

# New Advances on Privacy-Preserving Policy Reconciliation

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## Abstract

Entities define their own set of rules under which they are willing to collaborate, e.g., interact, share and exchange resources or information with others. Typically, these individual *policies differ for different parties*. Thus, collaboration requires the resolving of differences and reaching a consensus. This process is generally referred to as policy reconciliation.

Current solutions for policy reconciliation do not take into account the privacy concerns of reconciling parties. This paper addresses the problem of preserving privacy during policy reconciliation. We introduce new protocols that meet the privacy requirements of the organizations and allow parties to find a common policy rule which *optimizes* their individual preferences.

## 1 Introduction

Enabling collaboration between organizations is a very challenging task. The main difficulty lies in determining the policy rules that should govern this process. That is, the (two or more) participants must accept a set of rules that they will follow for the duration of the collaboration. Each party has to express their desired rules in a common format and follow a protocol with the other parties. The process will determine which rules control their future collaboration. This protocol is called a *reconciliation protocol* and its output is a policy that is consistent with the requirements of all the participants. If such a policy exists, the participants can continue their collaboration. Otherwise, they can decide not to collaborate or they can decide to modify their individual requirements and repeat the protocol.

Consider the following example: A company has posted a job opening. Multiple applications have been received and HR would like to schedule interviews with some of the applicants. To successfully schedule an interview, both HR and the respective applicant need to reach an agreement on the date and time for the interview. I.e., they need to reconcile their policies, which—in this case—regulate the dates and times when the individual parties are available for the interview.

Obviously, this is a simple example with respect to policy reconciliation and it is very unlikely that the two parties will make use of any sophisticated reconciliation methods for scheduling such an interview. However, we believe this example highlights some of the shortcomings of current policy reconciliation processes. To date, policy reconciliation does not consider privacy. Continuing with our example, either party may want certain information not to be disclosed to the other party during the reconciliation process, i.e., when trying to find a date/time for the interview. For example, HR may not want to disclose its schedule to the applicants in order not to allow for the applicants to infer the number of applicants interviewed for the opening. Similarly, an applicant may not want to disclose its schedule to the HR department of its potential new employer as the applicant may not want them to learn certain aspects of his personal circumstances, e.g., regularly scheduled doctor’s appointments or a second job. Yet, state-of-the-art policy reconciliation mechanisms require that at least one of the parties discloses all the information in order to allow for the reconciliation process to work.

It is in this context that this paper introduces preferences and privacy into the policy reconciliation processes and as such provides for a major advancement in this area. In particular, with respect to privacy,

we propose new two-party protocols that guarantee that parties participating in the reconciliation process learn nothing about the other party’s policies other than the policy they will eventually agree on. In our initial example above, both the applicant and the HR department will learn nothing about each other’s schedules other than the date and time at which the interview of this particular applicant will take place (or the fact that there is no mutually agreeable time and date if such a match cannot be found). In addition, our work is the first to introduce mechanisms that consider the privacy requirements and still permit optimizing individual preferences that the parties may have. For example, HR may have preferences on interviewing applicants based on its expectation to hear back from other applicants to which they have already made an offer. If a higher ranked applicant accepts, this will eliminate the need to interview other applicants and thus result in a saving of time. In this paper, we introduce a fair mechanism for parties to reconcile their policies such that the preferences of all parties are optimized while none of the parties will have to disclose any of its preferences.

**Outline:** The remainder of the paper is organized as follows: In the next section, we discuss previous work in the area of policy reconciliation and privacy preserving set intersection. In Section 3, we provide details on the policy representation, define the new privacy objectives, and review existing privacy-preserving tools. The main contributions of this paper are in Section 4 where we present and discuss our new privacy-preserving policy reconciliation protocols which allow the optimization of the preferences of the individual parties. In Appendix A, we additionally outline some privacy-preserving policy reconciliation protocols without considering preferences.

## 2 Related Work

In general, a policy is a collection of rules that express which actions are permitted and disallowed in a system [22, 2, 29, 27]. They can take the form of specific access control rules [28], policy credentials [4, 3, 11, 10], or security policy language statements [8, 26]. In this paper, we address policies that govern collaboration and communication between a number of parties. In particular, these policies specify the algorithms, protocols, and any other parameters that must be agreed upon to ensure that the conditions and requirements of all parties are met.

**Policy Reconciliation** In [15] Gong and Qian analyze the complexity of secure interoperation between systems with heterogeneous access control structures. They prove that composing authorization policies is NP-complete. McDaniel and Prakash define the Ismene policy language [23] which permits the specification and reconciliation of group security requirements. Policy rules are expressed as conditionals which contain zero or more predicates that need to be satisfied for the policy to hold. In [24] McDaniel *et al.* specify an algorithm for efficient two-policy reconciliation and show that, in the worst-case, reconciliation of three or more policies is intractable.

Wang *et al.* demonstrate that it is possible to structure security policies in such a way that policy reconciliation becomes tractable [30]. Specifically, they use a graphical policy representation. A graphical policy is a series of policy operations represented in a directed acyclic graph with a single root. One reads policies starting from the root node. The authors present a recursive algorithm for generating the conjunction of graphical policies. The conjunction results in the reconciled policy. Their scheme also allows for specifying preferences. In that case, the authors rank the graphical policies in preferential order before running their conjunction algorithm.

Zao *et al.* propose the Security Policy System (SPS) which resolves IPsec security associations between domains of communication [32]. Reconciliation is achieved by intersecting sets of policy values. Dinsmore *et al.* [9] present the Dynamic Cryptographic Context Management project in which security policies are negotiated between dynamic groups of participants. Their protocol involves multiple rounds of negotiation between the participants, eventually producing a common policy that all of them agree upon.

Our work focuses on ensuring privacy during policy reconciliation and on taking preferences into account. Previous work on policy reconciliation focused on how to make policy reconciliation tractable with respect to performance under various conditions without taking privacy concerns of the participants into account. For

this purpose, McDaniel *et al.* [24] introduced a tree-based policy representation. In this paper, we represent a policy as a matrix and each policy rule as a row in the matrix. This is very simple and straightforward to use, especially when optimizing for privacy and not for performance.

**Privacy-Preserving Protocols** Freedman *et al.* [12] proposed the first protocol specifically designed for private intersection of datasets based on representing set elements as roots of polynomials. The proposed protocol is a two-party protocol, which, in its simplest version, is secure in the semi-honest model. This seminal work was extended by Kissner *et al.* [19, 20] to multiple parties and more set operations on multisets. In particular they propose privacy-preserving protocols for set intersection, set union, and element reduction of multisets. In order to reach security in the malicious model Kissner *et al.* propose the use of a zero-knowledge construction. Hohenberger *et al.* [17] constructed a more efficient two-party version of set intersection that is secure against malicious provers. Camenisch *et al.* in [5] suggest to make use of a trusted third party that certifies the sets of both parties in order to protect against either party being malicious and in order to ensure that sets cannot be changed on several subsequent interactions. All of the approaches mentioned so far are based on the oblivious polynomial evaluation construction introduced by Freedman *et al.* [12].

Another approach to private set intersection is based on oblivious pseudo-random function evaluation. This approach was first introduced by Hazay *et al.* [16] and subsequently further improved by Jarecki *et al.* [18]. The two-party protocol suggested in [16] is more efficient than the protocols based on oblivious polynomial evaluation. However, it is secure only in a relaxed version of the malicious model. Jarecki *et al.* [18] improved this protocol to provide security in the standard malicious model with the help of requiring the parties to commit on their input prior to the private set intersection. The computational effort of the suggested protocol is linear in the cardinality of the input sets.

Finally, and most recently, a private set intersection variant based on blind RSA signature schemes was proposed by Cristofaro *et al.* in [6]. The proposed construction was first introduced in [7] for privacy-preserving policy-based information transfer. The two-party private set intersection protocol proposed in [6] is linear in the maximum of the cardinalities of the two private input sets and thus as efficient as the oblivious pseudo-random function construction by Jarecki *et al.* [18]. Cristofaro *et al.* show that using pre-computation their protocol can outperform all previously suggested protocols. Unfortunately, in practice, pre-computation is not always usable. In particular, in the case of policy reconciliation, the private set of each party may change over time and depends on the context in which the parties interact.

The main contribution of our paper is that we build on the privacy-preserving set intersection results to construct two new and more complex privacy-preserving protocols for policy reconciliation with *preferences for two different notions of fair reconciliation*. While any of the aforementioned private intersection protocols can be used in our new construction, we detail our approach for the set intersection protocol introduced by Freedman *et al.* in [12]. As we will show later on, this particular set intersection protocol allows for a reduction of the communicational overhead in our construction. In the appendix, we additionally demonstrate how the existing results can be applied to the problem of security policy reconciliation in the absence of preferences in a straight-forward manner.

Kursawe *et al.* [21] address a similar problem of reconciling privacy policies in a privacy-preserving manner. Their solution is based on modeling the function to evaluate as boolean circuits and evaluating it on inputs encrypted with a threshold homomorphic cryptosystem. As opposed to this, we use privacy-preserving set intersections [12] for our reconciliation protocols. While Kursawe *et al.* recognize the objective of privacy-preserving preference-maximizing policy negotiation, their proposed solution is restricted to the problem of finding the intersection of two sets of policy rules. As opposed to this, we provide solutions for both, the privacy-preserving common policy as well as the preference-maximizing objective. To the best of our knowledge our protocols are the first solutions proposed for the preference-maximizing objective.

|        | Applicant |            |            |            |            | HR        |            |            |            |            |
|--------|-----------|------------|------------|------------|------------|-----------|------------|------------|------------|------------|
|        | <i>Mo</i> | <i>Tue</i> | <i>Wed</i> | <i>Thu</i> | <i>Fri</i> | <i>Mo</i> | <i>Tue</i> | <i>Wed</i> | <i>Thu</i> | <i>Fri</i> |
| Rule 1 | 1         | 0          | 0          | 0          | 0          | 0         | 0          | 1          | 0          | 0          |
| Rule 2 | 0         | 1          | 0          | 0          | 0          | 0         | 1          | 0          | 0          | 0          |
| Rule 3 | 0         | 0          | 1          | 0          | 0          | 1         | 0          | 0          | 0          | 0          |
| Rule 4 | 0         | 0          | 0          | 1          | 0          | 0         | 0          | 0          | 1          | 0          |
| Rule 5 | 0         | 0          | 0          | 0          | 1          | 0         | 0          | 0          | 0          | 1          |

Figure 1: Policy rules expressed as bit strings and ranked in order of preference.

### 3 Preliminaries

In this section, we summarize the definitions, notation, and objectives used throughout this paper. Furthermore, we briefly review existing privacy-preserving primitives that we use as tools in our new privacy-preserving policy reconciliation protocols introduced in Section 4.

#### 3.1 Policy Representation

To reconcile their policies, organizations must first agree on a common representation. This allows them to compare their policies and determine whether a common subset exists. Otherwise the problem of policy reconciliation becomes intractable [15, 24]. In this work, we represent a policy as a matrix. The rows represent individual policy rules and the columns are the attributes for each rule. Consequently, policies are represented as bit strings, which can be easily manipulated and operated on.

We illustrate our policy representation by continuing the example from Section 1. The first step is for the participants to agree on a set of attributes that will be used to define policy rules. In our example, we have settled for five attributes defining the day of the week on which the interview could take place, *Monday*, *Tuesday*, *Wednesday*, *Thursday*, and *Friday*. (Obviously, in reality this would be much more fine grained, i.e., one attribute could be *Monday: 8:00-9:00AM*.)

In some scenarios finding common policy rules will be the main objective of the participants. However, in some scenarios, the participants may not only want to express which combinations of attributes are acceptable for them but may also want to order these combinations according to their preferences. In these cases the objective of the participants is to find a common policy rule that maximizes their preferences.

Taking preferences into account, each participant represents its requirements by defining rules in order of preference. In our example, the applicant prefers to do the interview on Monday, but could do any other day with lower preference. In turn, HR prefers to do the interview on Wednesday but can accommodate any of the other days as well.

**Definition 3.1** A policy rule  $a_i = (a_{i1}, \dots, a_{in}) \in \{0, 1\}^n$  is a bit string of length  $n$  indicating whether a field  $a_{ij}$ ,  $j = 1, \dots, n$  is defined or not. A policy  $P_A$  is a set of rules  $a_1, \dots, a_k$  represented as a matrix  $P_A = (a_{ij})_{1 \leq i \leq k, 1 \leq j \leq n} \in \{0, 1\}^{k \times n}$ . Attribute  $\mathcal{A}_j$  is a string of characters that uniquely represents the  $j$ -th field of the policy rules.

In our example from Figure 1, *Monday*, *Tuesday*, *Wednesday*, *Thursday*, and *Friday* are the attributes defined in the policy. Rule  $a_1$  for the applicant is the bit string  $(1, 0, 0, 0, 0)$  specifying that his top priority is to do the interview on a *Monday*.

**Remark 3.1** Assuming parties  $A$  and  $B$  with policies  $P_A$  and  $P_B$ , attributes  $\mathcal{A}_1, \dots, \mathcal{A}_u$  and  $\mathcal{B}_1, \dots, \mathcal{B}_v$ , policy reconciliation for these parties requires  $u = v$  and  $\mathcal{A}_j = \mathcal{B}_j$  for  $j = 1, \dots, u$ . I.e., the policy rules of both parties have the same length and both parties associate the same attribute with each bit in the policy rule.

**Definition 3.2** A pre-order on a set  $X$  is a reflexive, transitive, binary relation  $R$  on  $X$ . A pre-order is total if all  $x_1, x_2 \in X$  are comparable, i.e.,  $x_1 R x_2$  or  $x_2 R x_1$ .

**Remark 3.2** Let  $X$  be a set and  $f$  be a real-valued function. Then  $f$  induces a total pre-order  $R$  on  $X$ , by  $xRy$  iff  $f(x_1) \leq f(x_2)$ .

**Remark 3.3** If  $f$  is a bijective function, then  $f$  induces a total order on  $X$ .

Throughout this paper we assume that a party  $A$  is able to totally order the policy rules in its policy  $P_A$  according to its preferences. We denote  $P_A = \{a_1, \dots, a_k\}$ , where  $a_1$  is the rule that is most preferred and  $a_k$  is the rule that is preferred least. That is the policy rules are listed in decreasing order  $a_k \leq_A a_{k-1} \leq_A \dots \leq_A a_1$ . In other words we assume that the policy rules in  $P_A$  are numbered such that  $f(a_i) := k - i + 1$  ( $i = 1, \dots, k$ ) is a bijective function that induces a total order  $\leq_A$  on  $P_A$ . In the sequel, we refer to this function  $f(a_i)$  as  $\text{rank}_A(a_i)$ , i.e., the rank which induces a so-called simple preference order  $\leq_A$  on the set of policy rules  $P_A$ .

**Definition 3.3** Let  $\leq_A$  be the simple preference order induced on the set of policy rules  $P_A$  (by  $\text{rank}_A$ ) and  $\leq_B$  be the simple preference order induced on the set of policy rules  $P_B$  (by  $\text{rank}_B$ ). A combined preference order  $\leq_{AB}$  is a total pre-order induced on the set of policy rules  $P_A \cap P_B$  by a the real-valued function  $f$ —in the sequel referred to as preference order composition scheme.

We focus on two specific preference order composition schemes:

**Definition 3.4** The sum of ranks composition scheme combines the simple preference orders  $\leq_A$  induced by  $\text{rank}_A$  on  $P_A$  and  $\leq_B$  induced by  $\text{rank}_B$  on  $P_B$  to the combined preference order  $\leq_{AB}$  induced by  $f$  on  $P_A \cap P_B$  defined as  $f(c) := \text{rank}_A(c) + \text{rank}_B(c)$  for  $c \in P_A \cap P_B$ . I.e., if  $x, y \in P_A \cap P_B$ , then  $x \leq_{AB} y \Leftrightarrow \text{rank}_A(x) + \text{rank}_B(x) \leq \text{rank}_A(y) + \text{rank}_B(y)$ .

**Definition 3.5** The maximized minimum of ranks composition scheme combines the simple preference orders  $\leq_A$  induced by  $\text{rank}_A$  on  $P_A$  and  $\leq_B$  induced by  $\text{rank}_B$  on  $P_B$  to the combined preference order  $\leq_{AB}$  induced by  $f$  on  $P_A \cap P_B$  defined as  $f(c) := \min\{\text{rank}_A(c), \text{rank}_B(c)\}$  for  $c \in P_A \cap P_B$ . I.e., if  $x, y \in P_A \cap P_B$ , then  $x \leq_{AB} y \Leftrightarrow \min\{\text{rank}_A(x), \text{rank}_B(x)\} \leq \min\{\text{rank}_A(y), \text{rank}_B(y)\}$ .

**Remark 3.4** The functions  $f(c) := \text{rank}_A(c) + \text{rank}_B(c)$  and  $f(c) := \min\{\text{rank}_A(c), \text{rank}_B(c)\}$  are not bijective. Consequently, the induced combined preference orders are total pre-orders but not total orders.

## 3.2 Protocols for Privacy-Preserving Policy Reconciliation

Drawing on the previous definitions, we now introduce the protocols for policy reconciliation and define when we call these protocols privacy-preserving.

Policy reconciliation in general has the objective of two parties determining those policy rules they have in common. In the course of conventional reconciliation protocols, at least one of the two parties learns more of the other party's policies than just what the two parties have in common. As discussed previously, the latter constitutes a major problem in situations where privacy is of primary concern. The objective of privacy-preserving policy reconciliation is not to reveal any more information about a party's policy rules to the other party than the common policy rules.

Let us now assume that two parties have total preference orders on their policies and have agreed upon a preference order composition scheme. Then preference-maximizing policy reconciliation for a composition scheme has the objective of determining a policy rule that maximizes the combined preference order. Again, this problem could be solved by one party providing its policy as well as its total preference order to the other party. However, in this case, the other party could chose a policy rule that only maximizes its own preferences. The objective of privacy-preserving common policy reconciliation is to find a policy rule that maximizes the combined preference order without revealing any information about a party's policy rules and preferences to the other party than the maximizing policy rule.

In both cases, with and without considering preferences, a trusted third party could be used to solve the privacy problem. However, in practice such a trusted third party barely ever exists. Thus, the goal in secure

multi-party computation in general, and here in particular, is to define protocols without a trusted third party that provide the same view to each of the parties as if a trusted third party was present.

As we will see in the course of this paper, it is comparatively easy to implement privacy-preserving policy reconciliation schemes that do not take preferences into account. We illustrate this with the help of the private set intersection techniques introduced in [12]. Kursawe *et al.* reach the same goal with the help of a boolean circuit and using efficient two-party computation techniques based on threshold homomorphic cryptosystems [21]. However, implementing privacy-preserving preference-maximizing policy reconciliation seems not quite that straightforward.<sup>1</sup> Here, we introduce the slightly weaker notion of a privacy-preserving *multi-round* preference-maximizing policy reconciliation scheme. In addition to a preference-maximizing policy rule, such a scheme reveals the rank the other party has assigned to the resulting policy rule. Note that the additional leakage of the rank of the result in the other parties preference order seems acceptable in many situations as at the time of leakage the agreement has already been reached such that the other party cannot use the additional information to influence the result anymore.

Keeping these considerations in mind, we define three different protocols for policy reconciliation as follows:

**Protocol 1** A privacy-preserving common policy scheme (PCP) is a two-party protocol between parties  $A$  and  $B$ . Their respective policies  $P_A$  and  $P_B$  are drawn from the same domain of policy rules (see Remark 3.1). Upon completion of the protocol,  $A$  and  $B$  learn nothing else about each other’s private policies but which policy rules they have in common. I.e., if a PCP takes  $P_A$  and  $P_B$  as input, then  $A$  and  $B$  learn  $P_A \cap P_B$ .

In our example, this means that the parties determine all dates and times that would work for an interview for both HR and the applicant.

**Protocol 2** A privacy-preserving common policy cardinality scheme ( $PC^2$ ) is a two-party protocol between parties  $A$  and  $B$ . Their respective  $P_A$  and  $P_B$  are drawn from the same domain of policy rules (see Remark 3.1). Upon completion of the protocol,  $A$  and  $B$  learn nothing else about each other’s private policies but the number of policy rules they have in common. I.e., if a  $PC^2$  takes  $P_A$  and  $P_B$  as input, then  $A$  and  $B$  learn  $|P_A \cap P_B|$ .

A  $PC^2$  thus allows two parties  $A$  and  $B$  to determine how many policy rules they have in common *without* revealing these policy rules to each other. A  $PC^2$  protocol could, for example, be used by  $A$  and  $B$  to first determine the number of policies they have in common *before* reconciling their policies through a PCP protocol.

In our previous example, this would translate into the parties determining how many dates and times would work for both of them.

**Protocol 3** A privacy-preserving preference-maximizing multi-round policy reconciliation scheme for a preference order composition scheme  $\mathcal{C}$  ( $3PR^{\mathcal{C}}$ ) is a multi-round two-party protocol between parties  $A$  and  $B$ . Their respective policies  $P_A$  and  $P_B$  are drawn from the same domain of policy rules (see Remark 3.1). Upon completion of the protocol,  $A$  and  $B$  learn nothing about each other’s policies but one common policy rule  $max$  that maximizes the combined preference order  $\leq_{AB}$  of  $\leq_A$  and  $\leq_B$  under  $\mathcal{C}$  as well as in which round of the protocol  $max$  was determined. I.e., if  $3PR^{\mathcal{C}}$  takes  $P_A$ ,  $P_B$ ,  $\leq_A$ , and  $\leq_B$  as input, then  $A$  and  $B$  learn  $\max_{x \in P_A \cap P_B; \leq_{AB}} \{x\}$ .

Note that in a  $3PR^{\mathcal{C}}$  scheme, the two parties should not learn anything about any other policy rules of the respective other party and nothing about the other party’s preferences other than what can be deduced from the run or the output of the protocol. Furthermore, the scheme must enforce the output to maximize the combined preference order for the composition scheme in question. This guarantees that the two parties can reconcile their preferences in a fair way, i.e., according to an agreed upon preference composition scheme. Consequently, none of the parties has the power to set its preferences over the other party’s preferences. The

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<sup>1</sup>Note that in [21] the problem of taking preferences into account is recognized but no solution for this case is proposed.

different preference composition schemes can hereby be used to express different notions of fairness in the reconciliation process.

In our example, the use of a  $3PR^C$  scheme ensures that the interview will take place at a time and date that optimizes, i.e., best meets the preferences of both the HR department and the applicant.

### 3.3 Adversary Model and Privacy Requirements

We now describe the adversary models used in the remainder of this paper. Furthermore, we define the security and privacy requirements for PCP,  $PC^2$ , and  $3PR^C$  protocols.

**Semi-Honest Model.** In the semi-honest model, all parties act honestly, but may be curious. That is, all parties act according to their prescribed actions in the protocol.<sup>2</sup> This includes that all parties use their correct private inputs, i.e. they do not lie about their policy rules (and preference orders). Yet, the participants may try to learn as much as possible in the process of the protocol and may perform any additional arbitrary polynomial-time computations apart from the prescribed protocol actions [14]. In particular, any party may store and use any intermediate result of the protocol. Intuitively, a two-party protocol is said to be *privacy-preserving* in the *semi-honest model*, if no party gains information about the other party’s private input other than what can be deduced from the desired output of the protocol and the party’s own private input. In other words, for each party there exists a simulator that produces an output distribution which is computationally indistinguishable from the other party’s view executing the real protocol [13].<sup>3</sup> Note that while for a PCP and a  $PC^2$  scheme the private inputs are the policies  $P_A$  and  $P_B$  only, the private input in the  $3PR^C$  additionally includes the preference orders of  $A$  and  $B$ .

**Malicious Model.** In the malicious model, each party may behave arbitrarily. As detailed in [13], one cannot prevent a party from (1) refusing to participate in the protocol; (2) substituting its private input at the beginning of the protocol; or (3) aborting the protocol before completion. Intuitively, a two-party protocol is said to be *privacy-preserving* in the *malicious model*, if apart from the unavoidable deviations no other deviation of one malicious party leads to information leakage about the other (honest) party’s private input, other than what can be deduced from the output of the protocol.<sup>4</sup> Similarly, we say that a  $3PR^C$  scheme is *preference-maximizing in the malicious model*, if apart from the unavoidable deviations no other deviation of one malicious party can lead to an output the malicious party prefers over the one that maximizes the combined preference order.

## 4 Privacy-Preserving Reconciliation with Preferences

The main contribution of this paper is the introduction of a new  $3PR^C$  scheme for the *sum of ranks* composition scheme and a new  $3PR^C$  scheme for the *maximized minimum of ranks* composition scheme. These protocols consist of several rounds. Each round uses a privacy-preserving set intersection protocol (PPSI) as building block. In each round, the two parties commit to those policy rules that lead to the same rank in their combined preference order. As soon as a match is found, the protocol terminates. The order in which the parties commit to their policy rules thus guarantees the optimization of the combined preference order.

We recall that the objective of the sum of ranks composition scheme is for the two parties  $A$  and  $B$  to determine one common policy rule  $max$  in a privacy-preserving manner that maximizes the combined preference order on  $P_A \cap P_B$  defined by  $x \leq_{AB} y \Leftrightarrow \text{rank}_A(x) + \text{rank}_B(x) \leq \text{rank}_A(y) + \text{rank}_B(y)$ . Using a PPSI as a building block, the protocol can generically be implemented as illustrated in Figure 2 on an

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<sup>2</sup>Note that the parties may keep a record of all their intermediate computations.

<sup>3</sup>As generally is the case with secure multi-party computation, we assume the channel over which messages are exchanged to be an authenticated channel.

<sup>4</sup>As a consequence of the three above mentioned unpreventable actions a malicious party can take, a PCP scheme, for example, without any further external protection mechanism cannot prevent a malicious party from extracting the other parties policy: the malicious party simply substitutes its own input with a policy containing all possible policy rules and consequently learns the honest parties policy as output of the PCP scheme. Similarly, a  $PC^2$  scheme cannot protect the cardinality of an honest party’s private input policy against a malicious party.

example where both parties  $A$  and  $B$  have four policies each, sorted in decreasing order of their individual preferences. In order to determine a policy that maximizes the preferences of both parties  $A$  and  $B$ , the

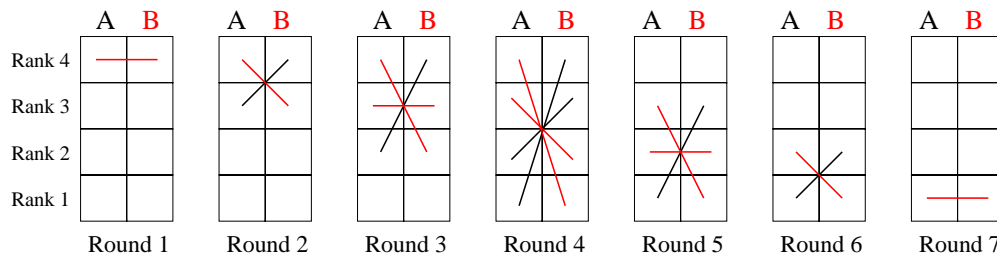


Figure 2: Sum-of-ranks: order in which  $A$  and  $B$  compare policy rules in case of 4 rules

protocol progresses in a number of rounds. Each round consists of a number of PPSIs (each indicated by a line in Figure 2). For example, in Round 1, party  $A$  carries out one PPSI to determine whether there is a match between its top policy and that of party  $B$ . If so, the protocol terminates as it found a common policy rule that maximizes the combined preference order. Otherwise, the protocol moves on to the next round. All PPSIs carried out in one round result in the same sum of ranks. In particular, the sum of ranks in Round 1 is eight (in the example, or  $2k$  in case of both parties holding  $k$  policy rules). In each round, the sum decreases by one, i.e., Round  $i$  corresponds to a sum of ranks of  $2k - i + 1$  thus guaranteeing that the protocol will in fact always maximize the sum of ranks. In the worst case, the protocol will carry out  $2k - 1$  rounds of PPSIs.

For the maximized minimum of ranks composition scheme, the order of executing PPSIs to obtain the  $3PR^C$  is slightly different as the two parties  $A$  and  $B$  strive to determine a common policy rule  $max$  in a privacy-preserving manner such that it maximizes the combined preference order on  $P_A \cap P_B$  defined by  $x \leq_{AB} y \Leftrightarrow \min(\text{rank}_A(x), \text{rank}_B(x)) \leq \min(\text{rank}_A(y), \text{rank}_B(y))$ . Figure 3 illustrates the generic implementation of the multi-round protocol using some PPSI as a building block. Unlike before, the focus in each

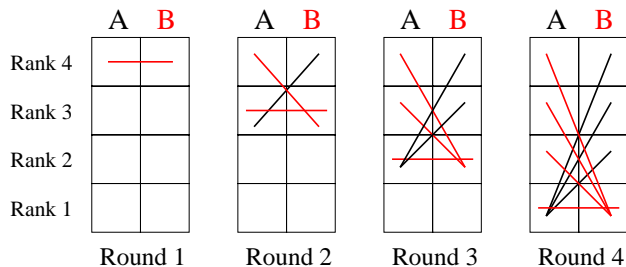


Figure 3: Maximized-minimum-of-ranks: order in which  $A$  and  $B$  compare policy rules in case of 4 rules

round is now on the policy rule with the smaller preference as the goal is to maximize that. Consequently, the respective  $3PR^C$  requires fewer rounds and executes the PPSI in a different fashion. In fact, the number of protocol rounds never exceeds the number of policy rules the parties hold. As before, both parties  $A$  and  $B$  each carry out a certain number of PPSIs in each round of the  $3PR^C$ . For example, in Round 3 in Figure 3, party  $B$  will carry out up to two PPSIs, that is, the PPSI between its top policy and party  $A$ 's third policy and possibly a PPSI with its second policy and  $A$ 's third policy. Obviously, the minimum preference of all policies considered in this round is two. If no intersection is found, the protocol will move on to the next round which is characterized by the fact that the minimum of the preferences of the policy rules considered is decreased by one. This procedure ensures that the protocol will determine a common policy rule that maximizes the combined preference order.



Assuming that the PPSI is privacy-preserving in the semi-honest model automatically implies that the new  $3\text{PR}^C$  protocols are privacy-preserving in the semi-honest model—irrespective of the PPSI and combined preference order used. This is due to the fact that in the semi-honest model both parties will follow the protocol. Consequently, if the PPSI used is privacy-preserving in the semi-honest model, then a party will not learn anything about any policies unless a common policy is determined through the respective PPSI. Obviously, an analogous statement for the malicious model does not hold true as malicious behavior in the  $3\text{PR}^C$  protocols may come into play both within a specific round (including multiple PPSIs) as well as in between different rounds.

While any PPSI may be used as building block for our  $3\text{PR}^C$  protocols, in the following we will focus our attention on the PPSI introduced by Freedman *et al.* in [12]. In particular, we will detail and optimize our protocols using the PPSI constructions by Freedman *et al.* which is based on private polynomial evaluation. While any other PPSI can be employed in a generic straight-forward manner as explained above, we expect that the use of some specific PPSIs (see Section 2) can lead to protocols that are more efficient than others.

#### 4.1 Privacy-Preserving Tools by Freedman *et al.*

**Privacy-Preserving Set Intersection** The PPSI by Freedman *et al.* [12] is a two-party protocol between a chooser  $C$  and a sender  $S$ . At the beginning of the protocol, both parties have private data sets ( $Z_C$  and  $Z_S$ ) drawn from some common domain. At the conclusion of the protocol, the chooser learns the intersection  $Z_C \cap Z_S$ , but nothing about any other data in  $Z_S$ . The sender learns nothing about any data in  $Z_C$ . That is, Freedman *et al.* prove that their protocol is privacy-preserving in the semi-honest model. For data sets of size  $O(k)$ , the protocol results in a communication overhead of  $O(k)$  and computational overhead of  $O(k \ln \ln k)$ .

The Freedman protocol is based on a semantically secure homomorphic encryption scheme: If  $E$  is a public encryption function of a homomorphic encryption scheme, then, given the ciphertexts  $c_1 = E(m_1)$  and  $c_2 = E(m_2)$ , the ciphertext  $c^* = E(m_1 + m_2)$  can be computed efficiently without knowledge of the private key. Similarly, given  $c = E(m)$  and some  $r$  from the group of plaintexts, then  $c^* = E(rm)$  can be computed efficiently without knowledge of the private key. A public encryption function  $E$  is semantically secure if it is computationally infeasible for an attacker to derive significant information about a plaintext given only its ciphertext and the public encryption key. An example of a semantically secure homomorphic encryption scheme is Paillier’s cryptosystem [25]. The homomorphic property of an encryption function  $E$  implies that anyone in possession of the encrypted coefficients of a polynomial  $f(X)$  can compute a valid encryption of  $f(y)$  for any  $y$  from the group of plaintexts without the knowledge of the private key or the coefficients. In particular, for any known plaintexts  $y_1, y_2$  and any known constant  $r$ , a valid encryption  $E(rf(y_1) + y_2)$  can be computed without the knowledge of the private key or the coefficients of  $f(X)$ . The property of the encryption scheme to be semantically secure is crucial for the protocols to be privacy-preserving. That is, if the encryption scheme was not semantically secure, then it would be computationally feasible to violate privacy, i.e., determine the plaintexts—which, in the context of Freedman’s work, are the elements of the private data sets of the parties—without knowledge of the private key. This would be possible by simply encrypting all candidate plaintexts using the party’s respective public key and checking the results against the publicly known ciphertexts.

**Private Cardinality Matching** In [12], Freedman *et al.* also present a protocol to compute the cardinality of the intersection of two data sets that is privacy-preserving in the semi-honest model. In fact, this protocol is a variant of the set intersection protocol. The chooser learns nothing about the data sets of the server, except for the cardinality of the intersection of the chooser’s and the server’s data sets.<sup>5</sup> For data sets of size  $O(k)$ , the protocols results in a communication overhead of  $O(k)$  and computational overhead of  $O(k \ln \ln k)$ .

As illustrated in Appendix A, building on the work of Freedman *et al.* it is possible to build protocols for  $\text{PC}^2$  and PCP in a straight-forward manner. However, implementing a  $3\text{PR}^C$  schemes requires some

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<sup>5</sup>It is important to note that in the Freedman *et al.* schemes the server learns the size of  $Z_C$ . Other schemes avoid this leakage at the cost of efficiency (*e.g.*, [1] in the case of private cardinality matching and [31] for private set intersection).

sophisticated protocol design.

In the following, we assume that prior to the execution of any of the protocols introduced in this section the two parties  $A$  and  $B$  agree upon a semantically secure homomorphic encryption scheme. The parties choose their public and private key pairs for the encryption scheme and exchange their public keys. We denote the public encryption functions of  $A$  and  $B$  with  $E_A$  and  $E_B$  and their private decryption functions with  $D_A$  and  $D_B$ . Parties  $A$  and  $B$  have policies  $P_A = (a_1, \dots, a_k)$  and  $P_B = (b_1, \dots, b_l)$  consisting of policy rules drawn from the same domain  $\{0, 1\}^n$  (Remark 3.1). In addition, in both  $3\text{PR}^C$  protocols we assume that  $P_A$  and  $P_B$  have the same number of policy rules, that is  $k = l$ . Furthermore, the policy rules in  $P_A$  and  $P_B$  are enumerated in decreasing order of  $\leq_A$  and  $\leq_B$  such that  $a_1$  is  $A$ 's favorite policy rule and  $a_k$  is  $A$ 's least favorite policy rule.

## 4.2 $3\text{PR}^C$ Protocol for the Sum of Ranks Composition Scheme

In this section we detail the  $3\text{PR}^C$  protocol for the sum of ranks composition scheme. The basic idea of the multi-round protocol using any private set intersection protocol was illustrated in Figure 2. In the following, we formally describe the protocol messages for the case that the private set intersection protocol introduced by Freedman *et al.* is used.

**$3\text{PR}^C$  Protocol:** For each policy rule  $a_i \in P_A$  ( $i = 1, \dots, k$ ) we define  $f_A^{(i)} := (X - a_i)$ . The polynomial with coefficients encrypted under  $E_A$  is denoted by  $E_A^{(i)}$ . Similarly, for each  $b_i \in P_B$  ( $i = 1, \dots, k$ ) we define  $f_B^{(i)}$  and  $E_B^{(i)}$ .

COMMITMENT PHASE:

ROUND 0:  $B$  sends  $E_B^{(1)}$  to  $A$ .

ROUND 1:  $A$  chooses a random  $r_{A,1}^{(1)}$ , computes  $c_{A,1}^{(1)} = E_B\left(r_{A,1}^{(1)} \cdot f_B^{(1)}(a_1) + a_1\right)$ , and sends it together with  $E_A^{(1)}$  to  $B$ .  $B$  decrypts  $c_{A,1}^{(1)}$  under  $D_B$  and compares the result to  $b_1$ . If  $b_1 = D_B(c_{A,1}^{(1)})$ , then  $b_1 = a_1$ , that is,  $B$  has found  $\text{max} := b_1 = a_1$  and continues with the *Match Confirmation Phase*. Otherwise,  $B$  sends  $E_B^{(2)}$  to  $A$  and  $A$  continues with *Round 2* of the *Commitment Phase*.

ROUND  $2 \leq i \leq k$ : For  $j = 1, \dots, \lceil i/2 \rceil$ ,  $A$  chooses random  $r_{A,j}^{(i-j+1)}$  and computes the ciphertexts

$$c_{A,j}^{(i-j+1)} := E_B\left(r_{A,j}^{(i-j+1)} \cdot f_B^{(i-j+1)}(a_j) + a_j\right)$$

and sends them as well as  $E_A^{(i)}$  to  $B$ . For  $j = 1, \dots, \lceil i/2 \rceil$   $B$  decrypts  $c_{A,j}^{(i-j+1)}$  with  $D_B$  and checks whether the decrypted value equals  $b_{i-j+1}$ . If for some  $j =: m$  the ciphertext  $c_{A,m}^{(i-m+1)}$  decrypts to  $b_{i-m+1}$ ,  $B$  has found  $\text{max} := b_{i-m+1} = a_m$  and continues with the *Match Confirmation Phase*. Otherwise, for  $1 \leq j \leq \lfloor i/2 \rfloor$ ,  $B$  chooses random  $r_{B,j}^{(i-j+1)}$  and computes the ciphertexts

$$c_{B,j}^{(i-j+1)} := E_A\left(r_{B,j}^{(i-j+1)} \cdot f_A^{(i-j+1)}(b_j) + b_j\right)$$

and sends them to  $A$ . For  $2 \leq i < k$   $B$  additionally sends  $E_B^{(i+1)}$  to  $A$ . For  $1 \leq j \leq \lfloor i/2 \rfloor$ ,  $A$  decrypts  $c_{B,j}^{(i-j+1)}$  with  $D_A$  and checks whether the decrypted value equals  $a_{i-j+1}$ . If  $c_{B,m}^{(i-m+1)}$  decrypts to  $a_{i-m+1}$ ,  $A$  has found  $\text{max} := a_{i-m+1} = b_m$  and continues with the *Match Confirmation Phase*. Otherwise,  $A$  continues with *Round  $i+1$*  of the *Commitment Phase*.

ROUND  $k < i < 2k - 1$ : For  $j = 1, \dots, k - \lfloor i/2 \rfloor$ ,  $A$  chooses random  $r_{A,i-k+j}^{(k-j+1)}$  and computes the ciphertexts

$$c_{A,i-k+j}^{(k-j+1)} := E_B\left(r_{A,i-k+j}^{(k-j+1)} \cdot f_B^{(k-j+1)}(a_{i-k+j}) + a_{i-k+j}\right)$$

and sends them to  $B$ . For  $j = 1, \dots, k - \lfloor i/2 \rfloor$   $B$  decrypts  $c_{A,i-k+j}^{(k-j+1)}$  with  $D_B$  and checks whether the decrypted value equals  $b_{k-j+1}$ . If, for some  $j =: m$  the ciphertext  $c_{A,i-k+m}^{(k-m+1)}$  decrypts to  $b_{k-m+1}$ ,  $B$  has found  $max := b_{k-m+1} = a_{i-k+m}$  and continues with the *Match Confirmation Phase*. Otherwise, for  $1 \leq j \leq k - \lfloor i/2 \rfloor$ ,  $B$  chooses random  $r_{B,i-k+j}^{(k-j+1)}$  and computes the ciphertexts

$$c_{B,i-k+j}^{(k-j+1)} := E_A \left( r_{B,i-k+j}^{(k-j+1)} \cdot f_A^{(k-j+1)}(b_{i-k+j}) + b_{i-k+j} \right)$$

and sends them to  $A$ . For  $1 \leq j \leq k - \lfloor i/2 \rfloor$ ,  $A$  decrypts  $c_{B,i-k+j}^{(k-j+1)}$  with  $D_A$  and checks whether the decrypted value equals  $a_{k-j+1}$ . If  $c_{B,i-k+m}^{(k-m+1)}$  decrypts to  $a_{k-m+1}$ ,  $A$  has found  $max := a_{k-m+1} = b_{i-k+m}$  and continues with the *Match Confirmation Phase*. Otherwise,  $A$  continues with *Round  $i + 1$*  of the *Commitment Phase*.

ROUND  $i = 2k - 1$ :  $A$  chooses random  $r_{A,k}^{(k)}$  and computes the ciphertext

$$c_{A,k}^{(k)} := E_B \left( r_{A,k}^{(k)} \cdot f_B^{(k)}(a_k) + a_k \right)$$

and sends it to  $B$ .  $B$  decrypts  $c_{A,k}^{(k)}$  with  $D_B$  and checks whether the decrypted value equals  $b_k$ . If  $c_{A,k}^{(k)}$  decrypts to  $b_k$ ,  $B$  has found  $max := b_k = a_k$  and continues with the *Match Confirmation Phase*. Otherwise,  $B$  sends a message to  $A$  indicating that no match was found and aborts the protocol.

**MATCH CONFIRMATION PHASE:** If  $B$  found the match  $b_1 = a_1 = max$  in the first round of the *Commitment Phase*, then  $B$  computes  $c_{B,1}^{(1)}$  and sends it to  $A$ .  $A$  decrypts the received ciphertext with  $D_A$  to  $a_1$ . Thus  $A$  and  $B$  both know that  $max = a_1 = b_1$ .

If  $B$  found  $max = b_{i-m+1} = a_m$  in *Round  $2 \leq i \leq k$*  of the *Commitment Phase*, then  $B$  computes  $c_{B,i-m+1}^{(m)}$  and sends it to  $A$ .  $A$  decrypts the received value under  $D_A$  to  $a_m$ . Thus,  $A$  and  $B$  both know that  $a_m = b_{i-m+1} = max$ .

If  $A$  found  $max = a_{i-m+1} = b_m$  in *Round  $2 \leq i \leq k$*  of the *Commitment Phase*,  $A$  computes  $c_{A,i-m+1}^{(m)}$  and sends it to  $B$ .  $B$  decrypts  $c_{A,i-m+1}^{(m)}$  with  $D_B$  and checks that  $D_B(c_{A,i-m+1}^{(m)})$  decrypts to a value  $b_m \in \{b_1, \dots, b_{\lfloor i/2 \rfloor}\}$ . Thus, both parties  $A$  and  $B$  know that  $a_{i-m+1} = b_m = max$ .

If  $B$  found  $max = b_{k-m+1} = a_{i-k+m}$  in *Round  $k < i < 2k - 1$*  of the *Commitment Phase*, then  $B$  computes  $c_{B,k-m+1}^{(i-k+m)}$  and sends it to  $A$ .  $A$  decrypts the received value under  $D_A$  to  $a_{i-k+m}$ . Thus,  $A$  and  $B$  both know that  $a_{i-k+m} = b_{k-m+1} = max$ .

If  $A$  found  $max = a_{k-m+1} = b_{i-k+m}$  in *Round  $k < i < 2k - 1$*  of the *Commitment Phase*,  $A$  computes  $c_{A,k-m+1}^{(i-k+m)}$  and sends it to  $B$ .  $B$  decrypts  $c_{A,k-m+1}^{(i-k+m)}$  with  $D_B$  and checks that  $D_B(c_{A,k-m+1}^{(i-k+m)})$  decrypts to a value  $b_{i-k+m} \in \{b_{i-k+1}, \dots, b_{\lfloor i/2 \rfloor}\}$ . Thus, both parties  $A$  and  $B$  know that  $a_{k-m+1} = b_{i-k+m} = max$ .

If  $B$  found  $max = b_k = a_k$  in *Round  $i = 2k - 1$*  of the *Commitment Phase*, then  $B$  computes  $c_{B,k}^{(k)}$  and sends it to  $A$ .  $A$  decrypts the received value with  $D_A$  to  $a_k$ . Thus  $A$  and  $B$  both know that  $a_k = b_k = max$ .

**Remark 4.1** Unlike in *PCP* and *PC<sup>2</sup>* we have assumed for the *3PR<sup>C</sup>* protocol for the sum of ranks composition scheme that  $A$  and  $B$  have the same number  $k$  of policy rules and each rank is assigned to exactly one policy rule. However, this does not limit  $A$  and  $B$  to define less than  $k$  valid policy rules, as  $A$  and  $B$  can simply augment their valid policies to contain  $k$  rules by appending special rules agreed upon to be dummy rules. E.g., policy rules containing only zeros for every attribute could be interpreted as such dummy rules. A matching zero policy as result of *3PR<sup>C</sup>* then indicates that  $A$  and  $B$  do not share a single valid policy rule.

Intuitively, the protocol works as follows: The homomorphic encryption function allows a party  $A$  to encrypt a polynomial corresponding to one of its own policy rules in a way that the encrypted polynomial does not reveal any information to party  $B$ . In addition, if  $B$  evaluates the encrypted polynomial on one of its own policy rules, then its policy rule is blinded and encrypted. From this blinded ciphertext  $A$  learns nothing

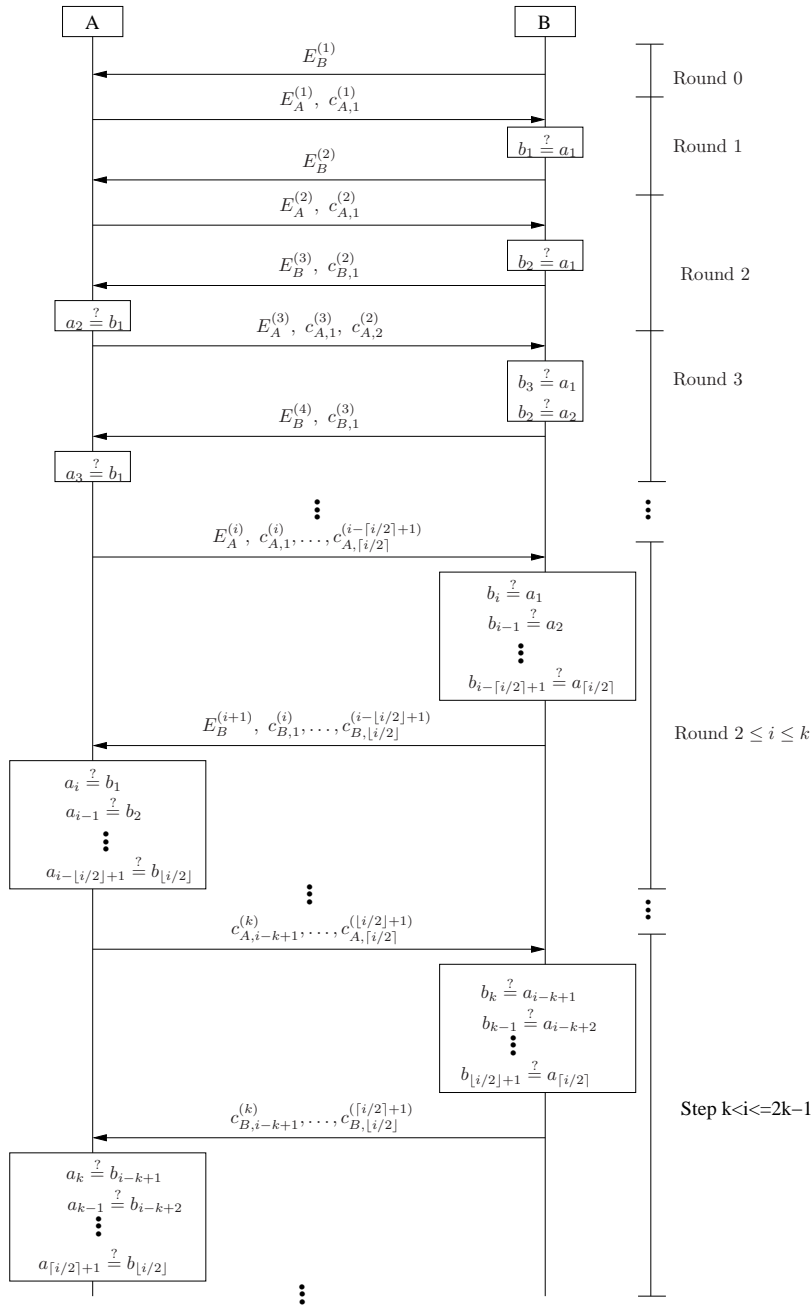


Figure 4: Commitment Phase of the sum of ranks  $3PR^C$ . For example, in Round  $2 \leq i \leq k$ ,  $A$  for  $j = 1, \dots, \lceil i/2 \rceil$  compares  $a_{i-j+1}$  with  $b_j$  and  $B$  for  $j = 1, \dots, \lceil i/2 \rceil$  compares  $b_{i-j+1}$  with  $a_j$  without obtaining knowledge of these values (unless they are equal), that is, in a privacy-preserving manner. Note that in each Round  $1 \leq i \leq 2k - 1$  all policy rules are compared that result in the same sum of ranks  $i + 1$ .

about  $B$ 's policy rule, unless the policy rule  $A$  used for the creation of the polynomial and the policy rule on which  $B$  evaluated the polynomial coincide. This is because, if and only if the policy rules coincide, the blinded ciphertext decrypts to  $A$ 's policy rule.  $A$  and  $B$  can thus determine a common policy rule

without revealing rules to each other that they do not have in common. Our protocols make use of this basic procedure in multiple rounds.

In each round, parties  $A$  and  $B$  exchange polynomials and blinded ciphertexts corresponding to previously received polynomials. They each decrypt the blinded ciphertext and compare the result to the policy rules corresponding to the previously sent polynomials. The order in which the information is exchanged guarantees that the protocol terminates when a common policy rule is found that maximizes the sum of ranks of the common policies of  $A$  and  $B$ . For example, in the first round of the protocol,  $A$  can check whether the two most preferred policy rules of both parties are the same ( $a_1 \stackrel{?}{=} b_1$ ). If this is not the case,  $A$  does not learn anything about  $b_1$ . As a general rule, in Round  $i$  of the protocol,  $A$  and  $B$  compare all policy rules that result in the same sum of ranks in the combined preference order of  $A$  and  $B$ .

### Discussion:

For  $P_A \cap P_B \neq \emptyset$ , the *Commitment Phase* of the 3PR<sup>C</sup> protocol always terminates with one of the parties finding a match. This is due to the fact that for each pair  $(l, s)$   $1 \leq l, s \leq k$ ,  $a_l$  is compared with  $b_s$  in Round  $l + s - 1$ . To be precise, for  $l < s$ ,  $a_l$  is compared with  $b_s$  by  $A$  and for  $s \leq l$ ,  $b_s$  is compared with  $a_l$  by  $B$  in Round  $l + s - 1$ . Let  $max = a_l = b_s$  be a match found in Round  $l + s - 1$ . Then no match was found in any previous round of the *Commitment Phase*. We claim that then  $max$  maximizes the sum of the ranks of all elements in the intersection  $P_A \cap P_B$ . If this was not the case, then there would be a pair  $(a_r, b_v)$  with  $a_r = b_v \in P_A \cap P_B$  and  $r + v < s + l$ . As a consequence,  $a_r$  would have been compared to  $b_v$  already in Round  $r + v - 1$  of the *Commitment Phase*. This obviously contradicts the assumption.

The 3PR<sup>C</sup> scheme uses one round of the private intersection protocol of Freedman *et al.* in each round. If  $A$  ( $B$ ) would learn anything besides preference-maximizing policy rules at the end of the protocol,  $A$  ( $B$ ) would have had to learn this in one of the rounds. As each round can be interpreted as running the Freedman protocol on a subset of policy rules, each round is privacy-preserving in the semi-honest model with respect to this subset. As a consequence  $A$  ( $B$ ) learns nothing in any round unless a match is found. If a match is found by  $A$  ( $B$ ),  $A$  ( $B$ ) may learn more than one preference maximizing policy rule.<sup>6</sup> This is due to the fact that more than one pair of policy rules is evaluated by  $A$  ( $B$ ) in each round. Upon termination of the protocol in Round  $i$  both parties also learn about the correlation of their preferences of  $max$  to  $i$ . In addition,  $A$  ( $B$ ) learns the ranks of all preference maximizing policy rules of  $B$  ( $A$ ) and  $B$  learns the rank of the preference maximizing policy rule  $A$  commits to. This leakage could partly be prevented by adding subrounds to the *Commitment Phase*, such that each party commits to only one policy rule in each subround of each round in the *Commitment Phase*. However, this would result in a higher communicational overhead. We do not see any possibility to prevent  $A$  from learning  $rank_B(max)$  and  $B$  from learning  $rank_A(max)$ . Obviously, the protocol with the additional subrounds is privacy-preserving in the semi-honest model.<sup>7</sup> It is important to note that while deviations from the protocol always imply privacy violations, a malicious party will not necessarily profit from deviations in terms of maximizing its preferences. This is due to the fact that the combined preference order depends on the preference order of the honest party. In order to profit from deviations a malicious party would need to know the honest party's preference order at the time of initiation of reconciliation. As a consequence, in situations where  $A$  and  $B$  reconcile their policies only once and have to follow the result later on, deviations from the protocol are unattractive for either party.

We evaluate the worst case performance of the protocol by counting (1) the number of times  $A$  and  $B$  have to compare a received decrypted policy rule of the other party with one of their policy rules, (2) the number of decryptions  $A$  and  $B$  have to perform, (3) the number of encryptions of coefficients of polynomials, (4) the number of ciphertext  $A$  and  $B$  have to compute to commit to their policy rules, (5) the number of messages exchanged between  $A$  and  $B$ , as well as (6) the overall size of the payload of all messages exchanged, counted in the number of ciphertexts included in all messages.

We count the above numbers for three different relations between the overall number of  $n$  of policy rules and the number  $k$  of policy rules  $A$  and  $B$  choose from the overall set of policy rules.

<sup>6</sup>However,  $A$  ( $B$ ) does not learn anything about policy rules of  $B$  ( $A$ ) that do not maximize the combined preference order.

<sup>7</sup>This is due to the fact that up to the point where a match is found,  $A$  ( $B$ ) receives only ciphertexts from  $B$  ( $A$ ) that decrypt to an arbitrary value. As soon as a match is found by one of the honest party's, this party acknowledges the match to the other party and the protocol terminates.

In the first case, we assume that  $n$  equals  $k$ . In this case,  $A$  and  $B$  share all policy rules and differ only in their preferences. The worst case occurs if the policy rules of  $A$  and  $B$  are in exactly the opposite order. In this case, the match is found in Round  $k$  of the protocol. Table 1 shows the results.

| $k = n$                          |   |
|----------------------------------|---|
| # Comparisons                    | $\frac{k(k-1)}{2} + 2$                                      |
| # Encryption of coefficients     | $4k - 3$  |
| # Decryptions                    | $\frac{k(k-1)}{2} + 2$                                      |
| # Commitment of rules            | $\frac{k^2+2}{2}$ ( $k$ even); $\frac{k^2+3}{2}$ ( $k$ odd) |
| # Messages                       | $2k + 1$  |
| Size of payload in # ciphertexts | $k^2/2 + 4k - 2$  |

Table 1: Sum-of-ranks: Worst case performance for  $n = k$ , where  $n$  is the overall number of policy rules  $A$  and  $B$  choose from and  $k$  is the number of policy rules  $A$  and  $B$  choose.

For example, the number of comparisons is counted as follows: In the worst case, the match is found in Round  $k$  by one comparison and confirmed in the confirmation phase by yet another comparison. The preceding  $k - 1$  rounds are unsuccessful. In the  $i$ -th round ( $i = 1, \dots, k - 1$ ),  $i$  comparisons take place. Therefore the overall number of comparisons is  $1 + 2 + \dots + k - 1 + 2 = \sum_{r=1}^{k-1} r + 2 = \frac{k(k-1)}{2} + 2$ .

In the second case, we assume that  $k \leq n \leq 2k - 1$ . That is  $A$  and  $B$  differ in at least one policy rule and have at least one policy rule in common. In this case, the worst case occurs if  $A$  and  $B$  share only exactly one policy rule and this policy rule is the least preferred rule of both parties. In this case, the match is found in Round  $2k - 1$  of the protocol. The results are shown in Table 2.

| $k \leq n \leq 2k - 1$           |                |
|----------------------------------|----------------|
| # Comparisons                    | $k^2 + 1$      |
| # Encryption of coefficients     | $4k$           |
| # Decryptions                    | $k^2 + 1$      |
| # Commitment of rules            | $k^2 + 1$      |
| # Messages                       | $4k - 1$       |
| Size of payload in # ciphertexts | $k^2 + 4k + 1$ |

Table 2: Sum-of-ranks: Worst case performance for  $k \leq n \leq 2k - 1$

Finally, in the third case, we assume that  $n > 2k - 1$ . In this case, the policies of  $A$  and  $B$  may be disjoint, which is also the worst case for this relation between  $n$  and  $k$ .  $A$  and  $B$  realize that they do not have a policy rule in common when no match is found after  $2k - 1$  rounds. Table 3 shows the results for this case.

| $n > 2k - 1$                     |            |
|----------------------------------|------------|
| # Comparisons                    | $k^2$      |
| # Encryption of coefficients     | $4k$       |
| # Decryptions                    | $k^2$      |
| # Commitment of rules            | $k^2$      |
| # Messages                       | $4k - 1$   |
| Size of payload in # ciphertexts | $k^2 + 4k$ |

Table 3: Sum-of-ranks: Worst case performance for  $n > 2k - 1$

Overall we can conclude that the computational overhead as well as the communication overhead of the protocol are bounded by  $O(k^2)$ .

### 4.3 $3PR^C$ Protocol for the Maximized Minimum of Ranks Composition Scheme

In this section we detail the  $3PR^C$  protocol for the maximized minimum of ranks composition scheme. The main difference to the  $3PR^C$  protocol for the sum of ranks composition scheme is the order in which private set intersections are executed (see Figure 3). In the following, we formally describe the protocol messages and processing for the case that the private set intersection protocol introduced by Freedman *et al.* is used.

**$3PR^C$  Protocol for Maximized Minimum Composition:** Within this protocol description, we reuse the definitions of  $f_A^{(i)}, f_B^{(i)}, E_A^{(i)}, E_B^{(i)}, c_{A,j}^{(i)}$ , and  $c_{B,j}^{(i)}$  introduced in the previous section.

COMMITMENT PHASE:

ROUND 0:  $B$  sends  $E_B^{(1)}$  to  $A$ .

ROUND 1:  $A$  sends  $E_A^{(1)}$  and  $c_{A,1}^{(1)}$  to  $B$ .  $B$  decrypts  $c_{A,1}^{(1)}$  under  $D_B$  and compares the result to  $b_1$ . If  $b_1 = D_B(c_{A,1}^{(1)})$ , then  $b_1 = a_1$ , that is,  $B$  has found  $max := a_1 = b_1$  and continues with the *Match Confirmation Phase*. Otherwise  $B$  sends  $E_B^{(2)}$  to  $A$  and  $A$  continues with *Round 2* of the *Commitment Phase*.

ROUND  $2 \leq i \leq k$ : For  $j = 1, \dots, i$ ,  $A$  computes the ciphertexts  $c_{A,j}^{(i)}$  and sends them as well as  $E_A^{(i)}$  to  $B$ .  $B$  decrypts  $c_{A,1}^{(i)}, \dots, c_{A,i}^{(i)}$  with  $D_B$  and checks whether any decrypted value equals  $b_i$ . If for some  $j =: m$  the ciphertext  $c_{A,m}^{(i)}$  decrypts to  $b_i$ ,  $B$  has found  $max := b_i = a_m$  and continues with the *Match Confirmation Phase*. Otherwise,  $B$  computes the ciphertexts  $c_{B,j}^{(i)}$  for  $1 \leq j \leq i - 1$  and sends them to  $A$ . For  $1 \leq i < k$   $B$  additionally sends  $E_B^{(i+1)}$  to  $A$ .  $A$  decrypts  $c_{B,1}^{(i)}, \dots, c_{B,i-1}^{(i)}$  with  $D_A$  and checks whether any decrypted value equals  $a_i$ . If for some  $j =: m$  the ciphertext  $c_{B,m}^{(i)}$  decrypts to  $a_i$ ,  $A$  has found  $max := a_i = b_m$  and continues with the *Match Confirmation Phase*. Otherwise, if  $i + 1 \leq k$ ,  $A$  continues with *Round  $i + 1$*  of the *Commitment Phase*. If  $i + 1 > k$ , the protocol terminates without a match being found.

MATCH CONFIRMATION PHASE: If it was  $A$  who found  $max$  in *Round  $i$*  of the *Commitment Phase*,  $A$  computes  $c_{A,i}^{(m)}$  and sends it to  $B$ .  $B$  decrypts  $c_{A,i}^{(m)}$  with  $D_B$  and checks that  $D_B(c_{A,i}^{(m)})$  decrypts to a value  $b_m \in \{b_1, \dots, b_i\}$ . Thus, both parties  $A$  and  $B$  know that  $a_i = b_m = max$ .

If it was  $B$  who found  $max$  in *Round  $i$*  of the *Commitment Phase*, then  $B$  computes  $c_{B,i}^{(m)}$  and sends it to  $A$ .  $A$  decrypts the received value under  $D_A$  to  $a_m$ . Thus,  $A$  and  $B$  both know that  $a_m = b_i = max$ .

**Remark 4.2** *Unlike in the  $3PR^C$  scheme for the sum of ranks composition scheme, the  $3PR^C$  scheme for the maximized minimum of ranks composition scheme allows the same rank to be assigned to multiple policy rules assuming that  $A$  and  $B$  still have the same number  $k$  of policy rules.*

Intuitively speaking, the difference between this and the previously described protocol is that the order in which  $A$  and  $B$  exchange information and compare policies is changed. As a general rule, in *Round  $i$*  of the protocol  $A$  and  $B$  compare all policy rules that lead to the same maximum of minimum of ranks.

#### Discussion:

For  $P_A \cap P_B \neq \emptyset$ , the *Commitment Phase* of the  $3PR^C$  protocol for the maximized minimum of ranks always terminates with one of the parties finding a match. This is due to the fact that for each  $1 \leq i \leq k$ ,  $a_i$  is compared with  $b_1, \dots, b_{i-1}$  by  $A$  in *Round  $i$* . Similarly, for each  $1 \leq i \leq k$ ,  $b_i$  is compared with  $a_1, \dots, a_i$  by  $B$ .

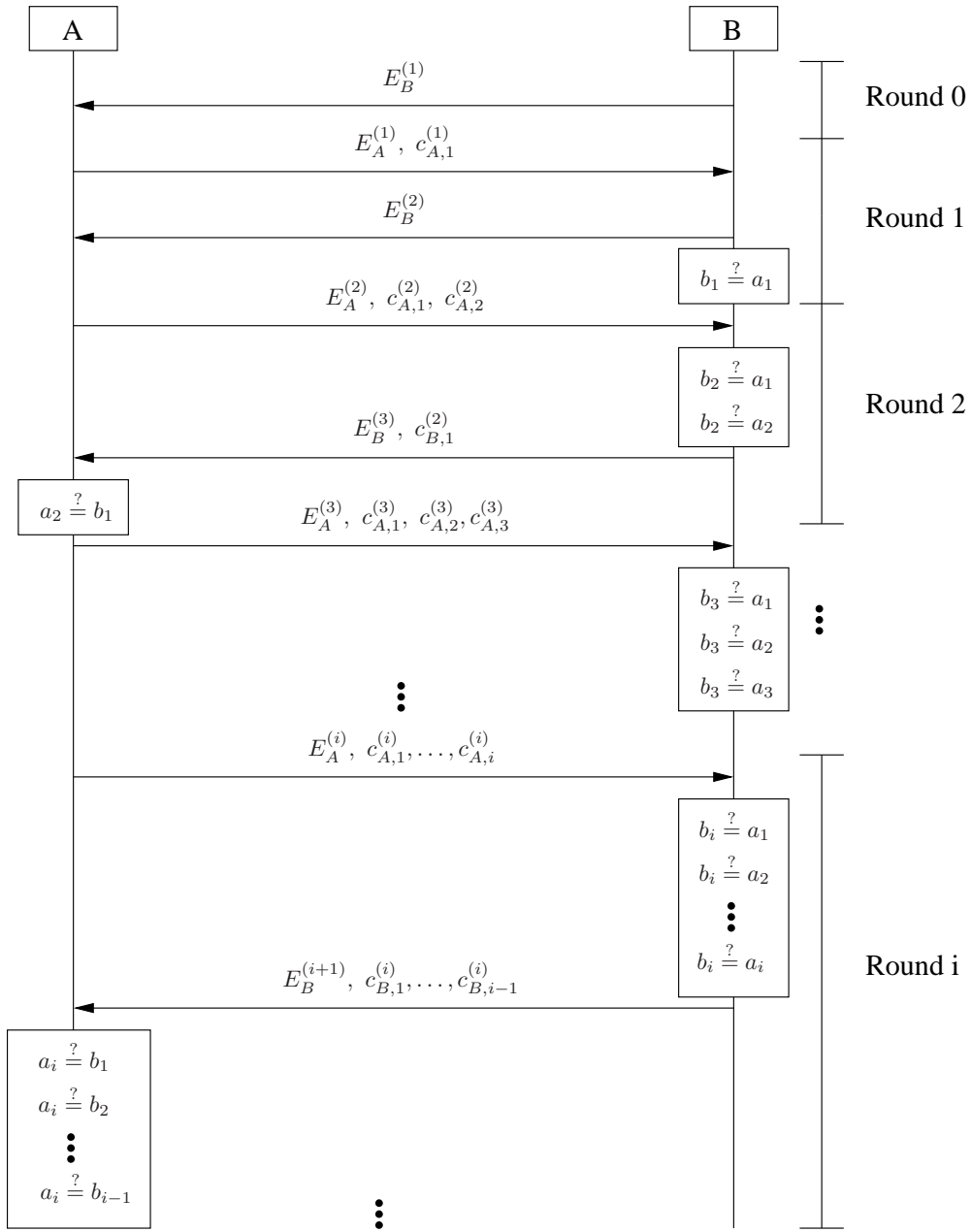


Figure 5: Commitment Phase of  $3PR^C$  for the maximized minimum of ranks composition scheme. In Round  $i$ ,  $A$  compares  $a_i$  with  $b_1, \dots, b_{i-1}$  and  $B$  compares  $b_i$  with  $a_1, \dots, a_i$  without obtaining knowledge of these values, that is, in a privacy-preserving manner.

Let  $max$  be the first match found in Round  $i$  of the *Commitment Phase* and let without loss of generality  $\max(\min(\text{rank}_A(max), \text{rank}_B(max))) = \text{rank}_A(max)$ . Then,  $max$  maximizes the minimum of the ranks of all policies in the intersection  $P_A \cap P_B$ . If this was not the case, then there was a policy rule  $p \in P_A \cap P_B$  with  $\min(\text{rank}_A(p), \text{rank}_B(p)) > \text{rank}_A(max)$ .

This implies that  $\text{rank}_A(p) > \text{rank}_A(max)$  and  $\text{rank}_B(p) > \text{rank}_A(max)$  and  $A$  and  $B$  would have



committed to  $p$  in a round prior to Round  $i$ . As a consequence,  $p$  would have been found in a prior round. This obviously contradicts the assumption.

The  $3PR^C$  for the maximized minimum of ranks scheme uses one round of the private intersection protocol of Freedman *et al.* in each round. If  $A$  ( $B$ ) would learn anything besides preference-maximizing policy rules at the end of the protocol,  $A$  ( $B$ ) would have had to learn this in one of the rounds. As each round can be interpreted as running the Freedman protocol on a subset of policy rules, each round is privacy-preserving in the semi-honest model, with respect to this subset of rules. Overall, this means that  $A$  ( $B$ ) learns nothing in any round unless a match is found. As argued before, this match always is a preference-maximizing policy rule. However, as in the  $3PR^C$  for the sum of ranks composition scheme,  $A$  ( $B$ ) may find more than one preference-maximizing policy rule. This is due to the fact that in each round of the *Commitment Phase*  $A$  ( $B$ ) evaluates several pairs of policy rules for which the maximized minimum of ranks is the same. Upon termination of the protocol in *Round*  $i$  both parties also learn about the correlation of their preferences of  $max$  to  $i$ . In addition,  $A$  ( $B$ ) learns the ranks  $B$  ( $A$ ) assigned to each of these policy rules. To avoid this leakage, additional subrounds could be added to each round of the *Commitment Phase*, such that each party commits to only one policy rule in each subround of the *Commitment Phase*. Consequently, the protocol is privacy-preserving in the semi-honest model.<sup>8</sup> It is important to note that while deviations from the protocol always imply privacy violations, a malicious party will not necessarily profit from deviations in terms of maximizing its preferences. This is due to the fact that the combined preference order depends on the preference order of the honest party. In order to profit from deviations, a malicious party would need to know the honest party's preference order at the time of initiation of reconciliation.

As in the sum of ranks case, we evaluate the worst case performance of the protocol by counting (1) the number of comparisons, (2) decryptions, (3) encryptions of coefficients, (4) ciphertext commitments, (5) messages exchanged, as well as (6) the overall size of the exchanged messages counted in number of ciphertexts. Again, we consider three different relations between the overall number of  $n$  of policies and the number  $k$  of policy rules  $A$  and  $B$  choose from the overall set of policies.

In the first case, we assume that  $n$  equals  $k$ . In this case,  $A$  and  $B$  share all policy rules and differ only in their preferences. The worst case occurs if the policy rules of  $A$  and  $B$  are in exactly the opposite order. In this case, the match is found in Round  $\lfloor k/2 \rfloor + 1$  of the protocol. Table 4 shows the results.

| $k = n$                          | $k$ odd                                     | $k$ even                                |
|----------------------------------|---|---|
| # Comparisons                    | $\frac{k^2+1}{4} + 2$                       | $\frac{k(k+2)}{4} + 1$                  |
| # Encryption of coefficients     | $2k + 2$                                    | $2k + 4$                                |
| # Decryptions                    | $\frac{k^2+1}{4} + 2$                       | $\frac{k(k+2)}{4} + 1$                  |
| # Commitment of rules            | $\frac{k-1}{2}(\frac{k-1}{2} + 1) + 2$      | $\frac{k}{2}(\frac{k}{2} + 1) + 1$      |
| # Messages                       | $k + 2$                                     | $k + 3$                                 |
| Size of payload in # ciphertexts | $2k + 4 + \frac{k-1}{2}(\frac{k-1}{2} + 1)$ | $2k + 5 + \frac{k}{2}(\frac{k}{2} + 1)$ |

Table 4: Maximized-minimum-of-ranks: Worst case performance for  $n = k$

In the second case, we assume that  $k \leq n \leq 2k - 1$ . In this case,  $A$  and  $B$  have at least one policy rule in common but may differ greatly in their preferences. In this case, the worst case occurs if  $A$  and  $B$  share only exactly one policy rule and this policy rule is the least preferred rule of both parties. In this case, the match is found in Round  $k$  of the protocol. The results are shown in Table 5.

Finally, in the third case, we assume that  $n > 2k - 1$ . In this case, the policies of  $A$  and  $B$  may be disjoint, which is also the worst case for this relation between  $n$  and  $k$ .  $A$  and  $B$  realize that they do not have a policy rule in common when no match is found after  $k$  rounds. Table 6 shows the results for this case.

<sup>8</sup>This is due to the fact that up to the point where a match is found,  $A$  ( $B$ ) receives only ciphertexts from  $B$  ( $A$ ) that decrypt to an arbitrary value. As soon as a match is found by one of the honest parties, this party acknowledges the match to the other party and the protocol terminates.

|                                  |            |
|----------------------------------|------------|
| $k \leq n \leq 2k - 1$           |            |
| # Comparisons                    | $k^2$      |
| # Encryption of coefficients     | $4k$       |
| # Decryptions                    | $k^2$      |
| # Commitment of rules            | $k^2$      |
| # Messages                       | $2k + 1$   |
| Size of payload in # ciphertexts | $k^2 + 4k$ |

Table 5: Maximized-minimum-of-ranks: Worst case performance for  $k \leq n \leq 2k - 1$

|                                  |            |
|----------------------------------|------------|
| $n > 2k - 1$                     |            |
| # Comparisons                    | $k^2$      |
| # Encryption of coefficients     | $4k$       |
| # Decryptions                    | $k^2$      |
| # Commitment of rules            | $k^2$      |
| # Messages                       | $2k + 1$   |
| Size of payload in # ciphertexts | $4k + k^2$ |

Table 6: Maximized-minimum-of-ranks: Worst case performance for  $n > 2k - 1$

Overall we can conclude that the computational overhead of the protocol is bounded by  $O(k^2)$  and that the communicational overhead is bounded by  $O(k^2)$ .

## 5 Conclusions

In this paper we introduced a new paradigm—preference-based privacy-preserving policy reconciliation. We proposed a new general multi-round construction that makes use of a set intersection protocol and maximizes the combined preferences of two parties reconciling their policies. We focused on two approaches for combining individual preferences to combined preferences: computing the sum of ranks assigned by each party or using the minimum of ranks assigned by the two parties. We showed that the new general construction is privacy-preserving in the semi-honest model as long as the set intersection protocol is privacy-preserving in the semi-honest model. We furthermore detailed our new construction for the private set intersection protocol based on oblivious polynomial evaluation introduced by Freedman *et al.* for two different notions of fairness and analytically determined their performance.

## A Appendix: Privacy-Preserving Policy Reconciliation in the Absence of Preferences

For reason of completeness, in this appendix, we provide the straight forward protocols for  $PC^2$  and  $PCP$  introduced in Section 3.2. As a main component we use the protocols of Freedman *et al.*  $PC^2$  and  $PCP$  are *straight-forward* adaptations of the protocols of Freedman *et al.* to the problem of privacy-preserving policy reconciliation in the absence of preferences. The description and discussion of these protocols are included here to provide a complete picture of how the privacy-preserving policy reconciliation problem can be tackled. As pointed out previously, the main contribution of this paper is, however, the design and analysis of protocols in the presence of preferences which is provided in Section 4.

We assume that prior to the execution of any of our protocols the two parties  $A$  and  $B$  agree upon a semantically secure homomorphic encryption scheme. The parties choose their public and private key pairs

for the encryption scheme and exchange their public keys. We denote the public encryption functions of  $A$  and  $B$  with  $E_A$  and  $E_B$  and their private decryption functions with  $D_A$  and  $D_B$ . Parties  $A$  and  $B$  have policies  $P_A = (a_1, \dots, a_k)$  and  $P_B = (b_1, \dots, b_l)$  consisting of policy rules drawn from the same domain  $\{0, 1\}^n$  (see Remark 3.1).

### A.1 Privacy-Preserving Common Policy Cardinality

The objective of the following protocol is for the two parties  $A$  and  $B$  to determine the number of policy rules they have in common in a privacy-preserving manner.

**PC<sup>2</sup> Protocol:** The parties  $A$  and  $B$  agree on some constant  $\gamma$ .  $A$  computes the polynomial

$$f_A(X) = (X - a_1)(X - a_2) \cdots (X - a_k) =: \sum_{i=0}^k \alpha_i X^i,$$

encrypts its coefficients  $\alpha_i$  ( $i = 0, \dots, k$ ) under  $E_A$ , and sends them to  $B$ . Similarly,  $B$  computes the polynomial

$$f_B(X) = (X - b_1)(X - b_2) \cdots (X - b_l) =: \sum_{i=0}^l \beta_i X^i$$

and encrypts its coefficients  $\beta_i$  ( $i = 0, \dots, l$ ) under  $E_B$ . Then, for each  $b_i \in P_B$  ( $i = 1, \dots, l$ ),  $B$  chooses a random  $r_i$  and computes  $c_{B,i} = E_A(r_i \cdot f_A(b_i) + \gamma)$ .  $B$  sends the ciphertexts  $c_{B,i}$  and the encrypted coefficients  $E_B(\beta_i)$  to  $A$ .  $A$  decrypts the received ciphertexts under  $D_A$ . For each  $b_i \in P_A$ , the ciphertext  $c_{B,i}$  will decrypt to  $\gamma$ , while for any other  $b_i$  the decryption of the ciphertext  $c_{B,i}$  under  $D_A$  will yield some arbitrary value. Consequently, the cardinality of the intersection  $P_A \cap P_B$  corresponds to the number of ciphertexts that decrypt to  $\gamma$ . Then, for each  $a_i \in P_A$  ( $i = 1, \dots, k$ ),  $A$  chooses a random  $r'_i$  and computes  $c_{A,i} = E_B(r'_i \cdot f_B(a_i) + \gamma)$ .  $A$  sends these ciphertexts to  $B$ . For each  $a_i \in P_B$ , the ciphertext  $c_{A,i}$  will decrypt to  $\gamma$ , while for any  $a_i \notin P_B$  the corresponding ciphertext will decrypt to some arbitrary value. Consequently,  $B$  also determines the cardinality of the intersection  $P_A \cap P_B$  as the number of ciphertexts that decrypt to  $\gamma$ .

**Discussion:** If parties  $A$  and  $B$  follow the PC<sup>2</sup> protocol, both will learn the cardinality of the intersection of their policies. Following the detailed proof in [12], each direction of our PCP is privacy-preserving in the semi-honest model. This is due to the fact that ciphertexts sent from  $A$  ( $B$ ) to  $B$  ( $A$ ) that do not correspond to a common policy rule of both parties decrypt to some arbitrary value. As the encryption function is semantically secure, the ciphertexts  $B(A)$  receives from  $A$  ( $B$ ) are for two inputs of  $A$  ( $B$ ) indistinguishable for  $B$  ( $A$ ).

We evaluate the complexity of the PC<sup>2</sup> protocol by counting (1) the number of comparisons  $A$  and  $B$  have to conduct, (2) the number of polynomial coefficients they need to encrypt, (3) the number of decryptions, and (4) the number of commitments of rules exchanged. The result is shown in Table 7.

|                              |             |
|------------------------------|-------------|
| # Comparisons                | $l + k$     |
| # Encryption of Coefficients | $l + k + 2$ |
| # Decryptions                | $l + k$     |
| # Commitment of rules        | $l + k$     |
| # Messages                   | 2           |

Table 7: Performance of PC<sup>2</sup>, where  $l$  and  $k$  are the number of policy rules of  $A$  and  $B$ .

## A.2 Privacy-Preserving Common Policy

The objective of the following protocol is for the two parties  $A$  and  $B$  to determine the policy rules they have in common in a privacy-preserving manner.

**PCP Protocol:**  $A$  computes the polynomial

$$f_A(X) = (X - a_1)(X - a_2) \cdots (X - a_k) =: \sum_{i=0}^k \alpha_i X^i,$$

encrypts the coefficients  $\alpha_i$  ( $i = 0, \dots, k$ ) under  $E_A$ , and sends the encrypted coefficients to  $B$ . Similarly,  $B$  computes the polynomial

$$f_B(X) = (X - b_1)(X - b_2) \cdots (X - b_l) =: \sum_{i=0}^l \beta_i X^i$$

and encrypts the coefficients  $\beta_i$  ( $i = 0, \dots, l$ ) under  $E_B$ . Then, for each  $b_i \in P_B$  ( $i = 1, \dots, l$ ),  $B$  chooses a random  $r_i$  and computes the ciphertexts  $c_{B,i} = E_A(r_i \cdot f_A(b_i) + b_i)$ .  $B$  sends the ciphertexts  $c_{B,i}$  ( $i = 1, \dots, l$ ) and the encrypted coefficients  $E_B(\beta_i)$  to  $A$ .  $A$  decrypts the received ciphertexts  $c_{B,i}$  ( $i = 1, \dots, l$ ) under  $D_A$ . For each  $b_i \in P_A \cap P_B$ , the ciphertext  $c_{B,i}$  will decrypt to  $b_i$  (matching some  $a_j \in P_A$ ). For each  $b_i \notin P_A \cap P_B$ ,  $c_{B,i}$  will decrypt under  $D_B$  to some arbitrary value.  $A$  thus learns all elements of the intersection, but nothing about any other rule in  $P_B$ . Then,  $A$  computes  $c_{A,i} = E_B(r_i \cdot f_B(a_i) + a_i)$  ( $i = 1, \dots, k$ ) and sends these ciphertexts to  $B$ .  $B$  decrypts the received ciphertexts under  $D_B$ . For each  $a_i \in P_A \cap P_B$ ,  $c_{A,i}$  will decrypt to  $a_i$  (matching some  $b_j \in P_B$ ). For each  $a_i \notin P_A \cap P_B$ ,  $c_{A,i}$  will decrypt under  $D_B$  to some arbitrary value.  $B$  thus also learns all elements in the intersection  $P_A \cap P_B$ .

**Discussion:** If parties  $A$  and  $B$  follow the PCP protocol, both will learn the intersection of their policies. The PCP protocol simply uses the private cardinality protocol of [12]. Following the detailed proof in [12], each direction of the protocol is privacy-preserving in the semi-honest model. This is due to the fact that ciphertexts sent from  $A$  ( $B$ ) to  $B$  ( $A$ ) that do not correspond to a common policy rule of both parties decrypt to some arbitrary value. Moreover, the views of  $B$  ( $A$ ) for two inputs of  $A$  ( $B$ ) are indistinguishable due to the semantical security of the encryption scheme used.

We again evaluate the complexity of the PCP protocol by counting (1) the number of comparisons  $A$  and  $B$  have to conduct, (2) the number of polynomial coefficients they need to encrypt, (3) the number of decryptions, and (4) the number of commitments of rules exchanged. The result are the same as shown in Table 7.

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