

XPIR : Private Information Retrieval for Everyone

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NOTE: XPIR is free (GPLv3) software and available at <https://github.com/XPIR-team/XPIR>, see the appendix for details.

Abstract

A Private Information Retrieval (PIR) scheme is a protocol in which a user retrieves a record from a database while hiding which from the database administrators. PIR can be achieved using mutually-distrustful replicated databases, trusted hardware, or cryptography. In this paper we focus on the later setting which is known as single-database computationally-Private Information Retrieval (cPIR). Classic cPIR protocols require that the database server executes an algorithm over all the database content at very low speeds which impairs their usage.

In [1], given certain assumptions, realistic at the time, Sion and Carbunar showed that cPIR schemes were not practical and most likely would never be. To this day, this conclusion is widely accepted by researchers and practitioners. Using the paradigm shift introduced by lattice-based cryptography, we show that the conclusion of Sion and Carbunar is not valid anymore: cPIR is of practical value. This is achieved without compromising security, using standard encryption schemes, and conservative parameter choices.

In order to prove this, we provide a fast and easy to use cPIR library and do a performance analysis, illustrated by use-cases, highlighting that cPIR is practical in a large span of situations. The library allows a server to process its data at a throughput ranging from 1 Gbps on a single core of a commodity CPU to almost 10 Gbps on a high-end processor using its multi-core capabilities. After replying to a first query (or through pre-computation), there is a x3 to x5 speedup for subsequent queries. The performance analysis shows for example that it is possible to privately receive an HD movie from a Netflix-like database (with 35K movies) with enough throughput to watch it in real time, or to build a sniffer over a Gbit link

with an obfuscated code that hides what it is sniffing.

1 Introduction

Homomorphic encryption has followed a curious path in the history of cryptography. Since the very beginning of public key cryptography, in the early seventies, it has been presented as a holy grail able to provide the most incredible and powerful applications. Yet, even with the recent breakthroughs due to lattice based cryptography, homomorphic encryption is almost never used in practice.

Among the potential applications of homomorphic encryption, one of the oldest and most emblematic is single-database computationally-Private Information Retrieval. With such a protocol, a user can retrieve a record out of n from a database, without having to reveal which one to the database administrators (security being derived from computational hardness assumptions). A trivial way to obtain such privacy is to simply download the whole database and to dismiss the elements the client is not interested in.

Private Information Retrieval (PIR) schemes aim to provide the same confidentiality to the user (with regard to the choice of the requested element) that downloading the entire database does, with sub-linear communication cost. PIR was introduced by Chor, Goldreich, Kushilevitz, and Sudan in 1995 [2]. They proposed a set of schemes to implement PIR through replicated databases that provide users with information-theoretic security, so long as some of the database replicas do not collude against the users.

Note, however, that PIR schemes do not ensure database confidentiality: a user can retrieve more than a database element using a PIR scheme without the database being aware of it. A PIR scheme ensuring that users retrieve a single database element with each query is called a Symmetric PIR (or SPIR) scheme. Generic transformations exist from PIR to SPIR but this is beyond the scope of this paper (see [3]).

In this paper, we focus on PIR schemes that do not

need the database to be replicated, and whose security is based on the computational security of a cryptographic algorithm, which are usually called single-database computationally-Private Information Retrieval (cPIR) schemes. This replaces the assumption of having replicas which do not collude by a computational security assumption. However, this comes at a price.

1.1 Performance Issues in cPIR

A major issue with computationally-private information retrieval schemes is that they are computationally expensive. In order to answer a query, a database must process all of its entries. If a protocol does not process some entries, the database will learn that the user is not interested in them. This would reveal to the database partial information on which entry the user is interested in, and therefore, it is not as private as downloading the whole database and retrieving locally the desired entry. The computational cost for a server replying to a cPIR query is therefore linear¹ on the database size. Moreover, most of the schemes have a very large cost per bit in the database, a multiplication over a large modulus. This restricts both, the database size and the throughput shared by the users and thus, limits their usage for many databases as well as for other applications such as private keyword search [5].

In NDSS'07, Sion and Carbunar presented a paper on cPIR practicality [1]. They showed that the existing, number theory based, cPIR protocols were not practical and that it was always faster to send the whole database than to compute a cPIR reply. Indeed, basing the security of the underlying number theoretic encryption schemes on the hardness to factor a 1024 bit RSA modulus, one could not expect a cPIR scheme to process the database at more than a megabit per second. Sending the whole database over most of the current Internet connections is at least an order of magnitude faster (and generally two orders of magnitude in local area networks). They also argued that this performance gap would continue as long as usual laws on computational power and bandwidth evolution do.

Focused issue: As in [1], we tackle the issue of practical usage of cPIR. The main performance metric we use is the time needed for a client to retrieve an element privately, supposing one or more clients are querying a server with a commodity-CPU and can exchange data with the server at various speeds (xDSL, FTTH, etc.). We consider that the client is ready to pay a significant overhead for privacy, and compare the time needed using different approaches (trivial full database download, number-theory based cPIR, lattice-based cPIR, etc.).

¹In fact, in [4], Lipmaa proves that using a particular representation, this lower bound is slightly sub-linear (in $O(n/\log(\log(n)))$).

1.2 Related Work

As number theoretic approaches failed to provide efficient cPIR schemes, some alternatives were explored [6, 7, 8], but all of them were based on non-standard problems and have been broken [9, 10, 11, 12, 13].

The (broken) schemes of Aguilar et al. [7] and Trosle and Parrish [8] represented the state-of-the-art in efficient private information retrieval, allowing to reach processing speeds of hundreds of megabits per second on high-end CPUs and up to one gigabit per second on GPUs [14]. Together, these works total about eighty citations, and have been used as a fundamental building block (or as a benchmark) in major and recent venues such as Usenix Security [15] (2011), NDSS [16, 17] (2013, 2014), and PETs [18, 19, 20, 21] (2010, 2012, 2014). This paper presents a potential replacement for them with some additional features: security is based on a standard problem, Ring-LWE[22], with conservative parameters choices; multi-gigabit per second processing throughput on an average CPU; and an auto-optimizer to simplify its usage by non specialists.

A noteworthy exception to this list of schemes is the cPIR scheme of Gasarch and Yerukhimovich [23] which relies on a lattice-based standard encryption scheme [24]. However, this underlying encryption scheme has an extremely large expansion factor (large ciphertexts encoding only a few bits) that compromises the efficiency of the cPIR scheme, which was never publicly implemented.

Alternatives to cPIR Oblivious RAM (ORAM) protocols, which are used to access (and write on) a database privately, can handle efficiently databases of many Terabits. However, ORAM and PIR protocols are used for different applications and cannot be exchanged. Indeed, in the ORAM setting the database content is encrypted data outsourced from the user. ORAM cannot be used directly to privately download elements from a public database (e.g. Netflix) which is the paradigm of PIR.

It is possible to transform an ORAM protocol into a PIR protocol using a trusted hardware module (e.g. see [25]). When using a trusted hardware module is an acceptable constraint, such protocols allow clients to send expressive queries (interpretable by the module) to define the elements to be retrieved and have very low overhead.

Instead of using a trusted hardware module, it is also possible to build extremely efficient PIR protocols using replicated databases as shown by Olumofin and Goldberg [26]. If replicating a database and ensuring that some of the replicas do not collude against the users is an acceptable constraint, such protocols allow clients to retrieve data privately with a very small computational and communication overhead.

A very interesting recent work by Devet and Goldberg[21] has proposed using replicated-database PIR

and cPIR jointly to achieve high performance results without compromising security when databases collude. This paper requires the database to be replicated, and therefore it does not correspond to our setting. The proposed protocol uses Aguilar et al.’s cPIR (broken) scheme [7] as a building block, replacing it with our protocol would result on an important performance boost and provide a secure instance of their construction.

Works considering only computational or communication costs In the Oblivious Transfer setting [27], the objective is to limit the computational cost for the user and the database without considering communication efficiency. The whole database is sent encrypted to the client together with some extra information, with the added benefit that the server is guaranteed that the client can retrieve information about one element only per query.

Some cPIR protocols focus only on communication efficiency without considering computational costs. In [28], a *communication* efficient cPIR protocol, from an asymptotic perspective, is built based on a fully-homomorphic scheme. The underlying encryption scheme we use is just an additively-homomorphic building block in [28] but our objective is to allow users to retrieve elements faster than the trivial solution of downloading the entire database in realistic settings. This implies taking into account computational and communication constraints.

In [29], an implementation of a fully-homomorphic encryption based scheme (close to what is done in [28]) is given. The contribution of this scheme is on the communication overhead, which they show to be very small in some settings (when multiple database elements are retrieved). Computational costs are considered but this paper does not give a contribution in this sense that the database is at best processed at 20Kbits/s which is below the processing throughput of classic, number-theory based, cPIR schemes. As already noted, sending the whole database can be done at a higher throughput in most settings allowing to retrieve an element privately much faster.

1.3 Contributions and Roadmap

First and foremost this paper shows that cPIR is a usable primitive in a large variety of settings, with standard security assumptions and conservative parameter choices. Section 3 is dedicated to prove this assertion. This contradicts the main result from Sion and Carbunar [1], which was the reference on cPIR usability. The analysis of Sion and Carbunar remains correct, but one of their main assumptions (that cPIR would be based on number-theoretic schemes) does not need to be true any more, thanks to the arrival of lattice-based homomorphic encryption schemes.

Second, the NTT and Ring-LWE based private information retrieval scheme and implementation we describe in this paper offer multi-gigabit processing through-

put on a commodity CPU, and an optimizer to automatically setup the system for a given setup (hardware/network/application/security). This contribution required a considerable conception and development effort, as in order to maximize performance we had to circumvent standard big number and linear-algebra libraries, and optimization for a large variety of settings required many extra remote measuring and configuration function orchestrated by an optimizer.

In Section 2, we present the basic tools a reader should be comfortable with in order to understand the rest of the paper: homomorphic encryption, which allows to compute over encrypted data; the objectives and the classical approaches to obtain private information retrieval protocols; and a special setting of cPIR called private keyword searching, in which instead of retrieving elements by their index as usually done in cPIR we retrieve elements based on the keywords they are associated to. In Section 3, we directly jump into the performance analysis of our library. The objective of this section is twofold: show how our library behaves on a large variety of settings and motivate the reader to dig into the details of Section 4, which presents the structure of our library and explains the performance results. The main part of the paper ends with a Conclusion. The first appendix presents first the cryptographic system based on Ring-LWE for which most of our performance results are presented as well as a discussion regarding security (parameter choices, randomness generation, etc.). This can thus be skipped by the non-specialist but is included in the paper to show that the performance obtained is by no means the result of aggressive parametrization or of using an underlying non-standard cryptosystem. The second appendix presents the interface of our client and server to illustrate its ease of use.

2 Basic Tools

2.1 Homomorphic Encryption

Additively homomorphic encryption schemes are defined by four algorithms: KeyGen, to generate keys; Enc the encryption function; Dec the decryption function; Sum which takes as input a set of ciphertexts $\alpha_1, \dots, \alpha_n$ with corresponding plaintexts a_1, \dots, a_n and outputs a ciphertext α with corresponding plaintext $a_1 + \dots + a_n$; and Absorb which takes as input some data m and a ciphertext of i and outputs a ciphertext of $i * m$. If $i = 0$ we say m is erased, and if $i = 1$ that it is effectively absorbed.

It is worth noting that to be secure (see the Appendix for a more formal definition) such a scheme *has* to be randomized. More formally, Enc is a randomized algorithm that for an input (pk, a) outputs a ciphertext from a large set following a given probability distribution. It is also worth noting that in our application of homomorphic encryption, the same entity encrypts and decrypts data and

Parameters	Max Sec	Plaintext	Ciphertext	F
(1024,60)	97	$\leq 20\text{Kbits}$	128Kbits	≥ 6.4
(2048,120)	91	$\leq 100\text{Kbits}$	512Kbits	≥ 5.12
(4096,120)	335	$\leq 192\text{Kbits}$	1Mbit	≥ 5.3

Figure 1: Parameter sets for our Ring-LWE encryption scheme. Ciphertexts are made of two polynomials. The first parameter defines the number of coefficients per polynomial and the second the number of bits per coefficient (stored in 64bit registers). From these values, ciphertext sizes can be easily deduced. Maximum theoretical security is only attained if enough noise is included in the ciphertexts and the noise generator matches this security. Plaintext size is slowly (logarithmically) reduced if we want to do a lot of Sum operations. Similarly, the expansion factor stays very close to its optimum. can use a secret key homomorphic encryption scheme.

As for each plaintext there are many possible ciphertexts, the ciphertexts space must be larger than the plaintext space and so must be their bitsize. We note F the expansion factor of the cryptosystem (which is defined as the size in bits of the ciphertexts divided by the size in bits of the plaintexts). This factor is typically a small number $F \geq 2$. As a reference, Figure 1 presents some plaintext and ciphertext sizes for different parameters of our Ring-LWE based encryption scheme.

In this paper, we use a Ring-LWE based homomorphic encryption scheme: the symmetric scheme presented in [28] with some pre and post-processing to improve performance in the cPIR setting. As the pre and post-processing is public and reversible, security is directly based on the ring learning with errors problem (Ring-LWE) [22], as for the unmodified scheme in [28]. The hardness of Ring-LWE is one of the major assumptions used to build lattice-based cryptosystems, and since it was presented at Eurocrypt’10, it has become probably the most standard and used one.

2.2 Private Information Retrieval

In this paper, we use a simple cPIR protocol based on [32], described hereafter. It can be used with any additively homomorphic encryption scheme. The protocol can be formally described as follows:

Basic cPIR Protocol

Setup (user):

1. Set up an instance of the encryption scheme with security parameter k .

Query Generation to retrieve element i_0 :

1. For i from 1 to n generate the i -th query element q_i as
 - A random encryption of zero if $i \neq i_0$
 - A random encryption of one if $i = i_0$
2. Send the ordered set $\{q_1, \dots, q_n\}$ to the database.

Reply Generation:

1. Compute and return $R := \text{Sum}_{i=1}^n \text{Absorb}(m_i, q_i)$.

Information extraction:

1. Decrypt R and recover m_{i_0} .

If the encryption scheme ensures that encryptions of 0 and encryptions of 1 are indistinguishable (which is the security definition required for the scheme as stated in the Appendix), the database cannot know which is the effectively absorbed element and which are the erased ones and thus cannot know which element has been retrieved.

With this simple approach, query size is n times the size of a ciphertext and reply is roughly $\ell \times F$, F being the expansion factor of the encryption scheme used. As is, the reply is a single ciphertext. If the database elements are too large to fit in a ciphertext, it is possible to split them and process each chunk iteratively. If database elements are too small, on the other hand, it is possible to aggregate them by groups of size α and obtain a database with $\lceil n/\alpha \rceil$ elements of size $\ell \times \alpha$. To reduce query size it is possible to use this protocol recursively. We won’t describe recursion here due to space restrictions but it can be considered as a black-box operation which takes as parameter an integer d called *dimension* and results in a scheme in which the client only needs to send $d \times n^{1/d}$ query elements (ciphertexts) and the reply will be of size $F^d \times \ell$. For example if $F = 2$ and we have a database with one million elements, it is possible to: send a query of 10^6 ciphertexts and get the database element with an expansion factor of 2 ($d = 1$, no recursion); send a query of 2×1000 ciphertexts and get the database element with an expansion factor of 4 ($d = 2$); send a query of 3×100 ciphertexts and get the database element with an expansion factor of 8 ($d = 3$); etc.

The reader is referred to [32] for a description of these techniques. It is possible to make different choices on how the database is split and to change the cryptographic parameters used on each level to improve the performance of recursion. For a complete description, generalization and optimization of this process, the reader is referred to [33] which proposes many interesting variants. In our library, we have decided to stick to the basic approach for recursion although it would be interesting to develop other optimizations, such as those proposed in [33].

2.3 Private Searching

The basic idea of private keyword search [34] is that the database can arrange its elements by grouping them using keywords. With this technique, users can get, using a cPIR protocol, all the database elements that match a given keyword. In this case, the query size is proportional to the amount of possible keywords D (Dictionary size) and the computational cost for the server may change as a database entry that is associated to multiple keywords will be copied once in front of each keyword. Thus, the computational cost will be the database size times the average amount of keywords a database element matches (which depends on the application).

It is also possible to use this approach to filter streamed

data based on private criteria [35]. The idea is to build ephemeral keyword-based databases for each message passing on the stream. These databases have null elements everywhere except in front of the keywords that the passing message matches. The computational cost to process a packet is therefore its size times the number of keywords it matches (null elements cost nothing to process). With such an approach it is possible to build a filter that outputs for every passing message an encryption of zero when the message does not match the keyword and an encryption of the message when it does.

We use this approach to build a sniffer over a gigabit link in Section 3 that is only interested in messages corresponding to a given IP address. In this sniffer, the streamed messages are the packets on the network, the keywords are the set of IP addresses used in a local area network, and a packet matches the IP-keyword corresponding to its source and destination address. The sniffer's code includes a cPIR query selecting the IP that is secretly being observed and thus even analyzing the code of the sniffer it is not possible to learn which is the IP address as the chosen keyword is hidden in the cPIR query.

Important note: After processing an input, the filter always outputs a ciphertext and it is not possible to distinguish useful outputs from encryptions of zero. If we store all these results we will do not better than a trivial PIR based equivalent (which would store unencrypted all the input data). The main interest of using cPIR, is that it is possible to compress the output so that encryptions of zero are packed and useful outputs preserved, even if it is not known which of the outputs are useful. These techniques are beyond the scope of this paper (see [36] for the most recent proposal on the subject), but it is possible to have efficient filters which have only a small overhead with respect to an unencrypted filter that would store only the keyword-matching data.

3 Performance Analysis and Use-Cases

Our library is modular and allows several choices of underlying encryption schemes. The optimizer tests which approach (full database download with no cryptography, cPIR with Paillier's cryptosystem, cPIR with the lattice-based encryption scheme) is able to give the best results and advises the cPIR client program to use it. In every single test presented in this section the best choice was cPIR with our Ring-LWE, lattice-based encryption scheme, or trivial PIR (full database download) for some very specific settings (e.g. databases with less than ten elements). As the other options (Paillier's cryptosystem, NTRU) always gave worse performance, they do not appear on the different figures.

In this section, we analyze the performance of XPIR using two metrics: latency and user-perceived throughput. The latency measurement is the round-trip time from the

moment the client starts generating the cPIR query to the moment it has finished to decrypt the reply received from the database. Our library pipelines the different phases: query generation and query sending in one direction; and reply generation, reply sending, reply reception and reply decryption in the other direction. Thus, latency is supposed to follow the formula: $\text{MAX}(\text{queryGenTime}, \text{querySendTime}) + \text{MAX}(\text{replyGenTime}, \text{replySendTime}, \text{replyDecTime})$. Our optimizer can take this into account and select the different available parameters to minimize this value if asked to.

User-perceived throughput is the throughput (measured in bits per second) at which the user is able to get the requested element. Again, due to the pipelining between the server and the client this value is supposed to follow the formula: $\text{MIN}(\text{processingTput}/n, \text{serverUpTput}, \text{clientDownTput}, \text{clientDecTput})$, n being the number of elements in the database. Indeed, the server processes the n elements iteratively at a given throughput, and sends a processed chunk of information for every n chunks of the database processed (hence the quotient in the first argument of the MIN function).

We will consider two types of settings for our databases: static databases in which pre-processing of the database elements can be done; and dynamic databases whose contents are ephemeral (TV Streams, sensor data, etc.) and which cannot be pre-processed ahead of time. Pre-processing is independently executed for each element at speeds that vary from 5Gbps (for a high-end laptop) to 10Gbps (for a high end server) as shown in Section 4.2. A database is thus considered static if the lifetime of an element is well larger than its conversion time (e.g. 1-2 seconds for a 10Gbit movie) and the elements are known early enough with respect to the first cPIR transaction in which they will be used.

To illustrate the versatility of our library, we highlight performance values with four use-cases combining dynamic/static settings and throughput/latency goals. For high throughput applications we use a Netflix-like server (relatively static data) and a sniffer that obfuscates what he is interested in (dynamic data). For low latency applications we use a Match.com-like online dating database server (relatively static data) and a private stock-market information service (dynamic data).

Experimental setting: To show that our library is usable by everyone for many applications we use commodity hardware in almost all the settings. Our cPIR Server runs on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz (mobile), and 8GB of DDR3 RAM. As our library is able to process database content very fast, the data storage medium considerably influences performance, specially if this data is pre-processed. In our evaluation, we use two media: RAM (100Gbit/s access), or an OCZ Vertex 460 SSD (4Gbit/s access). The contiguous read speed of our

SSD is sufficient to feed the server in all of the dynamic data settings. If data is static, we are able to process it quite faster than what a usual SSD disk can offer. If the database is in RAM this is of course not an issue, but in some applications such as the Netflix-like server, the database is huge and does not fit in RAM. We discuss this issue in the associated Section.

Security: In most of our performance results, the optimizer found that the best parameters for the Ring-LWE scheme were (2048, 120) or (1024, 60). According to the usual assumptions presented in the Appendix, the former set of parameters is able to provide 91 bits of security, and the latter 97. As noted in the appendix, we use noise large enough to attain such security. To generate this noise, we use Salsa20/20 [37] (Salsa20/20 is able to provide up to 256 bits of security), and thus even if a set of parameters for Ring-LWE is able to provide theoretically more security, 256 is thus an upper bound (this is the standard maximum security usually considered).

Security scales extremely well in lattice-based cryptography. For a constant moduli, security increases exponentially with the polynomial degree and computational costs increase only (almost) linearly. For example, if we use parameters (4096, 120) (instead of (2048, 120)), the theoretical security can go up to 335 bits. Again, in our implementation security is bounded to 256 bits. In such a high security setting, query generation, reply pre-computation, reply generation, and reply decryption have a cost that is just increased by a factor 2 (more precisely 2.18 for pre-computation and 2 for the rest). With such parameters, each ciphertext can contain more data (almost twice), and thus the security increase comes at very little cost. We will present the costs with the high security (4096, 120) parameter set in the first figure, and then let the optimizer choose the best parameters, with a minimum security set to 91 bits to be able to use the (2048, 120) parameters which are a good compromise between ciphertext size, reply generation throughput and security.

3.1 High Throughput on Static Databases

Figure 2 shows the user-perceived throughput achieved using our library on the experimental setting laptop. High-throughput applications (i.e. applications requiring a high user-perceived reception throughput) only make sense if the database elements are big enough, if they are very small and quickly sent we consider the essential issue is latency which will be studied in Section 3.3. We therefore consider here only databases with files going from 10Mbit and up. Our experimental results showed user-perceived throughput is independent of file sizes when they were in that range, henceforth the lines in this Figure are valid for any file size greater or equal to 10Mbit.

The red line shows performance when no recursion is done (i.e. when query size is proportional to n). This

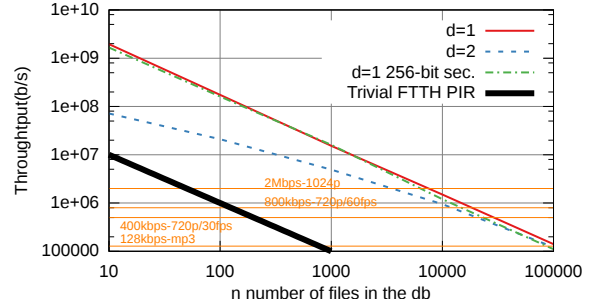


Figure 2: User-perceived throughput of XPIR streaming static data on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz. Trivial PIR over a 100Mbits/s FTTH line (thick black line) is between ten and two hundred times slower than cPIR. The red filled (91 bits security) and green dash-and-dotted (256 bits security) lines give throughput when no recursion is done (i.e. database is processed as a one dimension array) and the blue dashed line with one level of recursion (i.e. database is processed as a two dimension array). The horizontal lines correspond to the needed throughput to see a movie in 1024p (2Mbps), 720p 60Hz (800Kbps) and 720p 30Hz (400Kbps), or to listen to a 128Kbps audio file. Performance on a server with a better processor (e.g. ten-core Xeon E7-4870) roughly doubles and caps at that level as RAM bandwidth is saturated.

line was obtained using the best parameters for throughput (which were given by the optimizer): no recursion, no aggregation, and Ring-LWE cryptography with parameters (2048, 120). With these parameters, ciphertext size (and thus query element size) is 500Kbits and the expansion factor of encryption is $F \simeq 5$. Therefore, in order to get an element at a user-perceived throughput of 2Mbits/s actually 10Mbits/s of bandwidth will be used. This setting is the most favorable from a throughput point of view, but query size can be a problem when the number of elements n grows, as we will see in Figure 3. Note that this line is pretty close to the straight line defined by $15/n$ Gbps (more precisely values slowly drift from $19/n$ Gbps to $14/n$ Gbps for large n values).

The green line shows the same results as the red line in a higher security setting (256 bits security). As noted previously this has almost no impact on processing but doubles the size of each ciphertext and query size (as we will see in Figure 3). Note that the scale is logarithmic, and thus even if the difference with the red line is very small, in this setting performance is roughly 10% worse.

The blue line shows performance with one level of recursion (i.e. when the database is seen as a two-dimensional $\sqrt{n} \times \sqrt{n}$ array and query size is proportional to $2\sqrt{n}$). Recursion results in a significant computational overhead for small databases as the database is processed a first time resulting in an intermediate database of size $F\sqrt{n}$, that we have to process again before getting the final reply. In our implementation the cost of process-

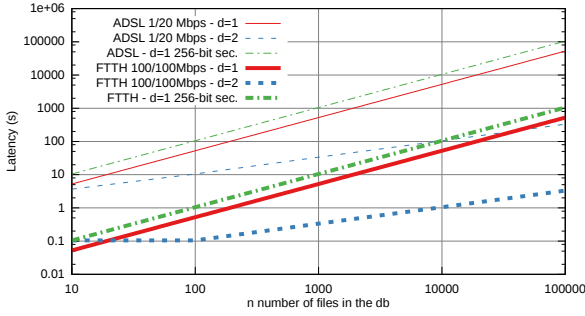


Figure 3: Initial latency before the user starts to receive streaming data (mainly due to query generation and transmission time to the server). There is no initial latency for trivial PIR. Thin lines are for ADSL and thick lines for FTTH. Colors and line styles are associated to the same settings as in Figure 2. The results highlight that latency grows linearly in n in dimension 1 and in \sqrt{n} in dimension 2, and that the main bottleneck is the available upload bandwidth.

ing this database is roughly ten times the usual cost. If $\sqrt{n} \gg 10F$ computation over this intermediate database is negligible as it is small enough with respect to the initial database. Indeed, the Figure shows that the overhead of a level of recursion fades out as n grows.

Initial latency: Even if obtaining the best user-perceived throughput is the goal of an application, an important parameter is how much the user will have to wait until he starts receiving the requested stream. Figure 3 highlights the benefit of using a level of recursion for databases with many elements. This is specially true when $n \geq 1000$ as we have seen that this implies almost no computational overhead in this case. On a FTTH line, latency will be below ten seconds (if we use $d=2$ for $n \geq 1000$). An ADSL line has limited upload bandwidth, henceforth latency ranges from 5 to 500 seconds. Therefore, in such a case, one level of recursion should definitely be used, even if it implies a significant overhead for the reply generation. The strange behaviour of the FTTH lines for a small number of elements comes from the fact that we use TCP sockets to transmit the queries and for very small time values, buffering and windowing gets in the way. It is possible to tune the low level sockets or to use UDP to have a more linear behaviour if needed.

The Netflix Use-case: The Netflix movie database is composed² of 100.000 movies that are stored as static files and can thus be pre-processed for performance improvement. H.265 - High Efficiency Video Coding (HEVC) is the forthcoming standard for video-streams compression[38, 39]. The attained compression levels with this codec enable to watch 720p streams at bit-rates between 400Kb/s for 30fps and 800Kb/s for 60fps and 1024p at 2Mb/s. A typical bit-rate for audio streams is 128Kbps for quality

²or was composed in 2009 according to the Wikipedia page for Netflix.

MP3s. These levels (128, 400Kbps, 800Kbps and 2Mb/s are represented by horizontal lines on Figure 2).

Henceforth, a private Netflix-like server based on XPIR can allow a user to privately receive a streamed movie with different trade-offs between privacy and quality. **If the user is willing to receive a 720p-30fps video stream he can hide his choice among 35K movies from the server.** He can get better video quality at the expense of some privacy, hiding his choice among *just* 17K movies he can get a stream at 720p-60fps and hiding it among 7K movies he can get it at 1024p-60fps.

To reach that level of privacy, the server has to dedicate one full processor per user. However, if k -anonymity is enough, the movie catalog could be randomly (and diversely) arranged in smaller sets of k files in order to reduce the computation necessary for the server. For example, **if movies are arranged in random anonymity sets of 100 movies, each processor can serve up to 350 users (twice that number with a higher tier processor than the one we used).** We are conscious that the use of cPIR in the Netflix scenario, while certainly good for privacy may prove to be a problem regarding both copyright management and accounting. We essentially used this use-case as an illustration of the excellent performance attained by XPIR, at a massive scale, and not to discuss the fact that Netflix should use cPIR to stream its clients, or that it would be commercially possible.

Medium Access Issues: Obtaining results with databases of up to 10 Gbits was simple as they fit in RAM. To obtain performance results with the largest databases, we processed them in large chunks that did fit in our RAM removing the disk transfer times for each chunk. If we use our SSD disk to access the data and take into account the transfer times, disk access is the bottleneck and thus we obtain as performance result a straight line at $2/n$ Gbps (our disk allows 4 Gbps access and pre-computed data is twice larger than the initial data). In the use-case described, this would mean that the anonymity sets (or amount of users a processor can handle) would be divided by a factor seven. We consider though that in applications requiring large databases and throughput, such as the Netflix use-case, the provider has high performance disks. In order to match the computational performance of our library it is possible to use for example two OCZ Vertex RevoDrive PCIe SSD in RAID 0 which delivers 30Gbps contiguous read throughput, at roughly a cost of 1000\$. Note that if threads access data synchronously, disk access costs are independent of the number of concurrent user, so scalability is not an issue.

3.2 High-Throughput on Dynamic Databases

At first sight, dynamic databases are similar to static ones apart that data is dynamic and cannot be pre-processed offline, such as it is the case with IPTV for example. How-

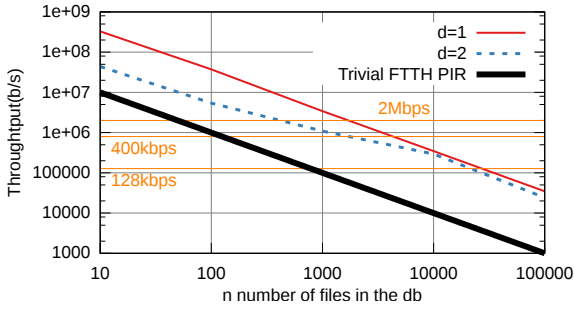


Figure 4: User-perceived throughput of XPIR streaming dynamic data on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz. Trivial PIR over a 100Mbits/s FTTH connection (thick black line) is between five and fifty times slower than cPIR. The red line gives throughput when no recursion is done (i.e. database is processed as a one dimension array) and the blue line with one level of recursion (i.e. database is processed as a two dimension array). The horizontal lines correspond to the needed throughput to see a movie in 1024p (2Mbps), 720p-60fps (800Kbps) and 720p-30fps (400Kbps), or to listen to a 128Kbps audio file. Performance on a server with a better processor (e.g. ten-core Xeon E7-4870) can be two to three times higher (note that scale is logarithmic).

ever, they can have a large span of shapes and contents and are not always a simple extension of static databases to "infinite size" files. An exhaustive analysis of dynamic databases is beyond the scope of this paper, but show two different settings : IPTV and a private sniffer.

The first setting is pretty simple : usual data streams that cannot be pre-processed such as for IPTV. Figure 4 presents the same results as 2 but with dynamic data. As one can see, the user-perceived throughput is roughly divided by six. For an IPTV like application, a single processor can handle one hundred 720p-30fps streams for 50 simultaneous clients (e.g. classical TV), or five thousand such streams for a single client (e.g. a large set of distant IP web cameras). The second setting is more tricky, as the dynamic data elements are most of the time null, and the non nulls can be very small. We describe this setting in our second use-case.

The Private Sniffer Use-Case: In this use-case we suppose someone creates a sniffer that stores all the packets that have a given source IP address, but wants to ensure that nobody that would find the sniffer and analyze its code could learn which IP the sniffer is interested in. Of course, it is possible to store every message (which corresponds to trivial PIR) but, as described in Section 2.3, using cPIR the storage can be much more compact.

With this approach, a cPIR query is generated and each query element is associated to a given source IP. The first question we can ask is: how large can be the IP range? Suppose we use either (1024, 60) parameters or (2048, 120) parameters with Ring-LWE encryption. Each

query element is 128Kbit long in the former case and 512Kbit in the latter. If we aim to cover a class B network range (65535 addresses) the query size will be 1Gbyte in the former case and 4Gbytes in the latter.³ It is important to note that this query size is not something that must be sent regularly, for most sniffers it will define how it behaves (it is an encrypted part of the sniffing program) and used to store large amounts of results in a local hard drive before being retrieved (of course results can also be sent through the network). This size does not affect performance either, as our results on processing throughput have proven to be independent of how many elements the query has, as long as it fits in RAM, which we assumed to be true.

For every packet the sniffer intercepts, he builds a database such that each query element is associated to a null element, except the query element corresponding to the source IP of the intercepted packet which is associated to the packet. Then the sniffer generates a cPIR reply storing the reply in the disk using the compression techniques described in Section 2.3. The dynamic database is thus pretty special as it is almost null and the element to process will be often much smaller (between 320 bits and 12Kbits) than what can be absorbed in a ciphertext (roughly 20Kbits for the smaller parameters and 90Kbits for the larger ones). A trivial implementation will thus not use all the power our library can provide in other settings.

The red line in Figure 5 gives the throughput at which the sniffer is able to process the intercepted packets. As packets are much smaller than classical plaintext size, we choose the smallest cryptographic parameters possible, i.e. (1024, 60). We consider that after absorption the ciphertext can undergo up to one thousand sums (for operations such as insertion on a bloom filter, etc.). Given the internal structure of our cryptosystem, this implies that plaintext size is 15Kbits. If we generate a cPIR reply for each 40 byte incoming packet, most of the space available in the resulting ciphertext will be lost, but the cPIR reply generation operation will not cost less (for null elements the operation is free, but for small elements the operation costs as much as for elements of the size of a plaintext). Thus, if we deal with packets of 400 bytes instead of 40, the cPIR reply generation costs the same, but we process ten times more information. As even for the largest sizes (we consider usual packet sizes, up to the classic Maximum Transmission Unit -MTU- of 1500 bytes), a packet always fits in the plaintext, the processing throughput is linear on the packet size.

If we consider a classic bi-modal distribution (40% very small packets, 40% close to MTU packets, 20% in-

³In fact, the IP range can be arbitrarily large if we associate multiple IPs, or a hash of the IP to each query element. In that case we will obtain packets from different IP sources and the size of the query will determine the efficiency of the filtering done.

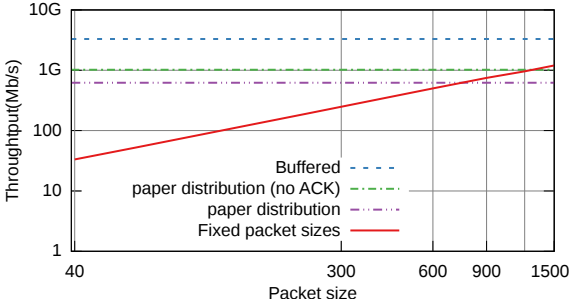


Figure 5: Packet processing throughput for the sniffer use-case using XPIR on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz. Trivial PIR performance does not make sense in this setting. The red line, measures performance each packet size, in bytes in the x-axis, independently (i.e. measuring performance just processing 40 bytes packets, then measure performance for 80 bytes packets etc.). The green line gives the processing throughput when the traffic follows a classic bi-modal distribution such as found in [40]. The purple line gives throughput for a traffic following the same pattern but for which we ignore packets smaller or equal to 60 bytes (basically ACKs). The blue line gives performance if we wait for traffic to fill buffers and only generate cPIR replies when enough information has been collected to fill a ciphertext.

between packets) such as those described in [40], **the sniffer is able process a link at 600Mbps** (purple line). **If we consider the sniffer is not interested in very small packets (ACKs mostly), it can process a link at slightly over 1Gbps** (green line). **If we buffer packets** and do not generate a cPIR reply until we have enough data from a given source IP address to fill a plaintext, we can do much better. In this case we can choose parameters giving better processing speeds such as (2048, 120). In such a setting **we can process a link at roughly 3Gbps** (blue line), for parameters (2048, 120) if we buffer 90Kbits of data for a given IP source before generating a cPIR reply (using the higher security parameters we get almost the same performance but with a query twice larger).

Of course, implementing a complete private searching prototype would imply looking into other concerns, such as making sure that other aspects (packet interception, compression function such as Bloom filters on the output, etc.) are able to cope with this throughput, but this is beyond the scope of this paper.

3.3 Low Latency on Static/Dynamic Databases

In this Section, we want to evaluate XPIR latency, *i.e.* round trip time (RTT), in settings where data is static or dynamic. Figure 6 shows the RTT achieved using our library on with static data and Figure 7 with dynamic data. The x-axis represents the size of the database ranging from 1Mb to 1Tb. The green line shows the request processing time (RP), the red line shows the RTT with no network (*i.e.* the client on the same machine as the server), and

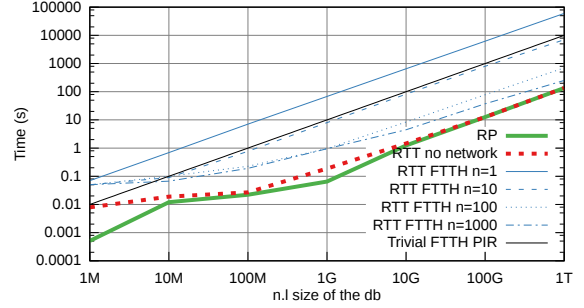


Figure 6: Round-trip (RTT) and request processing (RP) times of XPIR serving static data on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz on a FTTH network (database sizes are in bits). Trivial PIR (from top to bottom the second filled line) is faster than cPIR for databases with less than ten elements, which is natural as cPIR has a reply expansion factor around five. For databases with more elements cPIR can be up to fifty times faster. When the client is local RTT (red thick dashed line) matches RP (green thick filled line), specially for large databases. Each thin blue line gives RTT for a fixed n and varying database sizes. For large databases reply size is the limiting factor, which explains why performance is closer and closer to ideal RTT as n grows (when n grows for a fixed database size ℓ shrinks). For small databases, query size is the limiting factor. RTT does not grow as n grows because the optimizer uses aggregation to reach the best RTT.

the various blue lines represent the RTT with a FTTH network for different values for n . While, when considering throughput, the request processing and data importation were the most striving parameters, when looking at RTT, performance results of a balance between reply processing time and upload/download times.

It is very important to note that usual techniques in cPIR such as aggregation and recursion (see Sections 2.2 and 4.3) are mandatory to keep RTT low. In Figure 6 we used parameters (1024, 60) for the Ring-LWE cryptosystem and thus query element size is 128Kb and $F \approx 6$. For $n = 10000$ and $l = 1Mb$, if no aggregation and no recursion is used, sending the query ($10000 * 128Kb$) over the FTTH link takes 12.8 seconds and sending the reply ($6 * 1Mb$) takes 0.06 seconds while generating the query (at 2.2 Gbps) takes 0.05 second, processing it (at 10 Gbps) takes 0.1 second and decrypting the reply (at 5.6Gbps) takes about 1ms. Using recursion divides query sending time by a factor 50 and has little impact on the other times (as they are very small) so it is clearly beneficial.

Using aggregation and recursion, when beneficial, the optimizer can set the cPIR parameters in order to transform the shape of a database with a high n value into a database with a smaller n . This is why, on both Figures, the higher n the lower is the RTT. Indeed, the shape of the database is transformed in order to lower this parameter if a smaller n is more favorable. As one can observe, the high n lines tend to approach the RTT limit which is the

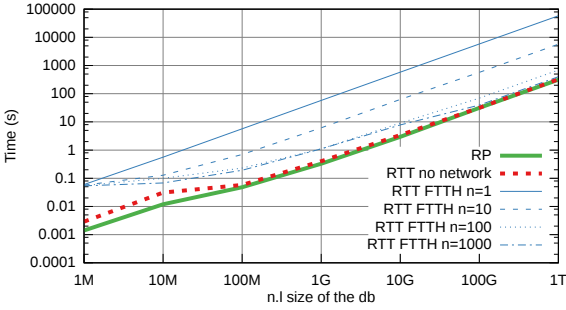


Figure 7: Round-trip (RTT) and request processing (RP) times of XPIR serving dynamic data on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz on a FTTH network (database sizes are in bits). Trivial PIR has been masked for clarity as the same remarks as most comments on Figure 6 also apply. As data is not already pre-processed, request processing time is higher, but upload/download times do not change. This explains why blue lines are almost identical except for the fact that the gap to reach ideal RTT is smaller. In practice this implies that RTT is not affected much by pre-processing except for very large databases.

RP line. The only difference between static and dynamic databases lies in the request processing speed that is impacted by the need to pre-process the data in the dynamic case. One can observe the different values of request processing (red dashed lines on both Figures). Henceforth, with dynamic databases, the high n lines will tend towards the RP line later, *i.e.* with larger databases. This implies that in most networked situations RTT will be similar for static and dynamic databases, except for the largest ones.

Match.com Use-Case: In this use-case we consider that an online dating database server wants to provide a paying private keyword search mechanism to its clients. When using this system, users can define some public criteria, such as the city in which they would like to meet people (which is anyways probably revealed by their IP). This set of public parameters will reduce the database size over which a second search, based on private criteria, will be done. The users can then do a cPIR-based keyword search (see Section 2.3) to get the profiles matching a set of private keywords. If we suppose the database has one million profiles, each of one megabit, the complete database will be of one Terabit. We must also take into account that each profile may match a set of keywords and that reply generation costs are multiplied by the average number of matching keywords in a private keyword search. If we suppose that the average profile has five keywords, using the RTT given in Figure 6 a user would have to wait for ten minutes before having a reply which is probably too much for a web experience. Using the public keyword pre-filtering we described we can hope to divide the size of the database by a factor 10 to 100 (if users are distributed in various cities and public keywords are spe-

cific enough) which would lower the waiting time to 6-60 seconds, a much more reasonable time for a search. Of course if we consider Match.com 5 Millions users (according to Wikipedia’s page which cites 2014 sources) and profiles of multiple megabytes, public filtering will have to be much more efficient. But the fact that we are able to grasp having usable cPIR protocols in such large social networks was unthinkable not that long ago.

NYSE Use-Case: In this last use-case, we are interested in using XPIR on dynamic streams with the lowest latency possible. The New-York Stock Exchange (NYSE) Secure Financial Transaction Infrastructure (SFTI) high-end service serves 5-10Gbps of data concerning various worldwide stock markets. The Bloomberg “snooping” scandal is a good illustration of why one would want to keep private the financial information one is interested in. One can see two different type of usages with this application: oriented towards throughput or towards latency. In the first case, a client may want to register to a given set of streams of information, and get served with all the information concerning the associated companies coming from stock markets, analysts, etc. with a constant stream of up to date information. In such a case, the application is very similar to an IPTV service where the data-stream concerns financial information instead of a TV stream. Refer to Section 3.2 for performance results.

In the second case, a client wants to retrieve as fast as possible the last bunch of information concerning a company. In this case, the stock market service can be seen as collecting data generated by remote sensors and giving access to this dynamic data to its clients on a per request basis. The most striving question is thus how long does it take for the client to retrieve the information on a given company, in other words, how fresh is the data? For example, suppose a user wants to grab some information from the last 100ms (we cannot expect to get much more recent data given the underlying network RTTs). In the SFTI 5Gbit stream the amount of data corresponding to 100ms should be 500Mbits. As such data is composed of many elements we can expect that latency will be close to the optimal line in Figure 7 and thus the user should get the information in roughly 100ms, which is a reasonable waiting time for information that already is old of 100ms.

4 Subroutine Analysis

4.1 General Architecture

From a logical point of view, our proposal has three different blocks: a set of homomorphic encryption schemes (Paillier, Ring-LWE-based, NTRU-based); a classic, homomorphic encryption based, cPIR protocol (client, server, query generator, reply generator, reply extractor); and an optimizer which provides the best parameter settings for the cPIR protocol and encryption scheme, given

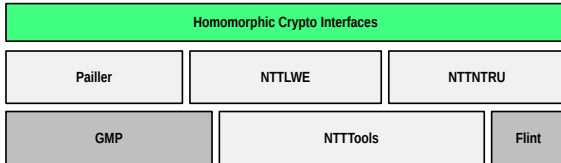


Figure 8: Encryption module architecture

a strategy (smallest RTT, least resources, lower price) and a set of fixed parameters (database description, security, bandwidth, computational power). We will therefore present the library following the same structure.

Modules are pluggable and only need to implement given interfaces to work together. Encryption modules can be easily added in our architecture. Replacing the cPIR application is also possible but requires more work and such a possibility is beyond the scope of this paper.

4.2 The Homomorphic Encryption Module

On the homomorphic encryption module our main contribution is a C++ class called NTTTools. This class provides a set of tools to manipulate polynomials on the ideal lattice setting (i.e. working modulo an integer and modulo a polynomial $X^n + 1$, n being a power of two). This class uses different techniques, namely the Number Theoretic Transform (NTT) and a Chinese Remainder Theorem (CRT) representation (see the following below for a detailed description) to ensure high performance.

Using this object we have implemented two lattice-based encryption schemes: NTTLWE, based on a classic Ring-LWE approach [22]; and NTRU, based on the recent provably secure versions of NTRU [41]. In order to do comparisons with classical homomorphic encryption schemes we have also done a Paillier implementation based on GMP [42]. In Fig. 8 we have tried to illustrate the fact that NTTLWE and NTRU essentially rely on NTTTools for their operations and the less possible on multi-precision libraries such as GMP and FLINT [43]. Paillier’s scheme, on the other hand, which is based on large integer modular exponentiation, is entirely based on GMP.

4.2.1 NTTTools

When working in an ideal lattice setting, such as the one of Ring-LWE and NTRU, we usually work with polynomials of a given degree n and coefficients are taken modulo a given integer p . Typically, n is a multiple of two above 512 and p is a product of primes of at least 30 bits. When many homomorphic operations are to be done p grows rapidly, and in the extreme case of fully-homomorphic encryption its bitsize grows to the hundreds. Additions of polynomials in these rings are done coefficient by coefficient and multiplications are polynomial products. Coefficients are reduced modulo an integer and polynomials are reduced modulo $X^n + 1$, which ensures constant rep-

Parameters	(1024, 60)	(2048, 120)	(4096, 120)
Input size (per poly)	20Kbits	100Kbits	192Kbits
Pre-processing (per poly)	4.2us	19us	38us
Pre-processing (PIR tput)	4.8Gbps	5.2Gbps	5Gbps
Processing (per poly)	0.57us	2.3us	4.8us
Processing (PIR tput)	18Gbits/s	22Gbits/s	20Gbits/s

Figure 9: PIR pre-processing and processing time and throughput on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz, for different crypto parameters. Input sizes are the maximum plaintext sizes given in Figure 1. Pre-processing of a polynomial corresponds to NTT and CRT transforms. Inverse transforms give similar results. Processing corresponds to a fused multiply and add (FMA). This operation’s throughput will vary a lot depending on memory saturation: in this setting, if all operands and result change on each operation, processing time is multiplied by three with respect to the given values. Here we used the same memory transfers as in our PIR scheme: for a given thread only one operand varies most of the time. Throughput is given with respect to input data: in pre-processing for each polynomial (Input size) bits are treated; in processing two polynomials must be processed to deal with (Input size) bits.

resentation size for the polynomials when going through such operations. Products with polynomials of such a high degree incur huge computation costs, with standard multiplication in $O(n^2)$ and even with other techniques such as Karatsuba in $O(n^{1.585})$.

In the NTTTools object we use two representations to reduce computational costs: NTT for polynomials [44] and Chinese Remainder Theorem (CRT) for integers. The Homomorphic-Encryption Library of Halevi and Shoup [45] implements the encryption scheme of Brakerski, Gentry and Vaikuntanathan [46]. They provide an object they called Double-CRT which provides NTT and CRT representation of polynomials as NTTTools does. We will compare to this work in this section.

Using the NTT and the CRT to accelerate polynomial multiplications is standard and will not be described in detail in this paper, we will just focus on the impact of their usage. The reader is for example referred to [45]. Using an NTT representation allows to compute polynomial multiplications with a linear cost in n instead of quadratic for the trivial algorithm. Transforming a polynomial into NTT form and back can be done in quasi-linear speed (in $O(n \log n)$). The CRT representation ensures that the multiplication cost is also linear in $\log p$, instead of quadratic for a trivial algorithm. Transforming an integer into CRT representation and back has a quadratic cost in $\log p$.

Figure 9 gives performance results for pre-processing, which corresponds to importing data into NTT/CRT form polynomials, and processing, which correspond to Fused Multiply and Add (FMA) operations. The data splitting and CRT (if done) operations are pretty fast, and the main performance bottleneck is computing the NTT in our

polynomial ring. Tests correspond to the same laptop as in Section 3 using all of its cores with multi-threading. Activating multi-threading is important as there are memory bandwidth issues that have an impact on performance. The tests shown are consistent with the performance results shown in Section 3: pre-processing is done roughly at 5Gbits/s and processing at 20Gbits/s. Using parameters (2048, 120) gives optimal performance as the input size to polynomial size ratio is the best.

Comparison with [45] The Double-CRT object proposed in [45] is much more elaborated than NTTTools and has many functions needed for fully-homomorphic encryption that we have not implemented. It is also more flexible as polynomial degrees can be arbitrary whereas in NTTTools polynomials degrees must be a power of two.

On the other side, the simplicity of our setting has allowed us to do some interesting choices. First we use Harvey’s NTT algorithm [47] which is very fast but only works for some polynomials degrees (powers of two). We also define statically the primes potentially forming the moduli which leads to various compile-time optimizations. And last but not least, we have built our library entirely from scratch without using any external library (Double-CRT is built over NTL which in turn is built over GMP) which results in a big performance improvement.

HElib supposes that the user defines the homomorphic computations he needs to do and then an underlying routine defines a complete FHE context for him. In particular the user cannot choose to just use one or two primes, so we had to tweak the code to do comparable tests.

Performance for polynomial multiplications and additions is slightly faster (between x2 and x3) with NTTTools, as Fig. 10 shows. The gap is much larger for pre-computation (x50). The reason for that is our choice to restrict ourselves to powers of two for polynomial degrees, which opens up the usage of nice algorithms such as the one in [47].

Finally, memory usage is much lower with NTTTools, which is not surprising given that we are in a simpler setting. For polynomials of degree 1024 and 60-bit coefficients, the memory footprint in NTTTools is of 8 Kbytes by default and twice that with pre-computed quotients. Using Double-CRT it is harder to evaluate the footprint as some data (such as the FHE context) is shared, but for large amounts of Double-CRT objects memory usage increases linearly at 40Kbytes per object.

NTTTools and the schemes we developed based on it will therefore be an interesting replacement of Double-CRT for those looking for fast basic polynomial computation on the ideal setting or simple homomorphic operations. Those looking for more advanced operations should use Double-CRT.

Parameters	(1024, 60 44)	(2048, 120 132)
Pre-processing (Double-CRT)	178us	1100us
Pre-processing (NTTTools)	4.2us	19us
Processing (Double-CRT)	5us	27us
Processing (NTTTools)	2.3us	9.6us

Figure 10: Pre-processing (NTT and CRT) and processing (multiply and add) times with Double-CRT and NTTTools. Modulus size must be a multiple of 44 in Double-CRT (this allows them to do double precision floating point operations for modular reductions). We chose moduli sizes to be the closest possible. Tests are *on a single-core* (as Double-CRT gave a segmentation fault with openmp) of a MSI GT60 laptop with a Core i7-3630QM 2.67GHz. Pre-processing is much faster with NTTTools (x50), mainly due to Harvey’s NTT algorithm (which is usable as we restricted ourselves to powers of two for polynomial degrees). In processing the gap is smaller (between x2 and x3) but NTTTools still performs better.

4.2.2 NTT-based Ring-LWE Encryption

Our scheme is basically the symmetric homomorphic encryption scheme of [28], which is described in the Appendix. The homomorphic encryption scheme resulting from the modifications we propose is, from a security point of view, equivalent to the scheme described in the appendix as all the modifications are public and reversible.

The basic idea is that the polynomials that usually describe the inputs (secret key, randomness, messages) are pre-processed by computing their NTT. After decryption an inverse NTT is performed to retrieve the message. With such a transformation, encryption and decryption can be done by coordinate-wise multiplication and additions which leads to very high performance results.

Describing how each algorithm is transformed by the usage of the NTT is of little interest and pretty straightforward. There are only two important points. The first is that each time there is a uniform polynomial in the encryption scheme algorithms we do not need to compute a NTT. Indeed the NTT and inverse NTT are one-to-one functions that map a finite space to itself and thus are permutations of their domain. Thus taking a uniform element and applying the NTT is exactly the same as just taking a uniform element. The second is that each time there is a product to compute, one of the two terms is long-lived (the secret key, or a constant). It is therefore always possible to use rapid modular multiplications using pre-computed data.

Having these two ideas in mind it is easy to see that encryption requires only the computation of a single NTT and some basic operations (negligible compared to the NTT). This is specially true as all the arithmetic operations we do are coordinate-wise and use a CRT representation allowing to handle numbers through the basic instruction set. This is not true for decryption. At first sight, the most costly operation in decryption will be the

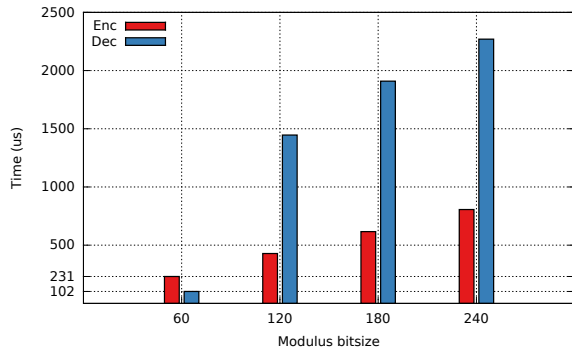


Figure 11: Encryption and decryption times for polynomial degree 4096 and varying modulus size, on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz. Note that encryption costs increase linearly in the modulus size but also the size of the associated ciphertexts and plaintexts. The large jump in decryption costs comes from the usage of GMP for moduli strictly above 60 bits.

inverse NTT. It is, if we use a modulus of 60 bits, but not for larger moduli. Indeed, it is important to notice that all the arithmetic operations use the basic instruction set *except* the separation of the noise and the message in the decryption function. If we are using more than one modulus, in order to separate the noise and the message in the scheme described in the Appendix, we need to get the value of each coordinate in non CRT representation. This is done by multiplying the elements of the CRT tuple by what we call *lifting coefficients*. This operation is done without modulus reduction and requires a few multiplications of $\log_2 q$ bits elements. For this operation we need to use a multi-precision library. In practice the decryption cost is multiplied by a factor 10 as soon as we start using such a library. Figure 11 shows this evolution.

This is the only point in which we use GMP on the NTTLWE object (by using the `poly2mpz` function of NTTTools). In practice this results in a very significant performance drop. Thus, even if higher moduli give better results for expansion factor or cPIR reply generation throughput, the optimizer will almost never choose parameters with a moduli beyond 120 bits as decryption costs quickly become the main bottleneck for performance.

Note however that for a modulus of 60 bits, performance is surprisingly high. We are able to generate a query at 2.2Gbits/s and decrypt an incoming reply at 5Gbits/s. This is quite independent of the polynomial degree as the costs of encryption and decryption increase linearly in it but ciphertext and plaintext size too. In practice, a laptop can send queries and receive and decrypt at max available bandwidths in all settings, using a single core. With a modulus of 120 bits, encryption scales well as it is possible to generate a query at 2.5Gbits/s, but decryption suffers from the CRT lifting and an incoming reply can "only" be decrypted at 710Mbits/s.

4.2.3 NTT-based NTRU Encryption

We used a similar approach to develop an NTT-based NTRU encryption scheme. However, even with a moduli of 60 bits, the decryption step requires a double precision floating point division for each coordinate of a ciphertext. The decryption performance is so low when compared with NTTLWE that NTTNTRU is never chosen by the optimizer as a suitable replacement of NTTLWE. For these reasons we will not provide specific details about this part of the library.

4.3 The cPIR Module

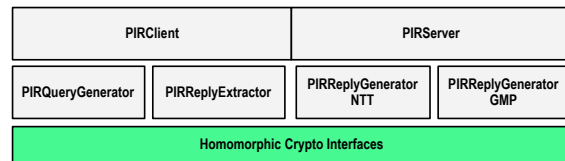


Figure 12: cPIR architecture

To be precise, the cPIR module as described in the general architecture is composed of a sub-module which contains all the cPIR objects and functions (query generator, reply generator, reply extractor); and a wrapper sub-module which provides the classical cPIR on a database application (client, server). This wrapper module also implements most of the interface to optimize this application through functions allowing to measure network and cPIR processing performance.

Our main contribution in this module is the generality and flexibility it provides. It can handle cPIR techniques such as recursion and aggregation (see 2.2) and can be used with any homomorphic encryption scheme implementing a given interface.

The Homomorphic Encryption Interface The cPIR module has been built so that any homomorphic encryption scheme implementing a given set of generic interfaces can be used with it. Of course, the encryption scheme must implement basic encryption operations such as encrypt and decrypt and basic homomorphic operations such as `Absorb` and `Sum`, but there are other less evident functions that need to be implemented. For example, the cryptosystem must be able to propose a set of instantiations for a given security level. It must also be able to do self-tests for client and server performance, and provide information such as plaintext, and ciphertext, and key sizes, etc. All these functions are documented in the library.

4.4 Optimizer

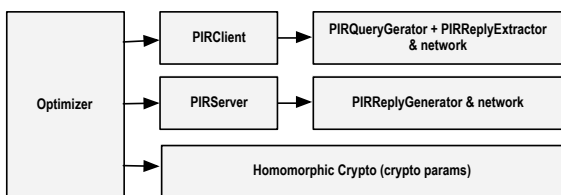


Figure 13: Optimization architecture

The optimizer module provides the best parameters given a target function: round trip time (since the query starts being generated until the reply is completely decrypted), total resources (total CPU time for the client and server plus total network time), or cost (based on a cloud service cost per second of CPU and Gigabyte of network usage of a quad-core server). By default these function are optimized in a *reasonable* mode in which the function to minimize is added to a scaled version of the total resources so that the amount of resources used does not grow to much for a small improvement on the unmodified target function. It is possible to change this behavior at compilation to strictly optimize unmodified target functions. Adding or modifying target functions is also very easy.

Modus Operandi The optimizer can be called directly. However, the cPIR client has some nice tools that are skipped if we use it that way. If a user only wants to obtain the optimizer results he can call the cPIR client in dry-run mode. The cPIR client, whether it is on dry-run mode or not, parses the options from the command line and configuration files, does network performance tests and gives a set of fixed variables to the optimizer. The optimizer searches the best parameters considering those fixed variables as constraints.

Among these variables there is a database description (number of elements and size), bandwidth values, minimum security bits, the target function and constraints on the different parameters. Among those constraints there can be maximums, minimums, or fixed values for parameters such as aggregation and recursion, and a given encryption scheme or even a given set of parameters for an encryption scheme. Given these constraints, the optimizer defines a space of possibilities to explore and does a full search estimating the target function values to find the best option. The only exception to full search is aggregation, for which there is a dichotomy until the number of possibilities is small enough. The reason why we do a dichotomy for aggregation is that its effects are pretty easy to evaluate when the space of possibilities is big: query related costs go down and reply related costs go up. For other parameters this is not true and thus we can hardly do convexity assumptions. Even with the full space search

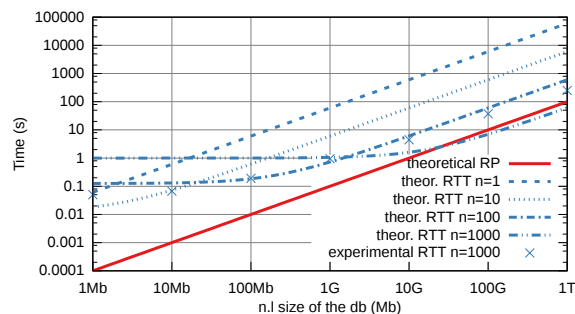


Figure 14: Theoretical and experimental Round-trip times (RTT) and theoretical request processing times (RP) of XPIR serving static data on a MSI GT60 laptop with a Core i7-3630QM 2.67GHz on a FTTH network. The experimental results (crosses) show that the optimizer defines the aggregation parameter to lower n (the number of database elements) when needed so that the performance result always matches the best theoretical line. Results are optimal for small databases and reasonable but not optimal for large databases.

for most of the parameters, the optimizer runs in a few milliseconds and gives very good results.

To illustrate the optimizer work, Figure 14 shows both the theoretical and experimental round trip time for various database sizes and n values. The red line represents the theoretical request processing necessary to handle the database size, the blue lines represent the theoretical RTT when it is bounded by networking issues (uploading requests or downloading replies). These theoretical lines represent what would be the RTT for various n when no aggregation nor recursion is used. For example, for $n = 1000$ in 1Mb to 1Gb databases, uploading the request would take 1 second. The blue crosses show the experimental results obtained with the help of the optimizer. As one can see, in practice, the optimizer chooses the cPIR parameters in order to match (almost all the time) the best RTT attainable. For example, in the case of 10Mb database, it used aggregation to match the theoretical $n = 10$ performance. The differences observed in some cases can be explained by practical concerns, *e.g.* the 0.7 second RTT for 1Mb database is due to delays introduced by the networking layers or the difference with the optimal RTT (near RP time) for large databases such as 100Gb and 1Tb are due to the fact that the optimizer chose recursion instead of aggregation but underestimated its cost. Generally speaking, we can say that the choices of the optimizer are not always the perfect ones but on the other hand are always reasonable.

5 Conclusion

Lattice based cryptography brought groundbreaking breakthroughs on worst-case to average-case reductions and on fully-homomorphic encryption. However it has been for a long time seen as impractical, despite its excel-

lent asymptotic results. This field of research has matured a lot. The arrival of the ideal lattice setting, and the development of many performance tweaks has changed completely the attainable performance in a non-asymptotic sense. cPIR has often been considered as a protocol that would never be practical [1]. Lattice-based cryptography brings a real overhaul on this, as cPIR becomes feasible even for people that don't own a high-end server. We have shown that our protocol can be used to process a wide range of databases in a few seconds, even for 100Gb databases. This would have taken thousands of seconds with a number theory cryptosystem as Pailier, which would have processed the database at 1Mbit/s. Sending the database, even over a 100Mbit/s link would have increased by a factor one hundred the times we presented in our experiments. These results are on a commodity laptop, using a high end server in a multi-core setting can only increase this difference further. However this is not our purpose, what we wanted to highlight is that lattice-based cryptography has transformed the utterly impractical into something feasible by everyone. As we want to show that it is feasible by everyone, we have included the auto-optimize tools that will allow anybody to use our library without being an expert on cryptography. We are eager to hear from these people's experiences.

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A Our Ring-LWE Encryption Scheme

This is basically the symmetric homomorphic encryption scheme of [28] with a composite modulus. Security reduction is preserved using the same arguments as in [48]. From the security point-of-view, one must achieve indistinguishability against chosen plaintext attacks which corresponds to the highest security an homomorphic encryption scheme can achieve (see e.g. [49]). Based on the analysis of [28], our scheme ensures indistinguishability if the standard lattice problem Ring-LWE is hard. This property offers strong guaranties on ciphertext secrecy as proved by Goldwasser and Micali [50]. When used for a cPIR protocol, an encryption scheme with indistinguishability against plaintext attacks ensures that two queries for two different elements of a database are indistinguishable, using a standard hybrid argument.

Notations: \mathbb{Z}_q denotes the set of relative integers modulo q (and not q -adic integers). If S is a set $x \leftarrow S$ represents a uniform sample from S , for a distribution χ , $x \leftarrow \chi$ represents a sample following that distribution. $R_q = \mathbb{Z}_q[X] / \langle X^n + 1 \rangle$ represents the polynomials such

that after each operation they are reduced by division modulo $X^n + 1$. Unless specified otherwise, all scalar operations are mod q . For two polynomials $a, b \in R_q$, $a + b$ is the polynomial obtained by adding their coefficients, $a * b$ is the usual polynomial multiplication reduced modulo $X^n + 1$, and $a \otimes b$ is the polynomial obtained by multiplying their coefficients coordinate-wise.

ParamGen($1^k, h_a$):

Input: A security parameter k ; A maximum number of additions h_a

Output: A modulus q ; A degree n for a quotient polynomial; A distribution χ

KeyGen(q, n):

Input: A modulus q ; A polynomial degree n

Output: A polynomial in $R_q = \mathbb{Z}_q[X] / \langle X^n + 1 \rangle$

1. Output : $s \leftarrow R_q$

Encrypt(s, m):

Input: A secret key s in the polynomial ring R_q ; A message m in the polynomial ring R_q with coefficients in $[0..t]$

Output: A ciphertext $(a, b) \in R_q^2$

1. $a \leftarrow R_q$
2. $e \leftarrow \chi$
3. $e' = e \otimes t_v + m$ where $t_v \in R_q$ has all its coefficients set to t
4. $b = (a * s) + e'$
5. Output: (a, b)

Decrypt($s, (a, b)$):

Input: A secret key $s \in R_q$; A ciphertext $(a, b) \in R_q^2$

Output: A plaintext $m \in \mathbb{Z}_t^n$

1. $e = b - (a * s)$
2. Output: $m = e \text{ mod } t$

Add((a_1, b_1), (a_2, b_2)):

Input: Two ciphertexts, encryptions of m_1 and m_2

Output: A ciphertext that decrypts to $m_1 + m_2 \text{ mod } t$

1. Output: $(a_1 + a_2, b_1 + b_2)$

Absorb($p, (a, b)$):

Input: A polynomial $p \in R_q$ with coefficients in $\{0..t-1\}$; A ciphertext $(a, b) \in R_q^2$, encryption of a polynomial m

Output: A ciphertext which decrypts to $m * p$

1. Output: $(p * a, p * b)$

ParamGen takes as an input a security parameter k and a maximum number of additions h_a and outputs a set of parameters. For performance reasons we force among the outputs of this function $n \in \{1024, 2048, 4096\}$ and q to be a multiple of 60-bit or 30-bit primes such that each prime is congruent to 1 modulo $2n$ (in order to be able to use the NTT). This function generates parameters following the same approach as in [51], with some more conservative choices. The noise distribution is a discrete gaussian of parameter $s = k$, the security parameter. For any value of k greater or equal to 80, we therefore use a noise level well above the bound needed by the security reductions $s > 2\sqrt{n}$ for all values of n . As usual we truncate this distribution taking into account the security to be below a statistical distance of 2^{-k} .

In order to obtain k bits of security we consider an attacker that wants to obtain an advantage $\epsilon = 2^{-k/2}$ with $\tau = 2^{-k/2}$ computing cycles. As noted in [51] this is the best strategy for an attacker in our setting. As a query can be composed of many ciphertexts, we suppose that the attacker is able to build an attack with an optimal amount of ciphertexts. For a couple of parameters (n, q) we start by setting k to a small value, iteratively increase it, and test if it fulfills the conditions of [51]. More precisely, for each test we follow the approach of [51] to fix the size of the aimed vector size for LLL using the advantage $\beta = (q/s)\sqrt{(\ln(1/\epsilon)/\pi)}$. We then define the best root Hermite factor δ the attacker is able to use in LLL using $\tau = 2^{-k/2}$ cycles which is given by $\log(\tau) = 1.8/\log(\delta) - 80$ (note that we consider cycles and not seconds, which changes the constant in this formula with respect to [51]). We then compute the shortest vector we can get with LLL given δ which is $2^{2\sqrt{n \log q \log \delta}}$ and see if it is below the aimed vector size. If so, the test is failed. If not, we increase k and do another test.

B Using the library

This section is a reshaped version of the file README.md at the root of <https://github.com/XPIR-team/XPIR>. It is included in the paper:

- to help the reader that wants to experiment with the library,
- to give some ideas of how installation/usage works for the reader that does not want or cannot experiment with it.

B.1 Installation

Requirements: $g++ \geq 4.8$, $gcc \geq 4.8$, on a 64-bit Linux OS XCode, Macports, $gcc \geq 4.8$, clang on Mac OSX.

Get a copy of the project with:

git clone <https://github.com/XPIR-team/XPIR.git>

Then execute the following commands to compile everything (boost, gmp, mpfr, create essential files, build

client and server):

```
$ cd xpire
$ make
```

When this is done you can check that the server/client work correctly with the following commands:

```
$ cd server
$ ./check-correctness
```

The first test should be pretty long (to build initial performance caches) and then a set of tests should display CORRECT or "Skipping test...". If you get INCORRECT tests then something went wrong ...

B.2 Usage

XPIR is composed of a server and a client. Both must be started on their respective directories. Thus to start the server execute:

```
$ cd server
$ ./build/PIRServer
```

And to start the client execute (on a different terminal):

```
$ cd client
$ ./build/PIRClient
```

By default the client tries to reach a local server but a given IP address and port can be specified, use `-help` to get help on the different options for distant connections.

If run without options the PIR server will look for files in a directory `db` inside the server directory and consider each file is a database element. The client will present a catalog of the files and ask the user to choose a file. When this is done the client will run an optimizer to decide which are the best cryptographic and PIR parameters to retrieve the file. Then he will send an encrypted PIR Query (i.e. a query that the server will mix with the database without understanding which element it allows to retrieve) to the server. The server then computes an encrypted PIR reply and sends it to the client. Finally, the client will decrypt this reply and store the resulting file in the reception directory inside the client directory.

B.3 Available options for the server (PIRServer command)

`-h, --help`

Print a help message with the different options.

`-z, --driven arg`

Server-driven mode. This mode is to be used when multiple clients will connect to the server with the same cryptographic and PIR parameters. This allows the server to import the database into RAM and to perform precomputations over the database for the first client which *significantly increases the performance for the following clients

if LWE-based cryptography is used*. The first client will ask for a given configuration (depending on its optimizer and on the command-line constraints given to the client). After this configuration client, the server will tell the following clients that he is in server-driven mode and that the configuration is imposed. The configuration given by the first client is stored in file `arg` or in `exp/PIRParams.cfg` if `arg` is not specified for further usage (see `-L` option).

`-L, --load_file arg`

Load cryptographic and PIR parameters from `arg` file. Currently unavailable (see issues).

`-s, --split_file arg (=1)`

Only use first file in `db` directory and split it in `arg` database elements. This allows to have a large database with many fixed size elements (e.g. bits, bytes, 24-bit depth points) into a single file which is much more efficient from a file-system point of view than having many small files. Building databases from a single file with more complex approaches (e.g. csv, or sqlite files) would be a great feature to add to XPIR.

`-p, --port arg (=1234)`

Port used by the server to listen to incoming connections, by default 1234.

`--db-generator`

Generate a fake database with random elements instead of reading it from a directory. This is useful for performance tests. It allows to deal with arbitrary databases without having to build them on the file-system and to evaluate performance costs without considering disk access limitations.

`-n, --db-generator-files arg (=10)`

Number of files for the virtual database provided by the DB generator.

`-l [--db-generator-filesize] arg (=12800000)`

Filesize in bytes for the files in the virtual database provided by the DB generator.

`--no-pipeline` No pipeline mode. In this mode the server executes each task separately (getting the PIR Query, computing the reply, sending it). Only useful to measure the performance of each step separately.

B.4 Available options for the client (PIRClient command)

`-h, --help`

Display a help message.

`-i, --serverip arg (=127.0.0.1)`

Define the IP address at which the client will try to contact the PIRServer.

`-p [--port] arg (=1234)`

Define the port at which the client will try to contact the PIRServer.

`-c, --autochoice`

Don't display the catalog of database elements and automatically choose the first element without waiting for user input.

`--dry-run`

Enable dry-run mode. In this mode the client does not send a PIR Query. It runs the optimizer taking into account the command-line options and outputs the best parameters for each cryptosystem (currently NoCryptography, Paillier and LWE) with details on the costs evaluated for each phase (query generation, query sending, reply generation, reply sending, reply decryption). If a server is available it interacts with it to set the parameters: client-server throughput and server-client throughput. It also requests from the server the performance cache to evaluate how fast the server can process the database for each possible set of cryptographic parameters. If no server is available it uses default performance measures. The other parameters are set for the default example: a thousand mp3 files over ADSL, aggregation disabled and security $k=80$. Each of these parameters can be overridden on the command line.

`--verbose-optim`

Ask the optimizer to be more verbose on the intermediate choices and evaluations (as much output as in the dry-run mode).

`--dont-write`

Don't write the result to a file. For testing purposes, it still will process the reply (decryption of the whole answer).

`-f, --file arg`

Use a config file to test different optimizations in dry-run mode (see `exp/sample.conf`). Must be used with the `--dry-run` option or it is ignored.

B.5 Available options for the optimizer (through PIRClient command)

`-n, --file-nbr arg`

Used in dry-run mode only: Override the default number of database elements.

`-l, --file-size] arg`

Used in dry-run mode only: Override the default database element size (in bits).

`-u, --upload arg`

Force client upload speed in bits/s (bandwidth test will be skipped). This is valid in dry-run or normal mode (e.g. if a user does not want to use more than a given amount of his bandwidth).

`-d, --download arg`

Force client download speed in bits/s (bandwidth test will be skipped). This is valid in dry-run or normal mode.

`-r, --crypto-params arg`

Limit with a regular expression `arg` to a subset of the pos-

sible cryptographic parameters. Parameters are dependent on each cryptographic system:

** NoCryptography if a trivial full database download is to be done after which PIRClient stores only the element the user is interested in.

** Paillier:A:B:C if Paillier's cryptosystem is to be used with A security bits, a plaintext modulus of B bits and a ciphertext modulus of C bits.

** LWE:A:B:C if LWE is to be used with A security bits, polynomials of degree B and polynomial coefficients of C bits.

For example it is possible to force just the cryptosystem with NoCryptography.* or LWE.*, or ask for a specific parameter set like Paillier:80:1024:2048. Specifying the security with this option is tricky as it must match exactly so better use `-k` for this purpose.

`-k, --security arg (=80)`

Minimum security bits required for a set of cryptographic parameters to be considered by the optimizer.

`--dmin arg (=1)`

Min dimension value considered by the optimizer. Dimension is also called recursion in the literature. It is done trivially (see the scientific paper) and thus for dimension d query size is proportional to $d \times n^{1/d}$ and reply size is exponential in d . For databases with many small elements a $d \geq 1$ can give the best results, but only in exceptional situations having $d > 4$ is interesting.

`--dmax arg (=4)`

Max dimension value considered by the optimizer.

`-a, --alphaMax arg (=0)`

Max aggregation value to test (1 = no aggregation, 0 = no limit). It is sometimes interesting to aggregate a database with many small elements into a database with fewer but larger aggregated elements (e.g. if database elements are one bit long). This value forces the optimizer to respect a maximum value for aggregation, 1 meaning that elements cannot be aggregated.

`-x, --fitness arg (=1)`

Set fitness method to:

0=SUM Sum of the times on each task

1=MAX Max of server times + Max of client times

2=CLOUD Dollars in a cloud model (see source code)

This sets the target function of the optimizer. When studying the different parameters the optimizer will choose the one that minimizes this function. 0 corresponds to minimizing the resources spent, 1 to minimizing the round-trip time (given that server operations have are pipelined and client operations are also, independently, pipelined), 2 corresponds to minimizing the cost by associating CPU cycles and bits transmitted to money using a cloud computing model.