

## NSEC5: Provably Preventing DNSSEC Zone Enumeration

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**Abstract**—This paper uses cryptographic techniques to study the problem of zone enumeration in DNSSEC. DNSSEC is designed to prevent network attackers from tampering with domain name system (DNS) messages. The cryptographic machinery used in DNSSEC, however, also creates a new vulnerability, *zone enumeration*, enabling an adversary to use a small number of online DNSSEC queries combined with offline dictionary attacks to learn which domain names are present or absent in a DNS zone.

We prove that the design underlying current DNSSEC standard, with NSEC and NSEC3 records, inherently suffers from zone enumeration: specifically, we show that security against network attackers and privacy against zone enumeration cannot be satisfied simultaneously unless the DNSSEC server performs online public-key cryptographic operations.

We then propose NSEC5, a new cryptographic construction that solves the problem of DNSSEC zone enumeration while remaining faithful to the operational realities of DNSSEC. NSEC5 can be thought of as a variant of NSEC3 in which the unkeyed hash function is replaced with an RSA-based keyed hashing scheme.

### I. INTRODUCTION

DNSSEC was introduced in the late 1990s to protect the Domain Name System (DNS) from network attacks. With DNSSEC, the response to a DNS query is authenticated with a digital signature; in this way, the resolver that issues the DNS query (“What is the IP address for `www.example.com`?”) can be certain that the response (“155.41.24.251”) was sent by an authoritative nameserver, rather than an arbitrary network attacker. The road to DNSSEC deployment has been rocky, and a variety of technical issues have forced the Internet community to rewrite the DNSSEC standard multiple times. One of the most interesting of these issues is the problem of *zone enumeration* [Ber11], [BM10], [AL01]. Zone enumeration allows an adversary to learn the IP addresses of all hosts in a zone (including routers and other devices), creating a foothold from which it can launch more complex attacks. While a number of standards (RFC 4470 [WI06], RFC 5155 [LSAB08]) have tried to fix the zone enumeration problem, a complete solution to the problem has remained mysteriously elusive. In this paper, we use cryptographic lower bounds to explain why previous techniques based on hashing failed to solve the problem. Our result shows that achieving privacy guarantees in this setting (while preserving the security property of DNSSEC) necessitates the use of public-key cryptographic operations

in the online phase of the protocol. Moreover, we provide a new cryptographic construction that addresses the problem of DNSSEC zone enumeration while remaining faithful to the operational realities of DNSSEC.

#### A. DNSSEC.

For the purpose of understanding the zone enumeration problem, we can partition the functionalities of DNSSEC into two distinct parts. The first is to provide an authenticated *positive* response to a DNS query. (For example, query: “What is the IP address for `www.example.com`?”; answer: “`www.example.com` is at 155.41.24.251”.)

The second is to provide an authenticated *denial of existence*, when no response to the query is available. (For example, query: “What is the IP address for `aWa2j3.example.com`?”; answer: “`aWa2j3.example.com` is a non-existent domain”.) DNSSEC deals with these functionalities in different ways.

For positive responses, the authoritative nameserver for the zone (*i.e.*, the nameserver that is authorized to answer DNS queries for domains ending in `example.com`) keeps a finite set  $R$  of signed resource records; each record contains a mapping from one domain name to its IP address(es) and is signed by the zone’s secret keys. Importantly, these signatures need not be computed online in response to live DNS queries, but instead are precomputed ahead of time and stored at the nameserver. This has the twin advantages of (1) reducing the computational load at the nameserver, and (2) eliminating the need to trust the nameserver (since it need not store the signing key). This second advantage is especially important because most zones have more than one authoritative nameserver, and some nameservers might even be operated by entirely different organizations than the one that administers the zone<sup>1</sup>. In what follows, we will use the term *primary nameserver* (or simply *primary*) to describe nameservers that are trusted, and *secondary nameservers* (or simply *secondary*) to describe those that are not.

#### B. The DNSSEC Zone Enumeration Problem

The zone enumeration problem becomes an issue when we consider DNSSEC negative responses. The trivial idea of responding to every query for a non-existent domain with the precomputed signed message “Non-existent domain” opens the system up to replay attacks. Another trivial idea of precomputing signed responses of the form “\_\_\_\_\_ is a non-existent domain” also fails, since the number of possible queries that deserves such a response is infinite, making precomputation of signed responses infeasible. Instead, RFC4034 [AAL<sup>+</sup>05b] defined an NSEC record to be used for precomputed denial-of-existence as follows: a lexicographic ordering of the names present in a zone is prepared, and every consecutive pair of names is signed; each pair of names is an NSEC record. Then,

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<sup>1</sup>For example, the zone `umich.edu` has two authoritative nameservers run by the University of Michigan (`dns1.itd.umich.edu` and `dns2.itd.umich.edu`) and one run by the University of Wisconsin (`dns.cs.wisc.edu`) [RS05].

non-existence of a name (`x.example.com`), the nameserver returns the precomputed NSEC record for the pair of existent names lexicographically before and after the non-existent name (`w.example.com` and `z.example.com`), as well as its associated DNSSEC signatures.<sup>2</sup> While this solution elegantly eliminates the need to trust the nameserver, and allows for precomputation, it unfortunately allows for trivial *zone enumeration attacks*; namely, an adversary can use NSEC records to enumerate all the domain names present in the zone.

Why is zone enumeration a problem? This question has created some controversy, with many in the DNSSEC community initially arguing that it is actually *not* a problem (e.g., RFC 4033 [AAL<sup>+</sup>05a]), before eventually arriving at consensus that it is a problem from some zones (RFC 5155 [LSAB08]). Zone enumeration allows an adversary to learn the IP addresses of all hosts in a zone (including routers and other devices); this information can then be used to launch more complex attacks, some of which are mentioned in RFC 5155:

Though the NSEC RR meets the requirements for authenticated denial of existence, it introduces a side-effect in that the contents of a zone can be enumerated. This property introduces undesired policy issues. ... An enumerated zone can be used, for example, as a source of probable e-mail addresses for spam, or as a key for multiple WHOIS queries to reveal registrant data that many registries may have legal obligations to protect. Many registries therefore prohibit the copying of their zone data; however, the use of NSEC RRs renders these policies unenforceable.

Indeed, some zones (e.g., `.de`, `.uk`) require protection against zone enumeration in order to comply with European data protection laws [San04], [Ait11, pg. 37].

Thus, in 2008, RFC 5155 [LSAB08] suggested NSEC3, a precomputed denial of existence technique, designed to make zone enumeration more difficult. With NSEC3, first each domain names present in a zone is cryptographically hashed, and then all the hash values are lexicographically ordered. Every consecutive pair of hashes is an NSEC3 record, and is signed by the authority for the zone. To prove the non-existence of a name, the nameserver returns the precomputed NSEC3 record (and the associated DNSSEC signatures) for the pair of hashes lexicographically before and after the *hash* of the non-existent name.<sup>3</sup>

Hashing the names makes trivial enumeration of the zone much more difficult, but the design nevertheless remains vulnerable to zone enumeration using an offline dictionary attack. Specifically, an adversary can issue several queries for random non-existent names, obtain a number of NSEC3 records, and then use rainbow tables (or other dictionary attacks for cracking hashes) to determine the names that are

present in the zone from the hashes in the NSEC3 records. In fact, Bernstein’s `nsec3walker` tool [Ber11] does just that, effectively checking up to  $2^{34}$  hash value guesses in one day, using a standard laptop and existing cryptographic libraries.

To blunt the impact of dictionary attacks, the RFCs do introduce a salt value (using the NSEC3PARAM record); however, in contrast to password-hashing applications that mitigate against dictionary attacks by using a unique salt for each user, NSEC3 commonly employs the same salt for the entire zone. Since changing the salt requires re-computing the signatures for the entire zone, RFC 6781 [KMG12] recommends updating the salt only when key-rollover takes place (a very infrequent—monthly, or even yearly—event), which makes the salt a fairly weak defense against dictionary attacks. Moreover, once an adversary has collected a number of NSEC3 records and the salt for the zone, it can use offline dictionary attacks to learn the records present in the zone. Indeed, RFC 5155 acknowledges this: “The NSEC3 RRs are still susceptible to dictionary attacks (i.e., the attacker retrieves all the NSEC3 RRs, then calculates the hashes of all likely domain names, comparing against the hashes found in the NSEC3 RRs, and thus enumerating the zone)” [LSAB08, Section 12.1.1].

### C. Our Model

Our story thus begins here. Today, DNSSEC deployments support NSEC and/or NSEC3 and remain vulnerable to zone enumeration attacks. In this paper, we use cryptographic lower bounds to explain why zone enumeration attacks could not be addressed by previous designs, and propose a new solution, called NSEC5, that protects against them.

Our first contribution is the following cryptographic model, which makes precise the desired notion of privacy:

**Model.** We have a trustworthy source, called a *primary nameserver*, which is trusted to determine the set  $R$  of names (`www.example.com`) present in the zone and their mapping to corresponding values (“155.41.24.251”). *Secondary nameservers* receive information from the primary nameserver, and respond to DNS queries for the zone, made by *resolvers*.

Our goal is to design a denial-of-existence mechanism that achieves the following:

**(1) Soundness.** The primary nameserver is trusted to determine the set  $R$  of names in the zone, and to provide correct responses to DNS queries. However, the secondary nameservers and other network adversaries are not trusted to provide correct responses to DNS queries. The soundness property ensures that bogus responses by secondaries or network adversaries will be detected by the resolver. This is the traditional DNSSEC security requirement of “data integrity and ... origin authentication” described in RFC 3833 [AA04].

**(2) Privacy.** Both primary and secondary nameservers are trusted to keep the contents of  $R$  private. (If they don’t, there is nothing we can do, since they already know  $R$ .) However, resolvers are not. The privacy property must ensure that the response to a query by a resolver must only reveal information about the queried domain name, and no other names. Our main definitional contribution is the formalization

<sup>2</sup>For simplicity of exposition, we ignore the issues of wildcard records and enclosers in our descriptions of NSEC and NSEC3; see RFC 7129 [GM14].

<sup>3</sup>There was also a subsequent Internet Draft [GM12] (that has since expired without becoming an RFC) proposing NSEC4. NSEC4 combines NSEC and NSEC3, allowing zones to opt-out from hashed names to unhashed names. Like NSEC3, NSEC4 is vulnerable to zone enumeration via offline dictionary attacks.

of this requirement to avoid zone enumeration, raised, *e.g.*, in RFC 5155 [LSAB08]

**(3) Performance.** We would like to limit the online computation that must be done by a nameserver in response to each query. This is discussed in *e.g.*, RFC 4470 [WI06].

The formal cryptographic model and security definitions are in Section II. We call a system satisfying these definitions a Primary-Secondary-Resolver (PSR) system.

#### D. Cryptographic Lower Bound

We demonstrate in Section IV that if the resolvers send queries in the clear (as they currently do in DNSSEC), then satisfying both the soundness and privacy goals implies that nameservers must *necessarily* compute a public-key cryptographic signature for each negative response. This explains why the approaches taken by NSEC and NSEC3, which limit the nameserver computation to cryptographic hashes, cannot prevent zone enumeration.

Moreover, we show that this problem cannot be solved on the resolver’s end of the protocol: we show that even if the resolvers pre-process the query, then resolver-to-secondary-nameserver protocol is *necessarily* a secure interactive message authentication protocol, for which the best known solution is a cryptographic signature anyway. In Section IV-C we discuss the question of whether our privacy requirements are “too strong” and argue that any meaningful relaxation still implies public-key authentication. Thus we conclude that preventing zone enumeration requires substantial (“public-key”) online computation, rather than just private-key computation such as evaluating a cryptographic hash function.

#### E. NSEC5: A Denial-of-existence Mechanism

Armed with the knowledge that privacy necessitates an online signature computation for every negative response, we present a new solution that requires two online hash computations and a single online RSA computation for each authenticated denial of existence. Our solution, called NSEC5, provably achieves soundness and privacy.

In designing NSEC5, our key observation is that we can “separate” our two security goals (soundness and privacy) using two separate cryptographic keys. To achieve soundness, we follow the traditional approach used in DNSSEC with NSEC and NSEC3, and allow only the primary nameserver to know the primary secret key  $SK_P$  for the zone; this primary secret key is used to ensure the soundness of the zone. However, we now make the crucial observation that, while the soundness definition does not allow us to trust the secondary nameserver, our privacy definition does (because if the secondary nameserver is untrusted, then privacy is lost, anyway, since it knows the entire zone). Thus, we achieve privacy by introducing a secondary key  $SK_S$ , that we provide to *both* the primary and secondary nameservers. The secondary key is *only* used to prevent zone enumeration by resolvers, and will have no impact on the soundness of the zone. The public keys  $PK_P, PK_S$  corresponding to  $SK_P$  and  $SK_S$

will, naturally, be provided to the resolver, using the standard mechanisms used to transmit public keys in DNSSEC.

We emphasize that privacy makes sense only when the secondary nameserver can keep some information secret (else,  $R$  is no longer private). Thus, the addition of  $SK_S$  to the secondary nameserver does not introduce any additional security vulnerability: if it is leaked, soundness is not compromised.  $SK_S$  can be distributed to secondary nameservers using the same mechanisms that are used to distribute the zone data.

**Construction.** Our NSEC5 construction is extremely similar to NSEC3: all we need to do is replace the unkeyed hash used in NSEC3 with a new “keyed hash”  $F$  that uses the secondary keys  $PK_S, SK_S$ . Our solution is as follows.

The secondary keys  $PK_S = (N_S, e_S)$  and  $SK_S = (N_S, d_S)$  are an RSA key pair. For each record  $x$  that is present in the zone  $R$ , the primary nameserver computes

$$S(x) = (h_1(x))^{d_S} \bmod N_S \quad \text{and} \quad F(x) = h_2(S(x)),$$

where  $h_1$  and  $h_2$  are hash functions. The resulting  $F$  values are lexicographically ordered, and each pair is signed by the *primary nameserver* using its key  $SK_P$  (just like in NSEC and NSEC3). The resulting pair of  $F$  values is an NSEC5 record.

To prove the non-existence of name  $q$  queried by the resolver, the *secondary* nameserver computes  $S(q)$  and  $F(q)$  using  $SK_S$ , and responds to the resolver with (1) the value  $S(q)$  and (2) the signed NSEC5 record for the hashes that are lexicographically before and after  $F(q)$ .

The resolver can then validate the response by first using  $PK_S$  to (1) check the RSA signature by verifying that  $(S(q))^{e_S} \bmod N_S = h_1(q)$ , (2) confirm that the NSEC5 record is validly signed by  $PK_P$ , and (3) check that  $h_2(S(q))$  is lexicographically between the hashes in the NSEC5 record. In other words,  $S(q)$  maintains soundness by acting as a “proof” that the value  $F(q)$  is the correct “keyed hash” of  $q$ . Note that it’s important that the keyed hash  $F(q)$  is a deterministic and verifiable function of  $q$ ; thus, our choice of the specific form of RSA signatures used to compute  $S$  is crucial (as opposed to signatures computed on the NSEC5 record itself using  $SK_P$ , which can be done using any secure signature algorithm).

**Security and Privacy.** In Section III we formally describe the NSEC5 scheme and prove that our construction satisfies both soundness and privacy as defined in Section II. Privacy follows because the resolver does not know the secondary key  $SK_S$ . This eliminates zone enumeration via offline dictionary attacks, since the resolver cannot compute the “keyed hash value”  $F(q)$  on its own; the only way it can learn  $F(q)$  is by asking online queries to the nameserver (or by breaking RSA!). Meanwhile, integrity follows because only the primary nameserver can sign NSEC5 records; the resolver can use the secondary public key  $PK_S$  to verify that the secondary nameserver computed  $S(q)$  correctly, and responded with the right NSEC5 record. If a malicious secondary wanted to announce a bogus non-existence record, he would not be able to produce a properly-signed NSEC5 record covering  $F(q)$ .

**Performance.** Our solution allows resolvers to verify using the same technologies they always used: hashing and validation

of RSA signatures. NSEC5 does, however, require a single online RSA computation at the secondary nameserver, making it more computationally heavy than NSEC and NSEC3 (and NSEC4). However, our lower bounds do prove this extra computation is necessary to eliminate zone enumeration. Additionally, only the zone administrators that require our strong privacy guarantees need to deploy NSEC5; others that don't can just use NSEC or NSEC3. We discuss the computational cost, as well as other issues regarding deployment in Section III-A.

We should note that online signing for denial of existence was already proposed in RFC 4470 [WI06] (and further discussed in RFC 4471 [SL06]). RFC 4470 suggested that every nameserver (even the secondary) be given the primary key for the zone, and used it to produce online signatures to responses of the form “ $q$  is a non-existent domain”. Some criticized the RFC 4470 solution because it compromises soundness (if a secondary nameserver is hacked or leaks its key). In contrast, our solution has the same computational complexity without suffering from the same risks to soundness, because the online signing is used only for looking up the correct NSEC5 record and cannot be used to produce a false denial of existence. Thus, a compromise of a secondary nameserver will not compromise soundness.

We therefore believe NSEC5 presents an attractive alternative to NSEC3 for those zone operators who require strong privacy against zone enumeration. Moreover, because NSEC5 is structurally very similar to NSEC3, it can incorporate the other performance and policy optimizations developed for DNSSEC, including NSEC3 opt-out or the space-saving techniques offered by NSEC4 [GM12].

#### F. Organization & Contributions

The organization of this paper follows the summary above. Section II presents our model and security definitions; we use a traditional DNSSEC notion of soundness, and our main definitional contribution is in our notion of privacy. Our next contribution is our NSEC5 construction; we present NSEC5 in Section III and prove it satisfies soundness and privacy. Our final contribution is a number of cryptographic lower bounds, which explain why NSEC5 requires online signing at the secondary nameserver in order to achieve simultaneous soundness and privacy, which we present in Section IV. Our results are supported by the standard cryptographic definitions (signatures, random oracles) in Appendix A.

#### G. Other related work

There are several tools and primitives in the cryptographic literature that are related to our work. The first is *zero-knowledge sets*, introduced by Micali, Rabin and Kilian (ZKS for short) and its generalization to zero-knowledge elementary databases [MRK03]. The latter is a primitive where a prover can commit to a database, and later open and prove the value in the database to a verifier in a zero knowledge fashion. One can use ZKS in our setting, where the resolver is the ZKS verifier, the primary nameserver is the ZKS prover that creates the

commitment to the set, the secondary nameserver is the online ZKS prover that provides online proofs to the verifier. We can't use the existing ZKS solutions as is, however, because even the best known constructions of ZKS [CHL<sup>+</sup>05] are too inefficient to be practical for DNSSEC<sup>4</sup>. On the other hand, the requirements in a ZKS are very stringent, in that one does not trust even the *primary nameserver* (i.e., the commitment to the database). In the DNSSEC setting, where the primary nameserver is trusted, this property is not necessary and by working in this less stringent setting, we are able to obtain more efficient constructions.

Data structures that come with soundness guarantees are also relevant (see e.g. [BEG<sup>+</sup>94], [NN00], [TT10], [MHKS14]). These data structures return an answer along with a proof that the answer is sound; “soundness” means that the answer is consistent with some external information. We also need soundness in our setting, but we augment this with the additional requirement of privacy against zone enumeration.

## II. MODEL AND SECURITY DEFINITIONS

We define the new primitive, Primary-Secondary-Resolver Membership Proof system, or PSR for short, with the goal of getting secure denial of existence while preventing zone enumeration. A PSR is an interactive proof system consisting of three parties. The *primary nameserver* (or simply *primary*) sets up the system by specifying a set  $R \subseteq U$ , where  $R$  represents the existing domain names in the zone and  $U$  represents the universe of all possible domain names. In addition to  $R$ , the primary specifies a value  $v(x) \in V$  (representing, for example, the corresponding IP address) for every  $x \in R$ . It then publishes a public key  $PK$  for the system (distributed via the usual DNSSEC mechanisms). The *secondary nameservers* (or simply *secondaries*) get  $PK$  and information  $I_S$  necessary to produce the responses. The *resolvers* get  $PK$ . After the setup phase is complete, the secondaries and resolvers function as a prover and verifier of statements of the sort “ $x \in R$  and  $v(x) = y$ ” or “ $x \notin R$ ”.

Following the design of DNSSEC, we consider only two-round protocols, in which a query is sent from the resolver to the secondary and a response is returned. More interactive protocols are possible, but we do not consider them here. DNSSEC standard has resolvers sending plain queries (i.e., send  $x$  in order to get  $v(x)$ ), which is also what our construction in Section III does. However, for the sake of generality, in defining our model and in proving our lower bound in Section IV, we permit resolvers to transform the query first; in particular, our model allows resolvers to keep state information between query issuance and answer verification (although our construction does not use it).

#### A. Algorithms for the Parties in PSR Systems

A PSR system consists of four algorithms. The *Setup* algorithm is used by the primary nameserver to generate the

<sup>4</sup> [CHL<sup>+</sup>05] requires the verifier to verify  $\log |U|$  mercurial commitments, where  $U$  is the universe of elements and each verification involves a “public-key operation”.

public key  $PK$ , which it publishes to all parties in the protocol, and the information  $I_S$ , delivered to secondary nameservers. A resolver uses the *Query* algorithm to generate a query for elements in the universe; it then sends this query to a secondary, who replies to a query using the *Answer* algorithm. The resolver finally uses *Verify* to validate the response from the secondary.

**Definition II.1.** Let  $U$  be a universe of elements and  $V$  a set of possible values. A Primary-Secondary-Resolver system is specified by four probabilistic polynomial-time algorithms (*Setup*, *Query*, *Answer*, *Verify*):

*Setup*( $R, v(\cdot), 1^k$ )

On input  $k$  the security parameter, a privileged set  $R \subseteq U$ , a value function<sup>5</sup>  $v : R \rightarrow V$ , this algorithm outputs two strings: a public key  $PK$  and the information  $I_S$  given to the secondaries.

*Query*( $x, PK$ )

On input  $x \in U$  and the public key  $PK$ , this algorithm outputs a query  $q$ . It also leaves state information for the *Verify* algorithm.

*Answer*( $q, I_S, PK$ )

The algorithm gets as input a query  $q$  for some element  $x \in U$ , the information  $I_S$  produced by *Setup*, and the public key. If  $x \in R$  then the algorithm outputs a bit  $b = \text{'yes'}$ , the value  $v(x)$ , and a proof  $\pi$  for  $x \in R$  and  $v(x)$ . Else it outputs  $b = \text{'no'}$ , an empty  $v$ , and a proof  $\pi$  for  $x \notin R$ .

*Verify*( $b, v, \pi$ )

The algorithm, which is given state information from the *Query* algorithm, including  $x$  and  $PK$ , gets a bit  $b$ , a value  $v$  (empty if  $b = \text{'no'}$ ), and the proof  $\pi$ . If  $b = \text{'yes'}$  then it checks that the proof  $\pi$  validates that  $x \in R$  and the value is  $v(x)$ . If  $b = \text{'no'}$  it checks to validate that  $x \notin R$ . If the proof is correct it returns 1 and otherwise 0.

For simplicity, our definition above considers only the case where the set  $R$  is static. It is determined when the primary sets up the system and we cannot change it afterwards. There are methods for handling it that borrow from the CRL world (e.g., we could use the Naor-Nissim certificate update and revocation scheme [NN00]) but we chose not to concentrate on this aspect in this work.

We will require the above four algorithms to satisfy three properties.

### B. Functionality and Soundness

The requirement that the system be functional is called, as is traditional in interactive proof systems, *completeness*. When the different parties are honest and follow the protocol, then the system should work properly; that is, resolvers will learn whether names are in the set  $R$  or not. We do allow a *negligible* probability of failure.

**Definition II.2. Completeness:** For all  $R \subseteq U$  and for all  $v : R \rightarrow V$  and  $\forall x \in U$ ,

$$\Pr \left[ \begin{array}{l} (PK, I_S) \stackrel{R}{\leftarrow} \text{Setup}(R, v(\cdot), 1^k); \\ q \stackrel{R}{\leftarrow} \text{Query}(x, PK); \\ (b, v, \pi) \stackrel{R}{\leftarrow} \text{Answer}(q, I_S, PK); \\ \text{Verify}(b, v, \pi) = 1 \end{array} \right] \geq 1 - \mu(k)$$

for a negligible function  $\mu(k)$ .

As for security, or *soundness*, we want that even a malicious secondary in the system would not be able to convince an honest resolver of a false statement with more than a negligible probability. We demand that this holds even when the malicious secondary gets to choose  $R$  and  $v$ , then gets  $(PK, I_S)$  and finally chooses the element  $x \in U$  it wishes to cheat on and its deceitful proof  $\pi$ .

**Definition II.3. Soundness:** for all probabilistic polynomial time stateful adversaries  $A$  we have

$$\Pr \left[ \begin{array}{l} (R, v(\cdot)) \stackrel{R}{\leftarrow} A(1^k); \\ (PK, I_S) \stackrel{R}{\leftarrow} \text{Setup}(R, v(\cdot), 1^k); \\ x \stackrel{R}{\leftarrow} A(PK, I_S); \\ q \stackrel{R}{\leftarrow} \text{Query}(x, PK); \\ (b', v', \pi) \stackrel{R}{\leftarrow} A(PK, I_S); \\ \text{Verify}(b', v', \pi) = 1 \wedge \\ ((x \in R \wedge (b' = \text{'no'} \vee v' \neq v(x))) \vee \\ (x \notin R \wedge b' = \text{'yes'})) \end{array} \right] \leq \mu(k)$$

for a negligible function  $\mu(k)$ .

Note that our definition is strong because it ensures (up to negligible probability) that adversary cannot find any  $x \in U$  violating either completeness or soundness even after getting the public-key  $PK$  and  $I_S$ .

### C. Privacy: Preventing Zone Enumeration

In our setting, privacy means preventing zone enumeration. We want to make sure that resolvers do not learn too much about the elements in the set  $R$ , apart from the responses to their queries. We formulate this requirement with a strong notion that we call *f-zero-knowledge* (*f-zk* for short), where  $f(R)$  is some information about the set which we can tolerate leaking to the resolvers. For example, our NSEC5 construction has  $f(R) = |R|$  (the number of names in the set  $R$ ). We formulate *f-zk* by requiring a PSR system to have a simulator with oracle access to the set  $R$  which receives  $f(R)$  and can fool a resolver into believing it is communicating with a real system. Later, in Section II-D we show that the *f-zk* notion implies a more “intuitive” security definition.

The idea behind our *f-zk* notion is that a resolver learns nothing from the responses it gets from the secondaries, besides the response to his query and the information  $f(R)$ , which might leak during the protocol’s execution. We require that the resolver cannot distinguish between: (1) a real system which provides the original proofs, and (2) a simulator that can only obtain the answer to each resolver’s query, but must

<sup>5</sup>This function will be used to map domain names to their corresponding IP addresses.

still be able to “forge” a satisfactory proof for that response. The use of such a simulator allows us to deduce the resolver has not learned much about  $R$  from the proofs; if he had, he would be able to distinguish between an interaction with the simulator and one with the real secondary (at least after he gets  $R$  explicitly). The use of simulators in order to prove that a protocol is zero knowledge is standard in cryptography (see [Gol01] Chapter 4 for a more comprehensive treatment of ZK and simulators).

More formally, we define a **PSR Simulator**. Let  $SIM$  be a probabilistic polynomial time algorithm with limited oracle access to  $R$ , meaning that  $SIM$  can ask on point  $x$  only when the adversary explicitly queries on an element  $x$ . On its first step  $SIM$  receives  $f(R)$  and outputs a fake public key  $PK^*$ , a fake secret key  $SK_{SIM}$  and the leaked information  $f(R)$ . On the following steps  $SIM$  receives queries from the adversary and needs to output a (simulated) proof of either  $x \in R$  plus  $v(x)$  or  $x \notin R$ ; to do this,  $SIM$  is allowed to query the  $R$ -oracle for the element  $x$ . The simulator’s output (public-key and proofs) should be computationally indistinguishable from the output generated by a real PSR system.

We divide this process into two phases. The first is an interactive protocol where the adversary communicates with the simulator or a PSR system. First the adversary gets the public key, either from a PSR system setup algorithm or from a simulator which gets  $f(R)$ . Then the adversary starts issuing queries  $q_i$  (adaptively), based on the public key and previous responses to queries it got. The simulator/PSR system responds to the queries with the answers  $(b_i, v_i, \pi_i)$  which the adversary can verify.

The second phase starts after the interactive protocol ends, where a distinguisher tries to tell apart the two views generated by the protocols. We say that the system is  $f$ -zk if for every adversary there exists a simulator such that no distinguisher who knows  $R$  can distinguish with more than a negligible advantage between the two views containing the public key,  $f(R)$ , queries and responses which were generated by either the system or the simulator.

The first step of the interactive protocol consists of the generation of keys, either by a PSR system:

$$(PK, I_S, f(R)) \stackrel{R}{\leftarrow} Setup(R, v(\cdot), 1^k)$$

or by the simulator that generates fake keys :

$$(PK^*, SK_{SIM}, f(R)) \stackrel{R}{\leftarrow} SIM^R(f(R), 1^k).$$

The rest is the interactive protocol of queries and responses described above, where the simulator uses the fake public key  $PK^*$  and the fake secret key  $SK_{SIM}$  to answer queries and the system uses the real keys  $(PK, I_S)$ .

**Definition II.4.** Let the leaked info  $f()$  be some function from  $2^U$  to some domain and let  $(Setup, Query, Answer, Verify)$  be a PSR system. We say that it is  $f$ -zero knowledge ( $f$ -zk for short) if it satisfies the following property for a negligible function  $\mu(k)$ :

There exists a simulator  $SIM$  such that for every probabilistic polynomial time algorithms  $Adv$  and distinguisher  $D$  a set

$R \subseteq U$  and  $v : R \rightarrow V$  the distinguisher  $D$  cannot distinguish between the following two views:

$$view^{real} = \{PK, f(R), q_1, (b_1, v_1, \pi_1), q_2, (b_2, v_2, \pi_2), \dots\}$$

and

$$view^{SIM} = \{PK^*, f(R), q_1, (b_1, v_1, \pi_1^*), q_2, (b_2, v_2, \pi_2^*), \dots\}$$

with an advantage greater than  $\mu(k)$ , even for  $D$  that knows  $R$  and  $v$  (the two views are generated by the protocols described above).

**Remark.** Note that the requirement of the simulation is online: there is no rewinding and the number of queries and nature of the queries to the  $R$ -oracle are restricted by the calls the resolver makes. This means our the simulator has little power, in the sense that the simulator only has the oracle access and  $f(R)$  to work with, but still manages to provide indistinguishable proofs with overwhelming probability. The less power the simulator has, the harder it is to construct a valid simulator that can fool an adversary, making the  $f$ -zk property more meaningful. Thus using this basic definition for a simulator makes our ZK requirement stronger.

Also note that this concept of a simulator receiving some  $f(R)$  may look similar to the definition of auxiliary input zero knowledge (see [Gol01] Chapter 4), but they are different. In the latter both the adversary and the simulator receive the same auxiliary information and we wish that the adversary is still unable to distinguish between the two views. In our case, the construction itself leaks the information  $f(R)$  and we would like to show that it doesn’t leak any additional information. The auxiliary input property can be incorporated into this definition as well in case we would like our resolvers to have some prior information about the set  $R$ , but they would still not be able to gain any additional information on  $R$  besides  $f(R)$  and the prior knowledge they received.

Note that the adversary is given the value  $f(R)$  on its first step. Also note that we choose to define  $f$ -zk for a 2-round interactive PSR protocol. One can easily generalize the  $f$ -zk property to include more rounds.

#### D. Zero-knowledge Implies Hardness of Zone Enumeration

We want to make sure that the zero-knowledge property with respect to the resolvers implies that they indeed cannot obtain information about additional elements other than those explicitly queried, thus preventing zone enumeration. In fact, we will prove that even a weak version of zone enumeration is impossible under our definition of  $f$ -zk. Specifically, we will show an adversarial resolver who tries to determine which of one of two known elements is in  $R$ , without querying for those two elements, will not succeed (except with negligible probability). We call this security property *selective membership security*; it is defined by a game where an adversary needs to guess correctly a bit with non-negligible advantage in order to win.

**Definition II.5. PSR security against selective membership.** A PSR protocol is said to be  $\varepsilon$ -secure against selective membership under an adaptive chosen message attack if every

probabilistic polynomial time algorithm  $A$  playing against a challenger wins the following game with probability at most  $\frac{1}{2} + \varepsilon$ .

- 1) The adversary  $A$  starts by sending the challenger a set  $S \subseteq U$ , two target elements  $x_0, x_1 \notin S$  and a value function  $v$  for the elements in  $S \cup \{x_0, x_1\}$ .
- 2) The challenger defines  $R = S \cup \{x_0\}$  with probability  $\frac{1}{2}$  and  $R = S \cup \{x_1\}$  otherwise. Next the challenger runs algorithm  $Setup(R, v(\cdot), 1^k)$ , sends the output  $PK$  to the adversary  $A$  and keeps  $I_S$  secret to himself.
- 3) Algorithm  $A$  mounts an adaptive chosen message attack by sending queries to the elements  $y_1, \dots, y_m$ , where the queries are  $q_i = Query(y_i, PK)$  and  $y_i \notin \{x_0, x_1\}$ . The challenger responds with proper answers to all the queries:  $A_1, \dots, A_q$ .
- 4) Finally  $A$  outputs one bit  $g$ , with  $g = 0$  if  $A$  believes that  $x_0 \in R$  and  $g = 1$  if it believes  $x_1 \in R$ .

We say that  $A$  won the game if the bit  $g$  is the correct guess, i.e., if  $x_g \in R$ .

We show that a PSR that is  $f$ -zk for  $f(R) = |R|$  is also secure against selective membership attacks for a negligible  $\varepsilon$ .

**Theorem II.6.** *Suppose that we have an  $f$ -zk PSR system ( $Setup, Query, Answer, Verify$ ) for  $f(R) = |R|$  and  $\mu_f$  as the bound on the advantage of the distinguisher in  $f$ -zk, then it is also  $\varepsilon$ -secure against selective membership under an adaptive chosen message attack, where  $\varepsilon = 2 \cdot \mu_f$*

*Proof:* We will show that the two possible views the adversary can witness in the security game, the one where  $R = S \cup \{x_0\}$  and the other where  $R = S \cup \{x_1\}$ , are computationally indistinguishable.

For any choice of  $(S, v : R \rightarrow V, x_0, x_1)$  we define four views. We will show that all four views are indistinguishable from one another and that two of them correspond to the two views of the adversary in the security game (either  $x_0 \in R$  or  $x_1 \in R$ ). Thus we can conclude that an adversary cannot find the additional element  $x_g \in R$ , because if it can find it with a non-negligible advantage then the adversary could also distinguish between the two views.

For  $j \in \{0, 1\}$  denote the view of an adversary in the security game when  $x_j \in R$  as  $view_j^{real}(S, v(\cdot), x_0, x_1)$  and denote the view when we switch from a secondary to the simulator as  $view_j^{sim}(S, v(\cdot), x_0, x_1)$ .

First let us see that the views  $view_j^{real}(S, v(\cdot), x_0, x_1)$  and  $view_j^{sim}(S, v(\cdot), x_0, x_1)$  are indistinguishable for  $j \in \{0, 1\}$ . According to the  $f$ -zk assumption for every choice of  $(R, v(\cdot))$  the view of any adversary communicating with the simulator is indistinguishable from that of the same adversary communicating with the real system, when both are given  $f(R) = |R|$ . The adversary chooses  $S$  and knows that  $|R| = |S| + 1$  and the simulator and real system also know the size of  $R$  by that same logic. So an adversary playing the security game cannot distinguish between cases where it is communicating with the simulator and ones where it communicates with the real system with advantage greater than  $\mu_f(k)$ , according to the definition of the  $f$ -zk property, which makes those views indistinguishable.

Now we notice that the views  $view_0^{sim}(S, v(\cdot), x_0, x_1)$  and  $view_1^{sim}(S, v(\cdot), x_0, x_1)$  are not only indistinguishable, but identical. This is true as the simulator  $SIM$  doesn't know the set  $R$ , it knows just its cardinality and it has an oracle to the set  $R$  which it uses whenever it is queried on some element and is not allowed to query any other elements. Thus during the key generation part both views are identically distributed as in both cases  $SIM$  gets the same  $f(R)$  and cannot query its oracle. Note that the adversary is not allowed to query for  $x_0, x_1$  because it is his target challenge, so the adversary can issue the same set of queries to the simulator and get the same answers to all of them. Thus both views are identically distributed and cannot be distinguished.

Combining it all, we get that  $view_0^{real}(S, v(\cdot), x_0, x_1)$  and  $view_1^{real}(S, v(\cdot), x_0, x_1)$  cannot be distinguished with probability greater than  $2 \cdot \mu_f(k)$ . This means that any probabilistic polynomial time adversary can win the selective security game with only a negligible advantage of  $2 \cdot \mu_f$ . ■

### III. NSEC5 CONSTRUCTION AND PROOF

We show a construction of an efficient PSR system based on the RSA permutation, hash functions, and any signature scheme. We prove the system secure in the random oracle model. Table 1 summarizes our notation.

Let the three algorithms  $(S_{rsa}, RSA, RSA^{-1})$  be the key generation, public (encrypting or verifying), and secret (decrypting or signing) computation of the RSA trapdoor permutation (see Appendix C for the description of RSA). The RSA keys are the secondary keys of the scheme; let  $N$  be the RSA modulus. Likewise, let the three algorithms  $(S_{sig}, Sig, Ver)$  be the setup, signature, and verification algorithms of any existentially unforgeable signature scheme (see Appendix B). The signature keys  $PK_P, SK_P$  are the primary keys of the scheme. Let  $h_1 : U \rightarrow \mathbb{Z}_N, h_2 : \mathbb{Z}_N \rightarrow \{0, 1\}^n$  be cryptographic hash functions, which will be modeled as random oracles (see Appendix A) for the security proof. For  $h_2$ , the output length  $n$  is chosen to prevent birthday attacks. The function  $F(x) = h_2(RSA_{SK_S}^{-1}(h_1(x)))$  will look random to any computationally bounded observer who does not know the secret RSA key, and the function  $S(x) = RSA_{SK_S}^{-1}(h_1(x))$  will be used to show that  $F(x)$  was computed correctly.

As explained in the introduction, we compute  $F$  over the entire set  $R$ , sort the values lexicographically and sign every adjacent pair of values  $(y_j, y_{j+1})$  with signature  $Sign(y_j, y_{j+1})$  using the  $SK_P$ . These  $\{y_j\}_{j=0}^r$  and  $\{Sign(y_j, y_{j+1})\}_{j=0}^r$  values are given to the secondaries. In order to respond to negative queries  $x \notin R$ , a secondary computes  $F(x)$  and its proof  $S(x)$  and sends  $S(x)$  together with the pair  $(y_j, y_{j+1})$  and the signature  $Sign(y_j, y_{j+1})$  such that  $F(x)$  is between  $y_j$  and  $y_{j+1}$ . The resolver can compute  $F(x)$  by applying  $h_2$  on  $S(x)$ , thus validating the response. Responses to positive queries are as in DNSSEC: the secondaries prove  $x \in R$  by sending the pair  $(x, v(x))$  and the signature on this pair, produced by the primary.

The four algorithms for our PSR system are:

**Setup:** The setup algorithm  $Setup(R, v(\cdot), 1^k)$  gets the set  $R$  and the values  $v$  associated with it as well as a security

$S_{rsa}, RSA, RSA^{-1}$	RSA algorithms
$PK_S, SK_S$	RSA keys (secondary keys)
$S_{sig}, Sig, Ver$	Signature scheme algorithms
$PK_P, SK_P$	Signature scheme keys (primary keys)
$h_1$	Random oracle from $U$ to $\mathbb{Z}_N$
$h_2$	Random oracle from $\mathbb{Z}_N$ to $\{0, 1\}^n$
$F : U \rightarrow \{0, 1\}^n$	The function $h_2(RSA_{SK_S}^{-1}(h_1(\cdot)))$
$S : U \rightarrow [N]$	The function $RSA_{SK_S}^{-1}(h_1(\cdot))$
$R = \{x_1, \dots, x_r\}$	Set of existent domain names
$U$	Universe of domain names
$V$	Universe of IP addresses
$v : R \rightarrow V$	Function mapping domain names to IP addresses

Fig. 1. Table of notation.

parameter. It uses the RSA key generation algorithm  $S_{rsa}(1^k)$  to obtain  $(PK_S, SK_S)$  for the RSA scheme and uses the key generation algorithm for the signature scheme  $S_{sig}(1^k)$  in order to obtain  $(PK_P, SK_P)$ . It chooses the two random oracles  $h_1$  and  $h_2$  as specified before. The public key is defined to be  $PK = (PK_S, PK_P, h_1, h_2)$ .

Now for every  $x \in R$  compute

$$y = F(x) = h_2(RSA_{SK_S}^{-1}(h_1(x))).$$

Order the  $y$  values so obtained lexicographically to get  $y_1, \dots, y_r$ . Add  $y_0 = 0^n$  and  $y_{r+1} = 1^n$ . Now for each  $j \in \{0, \dots, r\}$  use the signature scheme to create a signature:

$$Sign(y_j, y_{j+1}) = Sig_{SK_P}(y_j, y_{j+1}).$$

The pairs  $(y_j, y_{j+1})$  are the NSEC5 records.

Use the same signature scheme to compute for every  $x \in R$ :

$$Sign(x, v(x)) = Sig_{SK_P}(x, v(x)).$$

In DNSSEC terminology, all signatures are stored as RRSIG records.

Note that we assume that a  $(y_j, y_{j+1})$  pair cannot be confused for an  $(x, v(x))$  pair. This is true if  $\{0, 1\}^n$  does not intersect with  $U$ ; otherwise, it can be accomplished by putting an appropriate flag indicating the record type.

Let  $Y_S$  consist of the signed NSEC5 pairs  $\{Sign(y_j, y_{j+1})\}_{j=0}^r$  and the  $y$  values  $\{y_j\}_{j=1}^r$ . Let  $X_S$  consist of the pairs  $(x, v(x))$  for every  $x \in R$  and their corresponding signatures  $Sign(x, v(x))$ . The information given to the secondaries is  $I_S = (Y_S, X_S, SK_S)$  (see Figure 2). See Remark III.1 for the differences among the portions of  $I_S$ .

**Query generation:** The query is sent in the clear: algorithm  $Query(x, PK)$  simply outputs  $x$  as the query  $q$ .

**Answering a query:**  $Answer(q = x, I_S, PK)$  is performed by checking if  $x \in R$ . If so, return  $(\text{'yes'}, v(x), Sign(x, v(x)))$ . If not, compute  $S(x)$  and  $y = h_2(S(x)) = F(x)$ , find the index  $j$  for which  $y_j < y < y_{j+1}$ , and return  $(\text{'no'}, (S(x), Sign(y_j, y_{j+1}), (y_j, y_{j+1})))$ .

**Verifying the answer:**  $Verify(b, v, \pi)$ : If  $b = \text{'yes'}$  then verify that  $\pi$  is valid by returning  $Ver_{PK_P}(\pi, (x, v))$ . If

$b = \text{'no'}$  then parse  $\pi$  as  $(\pi_y, \sigma, (y_j, y_{j+1}))$  and verify that  $Ver_{PK_P}(\sigma, (y_j, y_{j+1})) = 1$ . If the signature is valid then check that  $y_j < h_2(\pi_y) < y_{j+1}$ , that  $\pi_y \in \mathbb{Z}_n$ , and that  $RSA_{PK_S}(\pi_y) = h_1(x)$ . If this is the case return 1, else return 0.

**Remark III.1.** We divide the information  $I_S$  received by the secondaries into three parts. The first part is  $Y_S$ ; it can be given to resolvers without any loss of privacy and can be easily obtained by any resolver issuing random queries. The second part is  $X_S$ . Some pieces of  $X_S$  can be obtained by resolvers, but only if they issue queries for  $x \in R$ . If a resolver learns all of  $X_S$ , it will know the entries in the zone. The third part,  $SK_S$ , cannot be obtained by a resolver; if a resolver learns  $SK_S$  and  $Y_S$ , it can learn the zone by performing a dictionary attack like the ones possible against NSEC3.

$$I_S = \begin{matrix} Y_S \left\{ \begin{array}{l} y_1, \dots, y_r \\ Sign(y_0, y_1), \dots, Sign(y_r, y_{r+1}) \end{array} \right. \\ X_S \left\{ \begin{array}{l} (x_1, v(x_1)), \dots, (x_r, v(x_r)) \\ Sign(x_1, v(x_1)), \dots, Sign(x_r, v(x_r)) \end{array} \right. \\ SK_S \end{matrix}$$

Fig. 2. Illustration of  $I_S$ .

#### A. Computational Requirements of NSEC5

The main computational cost of NSEC5 comes at the secondaries, who need to perform an online RSA signing computation (plus two hash evaluations and some table lookups, which are not significant in comparison) for a negative response. Note, however, that online signing has been considered and implemented in other DNSSEC solutions (such as [WI06], [Pow13, Sec. 4], and [Kam11]). The resolver's costs are similar to those in NSEC3, except for the additional cost of RSA exponentiation with the public exponent (which can be short) to verify  $S(x)$ ; this is relatively fast—no slower than the operation of verifying the signature on the NSEC record itself. The setup algorithm by the primary requires  $r = |R|$  computations of RSA with the secret exponent and  $2r + 1$  signatures; again this is not all that different than the requirements of NSEC3. Distributing  $SK_S$  from the primary to the secondaries should not present any additional problems, since it needs to be only as secret as the records that are anyway being sent from the primary to the secondaries.

Actual DNSSEC deployments are somewhat more complex than depicted here, due to the existence of relevant wildcard and enclosure records (see RFC 7129 [GM14]). We omitted these complications for better readability. In reality, two or three NSEC5 records and corresponding  $S(\cdot)$  values may need to be returned and verified, just like two or three NSEC3 records may need to be returned and verified (the wildcard flag proposal in the NSEC4 draft [GM12] can also be used with our proposal, reducing the number of records returned from three to two). Overall, our proposal will increase the length of



a DNSSEC response (vs. the current NSEC3 mechanism) by about 256–512 bytes, depending on whether 1024- or 2048-bit RSA is used for the  $(PK_S, SK_S)$  key pair.

### B. Proof of Security for NSEC5

We show that our system is complete, sound, and leaks nothing more than the size of the set  $R$ .

**Theorem III.2.** *The four algorithms described above constitute an  $f$ -zk PSR for the function  $f(R) = |R|$ .*

*Proof:* We start by proving a few useful properties of the function  $F$ . First we notice that for every  $x \in U$  there exists exactly one pair  $(y, \pi_y)$  for which it holds that  $F(x) = y$ ,  $h_1(x) = RSA_{PK_S}(\pi_y)$  and  $h_2(\pi_y) = y$ . This is true as  $h_1, h_2$ , and RSA are all deterministic algorithms and RSA is also a permutation.

The second property is verifiable pseudorandomness:

**Lemma III.3.** *For every  $x \in U$  the value  $F(x)$  is pseudorandom over  $\{0, 1\}^n$  in the following sense: no probabilistic polynomial-time adversary who gets  $x$  and can ask for  $F(x_i)$  and  $S(x_i)$  on any sequence of points  $x_1, x_2 \dots$  not equal to  $x$  can distinguish  $F(x)$  from a random value in  $\{0, 1\}^n$ .<sup>6</sup>*

*Proof:* Assume to the contrary that there exists an adversary  $A$  which gets  $x \in U$  and after the sequence of queries described, manages to distinguish  $F(x)$  and a random value with a non-negligible advantage. We show that using  $A$  we can invert the RSA permutation with the same non-negligible probability, violating the RSA hardness assumption as in Appendix C. Assume wlog that for every  $x_i \neq x$  that  $A$  asks to evaluate  $h_1(x_i)$  it also asks to see  $(F(x_i), S(x_i))$  and that the upper bound on the number of queries is  $q$ . Given a public key  $(N, e)$  and challenge  $z$  that we wish to invert, before  $A$ 's first query we draw uniformly at random  $c_1, \dots, c_q \in [N]$  (where  $[N]$  is the domain/range of the RSA permutation). We compute  $z_i = RSA_{PK_S}(c_i) = c_i^e \bmod N$ . Now every time  $A$  issues a new query  $x_i$  (on an element that wasn't queried before) we set  $h_1(x_i) = z_i$  and that determines that  $S(x_i) = c_i$  and  $F(x_i) = h_2(c_i)$ . When  $h_1$  is queried on  $x$  we return  $z$ . When  $h_2$  is queried we answer with a random and consistent (with previous answers) manner. When  $A$  queries  $h_2$  on a point  $p$  we check whether  $RSA_{PK_S}(p) = z$ . If it is equal, we are successful in the inversion.

The distribution  $A$  witnesses is identical to the real distribution. There are two possible cases: If  $A$  didn't query  $h_2$  on  $S(x) = RSA_{SK_S}^{-1}(z)$ , then it cannot distinguish between the two random values with greater than 0 advantage. If  $A$  queried  $h_2$  on  $S(x) = RSA_{SK_S}^{-1}(z)$  then we successfully managed to invert the RSA permutation over  $z$ . Thus,  $A$ 's advantage in distinguishing the two values is the probability of successfully inverting. ■

**Corollary III.4.** *The proof generalizes naturally from distinguishing the true value of  $F$  on a single element from a*

<sup>6</sup>Note that this means that the function  $F()$  combined with  $S()$  constitutes a VRF, as defined by Micali et al. [MRV99]. This is a very simple and efficient implementation of the primitive (albeit, proved only in the random oracle model).

*random value to distinguishing the true values of a whole set  $R \subset U$  from a set of random values, (recall that the hardness assumption on inverting any of a set of  $r$  values is as hard as a single element  $C^7$ ).*

Corollary III.4 helps us construct a simulator which can draw at random values in the range of  $F$  to represent the values of  $F$  on the set  $R$ , while keeping the two sets of values indistinguishable from one another.

In order to prove Theorem III.2, we need to show the following three properties (Definitions II.2, II.3 and II.4):

**Completeness.** For every  $R \subseteq U$ ,  $v : R \rightarrow V$  and  $x \in U$ , we need to show that that after we run  $Setup(R, v(\cdot), 1^k)$  to get  $(PK, I_S)$  and  $Answer(x, I_S, PK)$ , the  $Verify$  algorithm will output 1.

If  $x \in R$ , then by the way we defined the Setup algorithm, we generated

$$Sign(x, v(x)) = Sig_{SK_P}(x, v(x))$$

so the Answer algorithm will find the signature  $Sign(x, v(x))$  and it will be validated correctly by the verification algorithm with probability 1.

If  $x \notin R$ , then we claim that with overwhelming probability  $F(x) \neq y_j$  for every  $j \in [r]$ . Otherwise, we could guess  $F(x)$  with non-negligible probability without querying for  $F(x)$  and this violates the pseudorandomness of  $F$ , proved in Lemma III.3, as long as  $|R|/2^n$  is negligible. Furthermore an adversary could not even find an element  $x \notin R$  to violate the completeness property with non-negligible probability, otherwise it will again contradict the lemma.

To be exact, the probability for a collision for  $x \notin R$  is at most  $\frac{|R|}{|N|} + \frac{|R|}{2^n}$  (probability for a collision in  $h_1$  plus that of  $h_2$ ). Thus with  $q$  attempts one would get a violation to the completeness requirement with probability  $\frac{q \cdot |R|}{|N|} + \frac{q \cdot |R|}{2^n}$ . In the DNSSEC world the set  $R$  keeps changing all the time and if an adversary can affect the choice of the set  $R$  (after receiving the parameters  $(PK, I_S)$ ), he could find a collision with  $q$  attempts with probability  $\frac{q^2}{|N|} + \frac{q^2}{2^n}$ , due to the birthday paradox. The adversary can then put one the colliding elements in  $R$  and the second outside of  $R$ , thus finding a collision to violate the completeness requirement.

One could also get perfect completeness for NSEC5 by adding proofs for the special case of collisions. If  $x \notin R$  collides with  $x^* \in R$  ( $F(x) = F(x^*)$ ) then a valid proof for  $x \notin R$  would be  $(\text{'no'}, (S(x), S(x^*), x^*, v(x^*), Sign(x^*, v(x^*))))$ . A resolver would verify this proof by checking that  $F(x) = F(x^*)$  and verifying the signature  $Sign(x^*, v(x^*))$ . This would leak information about the set  $R$  (the fact that  $x^* \in R$  and its value is  $v(x^*)$ ) but as collisions happen with negligible probability this will not violate our privacy requirement.

**Soundness.** The soundness of our proposal follows from the existential unforgeability of the underlying signature scheme  $Sig$ . More formally, given an algorithm  $A$  that breaks soundness with probability  $\varepsilon$ , we can construct an algorithm  $B$  that,

<sup>7</sup>This is one place where the specific properties of RSA are used, rather than a generic trapdoor permutation, where we would have to loose a factor  $r$  in the advantage due to hybrid argument

given a public key  $PK_P$ , can win the existential unforgeability game with probability  $\varepsilon$ . Recall that in the existential unforgeability game,  $B$  gets to ask a signing oracle for signatures on arbitrary messages and must forge a signature on a new message.

Initially  $B$  receives the public key  $PK_P$  (and the security parameter  $k$ ). It runs  $A$  to obtain the set  $R$  and the function  $v(\cdot)$ . To return  $I_S$  to  $A$ ,  $B$  runs our setup algorithm, with the following changes:

- $B$  doesn't run the signature setup  $S_{sig}$ . Instead, it uses already given  $PK_P$  as the primary public key. (It still generates the secondary key pair using  $S_{rsa}$ ).
- To generate signatures without knowing  $SK_P$ ,  $B$  queries the signature oracle on the NSEC5 pairs  $(y_j, y_{j+1})$  for  $j \in \{0, \dots, |R| + 1\}$  and the pairs  $(x, v(x))$  for all  $x \in R$ .

$B$  then runs  $A$  to obtain  $x$ , and  $b', v', \pi$ . Suppose  $Verify(b', v', \pi) = 1$  for this  $x$ .

Suppose  $b' = 'no'$  but  $x \in R$ . Since  $\pi$  passes verification, it contains  $\pi_y \in \mathbb{Z}_n$  such that  $RSA_{PK_S}(\pi_y) = h_1(x)$ . It also contains a signature  $\sigma$  on some  $(y'_1, y'_2)$ , such that  $y'_1 < h_2(\pi_y) < y'_2$ . We want to show that a signature on  $(y'_1, y'_2)$  has not been requested by  $B$ . Indeed, since  $x \in R$ , during setup  $B$  computed  $S(x) = RSA_{SK_S}^{-1}(h_1(x))$ . Because RSA is a permutation over  $\mathbb{Z}_n$ ,  $\pi_y = S(x)$ . Therefore, during setup, the value  $y = h_2(\pi_y)$  was equal to  $y_j$  for some  $j$ . Since  $y'_1 < y_j$  and  $y'_2 > y_j$ , they are not neighboring values in the sequence  $y_0, \dots, y_{r+1}$ . Therefore,  $B$  outputs the message  $(y'_1, y'_2)$  and the signature  $\sigma$  as its forgery and wins the game because this signature was not requested by  $B$ .

Now suppose  $b' = 'yes'$  but  $x \notin R$  or  $v(x) \neq v'$ .  $B$  outputs the message  $(x, v')$  and the signature  $\sigma$  as its forgery and wins the game because this signature was not requested by  $B$ .

Therefore, we see that  $B$  succeeds whenever  $A$  succeeds in breaking the soundness, *i.e.*, with probability  $\varepsilon$ .

**Privacy.** In order to show that for  $f(R) = |R|$  the system NSEC5 is  $f$ -zk we need to show a suitable simulator SIM, where no probabilistic polynomial time adversary can distinguish an interaction with the real system and SIM.

On its first step of the computation  $SIM^R(1^k, 1^{|R|})$  runs the RSA setup algorithm and obtains  $(PK_S, SK_S)$  and also runs the setup algorithm of the signature scheme and obtains  $(PK_P, SK_P)$ . SIM then chooses the random oracles  $h_1, h_2$  as in the setup algorithm of the PSR. SIM randomly selects  $|R|$  values out of  $F$ 's range and sorts them lexicographically,  $y_1, \dots, y_r \in \{0, 1\}^n$  and creates the signatures  $\{Sign(y_j, y_{j+1}) = Sig_{SK_P}(y_j, y_{j+1})\}$  where we add the end points  $y_0 = 0^n$  and  $y_{r+1} = 1^n$  as the Setup algorithm does.

The simulator then outputs  $PK^* = (PK_S, PK_P, h_1, h_2)$  and a fake simulator key

$$SK_{SIM}^* = (SK_S, SK_P, \{Sign(y_j, y_{j+1})\}_{j=0}^r, \{y_j\}_{j=1}^r),$$

which we can see is very similar to the original parameters  $I_S$  that the *secondary* usually gets but it is missing the signatures  $\{Sign(x, v(x))\}$  for  $x \in R$  and has the secret key for the signature scheme instead.

On its next rounds the simulator does the following: for each query it receives  $q_i$ , SIM uses his oracle access to the set  $R$  to check if  $x_i \notin R$  or  $x_i \in R$  and its value  $v_i$  (remember  $q_i = x_i$ ). If  $x_i \in R$  then SIM generates a new signature  $s_{x_i} = Sig_{SK_P}(x_i, v_i)$  and returns  $(yes', s_{x_i}, (x_i, v_i))$ . Because the signer produces consistent signatures on the same query we will always get the same signature on the same message, *i.e.*  $s_{x_i} = Sign(x_i, v(x_i))$ . If  $x_i \notin R$  the simulator computes  $(F(x_i), S(x_i)) = (y_{x_i}, \pi_{x_i})$  and searches in  $SK_{SIM}^*$  for a  $j$  for which  $y_j < y_{x_i} < y_{j+1}$ . If we find such a  $j$  we return  $(no', \pi_{x_i}, Sign(y_j, y_{j+1}), (y_j, y_{j+1}))$ . If we don't find such a  $j$ , *i.e.*, a collision has occurred, we abort as we fail to produce a proof for  $x_i \notin R$ . Note this is exactly the case where our completeness requirement fails to hold and thus our simulator, like a real PSR system, fails to prove non-membership with negligible probability.

Now we need to show that the view of the adversary communicating with the simulator is indistinguishable from that of the adversary communicating with the real system. The public key  $PK^*$  is generated by the same algorithms the real system uses. Proofs regarding  $x \in R$  are signatures  $Sig_{SK_P}(x, v(x))$ , generated the same way the original proofs are created in the system, the only difference is that they are generated online instead of before hand during the setup phase, but this yields the same distribution. The only difference the adversary witnesses is that instead of real values of  $F$  on points of  $R$  it gets random values. However, we argued in Lemma III.3, that a polynomial time adversary cannot distinguish between  $\{F(x_i) | x_i \in R\}$  and a collection of  $|R|$  random values in  $\{0, 1\}^n$  with more than a negligible advantage. Thus, it cannot distinguish the simulation from a real execution. ■

#### IV. ON-LINE PUBLIC-KEY OPERATIONS ARE NECESSARY

In this section we show that the secondary responders in a PSR system must perform a public-key computation *on each query*. We do so by showing how to obtain a public-key signature scheme from a PSR system, with the complexity of the signer is roughly equal to the complexity of the secondary nameserver (plus the complexity of the query algorithm). The signature scheme will be secure as long as the PSR system is complete, sound, and private—even if it satisfies only the weaker notion of privacy in Definition II.5 rather than the full-fledged zero-knowledge of Definition II.4.

Since in a public-key signature system, the signers must perform a public-key operation for each message, the same holds for the PSR system. Of course, a limited number of signatures can be precomputed in a signature scheme, and the same holds for a PSR system (*e.g.*, all positive responses may be precomputed, as in most existing constructions, including ours). The rest—and, in particular, negative responses to unexpected queries—must be done on-line.

We obtain signatures only when the PSR system satisfies the following property: the query algorithm is deterministic or, if randomized, soundness holds even when the adversary has the knowledge of the random values used to generate  $q$ . Note that the systems in which  $q = x$  (such as our proposal and all the versions of DNS/DNSSEC) trivially satisfy this property.

Moreover, even when the PSR system does not satisfy this property, we obtain an interactive protocol that is very similar to signatures: namely a public-key authentication protocol (PKA), in which the sender transmits an authentic message to the receiver using some interaction. Again, in our obtained PKA protocol, the complexity of the sender is similar to that of the secondary responder in a PSR system. Since such a PKA protocol is not known to have any implementation that is much more efficient than a digital signature scheme, we can conclude that a non-trivial computational task is required of secondaries in PSR systems.

Both our transformations are in the random oracle model.

We first describe our result on transforming PSR schemes to PKA schemes, and then extend to signatures when the constraints on the query algorithm are satisfied.

#### A. Public-Key Authentication from PSR

**Defining Public-key Authentication Security** Public-key authentication (PKA; see [DDN00, Section 3.5]) can be seen as a relaxation of signature schemes in which we tolerate interaction between the sender and the receiver and give up the transferability property (*i.e.*, the receiver is no longer able to convince a third party that the signature is valid).

PKA schemes are related to, but are harder to build than *identification protocols*, in which there isn't even a message; instead the prover (sender) convinces the verifier that he is alive. (Such protocols can be used, for example, with key cards as provers in order to control access.) Identification protocols can be constructed from any zero-knowledge proof of knowledge [FFS87] for a computationally hard problem, but in practice no protocol where the efficiency of the prover is better than that of the signer in a signature scheme is known for either PKA or identification.

We define the relevant selective and existential security notions for public key authentication protocols.

**Definition IV.1. Public key authentication security against selective forgery.** A public key authentication protocol  $(PKA\_Setup, PKA\_Prove, PKA\_Verify)$  is said to be  $\epsilon$ -secure against selective forgery under an adaptive chosen message attack if every polynomial time probabilistic algorithm  $A$  playing against a challenger wins the game that will be described next with probability at most  $\epsilon$ .

- 1) The forger  $A$  starts by picking a target message  $M$ .
- 2) The challenger runs the setup algorithm for the PKA, sends  $PK$  to the forger  $A$  and keeps  $SK$  secret.
- 3) Algorithm  $A$  mounts an adaptive chosen message attack by sending messages to be authenticated by the challenger,  $M_1, \dots, M_m$ , where  $\forall i : M_i \neq M$  and for each one they engage in an authentication session.
- 4) At some point of  $A$ 's choosing it attempts to authenticate the message  $M$  to a verifier where  $A$  plays the role of the prover. Note that the sessions of authentication of the  $M_i$ 's may be running concurrently.

We say that  $A$  wins the game if the verifier accepts the authentication on  $M$ .

**Definition IV.2. Public key authentication security against existential forgery.** A Public key authentication protocol  $(Setup, Prove, Verify)$  is said to be  $\epsilon$ -secure against existential forgery under an adaptive chosen message attack if the same conditions as in Definition IV.1 hold, except  $A$  can choose  $M$  at any point in the game.

**From PSR to Selectively Secure PKA** We show how we can use a PSR system  $(PSR\_Setup, PSR\_Query, PSR\_Answer, PSR\_Verify)$  that is selectively secure against polynomial time adversaries (as in Definition II.5) and construct a Public key authentication protocol

$$(PKA\_Setup, PKA\_Prove, PKA\_Verify)$$

that is selectively secure against polynomial time adversaries.

- $PKA\_Setup(1^k)$ : Select uniformly at random a message  $M_R \in U$ , define  $R = \{M_R\}$  and denote  $v(\cdot)$  as the function that returns 1 on  $M_R$  and  $\perp$  otherwise. Run the setup algorithm  $PSR\_Setup(R, v(\cdot), 1^k)$  for the PSR, and obtain  $(PK, I_S)$ , which will be our public and secret keys.
- $PKA\_Prove(M_i, I_S, PK)$ : The prover acts as the *secondary* in the PSR system proving that  $M_i \notin R$ . It receives  $q$ , run the  $PSR\_Answer$  algorithm, and sends back its results.
- $PKA\_Verify(M_i, PK)$ : The verifier acts as the *resolver* in the PSR system. If runs the  $PSR\_Query$  algorithm to obtain and send  $q$ , receives the response, and accepts if the  $PSR\_Verify$  algorithm accepts the proof of non-membership.

**Remark IV.3.** Note that our PKA construction does not satisfy perfect completeness (if the verifier happens to choose  $M_R$ , we cannot authenticate that message). If the PSR system has perfect completeness, then we can also get a PKA system with perfect completeness by adding a bit to each element in the universe indicating whether it is 'real' or 'dummy', where we authenticate only the real elements. The set  $R$  should contain a single random dummy element and this way we can authenticate all real elements.

**Theorem IV.4.** Suppose we have a PSR system that is  $\epsilon$ -secure against selective membership under an adaptive chosen message attack then the derived Public key authentication protocol described above is  $\epsilon'$ -secure against selective forgery under an adaptive chosen message attack, where  $\epsilon' = 4\epsilon + \mu_s$  and  $\mu_s$  is the soundness parameter of the PSR.

*Proof:* Suppose that there exists a polynomial time forger  $B$  which manages to win the selective forgery security game for the derived PKA game with non-negligible probability  $\epsilon'$ . We describe an adversary  $A$  that uses the forger  $B$  as a subroutine to win the selective membership security game against the PSR in polynomial time with a non-negligible advantage  $\epsilon = \frac{\epsilon'}{4} - \frac{\mu_s(k)}{4}$ .

- The adversary  $A$  starts by obtaining the message  $M$  which  $B$  selects to forge.  $A$  draws at random a message  $M^*$ , sets the target set to be empty,  $S = \phi$ , denotes  $v(\cdot)$

as the function that returns  $v(M) = v(M^*) = 1$  and  $\perp$  otherwise and sends  $(S, v(\cdot), M, M^*)$  to the challenger.

- The challenger defines  $R = \{M\}$  with probability  $\frac{1}{2}$  and  $R = \{M^*\}$  otherwise. Next the challenger runs  $PSR\_Setup(R, v(\cdot), 1^k)$  and sends  $PK$  to  $A$ .
- After algorithm  $A$  receives the public key  $PK$  from the challenger it emulates  $B$  by acting as an intermediary between the challenger and  $B$  by relaying their authentication messages to each other.
- Finally  $B$  plays the role of a prover and tries to forge an authentication for  $M$ , where  $A$  plays the role of the verifier. If the verifier  $A$  accepts the authentication, then  $A$  returns 1 (which means  $A$  believes  $R = \{M^*\}$ ), else  $A$  chooses a bit uniformly at random and returns it.

If  $R = \{M^*\}$ , then  $B$  witnesses exactly the same view as in a real execution: the  $PSR\_Setup$  algorithm is defined as in the PKA protocol as well as the remaining parts. In this case  $B$  wins his game with probability at least  $\varepsilon'$ , and  $A$  identifies the success of the forgery attempt. So the probability  $A$  wins in this case is at least  $\varepsilon' + \frac{1-\varepsilon'}{2}$ , as either  $B$  succeeds in forging the authentication (probability  $\varepsilon'$ ) or  $A$  guesses the bit correctly (probability  $\frac{1-\varepsilon'}{2}$ ). If  $R = \{M\}$ , then it is no longer true that  $B$  sees the same view as in a real execution, however, due to the PSR's *soundness* property the probability that  $B$  can generate a proof for a false statement (and  $M \notin R$  is false in that case) is at most  $\mu_s(k)$  (which should be negligible). So the probability  $A$  wins in this case is at least  $\frac{1-\mu_s(k)}{2}$ . Since these two cases are equally likely, this means that  $A$  wins the game with probability at least

$$\frac{1}{2} \left( \varepsilon' + \frac{1-\varepsilon'}{2} \right) + \frac{1}{2} \left( \frac{1-\mu_s(k)}{2} \right) = \frac{1}{2} + \frac{\varepsilon'}{4} - \frac{\mu_s(k)}{4}$$

which is a non-negligible advantage in winning the security game ( $\varepsilon = \frac{\varepsilon'}{4} - \frac{\mu_s(k)}{4}$ ), in contradiction to the security assumption on the PSR system. ■

**From Selective to Existential Security** Next we prove that in the random oracle model using a PKA which is selectively secure (Definition IV.1) we can construct a PKA scheme which is existentially secure (Definition IV.2), thus showing that a PSR system implies a strong security notion for a PKA scheme. To do that we simply use a random oracle to hash the message we want to authenticate before authenticating it and modify the algorithms appropriately. As a result, the running time of the PKA sender will be greater than the running time of a PSR system secondary by only a single random oracle query.

**Theorem IV.5.** *Suppose that we have a Public key authentication protocol (Setup, Prove, Verify) which is  $\varepsilon'$ -secure against selective forgery under an adaptive chosen message attack then in the random oracle model the derived scheme above is  $\varepsilon$ -secure against existential forgery under an adaptive chosen message attack, where  $\varepsilon' = \varepsilon/q(k)$  and  $q$  is some polynomial in  $k$ .*

*Proof:* Suppose that there is an adversary  $B$  which wins the existential security game for public key authentication in the random oracle model with non negligible probability  $\varepsilon$ .

We use this adversary  $B$  to win the selective security game, contradicting our assumption.

Note that as we are in the random oracle model (see Appendix A) we control the random oracle and every time  $B$  wants to compute some  $h(M)$  it gets the value. As adversary  $B$  runs in polynomial time, we know  $B$  can make at most a polynomial number of queries to the random oracle, assume an upper bound on that number is  $q(k)$ . We describe adversary  $A$  which uses adversary  $B$  in order to win the selective security game:

- Our adversary  $A$  chooses uniformly at random a message  $M$  from the message space and declares  $M$  as the message it intends to forge.  $A$  also draws at random  $j \in [q(k)]$ .
- The challenger simply runs the setup algorithm for the authentication protocol and sends  $A$  the public key  $PK$ .
- $A$  starts by emulating  $B$ , by functioning as an intermediary between the challenger and  $B$  and relaying their authentication messages to each other. When  $B$  queries the random oracle  $h$ , answer with random values at all steps except the  $j^{\text{th}}$  one. At the  $j^{\text{th}}$  step, when  $B$  queries  $h$  for message  $m'$ , then set  $h(m')$  to be  $M$ . If at some point before the forgery attempt by  $B$ , it asks to authenticate the message  $m'$ ,  $A$  stops and declares failure.
- Finally  $B$  tries to forge an authentication for some message  $M^*$ , if  $h(M^*) = M$  then  $A$  uses this forged authentication to try and authenticate  $M$ , else it fails.

We may assume that  $B$  accesses  $h$  on the message it tries to forge (otherwise its probability of success is negligible). Therefore with probability  $\frac{1}{q(k)}$  adversary  $A$  sets the value of the random oracle over the message  $B$  tries to forge;  $h(M^*)$ , to be the message  $M$  that  $A$  tries to forge as well. This means that  $A$  wins the security game in the case that both  $B$  managed to successfully forge an authentication for his target message and the right  $j$  was picked, which happens with probability  $\varepsilon' = \frac{\varepsilon}{q(k)}$ . ■

## B. Digital Signatures from PSR with Simple Query Algorithms

We have seen that PSR systems can be used to construct public-key authentication schemes of the same complexity. Our goal in this section is to point out that for PSR systems that satisfy some restrictions on the query algorithm, we can actually get a signature scheme of about the same complexity, as well. This shows that on-line public-key operations on the responders are inherent for those schemes, including any scheme that simply sends  $x$  as the query.

Consider any PSR system in which the Query algorithm is deterministic and apply the transformation of Section IV-A to get a PKA scheme. Observe that interaction is not necessary in the resulting PKA scheme, because each side can compute the receiver's first message on its own. Thus, the resulting PKA scheme is actually a signature scheme. The complexity of the signer is the same as the complexity of the Query and Answer algorithms in the PSR schemes.

In case the Query algorithm is randomized, the same approach does not work, because the PKA sender cannot

be trusted to choose or even to know the randomness that the Query algorithm uses. We get around the problem of choosing the randomness by using the approach of Fiat and Shamir [FS86]: namely, apply the transformation of Section IV-A, but let the randomness for the Query algorithm be  $h(x)$ , where  $h$  is a random oracle. This allows the sender to know the randomness and thus to compute the receiver's first message  $q$ . However, now the security proof for the resulting signature scheme works only if soundness for the PSR schemes holds against an adversary who knows the randomness used in the Query algorithm.

Thus, we obtain the following theorem.

**Theorem IV.6.** *Consider any PSR system  $(PSR\_Setup, PSR\_Query, PSR\_Answer, PSR\_Verify)$  for which the  $PSR\_Query$  algorithm is deterministic or for which the randomness of the  $PSR\_Query$  can be given to the adversary without harming soundness. Such a system implies an existentially unforgeable digital signature scheme whose signing complexity is equal to the complexity of  $PSR\_Query$  plus  $PSR\_Answer$  (plus at most two random oracle queries).*

### C. Discussion

We have shown that we can use a PSR system satisfying the zero-knowledge requirement (Definition II.4) and hence the selective membership requirement (Definition II.5) in order to build signatures, PKA and identification schemes. We therefore want to claim that we demonstrated that the work involved in this task must be non-trivial, unlike the NSEC3 protocol which only uses hashing but does not prevent zone enumeration. One could protest and argue that our zero-knowledge requirement or even the selective membership requirement are too strong and it may be possible to have a more relaxed notion of privacy that still prevents zone enumeration. We now argue that this is not the case.

Suppose we modify the privacy notion and protect against an adversary that produces an element it did not explicitly query on (the essence of zone enumeration). A little more formally, suppose that there is some distribution on the set  $R$ . We require that for every probabilistic polynomial time adversary  $A$  there exists a simulator with oracle access to the set  $R$ , such that if  $A$  interacts with a PSR system as a *resolver* and outputs, at the end of the interaction, an element he believes to be in the set  $R$  which he has not explicitly queried (this is 'success'), there is a simulator that interacts with an oracle to the set  $R$ , which is successful as well with similar probability, where similar means that the difference is negligible. We can show that under this requirement we get a notion related to selective membership, where instead of two elements chosen by the adversary, the two elements of the challenge are chosen at random, under a similar reduction to Theorem II.6. We can also show that the latter implies public-key identification, under a similar reduction to Section IV-A. Therefore we claim that we have demonstrated that preventing zone enumeration requires non-trivial computation.

## V. FURTHER WORK

In a companion paper we generalize the constructions of this paper and show how to obtain PSR systems without random oracles. We suggest a general construction based on VRFs [MRV99] and in particular relatively efficient incarnations of it [DY05], [HW10]. We also provide a construction based on *hierarchical identity based encryption* and in particular the one by Boneh, Boyen and Goh [BBG05] which does not reveal any information about the set  $R$ , even not its cardinality. For both constructions the amount of work consists of a few bilinear operations and logarithmic in  $|U|$  number of multiplications.

We also plan to write an Internet Draft for NSEC5.

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## APPENDIX

### A. The Random Oracle model

As our construction is analyzed in the random oracle model we need to rigorously define this model. The random oracle model has been used quite extensively to analyze cryptographic protocols [BR93], [BR94], [BR96], [Cor00], [Sho01]. We define the model as in Canetti, Goldreich and Halevi [CGH04]. In a scheme set in the Random Oracle Model, all parties including adversaries interact with each other like they would at the standard model, but they can also make oracle queries. According to the security parameter  $k$  and a length function  $\ell_{out}(\cdot)$ , an oracle  $O$  is a function chosen uniformly at random out of all possible functions mapping  $\{0, 1\}^*$  to  $\{0, 1\}^{\ell_{out}(k)}$ . Every party has access to this oracle. Security is defined as usual, meaning that a system is still considered secure when its adversary has a negligible probability of success or a negligible advantage, where the probability is also taken over the choices of the random oracle. Note that in the proof of security the random oracles can be “programmed”, meaning that certain values of the random oracle can be set either before hand or on the fly to be specific values (chosen uniformly at random) by a simulator (see Nielsen [Nie02]). Values can be set only the first time someone wishes to know  $O(x)$  as the oracle must remain consistent.

### B. Signature schemes

We use signature schemes in our construction, for that end we define signature schemes and their properties as we need them for our constructions. We define public key signature schemes as in Goldreich [Gol04].

**Definition A.1.** *A signature scheme is defined by three (polynomial time) algorithms  $(G, S, V)$ : The key generator  $G$  gets the security parameter  $k$  and outputs two keys, a signing key  $sk$  and a verification key  $vk$ ,  $G(1^k) = (sk, vk)$ . The signing algorithm  $S$  takes the secret key  $sk$  and a message  $M \in \{0, 1\}^\ell$  and produces a signature. The verification algorithm  $V$  gets  $vk$  and a presumed signature to a message and verifies it, i.e., outputs ‘accept’ (‘1’) or ‘reject’ (‘0’). We require perfect completeness: For every pair of keys  $(sk, vk)$  generated by  $G(1^k)$  and for every message  $M \in \{0, 1\}^{\ell=p(k)}$  (every message of length at most polynomial in the security parameter) it holds that*

$$\Pr[V_{vk}(S_{sk}(M), M) = 1] = 1$$

We will assume that the signature scheme is deterministic in the sense that for every message  $m$  there is a single signature  $\sigma$  that the signing algorithm produces (even though the verification algorithm may accept many different signatures). This is true wlog because we can always add to the signing key  $sk$  a description of a pseudorandom function to provide the randomness needed to sign  $m$  (see [GGM86]).

The type of security we require from our signature scheme is “existential unforgeability against chosen message attacks”, which means that even an adversary who can gain access to a polynomial number of signatures to messages of his choosing will still not be able to generate a signature for any message the adversary did not explicitly request a signature for.

**Definition A.2.** *A signature scheme is existentially secure against chosen message attacks if every probabilistic polynomial time adversary  $A$  wins the following security game with negligible probability. The game is modeled as a communication game between the adversary and a challenger  $C$ .*

- *The challenger  $C$  runs the setup algorithm  $S(1^k)$  and obtains  $(sk, vk)$ , sends  $vk$  to the adversary and keeps  $sk$  secret to himself.*
- *The adversary  $A$  issues an adaptively chosen sequence of messages  $m_1, \dots, m_q$  to the challenger and gets in return a signature on each of those messages  $s_1, \dots, s_q$  where  $s_i = S_{sk}(m_i)$ . By adaptively chosen we mean that the adversary chooses  $m_{i+1}$  only after seeing signature  $s_i$ .*
- *The adversary chooses a message  $M$  together with a forged signature  $s$  and sends them to the challenger; The only restriction is that  $M \neq m_i$  for every  $i$ .*

*The adversary wins the game when  $V_{vk}(s, M) = 1$ , i.e., the forged signature is accepted as valid.*

### C. RSA and Trapdoor Permutations

Our construction needs a trapdoor permutation and we use the famed RSA function for that. An RSA scheme has three algorithms  $(G, RSA, RSA^{-1})$ . The key generator  $G$  gets the security parameter  $k$  and outputs two keys, a public key  $PK$  (used for the forward direction: encryption and verifying signatures) and a secret or private key  $SK$  (used for the backward direction: decryption and signing). The algorithm  $G$  chooses an exponent  $e$  (for efficiency we could select  $e$  to be small, say 3), two large prime numbers  $P$  and  $Q$  of length roughly  $k$  such that  $e$  is relatively prime to  $P-1$  and to  $Q-1$  and computes  $N = P \cdot Q$ . It then calculates  $d$  such that for  $L = lcm(P-1, Q-1)$  it holds that  $d \cdot e \equiv 1 \pmod L$ . It then sets  $PK = (N, e)$  and  $SK = (N, d)$ . The RSA forward algorithm takes a value  $m \in [N]$  and the public key and computes  $RSA_{PK,rsa}(m) \equiv m^e \pmod N \equiv \sigma \pmod N$ . The RSA backward algorithm takes a value  $\sigma \in [N]$  and the secret key and computes  $RSA_{SK,rsa}^{-1}(\sigma) \equiv \sigma^d \pmod N \equiv m \pmod N$ .

Here are a few known properties/assumptions of this encryption scheme which we will find useful.

**RSA is a permutation.** Every value  $x \in [N]$  is mapped by the encryption algorithm to some unique  $y \in [N]$  and the decryption algorithm maps  $y$  back to  $x$ .

**The RSA hardness assumption** wrt to exponent  $e$  and security parameter  $k$ . The assumption states that it is hard to compute the RSA inverse of a random value: for any polynomial time adversary  $A$ , for exponent  $e$ , random primes  $P, Q$  of length  $k$  where  $e$  is relatively prime to  $P-1$  and  $Q-1$  and  $N = P \cdot Q$ , for a random  $y \in [N]$ , it holds that

$$\Pr[A(y, N, e) = x \text{ and } x^e \equiv y \pmod N]$$

is negligible in the security parameter.

Note that succeeding in finding the RSA inverse of any element of a set of  $r$  random challenges is just as hard. The reason is that given a single random  $z$ , by selecting random  $w_i \in [N]$  and generating  $z_i = z \cdot w_i^e \pmod N$  we get a set of  $r$  numbers so that from the RSA inverse of any of them it is possible to get  $RSA^{-1}(z)$ .

**RSA is efficient.** We can use low exponent RSA encryption in our construction in order to increase efficiency. If we pick  $e$  to be small then the forward algorithm will work fast, as it will need to make a smaller number of modular multiplications. The inversion algorithm takes the same amount of time regardless of the size of  $e$ .