# Impossible Differential Cryptanalysis on E2 

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#### Abstract

E2 is a 128 -bit block cipher which employs a Feistel structure and 2 -round SPN in round function. It is an AES candidate and was designed by NTT. In the former publications, E2 is supposed no more than 5 -round impossible differential. In this paper, we describe some 6 -round impossible differentials of E2. By using the 6 -round impossible differential, we first present an attack on a 9 -round reduced version of E2256 without IT Function (the initial transformation) and FT-Function (the final transformation).


Key words: Block cipher, E2, Impossible differential attack, Data complexity, Time complexity

## 1 Introduction

Impossible differential cryptanalysis, proposed by Biham and Knudsen, was first applied to the cipher DEAL [8] and later to Skipjack [9]. The main idea is to specify a differential with probability zero over some rounds of the cipher. Then one can derive the right keys by discarding the wrong keys which lead to the impossible differential. Impossible differential cryptanalysis has been applied to AES, Camellia, MISTY1 and so on with very good results [11-17].

The key step of impossible differential cryptanalysis is to retrieve the longest impossible differential. The main technique is miss-in-the-middle, namely to find two differential characteristics with probability 1 from encryption and decryption, and connect them together when there are some inconsistencies, their combination is the impossible differential that we are looking for. Once the impossible differential is found, it can be used to distinguish the cipher from a random permutation. In [10], Kim et al. introduced the $\mathcal{U}$-method to find impossible differentials of various block ciphers. However, $\mathcal{U}$-method is so general that some information is often lost during calculating the impossible differentials. Some longer impossible differentials cannot be found by using the $\mathcal{U}$-method.

E2 [3] is a 128-bit block cipher designed and submitted to AES project by NTT. Its design criteria are conservative, adopting a Feistel network structure as a global structure and the 2-round SPN-structure in its round function. All
operations used in the data randomization phase are byte table lookups and byte xor's except 32 -bit multiplications in IT and FT, which successfully makes E2 a fast software cipher independent of target platforms.

A truncated differential cryptanalysis of reduced-round variants of E2 was presented by Matsui and Tokita in ref.[1]. They found a 7 -round byte characteristic, which leads to a possible attack on an 8 -round E2 without IT-Function and FT-Function. In ref.[2], Moriai et al. presented another 7-round truncated differential and improved the attack complexity of 8 -round E2 without IT/FT functions. Ref.[6] studies the impossible differentials of E2. To search the impossible differentials, the authors applied the Shrinking technique, the miss-in-themiddle technique and so on. However, no impossible differential is found for E2 without IT/FT functions with more than 5 rounds. They declared that E2 is secure against cryptanalysis with impossible differential using currently known techniques.

In this paper, the security of E2 against impossible differential attacks are investigated. We first find some 6 -round impossible differentials which lead to an attack of E2 reduced to 9 rounds without IT/FT functions. The attack is the first published attack on 9-round E2 without IT/FT functions. Like most cryptanalytic attacks on block ciphers, it is theoretical in the sense of the magnitude of the required data and time complexity and the attack does not have a serious impact on the full E2, since it has twelve rounds with IT and FT; however our results show that the security level of the E2 is much lower than the estimation of the designers.

The paper is organized as follows: Section 2 briefly introduces some notations and the E2 block cipher. In section 3, we describe some 6 -round impossible differentials. Then the attack are discussed in section 4 . Section 5 concludes the paper and summarizes our results.

## 2 Preliminaries

### 2.1 Notations

The following describes the notations which will be used in encryption and attack.
$L_{i}\left(R_{i}\right)$ : the left(right) half output of the $i^{\text {th }}$ round;
$\Delta L_{i}\left(\Delta R_{i}\right)$ : the difference of the left(right) half output of the $i^{t h}$ round;
$K_{i, j}^{(1)}$ : the $j^{\text {th }}$ byte of subkey used in the first layer of the $i^{t h}$ round function;
$K_{i, j}^{(2)}$ : the $j^{\text {th }}$ byte of subkey used in the second layer of the $i^{t h}$ round function;
$\oplus$ : xor(exclusive or);
$\mid: \quad$ bit string concatenation.

### 2.2 The E2 Block Cipher

E2 is a 12-round Feistel cipher with 2-round SPN structure in its round function and the linear layer used is proved to be optimal. The strategy of 2-round

SPN structure is proposed in ref.[7]. It based on using $m n$-bit round functions consisting of four-layers: 1st non-linear transformation layer with $n$ parallel $m$ bit $s$-boxes, 1st linear transformation layer, 2nd non-linear transformation layer with $n$ parallel $m$-bit $s$-boxes, and 2 nd linear transformation layer (sometimes the fourth layer is omitted). Ref.[7] shows that the round function with the 2round SPN structure requires one-forth as many rounds as the 1-round SPN structure to achieve the same differential and linear probabilities.

Besides, E2 has a preprocess, IT-Function, as well as a postprocess, FTFunction. The decryption process is the same as the encryption process except for the order of the subkeys. Fig. 1 shows the outline of the E2 encryption process.

Let $P$ and $C$ be the plaintext and cipertext respectively, $L_{r-1}$ and $R_{r-1}$ be the left and the right halves input of the $r^{t h}$ round, and $K_{r}$ be the subkey of the $r^{t h}$ round. Then the encryption process of E2 can be written as:

$$
\begin{aligned}
L_{0} \mid R_{0} & =I T(P) \\
L_{r} & =R_{r-1} \oplus F\left(L_{r-1}, K_{r}\right) \quad(r=1,2 \ldots, 12) \\
R_{r} & =L_{r-1} \\
C & =F T\left(R_{12} \mid L_{12}\right)
\end{aligned}
$$

In this paper, we will consider E2 without IT/FT functions. Fig. 2 outlines the round function. Round function consists of $S$-Function, $P$-Function, and $B R L$-Function. Refer to [3] for details of the specification and notations. For readers' convenience, we give algebraic description of the variable $z_{i}^{\prime}$ in the round function in terms of the intermediate values $z_{i}$ as follows:

$$
\begin{aligned}
& P:\left(\mathbb{F}_{2}^{8}\right)^{8} \rightarrow\left(\mathbb{F}_{2}^{8}\right)^{8}: z_{1}\left|z_{2}\right| z_{3}\left|z_{4}\right| z_{5}\left|z_{6}\right| z_{7}\left|z_{8} \rightarrow z_{1}^{\prime}\right| z_{2}^{\prime}\left|z_{3}^{\prime}\right| z_{4}^{\prime}\left|z_{5}^{\prime}\right| z_{6}^{\prime}\left|z_{7}^{\prime}\right| z_{8}^{\prime} \\
& z_{1}^{\prime}=z_{2} \oplus z_{3} \oplus z_{4} \oplus z_{5} \oplus z_{6} \oplus z_{7} \\
& z_{2}^{\prime}=z_{1} \oplus z_{3} \oplus z_{4} \oplus z_{6} \oplus z_{7} \oplus z_{8} \\
& z_{3}^{\prime}=z_{1} \oplus z_{2} \oplus z_{4} \oplus z_{5} \oplus z_{7} \oplus z_{8} \\
& z_{4}^{\prime}=z_{1} \oplus z_{2} \oplus z_{3} \oplus z_{5} \oplus z_{6} \oplus z_{8} \\
& z_{5}^{\prime}=z_{1} \oplus z_{2} \oplus z_{4} \oplus z_{5} \oplus z_{6} \\
& z_{6}^{\prime}=z_{1} \oplus z_{2} \oplus z_{3} \oplus z_{6} \oplus z_{7} \\
& z_{7}^{\prime}=z_{2} \oplus z_{3} \oplus z_{4} \oplus z_{7} \oplus z_{8} \\
& z_{8}^{\prime}=z_{1} \oplus z_{3} \oplus z_{4} \oplus z_{5} \oplus z_{8}
\end{aligned}
$$

## 3 Some 6-Round Impossible Differentials

In ref.[6], the authors drew the conclusion that there was no impossible differentials for E2 without IT/FT functions with more than 5 -round. In this section, we show one impossible differential of 6-round E2 in Fig. 3.

We assert that the 6 -round differential


Fig. 1. Encryption Process of E2


Fig. 2. Round Function of E2

$$
(0|0| 0|0| a|0| 0|0,0| 0|0| 0|0| 00 \mid 0) \xrightarrow{6-\text { round }}(0|0| 0|0| 0|0| 0|0,0| 0|0| 0|0| h|0| 0)
$$

is impossible, where $a$ and $h$ denote any non-zero value.
Consider an input difference $\left(\Delta L_{0}, \Delta R_{0}\right)=(0|0| 0|0| a|0| 0|0,0| 0|0| 0|0| 0|0| 0)$, after passing through the first and the second round, it becomes as follows(where $c_{i}$ also denote non-zero value):

$$
\begin{aligned}
& \left(\Delta L_{1}, \Delta R_{1}\right)=(0|0| 0|0| 0|0| 0|0,0| 0|0| 0|a| 0|0| 0), \\
& \left(\Delta L_{2}, \Delta R_{2}\right)=\left(0|0| 0|0| a|0| 0|0,0| c_{2}\left|c_{3}\right| c_{4}|0| 0\left|c_{7}\right| c_{8}\right)
\end{aligned}
$$

In the third round, after the first subkey addition and the $S$ layer, $\Delta R_{2}$ becomes $\left(0\left|c_{2}^{*}\right| c_{3}^{*}\left|c_{4}^{*}\right| 0|0| c_{7}^{*} \mid c_{8}^{*}\right)$, where $c_{i}^{*}$ is non-zero value. After the linear layer $P$ it becomes ( $d_{1}\left|d_{2}\right| d_{3}\left|d_{4}\right| d_{5}\left|d_{6}\right| d_{7} \mid d_{8}$ ), thus the output difference of the second subkey addition and the $S$ layer in the third round has the form of $\left(e_{1}\left|e_{2}\right| e_{3}\left|e_{4}\right| e_{5}\left|e_{6}\right| e_{7} \mid e_{8}\right)$. Whether the values of $d_{i} \mathrm{~s}$ and $e_{i} \mathrm{~s}(i=1 \ldots 8)$ are zero or not is uncertain. The BRL-function makes the output difference be ( $e_{2}\left|e_{3}\right| e_{4}\left|e_{5}\right| e_{6}\left|e_{7}\right| e_{8} \mid e_{1}$ ). Therefore the 3 -round differential ends with

$$
\left(\Delta L_{3}, \Delta R_{3}\right)=\left(0\left|c_{2}\right| c_{3}\left|c_{4}\right| 0|0| c_{7}\left|c_{8}, e_{2}\right| e_{3}\left|e_{4}\right| e_{5}\left|e_{6} \oplus a\right| e_{7}\left|e_{8}\right| e_{1}\right)
$$

Consider the other direction now, when rolling back the $6^{\text {th }}$ round difference ( $0|0| 0|0| 0|0| 0|0,0| 0|0| 0|0| h|0| 0$ ) though 3-round transformation, we get the following differences ( $f_{i}$ is non-zero value):

$$
\begin{aligned}
\left(\Delta L_{5}, \Delta R_{5}\right) & =(0|0| 0|0| 0|h| 0|0,0| 0|0| 0|0| 0|0| 0), \\
\left(\Delta L_{4}, \Delta R_{4}\right) & =\left(f_{1}|0| f_{3}\left|f_{4}\right| f_{5}|0| 0\left|f_{8}, 0\right| 0|0| 0|0| h|0| 0\right) .
\end{aligned}
$$

From the Feistel structure of the cipher, we know that $\Delta L_{4}=\Delta R_{3}$, hence, $\left(f_{1}|0| f_{3}\left|f_{4}\right| f_{5}|0| 0 \mid f_{8}\right)$ is the same as $\left(e_{2}\left|e_{3}\right| e_{4}\left|e_{5}\right| e_{6} \oplus a\left|e_{7}\right| e_{8} \mid e_{1}\right)$, So we have $e_{3}=e_{7}=e_{8}=0$, thus $d_{3}=d_{7}=d_{8}=0$ since subkey addition and $S$-boxes transformations are bijective. $d_{i}$ can be expressed as the linear combination of $c_{i}^{*}$ according to the linear layer $P$, which implies the following equations hold(just $d_{3}=d_{7}=0$ is used):

$$
\begin{array}{r}
c_{2}^{*} \oplus c_{4}^{*} \oplus c_{7}^{*} \oplus c_{8}^{*}=0, \\
c_{2}^{*} \oplus c_{3}^{*} \oplus c_{4}^{*} \oplus c_{7}^{*} \oplus c_{8}^{*}=0 .
\end{array}
$$

From the above equations we know that $c_{3}^{*}$ is zero, which contradicts with $c_{3} \neq 0$ since subkey addition doesn't change the difference and $S$-boxes transformations are bijective.

Similarly, we can get other 6 -round impossible differentials of $E 2$. We define $w_{i}$ as 8 -byte vector, in which only the $i^{\text {th }}$ byte is non-zero, for example, $w_{1}$ denotes $(a|0| 0|0| 0|0| 0 \mid 0)$. If $\left(w_{i}, 0\right) \rightarrow\left(0, w_{j}\right)$ is an impossible differential, then $\left(w_{j}, 0\right) \rightarrow\left(0, w_{i}\right)$ is also an impossible differential since the encryption and the decryption are the same for Feistel cipher. The 6 -round impossible differentials of E2 found by the way of Section. 3 can be written as follows(for $i \leq j$ ).


Fig. 3. 6-Round Impossible Differential of E2


## 4 Impossible Differential Attack on E2 Reduced to 9 Rounds

With the 6-round impossible differential, a 9-round impossible differential attack on E2 without IT/FT function can be obtained. The attack is based on the above 6 -round impossible differentials with additional two rounds at the beginning and one round at the end as shown in Fig. 4.


Fig. 4. 9-Round Impossible Differential Attack to E2

The attack procedure is as follows:
Step 1 Precalculation: for S-box, define $T(\alpha, \beta)=\left\{x \in \mathbb{F}_{2}^{8} \mid S(x \oplus \alpha) \oplus S(x)=\right.$ $\beta\}$, then take all possible values of $(\alpha, \beta)$, and store $T(\alpha, \beta)$ in a table.

Step 2 Choose structure of plaintexts as follows:

$$
\begin{aligned}
L_{0} & =\left(y_{1}\left|y_{2}\right| y_{3}\left|y_{4}\right| y_{5}\left|y_{6}\right| y_{7} \mid y_{8}\right) \\
R_{0} & =\left(\alpha_{1}\left|x_{2}\right| x_{3}\left|x_{4}\right| \alpha_{5}\left|\alpha_{6}\right| x_{7} \mid x_{8}\right)
\end{aligned}
$$

where $x_{i}(i=2,3,4,7,8), y_{i}(1 \leq i \leq 8)$ take all possible values in $\mathbb{F}_{2}^{8}, \alpha_{i}(i=$ $1,5,6)$ and $\beta_{i}(2 \leq i \leq 8)$ are constants in $\mathbb{F}_{2}^{8}$. For each possible value of $\left(y_{1}, y_{2}, y_{3}, y_{4}, y_{5}, y_{6}, y_{7}, y_{8}, x_{2}, x_{3}, x_{4}, x_{7}, x_{8}\right)$, we can get a unique 128 -bit string. Hence, a structure includes $2^{104}$ plaintexts and there are $2^{104 \times 2} / 2=2^{207}$ plaintext pairs in a structure. So the $2^{17}$ structures yield a total of $2^{224}$ plaintext pairs.

Step 3 Keep only the pairs whose ciphertexts differential ( $\Delta L_{9}, \Delta R_{9}$ ) satisfy the following:

$$
\begin{aligned}
\Delta L_{9} & =(0|0| 0|0| 0|h| 0 \mid 0) \\
\Delta R_{9} & =\left(t_{1}|0| t_{2}\left|t_{3}\right| t_{4}|0| 0 \mid t_{8}\right)
\end{aligned}
$$

where $t_{i}(i=1,2,3,4,8)$ are unknown non-zero values. The expected number of remaining pairs is about $2^{224} \times 2^{-80}=2^{144}$.

Step 4 Guess the 64 -bit subkey $K_{9}^{(1)}$ and 5 subkey bytes $K_{9,1}^{(2)}, K_{9,2}^{(2)}, K_{9,4}^{(2)}$, $K_{9,5}^{(2)}, K_{9,6}^{(2)}$.

Step 4.1 For every remaining pair $\left(L_{0}, R_{0}\right)$ and $\left(L_{0}^{*}, R_{0}^{*}\right)$, guess the 64 -bit subkey $K_{9}^{(1)}$ and compute

$$
\begin{aligned}
Z_{9} & =P S\left(L_{9} \oplus K_{9}^{(1)}\right) \\
Z_{9}^{*} & =P S\left(L_{9}^{*} \oplus K_{9}^{(1)}\right)
\end{aligned}
$$

Step 4.2 Guess the 5 bytes of $K_{9}^{(2)}$ and compute

$$
\begin{aligned}
& q_{1}=s\left(Z_{9,1} \oplus K_{9,1}^{(2)}\right) \oplus s\left(Z_{9,1}^{*} \oplus K_{9,1}^{(2)}\right) \oplus R_{9,8} \oplus R_{9,8}^{*}, \\
& q_{2}=s\left(Z_{9,2} \oplus K_{9,2}^{(2)}\right) \oplus s\left(Z_{9,2}^{*} \oplus K_{9,2}^{(2)}\right) \oplus R_{9,1} \oplus R_{9,1}^{*}, \\
& q_{3}=s\left(Z_{9,4} \oplus K_{9,4}^{(2)}\right) \oplus s\left(Z_{9,4}^{*} \oplus K_{9,4}^{(2)}\right) \oplus R_{9,2} \oplus R_{9,2}^{*}, \\
& q_{4}=s\left(Z_{9,5} \oplus K_{9,5}^{(2)}\right) \oplus s\left(Z_{9,5}^{*} \oplus K_{9,5}^{(2)}\right) \oplus R_{9,3} \oplus R_{9,3}^{*}, \\
& q_{5}=s\left(Z_{9,6} \oplus K_{9,6}^{(2)}\right) \oplus s\left(Z_{9,6}^{*} \oplus K_{9,6}^{(2)}\right) \oplus R_{9,4} \oplus R_{9,4}^{*} .
\end{aligned}
$$

Then check whether $q_{i}=0(1 \leq i \leq 5)$ and keep only the qualified pairs. Since the probability is about $2^{-40}$, the expected number of the remaining pairs is $2^{144} \times 2^{-40}=2^{104}$.

Step 5 Guess the 64-bit subkeys $K_{1}^{(1)}$ and $K_{1}^{(2)}$, for every remaining plaintext pair $\left(L_{0}, R_{0}\right)$ and ( $L_{0}^{*}, R_{0}^{*}$ ),

$$
\begin{aligned}
& L_{0}=\left(y_{1}\left|y_{2}\right| y_{3}\left|y_{4}\right| y_{5}\left|y_{6}\right| y_{7} \mid y_{8}\right) \\
& R_{0}=\left(\alpha_{1}\left|x_{2}\right| x_{3}\left|x_{4}\right| \alpha_{5}\left|\alpha_{6}\right| x_{7} \mid x_{8}\right) \\
& L_{0}^{*}=\left(y_{1}^{*}\left|y_{2}^{*}\right| y_{3}^{*}\left|y_{*}\right| y_{5}^{*}\left|y_{6}^{*}\right| y_{7}^{*} \mid y_{8}^{*}\right) \\
& R_{0}^{*}=\left(\alpha_{1}\left|x_{2}^{*}\right| x_{3}^{*}\left|x_{4}^{*}\right| x_{5}\left|\alpha_{6}\right| x_{7}^{*} \mid x_{8}^{*}\right)
\end{aligned}
$$

Compute ( $L_{1}, R_{1}$ ) and ( $L_{1}^{*}, R_{1}^{*}$ ), choose pairs whose difference satisfy $R_{1} \oplus R_{1}^{*}=$ $(0|0| 0|0| 0|h| 0 \mid 0)$ where $h$ is not zero. Since the probability is about $2^{-56}$, the expected number of the remaining pairs is $2^{104} \times 2^{-56}=2^{48}$.

Step 6 Guess the 64 -bit subkey $K_{2}^{(1)}$ and 5 subkey bytes $K_{2,1}^{(2)}, K_{10,2}^{(2)}, K_{10,3}^{(2)}$, $K_{10,4}^{(2)}, K_{10,8}^{(2)}$, perform the following:

Step 6.1 For every remaining pair $\left(L_{0}, R_{0}\right)$ and $\left(L_{0}^{*}, R_{0}^{*}\right)$, and the corresponding output of the first round $\left(L_{1}, R_{1}\right)$ and $\left(L_{1}^{*}, R_{1}^{*}\right)$, guess $K_{2}^{(1)}$ and compute:

$$
\begin{aligned}
& Z_{2}=P S\left(R_{1} \oplus K_{2}^{(1)}\right) \\
& Z_{2}^{*}=P S\left(R_{1}^{*} \oplus K_{2}^{(1)}\right)
\end{aligned}
$$

Step 6.2 Guess the 5 bytes of $K_{2}^{(2)}$ and compute

$$
\begin{aligned}
& q_{1}=s\left(Z_{2,1} \oplus K_{2,1}^{(2)}\right) \oplus s\left(Z_{2,1}^{*} \oplus K_{2,1}^{(2)}\right) \oplus R_{1,8} \oplus R_{1,8}^{*}, \\
& q_{2}=s\left(Z_{2,2} \oplus K_{2,2}^{(2)}\right) \oplus s\left(Z_{2,2}^{*} \oplus K_{2,2}^{(2)}\right) \oplus R_{1,1} \oplus R_{1,1}^{*}, \\
& q_{3}=s\left(Z_{2,4} \oplus K_{2,4}^{(2)}\right) \oplus s\left(Z_{2,4}^{*} \oplus K_{2,4}^{(2)}\right) \oplus R_{1,2} \oplus R_{1,2}^{*}, \\
& q_{4}=s\left(Z_{2,5} \oplus K_{2,5}^{(2)}\right) \oplus s\left(Z_{2,5}^{*} \oplus K_{2,5}^{(2)}\right) \oplus R_{1,3} \oplus R_{1,3}^{*}, \\
& q_{5}=s\left(Z_{2,6} \oplus K_{2,6}^{(2)}\right) \oplus s\left(Z_{2,6}^{*} \oplus K_{2,6}^{(2)}\right) \oplus R_{1,4} \oplus R_{1,4}^{*} .
\end{aligned}
$$

Then check whether $q_{i}=0(5 \leq i \leq 1)$. If yes, discard the candidate value of $\left(K_{1}^{(1)}, K_{1}^{(2)}, K_{2}^{(1)}, K_{2, i}^{(2)}, K_{9}^{(1)}, K_{9, i}^{(2)}\right)(i=1,2,4,5,6)$.

Since such a difference is impossible, every key that proposes such a difference is a wrong key. After analyzing $2^{48}$ ciphertexts pairs, there remain only about $2^{336}\left(1-2^{-40}\right)^{2^{48}}$ wrong candidate value of $\left(K_{1}^{(1)}, K_{1}^{(2)}, K_{2}^{(1)}, K_{2, i}^{(2)}, K_{9}^{(1)}, K_{9, i}^{(2)}\right)(i=$ $1,2,4,5,6)$, which is much less than 1 .

The time complexity of Step 4.1 requires about $2^{144} \times 2^{64} \times 2=2^{209}$ one round operations. The precalculation can decrease the complexity of Step 4.2, one can look up the table $T\left(Z_{9, k} \oplus Z_{9, k}^{*}, R_{9, i} \oplus R_{9, j}\right)$ to judge whether the $q_{i} s$ are zero or not. This Step needs about $2^{144} \times 2^{64} \times 5 \approx 2^{210}$ table lookups. Step 5 has a time complexity of about $2^{104} \times 2^{128} \times 2=2^{233}$ one round operations. Step 6 needs $2^{48} \times 2^{64} \times 2=2^{113}$ one round operations and $2^{48} \times 2^{64} \times 5 \approx 2^{114}$ table lookups respectively.

Consequently, this attack requires about $2^{121}$ chosen plaintexts and less than $2^{230}$ encryptions of 9-round E2 and $2^{210}$ table lookups.

## 5 Conclusion

The block cipher E2 was proposed as an AES candidate. It employs a Feistel structure and a 2-layer SPN structure in round function. In this paper we describe some 6 -round impossible differentials of E2, and present a 9 -round attack on E2 without IT/FT when used with 256 key bits. Cryptanalysis given in this paper is the first security evaluation of E2 against impossible differential cryptanalysis.

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