secret has not the master key  $s$  and we can also modify the bilinear map to get an Authenticated Key Agreement Without Escrow likewise.

## 6. Comparison of computation and security

We have compared the security attributes between some famous protocols in Figure 8. There are only four protocols that provide all the desirable security attributes. But Shim's protocol was vulnerable to man-in-middle attack[28], so Wang's protocol and our are more secure than others.

At last we compare our new protocols with Wang's in computational cost. In ID-2-AKP II, Pairing calculation is only once for A, i.e.  $\hat{e}(r_B P_A, S_A)$ , and used by twice. There is no other Pairing calculation as the system public parameter  $\hat{e}(P, P)$  is public. The same is to B and the result of comparison is shown in Figure 9.

security attributes→ ↓ protocols	Know - key security	PFS	KCI	Unknown key share	Key Control
Smart[13]	✓	×	✓	✓	✓
Chen-Kudla[14]	✓	×	✓	✓	✓
Shim[16]	✓	✓	✓	✓	✓
McCullagh-Barreto[6]	✓	✓	×	✓	✓
Xie[5]	✓	✓	×	✓	✓
Wang[18]	✓	✓	✓	✓	✓
ID-2-AKP I	✓	✓	✓	✓	✓
ID-2-AKP II	✓	✓	✓	✓	✓

**Figure 8: Comparison of the Security Attributes**

Protocols→ ↓ Calculations	Wang' s	ID-2-AKP I	ID-2-AKP II
Pairing	1	1	1
EC Scalar Multiplication	2	2(1)	2(1)
EC Addition	1	1(1)	1(1)
Finite field Multiplication	1	2	1
Finite field Power-Multiplication		1	2
Finite field Addition	1		1
$\bar{X}$		2	
Hash	4(2)	1(1)	1(1)

**Figure 9: Comparison of New ID-2-AKPs with Wang's in Computational Cost**

As is known to all, the arithmetics in EC spend much more time than in finite field(see,[21,22]). Hash is very time-consuming and modular arithmetic spends less time than Hash's arithmetic in evidence. The calculation of finite field Power-Multiplication maybe consumes much less time than the modular arithmetic  $\overline{X}$ . But it bears on the conditions much more. So with the help of pre-calculations (figures in brackets) our modified protocols needs less time in the calculations. In protocol I it is important to choose some modular arithmetic. In protocol II we only need get a good arithmetic for finite field power and prevent the particular values in the key agreement by checking them. The selection of  $G_2$  is also very important in protocol II from our analysis above.

## 7. Conclusion

We have proposed two new ID-2-AKPs that are more security and more efficient than existing protocols and it seems the ID-2-AKP II is more efficient between them. Indeed, we have not proved our protocols to be secure. But several of these protocols were proved to be secure in the Bellare-Rogaway model for key agreement protocols and the proofs were found flawed later. For example, Chen and Kudla [14] proved that their protocol is secure in the Bellare-Rogaway model. However, Cheng et al. [22] pointed out that the proof in [14] is flawed. Similarly McCullagh, Barreto and Xie's proofs in their protocols [5,6] are subsequently found invalid by Cheng et al. in [24]. The practical model of provable security is still expectant.

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