

Secure *Committed* Computation

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Abstract

We introduce *secure committed two-party computation*, where parties commit in advance to compute a function over their private inputs, by providing some (validated) *compensation*, such that if a party fails to provide an appropriate input during protocol execution, then the peer receives the compensation. Enforcement of the commitments requires a *trusted enforcement authority* (TEA); however, the protocol protects confidentiality even from the TEA. Our secure committed computation protocol is *optimistic*, i.e., the TEA is involved only if a party fails to participate (correctly). Secure committed computation has direct practical applications, such as sensitive trading of financial products, and could also be used as a building block to motivate parties to complete protocols, e.g., ensuring unbiased coin tossing.

The commitment can be either symmetric (both parties commit) or asymmetric (e.g., only server commits to client). Symmetric commitment should also be *fair*, i.e., one party cannot obtain commitment by the other party without committing as well.

The protocol we present uses two new building blocks, which may be of independent interest. The first is a protocol for *optimistic fair secure computation*, which is simpler and more efficient than previously known. The second is a protocol for *two party computation secure against malicious participants*, which is simple and efficient, and for the preprocessing phase relies on an (offline) third party. This protocol can be useful where a trusted third party is unavoidable, e.g., in secure committed or fair computation protocols.

Keywords: Two-party computation, trusted third party, optimistic protocols, cryptographic protocols.

1 Introduction

This work investigates the combination of two important areas of research related to secure distributed systems: the beautiful theory of *secure computation*, and the applied area of *committed network services*. As we explain, this combination is natural and interesting; furthermore, it has important practical applications, as well as theoretical significance.

Secure computation, beginning with the seminal papers of Yao [34] and Goldreich et al. [18], investigates how to securely compute functionalities over inputs from multiple players, under different circumstances and in the presence of different adversaries. Such computation can trivially be done securely by a trusted third party; the goal of secure computation is to achieve the same security impact without a trusted party, running only a protocol between the parties. However, as shown in [10], two-party protocols cannot achieve fairness for general computation without an honest majority. Furthermore, for some critical applications, fairness alone may not suffice and an honest participant should receive an output (albeit not the output from the computation of an agreed upon function) even in case of early abort or failure to conclude the protocol by the other party. This property is called *guaranteed output delivery*. Our focus is on the problem of delivery failures, aka *abort attacks*, and *fairness*. Namely, what should the result of a secure computation be, when a party fails to deliver (‘valid’) input?

Committed network services focus on the problem of delivery failures. As network services become more and more important, failure to provide services can become a serious concern. Many works (and systems) address the

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basic concerns of unintentional failures and congestion, as well as (intentional) denial-of-service attacks, e.g., see [23]. A more difficult issue is the *intentional delivery failures* by one of the parties, e.g., a service provider. For example, suppose a customer bought, say from his broker, an option to buy or sell some shares (or other financial product) at a fixed price; and suppose the customer sends an order to execute the option, close to its expiration time. A failure to process the order by the broker could cause significant loss to the customer (and illegitimate gain to the broker).

Secure *committed* computation, introduced in Section 5, provides an interesting variant, where parties have an *incentive* to complete the protocol. This incentive is achieved, by running the computation in two phases: *commitment phase* and *execution phase*. In the first, commitment, phase, a party commits to participate in the second, execution, phase, by inputting some secret value whose exposure would penalise that party (and compensate the other party); in the second phase, if a party does not participate correctly, then the protocol exposes its commitment from the first phase. To enforce compensation we involve an additional, weakly trusted, participant, which we call the TEA (Trusted Enforcement Authority), who does not provide inputs, but helps to identify and penalise faulty participants. Specifically, in the commitment phase, the parties agree on the terms and send to the TEA a pre-agreed *compensation*, e.g., a signed payment order. Later, in the execution phase, if the service is not performed correctly, i.e., the other participant fails to deliver the agreed upon service or content, e.g., digitally signed payment, (either due to early abort, if it is malicious, or due to communication failures), the TEA compensates the honest party. The compensation is based on the inputs sent to the TEA in advance by both parties. This provides an incentive for the parties to complete protocol execution correctly, i.e., to provide the services that they committed to. The solution can extend secure computation protocol to be used as a building block in design of more complex incentive-based protocols, ensuring security goals which involve rational adversaries.

In a naïve implementation, the TEA is aware of the terms of the service, as well as of the inputs provided by the parties and of the compensation, e.g., see [1, 2] for works on certified mail, non-repudiation (evidences), fair exchange (esp. of signed documents). Yet confidentiality can be very important, e.g., the exposure of (future) trading positions can allow entities to react, possibly harming the customer. This limits the use of sensitive transactions, and as a result, the potential of the Internet, to allow arbitrary parties to perform commerce, with automated, trustworthy dispute-resolution and compensation mechanisms, is only partially used. We believe that in this paper, we make a significant, if yet an initial, step towards this goal. Our focus is on minimising the exposure of the private inputs and outputs, and we ensure that the TEA is *oblivious* to the terms, inputs and compensation. Namely, in case of attempted cheating the TEA engages in secure computation with the parties, and as a result either the service is provided correctly, or compensation is given, while the TEA is unaware of the inputs and outputs of the process, which contain sensitive data of the parties.

The definition of correct service can be trivial, e.g., when the service is the exchange of well defined signed documents, such as contracts, or payment orders (e.g., in different currencies). Often, the correct service is more complex, and may involve computation based on inputs from both parties. For example, a customer sends a complex order involving multiple stocks, and the broker has to provide updated, valid (signed) quotas, and if there is a match then the result will be specific buy and/or sell transactions.

The discussion above focused on the case of asymmetric commitment: only Bob (the service provider) commits to Alice (the client). We extend this setting, in Section 5.2, and present a protocol that supports symmetric commitment, where both peers initially ‘deposit’ some ‘compensation’ at the TEA, and can later participate in the transaction. This protocol also ensures *fairness*, i.e., Bob receives Alice’s commitment if and only if Alice receives Bob’s commitment.

Our secure committed computation protocols make use of two sub-protocols, that may be of independent interest. The first is a simple and efficient protocol for *optimistic fair secure two-party computation*, in Section 4.2, which we use as a module in our committed secure two-party computation protocol, to ensure that the commitment process is *fair*, i.e., one party cannot obtain commitment by other party without committing as well. As other protocols for optimistic fair secure computation, our protocol also involves a third party, however this party is both very simple and also only weakly trusted, i.e., even if it is rogue, the implication would be on fairness only, but not on correctness or privacy. The protocol is *optimistic* in the sense that the third party is involved only if one of the two parties fails to complete the protocol properly. Note that a weakly-trusted third party is necessary to support fairness for computation of arbitrary functionalities (although it may be avoided for some specific functionalities, see [22]). Optimistic fair secure computation protocols were presented before [7], however, our protocol is more efficient (also, the protocol in [7] was not proven secure yet). The second sub-protocol is an efficient two-party computation protocol in the malicious setting, that allows output at Bob only. This protocol uses a offline third party for the preprocessing phase, and improves efficiency over the existing protocols, see Section 3.2.1 for analysis and comparison.

1.1 Outline of the Contributions and Techniques

Our central contribution is committed computation with compensation of the honest party in case of misbehaviour by a malicious peer. In Section 5, we present the notion of committed computation that ensures either fairness or guaranteed output delivery. This is accomplished by having the parties commit to participate in protocol execution, e.g., by exchanging signed checks, and the commitment is executed by the TEA (trusted enforcement authority) in case of failures. Even if the \mathcal{F}_{tea} is malicious, it can not learn the inputs or the outputs of the parties and will not be able to generate an incorrect result without the parties detecting this. We construct the committed computation protocol using two sub protocols, which we describe next.

In Section 3 we present a protocol with output at one party only, secure against malicious adversaries. The protocol relies on an offline trusted third party $\mathcal{F}_{\text{offline}}^e$, that generates the garbled circuit during the preprocessing phase; the parties then evaluate that garbled circuit during the execution phase. Next, in Section 4, we define a Δ -delayed fairness where a malicious party can delay the output of the honest party by at most a factor of Δ . We then construct a protocol with output at both parties, using as a building block, a two-party protocol secure against malicious adversaries with output at one party, that we constructed in Section 3. The resulting fair protocol involves a resolver $\mathcal{F}_{\text{Resolve}}$ only in case one of the parties misbehaves, or in case of faults. The resolver is oblivious and optimistic, and performs the resolution without learning the private inputs or outputs of the participants. Even if the resolver is malicious, and deviates from the protocol or colludes with one of the parties, it can only breach fairness, but confidentiality and integrity of the inputs and the corresponding outputs of the parties are ensured, and the resolver cannot make the honest party accept an incorrect output; this is a direct implication of the fact that the resolver is oblivious, and its view is comprised of the private inputs and outputs of the parties encrypted and authenticated with their respective secret keys.

We separate the functionalities of the third parties since we believe this to be a reasonable approach in practice. However, we note that it is also possible to use one entity, if it is sufficiently trusted by both participants, to perform all the functionalities.

1.2 Related Work

There are many works, beginning with Yao [34], investigating two-party secure computation. Yao’s work showed that any two-party function can be securely evaluated, while ensuring privacy and correctness, by using garbled circuits, but only against passive adversaries, i.e., when honest or semi-honest behaviour of the participants is assumed. This was extended by Goldreich et al. [18] to ensure security against malicious adversaries, and several works improved efficiency [7, 27, 24, 9].

In malicious model, an adversary can always abort after receiving its output and before the honest party receives output. Cleve [10] showed that fairness cannot be achieved for general computation without an honest majority. Hence, different approaches towards achieving fairness for general computations were considered. One approach, the gradual release, see [6, 3, 11, 5, 20, 12, 32, 15, 21], considers a relaxed notion of fairness, where the output is revealed gradually, and a cheating party does not obtain a significant advantage over the honest party, by aborting early. In order to release the output gradually many rounds of interaction are required, which may render this approach impractical for realistic applications.

Another approach is to use a trusted third party, preferably, with limited trust and/or limited involvement. This approach is highly efficient compared to the gradual release of secrets and allows to restore complete fairness in case one of the parties aborts. In particular, *optimistic* protocols involve the third party only in case one of the parties misbehaves. In [25], Lindell considered a relaxed notion of fairness, and presented the *legally enforceable fair* secure two-party computation, using trusted third parties. An outcome of the protocol is that either both parties receive the output, or only one receives the output while the other receives a digitally signed check from the other party which can be then used at a court of law or a bank. In contrast to optimistic model, [25] provides a weaker security guarantee by allowing an adversary to breach fairness.

Optimistic protocols were mostly proposed for specific tasks, esp. fair exchange [1, 2, 29]. Cachin and Camenisch, [7], presented optimistic fair secure computation protocol, with constant number of interactions. Our protocols essentially improve over this earlier work, in efficiency, see comparison and analysis in Section 4.2.1, provable security, and most notably, by allowing commitment to the computation.

Organisation

In Section 2 we present the preliminaries (model, notations, building blocks). In Section 3, we present a basic building block used by our protocols: an efficient, practical protocol to securely compute any two-party functionality,

using a third party, but limiting the involvement of the third party to preprocessing prior to receiving inputs, i.e., off-line. In Section 4 we present an optimistic fair secure computation protocol. The resulting protocol is practical - simple, efficient and *optimistic*, i.e., it makes use of a weakly trusted third party only when faults occur. It improves on the known optimistic secure computation protocol of [7] in efficiency and security¹. In Section 5 we define ideal functionality for committed fair secure computation, and present a protocol realising it.

2 Preliminaries

This section presents the model along with cryptographic assumptions and notations.

Model

We present simulation based security definitions and prove security of our protocols in the universal composability framework, which ensures that security of the protocols is maintained under a composition with arbitrary other protocols in the system, see [8] for more details. The functionality expected from the protocol is captured by a universally trusted party, that performs the computation on behalf of the participants. The algorithm run by the trusted party is called an ideal functionality. The protocol is secure if real protocol execution can be emulated by the ideal functionality. In real protocol execution, the parties run the protocol and the adversary controls the communication channels and the corrupt parties. We consider static corruptions, i.e., corrupted party is fixed prior to protocol execution; and assume malicious and semi-honest adversaries. Malicious adversary can arbitrarily deviate from the protocol, while semi-honest adversary follows the prescribed steps of the protocol, but may try to infer additional information based on its view, and all intermediate steps of the protocol.

We assume synchronous communication model with bounded delay. Let Δ_C be a bound on the channel communication delay, then $\zeta(\Delta_C)$ (for some function ζ) is the maximal waiting time. For instance, after sending a message to Alice, Bob has to wait $\zeta(\Delta_C) = 2\Delta_C$, for his message to reach Alice and for Alice's response to arrive to him. We assume faulty channels between Alice and Bob and that messages that the parties exchange may be lost or delayed by at most a factor of $\zeta(\Delta_C)$. We assume ideal channels between ideal functionalities and participants in the protocol, i.e., the messages are never lost and are delivered within the assumed delay bound.

Notations and Building Blocks

In all our constructions we use an authenticated encryption scheme $(\mathcal{K}, \mathcal{E}, \mathcal{D})$ to ensure confidentiality and integrity of the inputs and outputs of the participants. For ease of exposition, we consider the message authentication code (MAC) key and the secret encryption key as one key K comprised of K_1 for authentication and K_2 for encryption, e.g., see authenticated encryption in [4]; an alternative implementation can be based on a one-time pad encryption with information theoretic MAC, see [27]. When applying $\mathcal{E}_{K_P}(x)$ we perform an authenticated encryption of input x using the key K_P of party P .

We use a non-malleable encryption (see [13] for details) $(\mathcal{N}\mathcal{G}, \mathcal{N}\mathcal{E}, \mathcal{N}\mathcal{D})$ to ensure fairness, and a signature scheme $(\mathcal{G}, \mathcal{E}, \mathcal{D})$, to ensure integrity. When validating authenticated inputs, we use \perp to denote authentication failure. In subsequent sections we use ideal functionality $\mathcal{F}_{\text{ot}}^2$ (a functionality implementing a two-party (1-2) oblivious transfer protocol), and \mathcal{F}_{ca} (representing certification authority).

3 Secure Two-Party Computation in Malicious Setting

Two-party computation involves two parties, Alice and Bob, that wish to evaluate a common function on their private inputs, while ensuring privacy of inputs and integrity of computation (correctness), see e.g., [26, 27], for standard definitions of two-party computation. In this section we consider functionalities with output only at Bob (the circuit evaluator). Let $e : \{0, 1\}^n \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ be a two-party functionality, and let a, b be the inputs of Alice and Bob respectively. Then, after evaluating the functionality e on a and b , Bob obtains $e(a, b)$, while Alice learns nothing at all.

Secure function evaluation based on garbled circuits, see [34], allows to perform such a computation in a secure manner, i.e., ensuring privacy, correctness and inputs independence (see proof in [26]). Specifically, during the generation phase, Alice (the originator) constructs the garbled circuit, and then during protocol execution,

¹Security is not proven in [7], in fact, their protocol appears amenable to 'input corruption' attack, where a party holding the encodings of bits, corrupts the encoding of the 0 value of an input bit, to detect the bit its peer has provided in an input to the oblivious transfer protocol.

Alice transfers the circuit along with the encodings of the inputs, to Bob, that evaluates the circuit and obtains the result. The basic protocol based on Yao’s garbled circuits, ensures security only against semi-honest adversaries, i.e., adversaries that follow the steps of the protocol, but may try to infer additional information from the inputs-outputs. When considering malicious adversaries, additional security concerns arise. In particular, Alice may attempt to expose secret inputs of Bob by providing incorrect encodings of his input bits, and based on Bob’s reaction (abort or successful completion of protocol) will learn his input. Alternately, Alice may provide an incorrect circuit, e.g., one that computes a different function which may expose the input of Bob. Although, any two-party protocol can be securely computed in the malicious setting, e.g., see [18, 16], they are inefficient for practical purposes, and a series of works [30, 33, 27, 31] attempt to improve on the efficiency, by reducing the computation and the communication complexity, as well as the number of rounds required by the two-party protocol, see Section 3.2.1 for comparison. We take an alternative approach, and attempt to improve efficiency by using an additional offline third party, with reduced trust, i.e., it does not learn anything about the inputs of the participants or of the result of the computation.

3.1 Offline Functionality $\mathcal{F}_{\text{offline}}^e$

An Offline Party functionality $\mathcal{F}_{\text{offline}}^e$, in Algorithm 1, is used during the preprocessing phase to ensure privacy and correctness against malicious Alice. The functionality $\mathcal{F}_{\text{offline}}^e$ runs with two security parameters n and s (presented below), and is parametrised by a function $e : \{0, 1\}^n \times \{0, 1\}^n \rightarrow \{0, 1\}^n$. Upon inputs ID_A, ID_B from Alice (the originator) and Bob (the circuit evaluator) respectively, $\mathcal{F}_{\text{offline}}^e$ generates a garbled circuit C that computes e . Then it modifies the circuit C to a circuit \mathbf{C} where each input wire of Bob is replaced with a XOR-gate with s input wires; Bob later uses this redundancy, to thwart the attempts by a malicious Alice to expose his secret inputs, by providing Bob with incorrect random strings for input his values (during the oblivious transfer protocol); see [27] for details. Next, $\mathcal{F}_{\text{offline}}^e$ garbles the circuit \mathbf{C} , by selecting random encodings for each possible value of each of Alice’s and Bob’s input and output bits, and sends the random input strings (corresponding to all possible inputs) to Alice, and the garbled gates and output decryption tables to Bob². The fact that a trusted party generates the circuit ensures that the garbled circuit computes the correct function.

Input: ID_A from Alice, or ID_B from Bob, security parameters n, s

Registration Phase

- generate signature key-pair: $(vk_T, sk_T) \leftarrow \mathcal{G}(1^n)$
- register the verification key: $(\text{register}, \text{offline}, vk_T)$ to \mathcal{F}_{ca}

end

Computation Phase

1. Construct a circuit C that computes e
2. Construct \mathbf{C} from C , by replacing each input wire of Bob with a XOR-gate of s new input wires of Bob
3. Garble the resulting circuit \mathbf{C} and obtain \mathcal{C} , consisting of:
 - a. Random strings corresponding to all possible input bits of Alice: $\mathcal{K}_A = ((\mathcal{K}_A^0[0], \mathcal{K}_A^1[0]), \dots, (\mathcal{K}_A^0[n], \mathcal{K}_A^1[n]))$
 - b. Random strings corresponding to all possible input bits of Bob: $\mathcal{K}_B = ((\mathcal{K}_B^0[0], \mathcal{K}_B^1[0]), \dots, (\mathcal{K}_B^0[sn], \mathcal{K}_B^1[sn]))$
 - c. Garbled boolean tables \mathcal{T}_G for each garbled gate G of the circuit C
 - d. Output decryption tables \mathcal{T}_D mapping output strings to bits
4. Sign the random input strings \mathcal{K}_A of Alice: $\bar{\sigma}_A = ((\sigma_A^0[0], \sigma_A^1[0]), \dots, (\sigma_A^0[n], \sigma_A^1[n]))$ where $\forall i, j, \sigma_A^j[i] = \mathcal{S}_{sk_T}(\mathcal{K}_A^j[i], i)$
5. Sign the random input strings \mathcal{K}_B of Bob: $\bar{\sigma}_B = ((\sigma_B^0[0], \sigma_B^1[0]), \dots, (\sigma_B^0[sn], \sigma_B^1[sn]))$ where $\forall i, j, \sigma_B^j[i] = \mathcal{S}_{sk_T}(\mathcal{K}_B^j[i], i, j)$

end

Output: send $(\mathcal{K}_A, \bar{\sigma}_A), (\mathcal{K}_B, \bar{\sigma}_B)$ to Alice
send $\mathcal{T}_G, \mathcal{T}_D$ to Bob

Algorithm 1: The functionality $\mathcal{F}_{\text{offline}}^e$ for generating a garbled circuit \mathcal{C} that computes e , in order to ensure integrity of computation and prevent exposure of the input of Bob.

3.2 Secure Two-Party Protocol Against Malicious Adversaries

We present an implementation, in Algorithm 2, of Yao’s protocol using an offline third party, in Algorithm 1 for the preprocessing phase. The protocol allows for output at Bob only and securely realises two-party computation

²Depending on the application, e.g., if Bob is not available during the preprocessing phase, $\mathcal{F}_{\text{offline}}^e$ can send both the tables encoding all possible inputs and the circuit to Alice. In this case $\mathcal{F}_{\text{offline}}^e$ also has to sign the circuit, i.e., the garbled tables.

against static malicious adversaries with security with abort (see [25, 21, 22] for standard definition of security with abort). The phase ensures that the circuit was correctly constructed and prevents cheating by either party, essentially avoiding the computation and communication overhead, which are required against malicious adversaries. Next, at the execution phase, Alice sends the strings representing her input to Bob, and runs an oblivious transfer protocol with Bob for his input bits. Once Bob obtains all the inputs, he evaluates the function, and obtains the result of the computation, thus concluding the protocol.

Other instantiations of $\mathcal{F}_{\text{offline}}^e$ can be used: e.g., to reduce the trust in Offline Party, the generation of the circuit can be distributed among n offline parties, by having them run a multi-party protocol, and as long as at least t ($t < n$) out of n parties are honest, the circuit is correctly generated. Alternately, we can avoid the use of third parties entirely; the $\mathcal{F}_{\text{offline}}^e$ functionality can be implemented with a secure two-party computation protocol; e.g., [31, 27].

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Input: security parameters  $n, s$ 
Output:  $y_B = e(a, b)$ 
Offline Generation Phase
  Alice receives  $\bar{a} = [a_i]_{i=1}^n$ 
  Bob receives  $\bar{b} = [b_i]_{i=1}^n$ 
   $(b_1^1, \dots, b_s^1, \dots, b_1^n, \dots, b_s^n) \leftarrow \text{encodeInput}(\bar{b})$ 
  (see implementation in Algorithm 8)
  Alice and Bob send  $\text{ID}_A, \text{ID}_B$  (respectively) to  $\mathcal{F}_{\text{offline}}^e$ 
  Alice receives  $(\bar{\mathcal{K}}_A, \bar{\sigma}_A), (\bar{\mathcal{K}}_B, \bar{\sigma}_B)$ 
  Bob receives  $\bar{\mathcal{T}}_G, \bar{\mathcal{T}}_D$ 
end
Computation Phase
  Alice: sends to Bob:  $((\mathcal{K}_A^{a[0]}[0], \sigma_A^{a[0]}[0]), \dots, (\mathcal{K}_A^{a[n]}[n], \sigma_A^{a[n]}[n]), (\forall i, \mathcal{K}_A^{a[i]}[i] \in \bar{\mathcal{K}}_A, \sigma_A^{a[i]}[i] \in \bar{\sigma}_A)$ 
  Bob:
    send (retrieve, offline) to  $\mathcal{F}_{\text{ca}}$  and obtain  $vk_T$ 
    if  $\exists (\mathcal{K}_A^{a[i]}[i], \sigma_A^{a[i]}[i]), s.t., \mathcal{V}_{vk_T}(\mathcal{K}_A^{a[i]}[i], i, \sigma_A^{a[i]}[i]) = \text{false}$  then
      | output  $\perp$  and halt
    for  $i \leftarrow 1$  to  $n \cdot s$  do
      | run with Alice  $\mathcal{F}_{\text{ot}}^2((\mathcal{K}_B^0[i], \sigma_B^0[i]), (\mathcal{K}_B^1[i], \sigma_B^1[i]), b'_i)$ 
      | //run oblivious transfer, Alice provides  $(\mathcal{K}_B^0[i], \sigma_B^0[i]), (\mathcal{K}_B^1[i], \sigma_B^1[i])$  and Bob  $b'_i$ 
      | receive  $(\mathcal{K}_B^{b'[i]}[i], \sigma_B^{b'[i]}[i])$ 
      | if  $\mathcal{V}_{vk_T}(\mathcal{K}_B^{b'[i]}[i], \sigma_B^{b'[i]}[i]) == \text{false}$  then
        | | output  $\perp$  and halt
      |  $(y_B = (y_B[0], \dots, y_B[n])) \leftarrow \mathcal{C}(\bar{\mathcal{K}}_A, \bar{\mathcal{K}}_B)$ 
      | (see implementation in Algorithm 8)
    end
end

```

Algorithm 2: Secure Two Party Protocol Π_e^E in the $(\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{\text{ot}}^2, \mathcal{F}_{\text{ca}})$ -hybrid model, for computing $e(a, b) = y_B$, where $e : \{0, 1\}^n \times \{0, 1\}^n \rightarrow \{0, 1\}^n$.

Claim 1 Let $e : \{0, 1\}^n \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ be a polynomial time two-party functionality. Assume that the signature scheme $(\mathcal{G}, \mathcal{S}, \mathcal{V})$ is existentially unforgeable under chosen-message attack. Then protocol Π_e^E securely realises a two-party functionality with abort, with output at Bob only, in the presence of malicious static adversaries in the $(\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{\text{ot}}^2, \mathcal{F}_{\text{ca}})$ -hybrid model with abort.

Proof: see Appendix, Section A.1, Propositions 4 and 5.

3.2.1 Efficiency Analysis and Comparison

The classical way of producing two-party protocols secure against malicious adversaries, see [17], is based on running a zero-knowledge protocol, see [18, 19], which renders them inefficient for practical purposes. In [30] the authors apply the cut-and-choose approach to Yao's protocol, which reduces the probability of evaluating an incorrect circuit, and the efficiency is correlated to the cheating probability; specifically, their protocol has a communication overhead of $\mathcal{O}(s|C| + sn^2)$ (where n is the number of input bits to the circuit C and s is the statistical security parameter). Then [33] improved the communication complexity of [30] to $\mathcal{O}(s|C|)$ using expanders. However as [27] observed the protocol in [30] is susceptible to 'input corruption' attack (see [27] for details); [27] also present

a protocol with roughly the same communication complexity as [30], of $\mathcal{O}(s|C| + s^2n)$ (this protocol was also implemented in [28]). Another improvement to two-party computation in malicious setting was made by [24] using homomorphic encryption; their protocol has a constant number of rounds, and has a communication complexity of $\mathcal{O}(|C|)$ (cf. $\mathcal{O}(s|C| + s^2n)$ in [27]) and computational complexity of $\mathcal{O}(|C|)$ (as opposed to $\mathcal{O}(n)$ in [27]). Subsequently, the work of [31], also followed the cut-and choose approach in a different manner and improved the complexity to $\mathcal{O}(\frac{s|C|}{\log(|C|)})$.

Our protocol, in Algorithm 2, is computationally efficient as it uses public key operations only for signing (by $\mathcal{F}_{\text{offline}}^e$) and verifying (by Bob) the strings supplied by Alice to Bob, and for oblivious transfer (for every input bit of Bob). The communication and computational overhead is $\mathcal{O}(|C|)$ (roughly as that of the original Yao’s protocol). Specifically during the (offline) preprocessing the $\mathcal{F}_{\text{offline}}^e$ sends the corresponding random strings and tables of the circuit to Alice and Bob, then during the execution Alice sends to Bob strings corresponding to her input, and they run an oblivious transfer protocol only for every input bit of Bob. Note that we added (to the original construction of Yao’s protocol) the signatures on input strings of Bob by the $\mathcal{F}_{\text{offline}}^e$ during the preprocessing phase, and a verification thereof later by Bob. Thus the resulting protocol is of similar computational and communication complexity as the construction of Yao’s garbled circuit, [34, 26]. Our protocol is efficient in that it has only a constant number of rounds and uses one oblivious transfer per input bit only. This is in contrast to the complexity of [27], which due to the cut-and-choose incur a multiplicative increase by a factor of s (the statistical security parameter) and results in communication complexity of $\mathcal{O}(s|C| + s^2n)$. Note that our protocol allows general two-party computation, and efficiency can be further improved by adjusting our protocols to specific tasks.

4 Fair Two-Party Protocol Against Malicious Adversaries

Often protocols are required to allow for output at both parties, which requires an additional property of fairness. Specifically, Alice receives her output if and only if Bob receives his, or no party receives the output. Fairness is trivial to achieve in honest or semi-honest setting. However, this is not so when considering malicious adversaries that may arbitrarily deviate from the protocol.

In Algorithm 5, we present an optimistic weakly trusted (oblivious) third party, involved only for resolution in case one of the parties misbehaves. We believe that the model based on the separation between the functionality the offline generation and evaluation phases, is suitable for protocols that are to be run by ad-hoc parties in order to execute a variety of transactions over the Internet, while ensuring privacy, correctness and fairness³. Specifically, the (offline) third party that is used during the generation phase, ensures correctness and privacy, and the optimistic third party, involved during the evaluation phase in case of malicious behaviour, ensures fairness of the computation. The third parties do not learn anything about the inputs or the result of the computation.

We define the $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ functionality in Algorithm 3, and in Algorithm 4 we construct a protocol Π_f^F that realises it. Specifically, protocol Π_f^F computes functionality $f(a, b) = (f_A(a, b), f_B(a, b))$, where $f : \{0, 1\}^m \times \{0, 1\}^m \rightarrow \{0, 1\}^m \times \{0, 1\}^m$, providing output at both Alice and Bob while ensuring Δ -delayed fairness, i.e., either no one receives output or both participants do, such that honest party’s output will be delayed by at most a factor of Δ . To construct Π_f^F we use the protocol Π_e^E , in Section 3 (Algorithm 2), that allows to compute securely any functionality $e : \{0, 1\}^n \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ with output only at Bob. Then $\mathcal{F}_{\text{offline}}^e$ generates circuits that produce output encrypted with the key ek_R . We use Π_e^E to evaluate a family of functions $\mathbb{E} = \{e_{ek_R}\}_{ek_R \in \mathcal{NG}(1^n)}$, i.e., functions defined by a public encryption key. Let $(dk_R, ek_R) \leftarrow \mathcal{NG}(1^n)$ be the key pair of the resolver $\mathcal{F}_{\text{Resolve}}$ (see Algorithm 5). We take the function e for Π_e^E (that provides output at Bob only) to be the function computing the following: $e_{ek_R}((a, K_A), (b, K_B)) = \mathcal{N}\mathcal{E}_{ek_R}(c_A || c_B) || (\mathcal{E}_{K_A}(f_A(a, b), c_B))$, where $c_A = \mathcal{E}_{K_A}(f_A(a, b))$ and $c_B = \mathcal{E}_{K_B}(f_B(a, b))$.

4.1 Δ -delayed fairness

In Algorithm 3 we present the notion of Δ -delayed fairness, where either both parties receive the output or no one does, and a corrupt party can delay the output of the honest party by at most a factor of Δ . In our definition Alice receives her output first (the case where Bob receives output first is symmetric), and should send to Bob his output. If Alice responds with fair the ideal functionality sends the output to Bob. If Alice responds with unfair or does not respond, the functionality waits the remaining time for the maximal delay of $\Delta = 4\Delta_C$, and sends the output to Bob.

³We note that having one party perform all the functionalities is also possible, albeit, less appealing in practice, due to required trust (by everyone) in one such entity.

```

Input:  $n, \Delta_C, \Delta$ 
          $a$  from Alice,  $b$  from Bob
Computation Phase
  if  $a == \perp \vee b == \perp$  then
    | send  $\perp$  to Alice and to Bob, and halt
  else
    | send  $y_A = f_A(a, b)$  to Alice
    | sleep('wait for response',  $2\Delta_C$ )
    | onReceive(fair)
    |   stopTimer('wait for response')
    |   send( $y_B = f_B(a, b)$ ) to Bob
    |   onWakeup('wait for response')
    |   sleep( $\Delta - 2\Delta_C$ )
    |   send( $y_B = f_B(a, b)$ ) to Bob
  end

```

Algorithm 3: The ideal functionality $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ for computing a function $f(a, b) = (f_A(a, b), f_B(a, b))$ in Δ -delayed fairness model, running with Alice and Bob, and an adversary S .

4.2 Fair Two-Party ($\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{ca}, \mathcal{F}_e$)-Hybrid Protocol Π_f^F

In Algorithm 4 Alice and Bob retrieve the public encryption key ek_R of the resolver $\mathcal{F}_{\text{Resolve}}$ which defines the function that they agree to compute. At the execution, Alice has input a and Bob has input b ; they both generate secret keys, K_A and K_B respectively, for symmetric authenticated encryption $(\mathcal{K}, \mathcal{E}, \mathcal{D})$, that will protect their corresponding outputs; then they run a protocol Π_e^E and provide their inputs, $(a||K_A)$ and $(b||K_B)$ respectively. The protocol Π_e^E evaluates the function over the inputs and generates output at Bob. The output consists of two parts: one encrypted with Alice's key and another encrypted with the key ek_R of the $\mathcal{F}_{\text{Resolve}}$ (containing both the output of Bob and of Alice). The output part of the $\mathcal{F}_{\text{Resolve}}$ is encrypted with a non-malleable encryption scheme $(\mathcal{NG}, \mathcal{NE}, \mathcal{ND})$ (see [13] for details) and is used in case of malicious behaviour, for resolution (non-malleability is required to ensure that the output cannot be maliciously altered in a meaningful way). Since Bob performed the computation, he is assured that the output is constructed correctly. Bob sends the output (encrypted with Alice's key) to Alice. If Alice does not respond, Bob contacts the resolver with the part of the output encrypted with the key of the resolver. The $\mathcal{F}_{\text{Resolve}}$ validates, decrypts and sends to Alice her output, and to Bob his (restoring fairness).

Upon receipt of an output from Bob, Alice validates and decrypts her part of the output and Bob's output encrypted with his secret key. Alice then sends this part to Bob, who validates and decrypts the result, which concludes the protocol.

Claim 2 *Let $f : \{0, 1\}^m \times \{0, 1\}^m \rightarrow \{0, 1\}^m \times \{0, 1\}^m$ be a polynomial two-party functionality, let $(\mathcal{K}, \mathcal{E}, \mathcal{D})$ be a secure symmetric authenticated encryption scheme, and let $(\mathcal{NG}, \mathcal{NE}, \mathcal{ND})$ be a secure non-malleable encryption scheme. Then, the protocol Π_f^F securely realises $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ in the presence of malicious static adversaries in the $(\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{ca}, \mathcal{F}_e)$ -hybrid model with Δ -delayed fairness.*

Proof: see Appendix, Section A.2, Propositions 6 and 7.

4.2.1 Efficiency Analysis and Comparison

There are two central approaches to achieving fairness, the *gradual release* of secrets and the *optimistic model*. The gradual release imposes high communication complexity (even in case the parties are honest). A two-party protocol, for general functions, based on gradual release (with the number of rounds proportional to the security parameter) was presented in [32]. The optimistic model relies on a third party that is involved in case of misbehaviour to restore fairness. In [7], the authors designed an efficient optimistic fair protocol using proofs of knowledge. The number of rounds in their protocol is constant, and does not depend on the security parameter. Yet their protocol incurs a significant efficiency degradation, since the zero-knowledge proofs are required for every gate of the circuit, resulting in $\mathcal{O}(s|C|)$ communication and computational complexity. Furthermore, the protocol of [7] seems to be susceptible to 'inputs corruption' attack, whereby Alice corrupts one of the inputs to oblivious transfer protocol, and based on the behaviour of Bob learns the corresponding value of his input bit. In addition, the work of [7] lacks a full proof of security. We are not aware of other works that provide fairness for general computations.

In our protocol, when the parties are honest and follow the steps of the protocol (which is the typical case), the computation complexity is roughly as that of the Yao's original protocol (see Section 3.2.1 for discussion and

Input: security parameters n, s , maximal communication delay Δ_C , $a = [a_i]_{i=1}^n$ from Alice, $b = [b_i]_{i=1}^n$ from Bob

Output: $y = (y_A, y_B)$

Alice and Bob send (retrieve, resolve) to \mathcal{F}_{ca} and obtain ek_R (each)

Computation Phase

```

Alice and Bob do:
  generate secret keys  $K_A$  and  $K_B$  respectively
  run a protocol  $\Pi_{ek_R}^E(a||K_A, b||K_B)$  (in Algorithm 2)
  Alice provides  $(a||K_A)$  and Bob provides  $(b||K_B)$ 

Bob:
  onReceive( $y_B$ )
  if ( $y_B == \mathcal{E}_{K_A}(f_A(a, b), c_B) || \mathcal{N}_{\mathcal{E}_{ek_R}}(c_A, c_B)$ ) then
    send( $\mathcal{E}_{K_A}(f_A(a, b), c_B)$ ) to Alice
    sleep('time to Alice',  $2\Delta_C$ )
  else output  $\perp$  and halt
  onReceive( $c_B$ )
  if ( $c_B == \text{valid}$ ) then
    stopTimer('time to Alice')
    recover and output  $y_B = f_B(a, b)$ 
  onWakeup('time to Alice')
  send  $\mathcal{N}_{\mathcal{E}_{ek_R}}(c_A, c_B)$  to  $\mathcal{F}_{\text{Resolve}}$ 
  onReceive( $c_B$ )
  stopTimer('time to  $\mathcal{F}_{\text{Resolve}}$ ')
  recover and output  $y_B = f_B(a, b)$ 
end

Alice:
  onReceive( $c$ )
  if ( $c == \text{valid}$ ) then
    recover and output  $y_A = f_A(a, b)$ 
    if ( $c == \mathcal{E}_{K_A}(f_A(a, b), c_B)$ ) then
      send( $c_B$ ) to Bob
  end
end
end
end

```

Algorithm 4: Secure Two Party Protocol Π_f^F in the $(\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{ca}, \mathcal{F}_e)$ -hybrid model for computing $f(a, b) = (f_A(a), f_B(b))$, where $f : \{0, 1\}^m \times \{0, 1\}^m \rightarrow \{0, 1\}^m \times \{0, 1\}^m$.

Input: n

generate encryption key-pair: $(dk_R, ek_R) \leftarrow \mathcal{NG}(1^n)$

register the encryption key: (register, resolver, ek_R) to \mathcal{F}_{ca}

Computation Phase

```

  receive  $c$ 
  set  $y_A = \perp, y_B = \perp$ 
  if  $\mathcal{N}_{\mathcal{D}_{dk_R}}(c) \neq \perp$  then
     $(y_A, y_B) \leftarrow \mathcal{N}_{\mathcal{D}_{dk_R}}(c)$ 
end

```

Output: send y_A to Alice
send y_B to Bob

Algorithm 5: The ideal functionality $\mathcal{F}_{\text{Resolve}}$

analysis). When one of the parties misbehaves, the protocol requires an additional round, to send the encrypted result to the resolver and to receive a decrypted response back.

5 Committed Two-Party Computation

Fairness alone may not suffice for some applications, since, a participant may decide to abort the protocol, or to provide an invalid input to the computation. Such an outcome may not be plausible in many applications, e.g., online market. Furthermore, parties often agree to participate in a computation in advance, possibly before they have inputs to that computation, by exchanging each others commitments, e.g., by signing a contract together. The commitment phase should ensure fairness and prevent a malicious party from aborting after it receives its commitment, if the honest party has not received a commitment. In addition, the commitments should be validated to prevent the malicious party from providing an invalid commitment, e.g., one that expired. Fairness does not encompass these requirements. We introduce the \mathcal{F}_{tea} (trusted enforcement authority), in Algorithm 7, that enforces guaranteed output, by compensating the honest party in case of failure to participate by the other.

For applications based on the client-server architecture, it suffices to ensure one sided, asymmetric, commitment,

since most Internet transactions are asymmetric. We focus on symmetric commitments, where both parties commit to participate in a protocol. We define the symmetric commitment functionality, ensuring guaranteed output delivery, in Algorithm 6, and then construct a protocol, in Algorithm 8, realising it.

5.1 Committed Two-Party Computation Functionality $\mathcal{F}_{\text{committed-computation}}^{v,g}$

The committed two-party computation functionality $\mathcal{F}_{\text{committed-computation}}^{v,g}$, in Algorithm 6, consists of two-phases: during the first phase the parties provide their respective commitments, a_1 and b_1 , e.g., compensations, to the ideal functionality. The functionality validates the commitments (using v_1) and if valid sends the corresponding commitments to Alice and Bob, and proceeds to second phase. During the second phase, the parties provide their inputs a_2 and b_2 , which are again validated (using v_2) against the commitments from the first phase (along with the time when each input was received); v_1 and v_2 are validation predicates used in first and second phases respectively. In case one of the inputs is invalid, the party with the valid input is compensated (by recovering the commitment of the other). Then if validation succeeds, the functionality evaluates the inputs over the agreed function g , and sends the result to Bob (since he is the first to receive the output). If Bob is malicious he can delay the output of Alice by at most a factor of $4\Delta_C$, by responding with unfair (or not responding at all). Otherwise, the functionality sends the output to Alice without additional delay.

During the second phase the functionality may not receive inputs from both parties at the same time. Thus upon input from one party, it records the time, and waits for input from the other party; if no input from the other party arrives within the interval defined in the validation function, the functionality validates the input that it received (along with the commitment of the other party) and if valid, recovers the commitment and grants it to the party which participated correctly.

```

Input:  $n$ , maximal channel delay  $\Delta_C$ , fairness delay  $\Delta$ 
Commitment Phase
  Input:  $a_1$  from Alice,  $b_1$  from Bob
   $v_1(a_1, b_1) == (y_A^1, y_B^1)$ 
  if  $y_A^1 == \perp \vee y_B^1 == \perp$  then
    | send  $\perp$  to Alice and Bob and halt
  else
    | send  $y_A^1, y_B^1$  to Alice and Bob respectively
  end
Computation Phase
  onReceive( $a_2$ ) from Alice
     $t_A \leftarrow \text{getTime}()$ 
    sleep('wait for input from Bob')
    onWakeup('wait for input from Bob')
      if  $(v_2(a_2, y_A^1, t_A, \text{getTime}()) \neq \perp)$  then
        send  $(b_1)$  to Alice
      if  $v_2(a_2, y_A^1, t_A, t_B) == \perp$  then
        | send  $a_1$  to Bob and halt
      if  $v_2(b_2, y_B^1, t_A, t_B) == \perp$  then
        | send  $b_1$  to Alice and halt
       $(y_A^2, y_B^2) \leftarrow g(a_2, b_2)$ 
      send  $y_B^2$  to Bob
      sleep('wait for response',  $2\Delta_C$ )
      onReceive(fair)
        stopTimer('wait for response')
        send  $(y_A^2)$  to Alice
      onWakeup('wait for response')
        sleep( $\Delta - 2\Delta_C$ )
        send  $(y_A^2)$  to Alice
  end
  onReceive( $b_2$ ) from Bob
     $t_B \leftarrow \text{getTime}()$ 
    sleep('wait for input from Alice')
    onWakeup('wait for input from Alice')
      if  $(v_2(b_2, y_B^1, t_A, \text{getTime}()) \neq \perp)$  then
        send  $(a_1)$  to Bob

```

Algorithm 6: The ideal functionality $\mathcal{F}_{\text{committed-computation}}^{v,g}$ for computing (v, g) with guaranteed output delivery, runs with Alice and Bob, and an adversary S , where $v = (v_1, v_2)$ is inputs validation function used at each phase.

5.2 Two-Party ($\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{\text{ca}}, \mathcal{F}_{\text{tea}}, \mathcal{F}_{\Delta\text{-delayed-fairness}}$)-Hybrid Protocol $\Pi_{(v,g)}^G$

Committed two-party computation, in Algorithm 8, is a two-phase protocol, s.t., during the first phase the parties commit to participate in protocol execution, and in second phase, they evaluate a function over their inputs. Both the commitments and the inputs are validated using validation predicate⁴ v (computed with circuit V). We embed the validation predicate v_2 into function⁵ g ; specifically, if validation fails, g produces \perp . If the commitment of one of the parties is not valid, the execution is terminated. Once the commitment phase completed, the parties can engage in computation of the second phase. At this stage each party holds the commitment by the other, and can contact the trusted enforcement authority functionality \mathcal{F}_{tea} (in Algorithm 7) in case a malicious party fails to participate, or provides an incorrect input to the computation. The \mathcal{F}_{tea} attempts to complete the protocol with the other party on behalf of the party originating the resolution. In case of failure, the \mathcal{F}_{tea} opens the commitment and sends it to the originating party. Otherwise, it concludes the protocol, and returns the result of the computation to the originating party. Let Π_f^F (Algorithm 4) be a protocol that computes $f : \{0, 1\}^m \times \{0, 1\}^m \rightarrow \{0, 1\}^m \times \{0, 1\}^m$, and allows for output at both parties, while ensuring fairness, and let $\mathcal{F}_{\text{offline}}^e$ be a functionality defined in Algorithm 1. To construct protocol $\Pi_{(g,v)}^G$ with output at both parties, we use Π_f^F during the commitment phase (to compute function v), and we use $\mathcal{F}_{\text{offline}}^e$ during the computation phase. The \mathcal{F}_{tea} uses a non-malleable encryption scheme $(\mathcal{NG}, \mathcal{NE}, \mathcal{ND})$, and Alice and Bob use an authenticated encryption scheme $(\mathcal{K}, \mathcal{E}, \mathcal{D})$.

Input: n, s, Δ_C

generates $(ek_T, dk_T) \xleftarrow{R} \mathcal{K}(1^n)$ and sends (register, TEA, ek_T) to \mathcal{F}_{ca}
 send (retrieve, offline) to \mathcal{F}_{ca} and obtains vk_T
 send (retrieve, Alice) to \mathcal{F}_{ca} and obtains vk_A

Computation Phase

```

   $y_B = \perp$ 
  onReceive( $\mathcal{NE}_{ek_T}(\mathcal{EK}_B(a_1))$ )
    send ('garbled inputs') to Alice
    sleep('response from Alice',  $2\Delta_C$ )
  onWakeup('response from Alice')
     $y_B \leftarrow \mathcal{ND}_{dk_T}(\mathcal{EK}_B(a_1))$ 
    send ( $y_B$ ) to Bob
  onReceive( $((\mathcal{K}_A^a, \bar{\sigma}_A^a), (\mathcal{K}_B, \bar{\sigma}), \mathcal{NE}_{ek_T}(\mathcal{EK}_A(b_1)))$ )
  if  $\forall i : (\mathcal{V}_{vk_T}(\mathcal{K}_A^{a[i]}[i], \bar{\sigma}_A^{a[i]}[i]) \neq \perp) \vee (\mathcal{V}_{vk_T}(\mathcal{K}_B^{b[i]}[i], \bar{\sigma}_B^{b[i]}[i]) \neq \perp)$  then
    send  $(\mathcal{K}_A^a, \bar{\sigma}_A^a)$  to Bob
    for  $i \leftarrow 1$  to  $n \cdot s$  do
      run  $\mathcal{F}_{\text{ot}}^2((\mathcal{K}_B^0[i], \sigma_B^0[i]), (\mathcal{K}_B^1[i], \sigma_B^1[i]), b_i)$  with Bob, Bob receives  $(\mathcal{K}_B^{b[i]}[i], \sigma_B^{b[i]}[i])$ 
    sleep('time to Bob',  $2\Delta_C$ )
    onReceive( $c_A$ )
    if  $(\mathcal{V}_{vk_A}(c_A, \sigma_A) \neq \perp)$  then
      stopTimer('time to Bob')
      send  $(c_A, \sigma_A)$  to Alice
    onWakeup('time to Bob')
      send  $\mathcal{EK}_A(b_1)$  to Alice
  else
    if  $y_B \neq \perp$  then
      send ( $y_B$ ) to Bob
  end
  end
  
```

Algorithm 7: The ideal functionality \mathcal{F}_{tea}

Claim 3 Let (g, v) be a polynomial two-party functionality, and let $(\mathcal{K}, \mathcal{E}, \mathcal{D})$ be a secure shared key encryption scheme, $(\mathcal{NG}, \mathcal{NE}, \mathcal{DE})$ be a non-malleable encryption scheme, and $(\mathcal{G}, \mathcal{S}, \mathcal{V})$ be an existentially unforgeable under chosen-message attack signature scheme. Then protocol $\Pi_{(v,g)}^G$ securely realises $\mathcal{F}_{\text{committed-computation}}^{v,g}$ in the presence of malicious static adversaries in the $(\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{\text{ca}}, \mathcal{F}_{\text{tea}}, \mathcal{F}_{\Delta\text{-delayed-fairness}})$ -hybrid model with Guaranteed Output Delivery.

Proof: see Appendix, Section A.3, Propositions 8 and 9.

⁴The expiration and validation of time are part of the validation predicate.

⁵We integrate the validation of inputs for the second phase into g for simplicity, and the protocol can be easily extended to support two separate validation functions.

Input: security params n, s , maximal communication delay Δ_C

Commitment Phase

Input: a_1 from Alice, b_1 from Bob

Alice and Bob do:

send (retrieve, tea) to \mathcal{F}_{ca} and both obtain ek_T

run $\Pi_{v_{ek_T}}^F(a_1, b_1)$ (in Algorithm 4), to generate and validate commitments

Bob receives $(\mathcal{N}_{\mathcal{E}_{ek_T}}(\mathcal{E}_{K_B}(a_1)) || \mathcal{E}_{K_B}(v(a_1)))$, Alice receives $(\mathcal{N}_{\mathcal{E}_{ek_T}}(\mathcal{E}_{K_A}(b_1)) || \mathcal{E}_{K_A}(v(b_1)))$

if $((\mathcal{E}_{K_A}(v(b_1)) == \perp \wedge \mathcal{E}_{K_B}(v(a_1)) == \perp) \vee ((v(b_1)) == \perp) \wedge (v(a_1)) == \perp)$ **then**

 Alice and Bob output \perp and halt

end

Computation Phase

Input: a_2 from Alice, b_2 from Bob

Bob encodes b_2 as $(b_1^1, \dots, b_s^1, \dots, b_1^n, \dots, b_s^n)$: $[b'_i]_{i=1}^{n \cdot s} \leftarrow encodeInput(b_2)$

Alice and Bob run functionality $\mathcal{F}_{offline}^e$ (in Algorithm 1) to generate circuit G computing function g

Bob sends (retrieve, offline) to \mathcal{F}_{ca} and obtains vk_T

Alice generates signature key-pair: $(sk_A, vk_A) \leftarrow \mathcal{G}(1^n)$, and registers: (register, Alice, vk_A) with \mathcal{F}_{ca}

Alice sends to Bob her encoded input a_2, K_A, sk_A : $((\mathcal{K}_A^{a[0]}[0], \sigma_A^{a[0]}[0]), \dots, (\mathcal{K}_A^{a[n]}[n], \sigma_A^{a[n]}[n]))$

if $\exists (\mathcal{K}_A^{a[i]}[i], \sigma_A^{a[i]}[i])$, s.t., $\forall_{vk_T} (\mathcal{K}_A^{a[i]}[i], i, \sigma_A^{a[i]}[i]) == \perp$ **then** Bob sends $\mathcal{N}_{\mathcal{E}_{ek_T}}(\mathcal{E}_{K_B}(a_1))$ to \mathcal{F}_{tea}

for $i \leftarrow 1$ **to** $s \cdot n$ **do**

 Alice and Bob run $\mathcal{F}_{ot}^2((\mathcal{K}_B^0[i], \sigma_B^0[i]), (\mathcal{K}_B^1[i], \sigma_B^1[i]), b_i)$, Bob receives $(\mathcal{K}_B^{b[i]}[i], \sigma_B^{b[i]}[i])$

if $\forall_{vk_T} (\mathcal{K}_B^{b[i]}[i], \sigma_B^{b[i]}[i]) == \perp$ **then** Bob sends $\mathcal{N}_{\mathcal{E}_{ek_T}}(\mathcal{E}_{K_B}(a_1))$ to \mathcal{F}_{tea}

Bob:

$((\mathcal{E}_{K_A}(y_A), \sigma_A) || y_B) \leftarrow \mathcal{C}(\bar{\mathcal{K}}_A, \bar{\mathcal{K}}_B)$

(see implementation in **Circuit Evaluation** below)

if $y_B == \perp$ **then** send $\mathcal{N}_{\mathcal{E}_{ek_T}}(\mathcal{E}_{K_B}(a_1))$ to \mathcal{F}_{tea}

else output y_B , send $(\mathcal{E}_{K_A}(y_A), \sigma_A)$ to Alice

onReceive($\mathcal{K}_A^a, \bar{\sigma}^a$) from \mathcal{F}_{tea}

 run \mathcal{F}_{ot}^2 with \mathcal{F}_{tea}

 obtain $\forall i, (\mathcal{K}_B^{b[i]}[i], \sigma_B^{b[i]}[i])$

$((\mathcal{E}_{K_A}(y_A), \sigma_A) || y_B) \leftarrow \mathcal{C}(\bar{\mathcal{K}}_A, \bar{\mathcal{K}}_B)$

 send $(\mathcal{E}_{K_A}(y_A), \sigma_A)$ to \mathcal{F}_{tea}

onReceive($\mathcal{E}_{K_B}(a_1)$) from \mathcal{F}_{tea}

 recover and output a_1

Alice:

sleep('response from Bob', $2\Delta_C$)

onReceive($\mathcal{E}_{K_A}(y_A), \sigma_A$)

if $((\mathcal{E}_{K_A}(y_A), \sigma) \neq \perp)$ **then**

 stopTimer('response from Bob')

 recover and output y_A

onWakeup('response from Bob')

 send $((\bar{\mathcal{K}}_A, \bar{\sigma}_A), (\bar{\mathcal{K}}_B, \bar{\sigma}_B), \mathcal{N}_{\mathcal{E}_{ek_T}}(\mathcal{E}_{K_A}(b_1)))$ to \mathcal{F}_{tea}

 onReceive($\mathcal{E}_{K_A}(b_1)$) from \mathcal{F}_{tea}

 recover and output b_1

onReceive('garbled inputs')

 send $((\bar{\mathcal{K}}_A, \bar{\sigma}_A), (\bar{\mathcal{K}}_B, \bar{\sigma}_B), \mathcal{N}_{\mathcal{E}_{ek_T}}(\mathcal{E}_{K_A}(b_1)))$ to \mathcal{F}_{tea}

Circuit Evaluation

$\mathcal{C}(\bar{\mathcal{K}}_A, \bar{\mathcal{K}}_B) \{$

$(\mathcal{K}_A^{a[0]}[0], \dots, \mathcal{K}_A^{a[n]}[n]) \leftarrow \bar{\mathcal{K}}_A, (\mathcal{K}_B^{b[0]}[0], \dots, \mathcal{K}_B^{b[sn]}[sn]) \leftarrow \bar{\mathcal{K}}_B$

$(\mathcal{K}_Y^{y[0]}[0], \dots, \mathcal{K}_Y^{y[n]}[n]) \leftarrow \bar{\mathcal{T}}_G((\mathcal{K}_A^{a[0]}[0], \dots, \mathcal{K}_A^{a[n]}[n]), (\mathcal{K}_B^{b[0]}[0], \dots, \mathcal{K}_B^{b[sn]}[sn]))$

 return $\omega \leftarrow \bar{\mathcal{T}}_D(\mathcal{K}_Y^{y[0]}[0], \dots, \mathcal{K}_Y^{y[n]}[n]) \}$

end

Input Encoding

$encodeInput([b_i]_{i=1}^n) \{ b' = \emptyset$

for $i \leftarrow 1$ **to** n **do**

 Let $b_1^i, \dots, b_s^i \in_R \{0, 1\}$ s.t. $b_i = b_1^i \oplus \dots \oplus b_s^i$

$b' = b' || b_1^i, \dots, b_s^i$

 return $b' \}$ //after n iterations $b' = [b'_i]_{i=1}^{n \cdot s} = (b_1^1, \dots, b_s^1, \dots, b_1^n, \dots, b_s^n)$

end

end

Algorithm 8: Committed fair secure two-party protocol $\Pi_{(v,g)}^G$ in the $(\mathcal{F}_{offline}^e, \mathcal{F}_{ca}, \mathcal{F}_{tea}, \mathcal{F}_{\Delta\text{-delayed-fairness}})$ -hybrid model for computing $v : \{0, 1\}^m \times \{0, 1\}^m \rightarrow \{0, 1\}^m \times \{0, 1\}^m$ and $g : \{0, 1\}^n \times \{0, 1\}^n \rightarrow \{0, 1\}^n \times \{0, 1\}^n$.

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A Security Proofs

A.1 Security Analysis of Protocol Π_e^E (Section 3.2)

We analyse Π_e in a hybrid model where there is a trusted party computing $\mathcal{F}_{\text{offline}}^e$, $\mathcal{F}_{\text{ot}}^2$ and \mathcal{F}_{ca} . The simulator S interacts with the ideal functionality \mathcal{F}_e and uses the adversary A in a black-box manner, simulating for A the real protocol execution and emulating the ideal functionalities $\mathcal{F}_{\text{offline}}^e$, $\mathcal{F}_{\text{ot}}^2$ and \mathcal{F}_{ca} .

Proposition 4 (Security Against Malicious Alice) *For every polynomial time adversary A corrupting Alice and running with Π_f with abort in a hybrid model with access to $\mathcal{F}_{\text{offline}}^e$, $\mathcal{F}_{\text{ot}}^2$ and \mathcal{F}_{ca} , there exists a probabilistic polynomial-time simulator S corrupting Alice and running in the ideal model with access to an ideal functionality \mathcal{F}_f , such that for every $a, b, z \in \{0, 1\}^*$ holds:*

$$\left\{ \text{IDEAL}_{f, S(z)}(a, b, n) \right\}_{n \in \mathbb{N}} = \left\{ \text{HYBRID}_{\Pi_f, A(z)}^{\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{\text{ca}}, \mathcal{F}_{\text{ot}}^2}(a, b, n) \right\}_{n \in \mathbb{N}}$$

Proof Let A be a malicious static adversary with Alice and Bob running the protocol in Algorithm 2. We construct an ideal model simulator S which has access to Alice and to the trusted party computing \mathcal{F}_e , and can simulate the view of the execution of the protocol. Assume that Alice is corrupted by a hybrid model adversary A . In Algorithm 9 we construct a simulator S given a black-box access to A . The view of A in a simulation with S is identical to its view in an $(\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{\text{ca}}, \mathcal{F}_{\text{ot}}^2)$ -hybrid execution of Π_e with a honest Bob. The joint distribution of A ’s view and Bob’s output in a hybrid execution is identical to the joint distribution of S and Bob’s output in an ideal model. In addition, there is a negligible probability for the adversary to forge the signature, thus the output distribution of the simulator and the honest party in the ideal model is identical to that of the adversary and the honest party in the real protocol execution.

```

S(a, ID_A, 1^n)
  ID_{A'} ←OfflineParty A(a, ID_A, 1^n)
  if ID_{A'} = ⊥ ∨ ID_{A'} ≠ ID_A then
    send ⊥ to the trusted party computing  $\mathcal{F}_f$  as Alice's input
    send ⊥ to A as its input from  $\mathcal{F}_{\text{offline}}^e$ 
    output whatever A outputs and halt
  else
    simulate functionality  $\mathcal{F}_{\text{offline}}^e$  for A:
    1. choose a key pair  $(vk, sk) \leftarrow \mathcal{G}(1^n)$ 
    2. construct a circuit C computing  $f'_A$ 
    3. construct  $\mathbf{C}$  from C, by replacing each input wire of Bob with a xor-gate consisting of s input wires of Bob
    4. garble the resulting circuit C and obtain  $\mathcal{C}$ , consisting of:
      a. Random strings corresponding to all possible input bits of Alice:  $\bar{\mathcal{K}}_A = ((\mathcal{K}_A^0[0], \mathcal{K}_A^1[0]), \dots, (\mathcal{K}_A^0[n], \mathcal{K}_A^1[n]))$ 
      b. Random strings corresponding to all possible input bits of Bob:  $\bar{\mathcal{K}}_B = ((\mathcal{K}_B^0[0], \mathcal{K}_B^1[0]), \dots, (\mathcal{K}_B^0[n], \mathcal{K}_B^1[n]))$ 
      c. Garbled boolean tables  $\bar{\mathcal{T}}_G$  for each garbled gate G of the circuit C
      Output decryption tables  $\bar{\mathcal{T}}_D$  mapping output strings to bits
    5. sign the random input strings  $\bar{\mathcal{K}}_B$  of Bob:  $\bar{\sigma} = S_{sk_T}(\bar{\mathcal{K}}_B)$ , where  $\bar{\sigma} = ((\sigma_0^0, \sigma_0^1), \dots, (\sigma_n^0, \sigma_n^1))$ 
    6. send  $(\bar{\mathcal{K}}_A, (\bar{\mathcal{K}}_B, \bar{\sigma}))$  to A as its output from  $\mathcal{F}_{\text{offline}}^e$ 
    A sends  $\bar{\mathcal{K}}_{A'}$  intended for Bob and  $(\bar{\mathcal{K}}_{B'}, \bar{\sigma}')$  for ideal functionality  $\mathcal{F}_{\text{ot}}^2$ 
    if  $((\bar{\mathcal{K}}_{A'} \neq \bar{\mathcal{K}}_A) \vee ((\bar{\mathcal{K}}_{B'}, \bar{\sigma}') \neq (\bar{\mathcal{K}}_B, \bar{\sigma})))$  then
      send input ⊥ to the trusted party computing  $\mathcal{F}_f$  as Alice's input
      send ⊥ to A as its input from  $\mathcal{F}_{\text{ot}}^2$ 
      output whatever A outputs and halt
    A outputs its view and halts, S outputs the same and halts
  end
end

```

Algorithm 9: Simulator S , simulating the view of Alice.

Proposition 5 (Security Against Malicious Bob) *For every polynomial time adversary A corrupting Bob and running with Π_f with abort in a hybrid model with access to $\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{\text{ot}}^2$ and \mathcal{F}_{ca} , there exists a probabilistic polynomial-time simulator S corrupting Bob and running in the ideal model with access to an ideal functionality computing \mathcal{F}_f , such that for every $a, b, z \in \{0, 1\}^*$ holds:*

$$\left\{ \text{IDEAL}_{f, S(z)}(a, b, n) \right\}_{n \in \mathbb{N}} = \left\{ \text{HYBRID}_{\Pi_f, A(z)}^{\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{ca}, \mathcal{F}_{\text{ot}}^2}(a, b, n) \right\}_{n \in \mathbb{N}}$$

Proof Let A be a malicious static adversary with Alice and Bob running the protocol in Algorithm 2. We construct an ideal model simulator S which has access to Bob and to the trusted party computing \mathcal{F}_f , and can simulate the view of the execution of the protocol. Assume that Bob is corrupted by a hybrid model adversary A . In Algorithm 10 we construct a simulator S given a black-box access to A . The security is based on the fact that the 1-2 oblivious transfer functionality $\mathcal{F}_{\text{ot}}^2$ is secure and as a result Bob learns only a single set of random strings, corresponding to its input. The view of A is identical to its view in a $(\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{\text{ot}}^2, \mathcal{F}_{ca})$ -hybrid execution of protocol Π_f with a honest Alice. In addition, the joint distribution of A and Alice's output in a hybrid execution of the protocol is identical to that of S and Alice's output in an ideal execution.

A.2 Security Analysis of Protocol Π_f^F (Section 4.2)

Proof We analyse Π_f^F in a $(\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{ca}, \mathcal{F}_e)$ -hybrid model, and show that the execution of Π_f^F is computationally indistinguishable from computation of f in the ideal model with Δ -delayed fairness. We prove the Claim 2 in Propositions 6 and 7 respectively.

Proposition 6 (Security Against Malicious Alice) *For every non-uniform polynomial time adversary A corrupting Alice and running Π_g with abort in a hybrid model with access to $\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{ca}$ and \mathcal{F}_e , there exists a non-uniform polynomial time simulator S corrupting Alice and running in the ideal model with access to an ideal functionality $\mathcal{F}_{\Delta\text{-delayed-fairness}}$, such that for every $a, b, z \in \{0, 1\}^*$ holds:*

$$\left\{ \text{IDEAL}_{f, S(z)}(a, b, n) \right\}_{n \in \mathbb{N}} = \left\{ \text{HYBRID}_{\Pi_f, A(z)}^{\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{ca}, \mathcal{F}_e}(a, b, n) \right\}_{n \in \mathbb{N}}$$

Proof We construct an ideal model simulator which has access to Alice and to the universally trusted party, and can simulate the view of the execution of the protocol. Assume that Alice is corrupted by a hybrid model adversary A . In Algorithm 11 we construct a simulator S given a black-box access to A .

```

S( $b, \text{ID}_B, 1^n$ )
   $\text{ID}_{B'} \xleftarrow{\text{OfflineParty}} A(b, \text{ID}_B, 1^n)$ 
  if  $\text{ID}_{B'} = \perp \vee \text{ID}_{B'} \neq \text{ID}_B$  then
    send  $\perp$  to the trusted party computing  $\mathcal{F}_f$  as Bob's input
    send  $\perp$  to  $A$  as its input from  $\mathcal{F}_{\text{offline}}^e$ 
    output whatever  $A$  outputs and halt
  else
    simulate functionality  $\mathcal{F}_{\text{offline}}^e$  for  $A$ :
    1. choose a key pair  $(vk, sk) \leftarrow \mathcal{G}(1^n)$ 
    3. when  $A$  sends (retrieve,  $\mathcal{F}_{\text{offline}}^e$ ) to  $\mathcal{F}_{\text{ca}}$ , respond with (retrieve  $\mathcal{F}_{\text{offline}}^e$ ,  $vk$ ):
    4. construct a circuit  $C$  computing  $f'_A$ 
    5. construct  $\mathbf{C}$  from  $C$ , by replacing each input wire of Bob with a xor-gate consisting of  $s$  input wires of Bob
    6. garble the resulting circuit  $C$  and obtain  $\mathcal{C}$ , consisting of:
      a. Random strings corresponding to all possible input bits of Alice:  $\tilde{\mathcal{K}}_A = ((\mathcal{K}_A^0[0], \mathcal{K}_A^1[0]), \dots, (\mathcal{K}_A^0[n], \mathcal{K}_A^1[n]))$ 
      b. Random strings corresponding to all possible input bits of Bob:  $\tilde{\mathcal{K}}_B = ((\mathcal{K}_B^0[0], \mathcal{K}_B^1[0]), \dots, (\mathcal{K}_B^0[n], \mathcal{K}_B^1[n]))$ 
      c. Garbled boolean tables  $\tilde{\mathcal{T}}_G$  for each garbled gate  $G$  of the circuit  $\mathbf{C}$ 
      Output decryption tables  $\tilde{\mathcal{T}}_D$  mapping output strings to bits
    7. sign the random input strings  $\tilde{\mathcal{K}}_B$  of Bob:  $\bar{\sigma} = \mathcal{S}_{sk_T}(\tilde{\mathcal{K}}_B)$ , where  $\bar{\sigma} = ((\sigma_0^0, \sigma_0^1), \dots, (\sigma_n^0, \sigma_n^1))$ 
    8. send  $\tilde{\mathcal{T}}_G, \tilde{\mathcal{T}}_D$  to  $A$  as its output from  $\mathcal{F}_{\text{offline}}^e$ 
    for  $i \leftarrow 1$  to  $|b|$  do
      run  $\mathcal{F}_{\text{ot}}^2((\mathcal{K}_B^0[i], \sigma_i^0), (\mathcal{K}_B^1[i], \sigma_i^1), b_i)$ , providing  $(\mathcal{K}_B^0[i], \sigma_i^0), (\mathcal{K}_B^1[i], \sigma_i^1)$  and  $A$  provides  $b_i$ 
       $A$  receives  $(\mathcal{K}_B^{b_i}[i], \sigma_i^{b_i})$ 
      output whatever  $A$  outputs and halt
    end
  end

```

Algorithm 10: Simulator S , simulating the view of Bob.

```

S generates  $(dk, ek) \leftarrow \mathcal{K}(1^n)$  and selects a random key  $K_S \in \{0, 1\}^n$ 
S invokes  $A$  with input  $a, \text{ID}_A, n$ 
When  $A$  sends (retrieve, resolve) for  $\mathcal{F}_{\text{ca}}$ ,  $S$  responds with (retrieve, resolve,  $ek$ )
S obtains  $A$ 's inputs  $(a', K_A, ek')$  for the trusted party  $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ 
if  $a' \neq a \vee ek' \neq ek$  then
  send  $\perp$  to  $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ 
  send  $\perp$  to  $A$ 
  output whatever  $A$  outputs and halt
else
   $S$  sends  $a$  to the trusted party computing  $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ , and receives back  $y_A$ 
   $S$  chooses a random string  $s_B \in \{0, 1\}^n$ , computes  $\mathcal{E}_{K_S}(y_A, \mathcal{E}_{K_S}(s_B))$ , and hands the encrypted result to  $A$ 
  if after  $2\Delta_C$  no response arrives from  $A$  then
    send unfair to trusted party.
  else
     $A$  sends  $c_B$ 
    if  $c_B == \mathcal{E}_{K_S}(s_B)$  then
      send fair to trusted party
  end
S outputs whatever  $A$  outputs.

```

Algorithm 11: The simulator S running in ideal model with trusted party computing $\mathcal{F}_{\Delta\text{-delayed-fairness}}$, and simulating the view of Alice.

The view of A in a simulation with S is identical to its view in an $(\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{\text{ca}}, \mathcal{F}_e)$ -hybrid execution of Π_f with a honest Bob. The joint distribution of A 's view and Bob's output in a hybrid execution is identical to the joint distribution of S and Bob's output in an ideal model.

Proposition 7 (Security Against Malicious Bob) *For every non-uniform polynomial time adversary A corrupting Alice and running Π_g with abort in a hybrid model with access to $\mathcal{F}_{\text{offline}}^e$ and \mathcal{F}_{ca} , there exists a non-uniform polynomial time simulator S corrupting Alice and running in the ideal model with access to an ideal functionality $\mathcal{F}_{\Delta\text{-delayed-fairness}}$, such that for every $a, b, z \in \{0, 1\}^*$ holds:*

$$\left\{ \text{IDEAL}_{f, S(z)}(a, b, n) \right\}_{n \in \mathbb{N}} = \left\{ \text{HYBRID}_{\Pi_f, A(z)}^{\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{\text{ca}}, \mathcal{F}_e}(a, b, n) \right\}_{n \in \mathbb{N}}$$

Proof We construct an ideal model simulator which has access to Bob and to the universally trusted party, and

can simulate the view of the execution of the protocol. Assume that Bob is corrupted by a hybrid model adversary A . In Algorithm 12 we construct a simulator S given a black-box access to A .

```

S generates  $(dk, ek) \leftarrow \mathcal{K}(1^n)$  and selects a random key  $K_S \in \{0, 1\}^n$ 
S invokes  $A$  with input  $b, \text{ID}_B, n$ 
When  $A$  sends (retrieve, resolve) for  $\mathcal{F}_{ca}$ ,  $S$  responds with (retrieve, resolve,  $ek$ )
S obtains  $A$ 's inputs  $(b', K_B, ek')$  for the trusted party  $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ 
if  $b' \neq b \vee ek' \neq ek$  then
  send  $\perp$  to  $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ 
  send  $\perp$  to  $A$ 
  output whatever  $A$  outputs and halt
else
  S sends  $b$  to the trusted party computing  $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ , and receives  $y_B$ 
  encrypts  $y_B$  with  $K_B$ 
  S chooses a random string  $s_A \in \{0, 1\}^n$ , computes  $c_A = \mathcal{E}_{K_S}(s_A, \mathcal{E}_{K_B}(y_B))$ , and  $c = \mathcal{N}\mathcal{E}_{ek}(c_A, c_B)$  and hands the
  encrypted result  $c_A || c$  to  $A$ 
  When  $A$  sends  $c'_A$ ,  $S$  checks if  $c'_A = \mathcal{E}_{K_S}(s_A, \mathcal{E}_{K_B}(y_B))$  then
    decrypts and sends  $\mathcal{E}_{K_B}(y_B)$  to  $A$ 
  else
    send  $\perp$  to trusted party
S outputs whatever  $A$  outputs.

```

Algorithm 12: The simulator S running in ideal model with trusted party computing $\mathcal{F}_{\Delta\text{-delayed-fairness}}$, and simulating the view of Bob.

The view of A in a simulation with S is identical to its view in an $(\mathcal{F}_{\text{Resolve}}, \mathcal{F}_{ca}, \mathcal{F}_e)$ -hybrid execution of Π_f with a honest Alice. The joint distribution of A 's view and Alice's output in a hybrid execution is identical to the joint distribution of S and Alice's output in an ideal model.

A.3 Security Analysis of Protocol $\Pi_{(v,g)}^G$ (Section 5.2)

Proof We analyse $\Pi_{(v,g)}^G$ in a $(\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{ca}, \mathcal{F}_{\text{tea}}, \mathcal{F}_{\Delta\text{-delayed-fairness}})$ -hybrid model, and show that the execution of $\Pi_{(v,g)}^G$ is computationally indistinguishable to computation of (v, g) in the ideal model with Guaranteed Output Delivery. We prove Claim 3 in Propositions 8 and 9 respectively.

Proposition 8 (Security Against Malicious Alice) *For every non-uniform polynomial time adversary A corrupting Alice and running $\Pi_{(v,g)}^G$ in a hybrid model with access to $\mathcal{F}_{\text{offline}}^e$, \mathcal{F}_{ca} , $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ and \mathcal{F}_{tea} , there exists a non-uniform polynomial time simulator S corrupting Alice and running in the ideal model with access to an ideal functionality $\mathcal{F}^{v,g}$ committed-computation, such that for every $a, b, z \in \{0, 1\}^*$ holds:*

$$\left\{ \text{IDEAL}_{f, S(z)}(a, b, n) \right\}_{n \in \mathbb{N}} = \left\{ \text{HYBRID}_{\Pi_f, A(z)}^{\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{ca}, \mathcal{F}_{\text{tea}}, \mathcal{F}_{\Delta\text{-delayed-fairness}}}(a, b, n) \right\}_{n \in \mathbb{N}}$$

Proof We construct an ideal model simulator which has access to Alice and to the universally trusted party, and can simulate the view of the execution of the protocol. Assume that Alice is corrupted by a hybrid model adversary A . In Algorithm 13 we construct a simulator S given a black-box access to A .

The view of A in a simulation with S is identical to its view in an $(\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{ca}, \mathcal{F}_{\text{tea}}, \mathcal{F}_{\Delta\text{-delayed-fairness}})$ -hybrid execution of $\Pi_{(v,g)}^G$ with a honest Bob. The joint distribution of A 's view and Bob's output in a hybrid execution is identical to the joint distribution of S and Bob's output in an ideal model.

Proposition 9 (Security Against Malicious Bob) *For every non-uniform polynomial time adversary A corrupting Bob and running $\Pi_{(v,g)}^G$ in a hybrid model with access to $\mathcal{F}_{\text{offline}}^e$, \mathcal{F}_{ca} , $\mathcal{F}_{\Delta\text{-delayed-fairness}}$ and \mathcal{F}_{tea} there exists a non-uniform polynomial time simulator S corrupting Bob and running in the ideal model with access to an ideal functionality $\mathcal{F}^{v,g}$ committed-computation, such that for every $a, b, z \in \{0, 1\}^*$ holds:*

$$\left\{ \text{IDEAL}_{f, S(z)}(a, b, n) \right\}_{n \in \mathbb{N}} = \left\{ \text{HYBRID}_{\Pi_f, A(z)}^{\mathcal{F}_{\text{offline}}^e, \mathcal{F}_{ca}, \mathcal{F}_{\text{tea}}, \mathcal{F}_{\Delta\text{-delayed-fairness}}}(a, b, n) \right\}_{n \in \mathbb{N}}$$

S generates $(dk, ek) \leftarrow \mathcal{K}(1^n)$ and selects a random key $K_S \in \{0, 1\}^n$
 S invokes A with input a_1, a_2, ID_A, n
When A sends (retrieve, TEA) for \mathcal{F}_{ca} , S responds with (retrieve, TEA, ek)
 S obtains A 's inputs (a'_1, K_A, ek') for the trusted party $\mathcal{F}^{v,g}_{\text{committed-computation}}$
if $a'_1 \neq a_1 \vee ek' \neq ek$ **then**
 send \perp to $\mathcal{F}^{v,g}_{\text{committed-computation}}$
 send \perp to A
 output whatever A outputs and **halt**
else
 S sends a_1 to the trusted party computing $\mathcal{F}^{v,g}_{\text{committed-computation}}$, and receives back y_A^1
 if $y_A^1 == \perp$ **send** \perp to A and **halt**
 Otherwise S chooses a random string $s_B \in \{0, 1\}^n$, computes $(\mathcal{N}\mathcal{E}_{ek}(\mathcal{E}_{K_A}(s_B)) || \mathcal{E}_{K_A}(y_A^1))$, and hands the result to A .
 Upon input a'_2 from A : **if** $a'_2 \neq a_2$ **then**
 send \perp to $\mathcal{F}^{v,g}_{\text{committed-computation}}$
 send \perp to A
 output whatever A outputs and **halt**
 else
 simulate $\mathcal{F}^e_{\text{offline}}$ for A according to steps in Algorithm 9
 Send a_2 to $\mathcal{F}^{v,g}_{\text{committed-computation}}$
 Upon input y_A^2 from $\mathcal{F}^{v,g}_{\text{committed-computation}}$, send $\mathcal{E}_{K_A}(y_A^2)$ to A
 S outputs whatever A outputs.

Algorithm 13: The simulator S running in ideal model with trusted party computing $\mathcal{F}^{v,g}_{\text{committed-computation}}$, and simulating the view of Alice.

S generates $(dk, ek) \leftarrow \mathcal{K}(1^n)$ and selects a random key $K_S \in \{0, 1\}^n$
 S invokes A with input b_1, b_2, ID_B, n
When A sends (retrieve, TEA) for \mathcal{F}_{ca} , S responds with (retrieve, TEA, ek)
 S obtains A 's inputs (b'_1, K_B, ek') for the trusted party $\mathcal{F}^{v,g}_{\text{committed-computation}}$
if $b'_1 \neq b_1 \vee ek' \neq ek$ **then**
 send \perp to $\mathcal{F}^{v,g}_{\text{committed-computation}}$
 send \perp to A
 output whatever A outputs and **halt**
else
 S sends b_1 to the trusted party computing $\mathcal{F}^{v,g}_{\text{committed-computation}}$, and receives back y_B^1
 if $y_B^1 == \perp$ **send** \perp to A and **halt**
 Otherwise S chooses a random string $s_A^1, s_A^2 \in \{0, 1\}^n$, computes $(\mathcal{N}\mathcal{E}_{ek}(\mathcal{E}_{K_B}(s_A^1)) || \mathcal{E}_{K_B}(y_B^1))$, and hands the result to A .
 Upon input b'_2 from A : **if** $b'_2 \neq b_2$ **then**
 send \perp to $\mathcal{F}^{v,g}_{\text{committed-computation}}$
 send \perp to A
 output whatever A outputs and **halt**
 else
 simulate $\mathcal{F}^e_{\text{offline}}$ for A according to steps in Algorithm 10
 Send b_2 to $\mathcal{F}^{v,g}_{\text{committed-computation}}$
 Upon input y_B^2 from $\mathcal{F}^{v,g}_{\text{committed-computation}}$, send $\mathcal{E}_{K_A}(s_A^2) || \sigma_A || y_B^2$ to A
 When A sends $\mathcal{E}_{K_A}(s_A^2) || \sigma_A$, check that the authentication is valid and that s_A^2 is correct
 if not, send \perp to $\mathcal{F}^{v,g}_{\text{committed-computation}}$
 S outputs whatever A outputs.

Algorithm 14: The simulator S running in ideal model with trusted party computing $\mathcal{F}^{v,g}_{\text{committed-computation}}$, and simulating the view of Bob.

Proof We construct an ideal model simulator which has access to Bob and to the universally trusted party, and can simulate the view of the execution of the protocol. Assume that Bob is corrupted by a hybrid model adversary A . In Algorithm 14 we construct a simulator S given a black-box access to A .

The view of A in a simulation with S is identical to its view in an $(\mathcal{F}^e_{\text{offline}}, \mathcal{F}_{\text{ca}}, \mathcal{F}_{\text{tea}}, \mathcal{F}_{\Delta\text{-delayed-fairness}})$ -hybrid execution of $\Pi_{(v,g)}^G$ with a honest Alice. The joint distribution of A 's view and Alice's output in a hybrid execution is identical to the joint distribution of S and Alice's output in an ideal model.