# Improved Linear (hull) Cryptanalysis of Round-reduced Versions of SIMON

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**Abstract.** SIMON is a family of lightweight block ciphers designed by the U.S. National Security Agency (NSA) that has attracted much attention since its publication in 2013. In this paper, we thoroughly investigate the properties of linear approximations of the bitwise AND operation with dependent input bits. By using a Mixed-integer Linear Programming based technique presented in Aasicrypt 2014 for automatic search for characteristics, we obtain improved linear characteristics for several versions of the SIMON family. Moreover, by employing a recently published method for automatic enumeration of differential and linear characteristics by Sun *et. al.*, we present an improved linear hull analysis of some versions of the SIMON family, which are the best results for linear cryptanalysis of SIMON published so far.

Specifically, for SIMON128, where the number denotes the block length, a 34-round linear characteristic with correlation  $2^{-61}$  is found, which is the longest linear characteristic that can be used in a keyrecovery attack for SIMON128 published so far. Besides, several linear hulls superior to the best ones known previously are presented as follows: linear hulls for the 13-round SIMON32 with *potential*  $2^{-28.99}$  versus previous  $2^{-31.69}$ , for the 15-round SIMON48 with *potential*  $2^{-42.28}$  versus previous  $2^{-44.11}$  and linear hulls for the 21-round SIMON64 with *potential*  $2^{-60.72}$  versus previous  $2^{-62.53}$ .

Keywords. SIMON, linear cryptanalysis, linear hull, key recovery

## 1 Introduction

SIMON is a family of lightweight block ciphers presented by the U.S. National Security Agency [4] with a feistel structure of different versions of block and key lengths. By far, SIMON has attracted many cryptanalysis such as differential analysis [1, 5, 11, 12], linear cryptanalysis [2, 3], impossible differential and zerocorrelation linear hull cryptanalysis [2, 13].

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Linear cryptanalysis [7] presented by Matsui is an important cryptanalysis method on block ciphers. It aims at finding a linear expression involving bits of plaintexts, "ciphertexts" (including inner states) and subkeys that deviates from a random linear expression. A key recovery attack can then be launched due to this nonrandomness. Linear expressions are usually obtained by linear characteristics that consists of masks for each round state and applies the piling-up lemma to concatenate. This method has been extended to linear hull cryptanalysis by Nyberg [8] in 1995 when several linear characteristics with same input and output masks are used. In this paper, we investigate linear characteristics with consideration of dependences of the S-boxes. By the methods of automatic enumeration of differential and linear characteristics presented in [10, 11], some improved results about the linear (hull) cryptanalysis are obtained in this paper.

Specifically, the longest linear characteristic known previously for key recovery on SIMON128 shown in paper [3] is a 34-round linear characteristic with correlation  $2^{-63}$  while we present one with correlation  $2^{-61}$  in this paper. Furthermore, the latter can be used to attack SIMON by Matsui's Algorithm 2 with the complexity  $2^{127}$  and probability of success 97% according to the calculating method in [9]. Besides, for SIMON32 the best linear hull known previously is a 13-round one with *potential*  $2^{-31.69}$  in [3] while we give one with *potential*  $2^{-28.99}$  in this paper. Moreover, a 15-round linear hull for SIMON48 with *potential*  $2^{-42.28}$  is presented, whereas the 15-round linear hull with *potential*  $2^{-44.11}$ proposed in paper [3] was the previous best result for this version. We also find a 21-round linear hull with *potential*  $2^{-60.72}$  and a 22-round linear hull with *potential*  $2^{-63.83}$  for SIMON64. The previous best linear hull for SIMON64 is a 21-round linear hull with *potential*  $2^{-62.53}$  proposed in paper [3]. The results are summarized in Table 1.

Version	# Rounds	Correlation	Reference
SIMON198	34	$2^{-63}$	[3]
511101120	34	$2^{-61}$	This paper
Version	# Rounds	Potential	Reference
SIMON22	13	$2^{-31.69}$	[3]
511/101/32	13	$2^{-28.99}$	This paper
CIMON 49	15	$2^{-44.11}$	[3]
511/10/1/40	15	$2^{-42.28}$	This paper
	21	$2^{-62.53}$	[3]
SIMON64	21	$2^{-60.72}$	This paper
	22	$2^{-63.83}$	This paper

Table 1. Summary on improvement of the best linear characteristic/hulls.

# Rounds: Number of rounds for linear characteristic/hulls. The paper is organized as follows. Section 2 gives a brief description of the block cipher SIMON. Section 3 presents a linear cryptanalysis as well as a linear characteristic/hull searching method on SIMON. The improved results with the linear (hull) cryptanalysis are given in Section 4. We finally conclude the paper in Section 5.

## 2 Brief description of SIMON

The SIMON2n/mn is a feistel structure block cipher with (2n)-bit block length and (mn)-bit key length, where n could be 16, 24, 32, 48, or 64 and m is required to be 2, 3, 4. All versions of SIMON with corresponding number of rounds are listed in Table 2. Before a further description of SIMON, we give the notations used in the paper.

Block size $(2n)$	Key size $(mn)$	Total rounds
32	64	32
19	72	36
40	96	36
64	96	42
04	128	44
06	96	52
90	144	54
	128	68
128	192	69
	256	72

 Table 2. Versions of SIMON

## 2.1 Notations

 $L^r$ : left half *n*-bit input for the *r*-th round  $R^r$ : right half *n*-bit input for the *r*-th round  $K^r$ : subkey for the *r*-th round X[j]: the  $(j \mod n)$ -th bit of X, where X[1] is the MSB of X  $n_k$ : the length of the master key  $X \lll i$ : left circular shift by *i* bits of X  $\oplus$ : bitwise XOR  $\wedge$ : bitwise AND

## 2.2 Round function of SIMON

The round function of SIMON is shown as follows:

$$L^{r+1} = R^r \oplus K^r \oplus (L^r \lll 2) \oplus ((L^r \lll 1) \land (L^r \lll 8))$$
$$R^{r+1} = L^r$$

We only consider single key cryptanalysis in this paper thus the key schedule is omitted here. More details on SIMON can be found in paper [4].

## 3 Linear cryptanalysis of SIMON

A linear approximation of bits in plaintexts, ciphertexts and subkeys is a Boolean function and we use correlation and bias to evaluate it. Let  $f: GF(2)^n \to GF(2)$  be a Boolean function. The correlation  $\epsilon_f$  of f is defined by

$$2^{-n} \cdot (\sharp \{x \in GF(2)^n : f(x) = 0\} - \sharp \{x \in GF(2)^n : f(x) = 1\})$$

and  $\delta_f = 1/2 \cdot \epsilon_f$  is denoted as the bias of f. We have  $\delta_f = 2^{-n} (\sharp(f(x) = 0)) - 1/2$ . The higher is the magnitude of the correlation,  $|\epsilon_f|$ , the fewer plaintexts are needed in a linear attack.

Nyberg defined the *potential* of a linear hull with the input and output masks  $\alpha$  and  $\beta$  for a block cipher C = f(P, K) in [8] as follows:

$$ALH(\alpha,\beta) = \sum_{\gamma} (Pr(\alpha \cdot P + \beta \cdot C + \gamma \cdot K = 0) - 1/2)^2.$$
(1)

Similarly, a linear hull with a higher potential value leads to a better linear attack as fewer plaintexts are required.

#### 3.1 Linear approximation of bitwise AND

We denote the unique non-linear layer in the round function of SIMON by

$$f^{N}(L^{r}) = (L^{r} \ll 1) \land (L^{r} \ll 8).$$

Regarding each bitwise  $\wedge$  as a 2 × 1 S-box, the function  $f^N$  is composed of n 2 × 1 S-boxes with inputs  $L^r[j+1]$  and  $L^r[j+8]$ , denoted by

$$f_j^N(L^r[j+1], L^r[j+8]) = L^r[j+1] \wedge L^r[j+8].$$

Consider the linear approximation of the function  $f_i^N$  with two input mask bits and one output mask bit. It is easily calculated that magnitude of the correlation of a linear approximation of a  $2 \times 1$  S-box is  $2^{-1}$  if it is with a nonzero output mask, is 0 if it is with the non-zero input mask and the zero output mask, and is 1 if it is with the all-zero input and output. Thus, the number of active S-boxes is the sum of the Hamming weights of output masks of the S-box layers for SIMON, where an active S-box means it is with a non-zero output mask. Improved Linear (hull) Cryptanalysis of Round-reduced Versions of SIMON

### 3.2 Dependences of S-boxes

As shown in [10], the dependence of active S-boxes should be taken into consideration in linear cryptanalysis. Here we illustrate it by an example.

Let  $Y^r$  be the output value of the nonlinear function  $f^N$  in round r,  $I_1^r$  and  $I_8^r$  be the input masks and  $O^r$  the output mask. Suppose two S-boxes  $f_j^N$  and  $f_{j+7}^N$  are active in one round, we have a linear approximation

$$I_{1}^{r}[j] \cdot L^{r}[j+1] \oplus I_{8}^{r}[j] \cdot L^{r}[j+8] \oplus Y^{r}[j] \oplus I_{1}^{r}[j+7] \cdot L^{r}[j+8] \oplus I_{8}^{r}[j+7] \cdot L^{r}[j+15] \oplus Y^{r}[j+7] \cdot L^{r}[j+7] \cdot$$

with correlation 0 or  $\pm 2^{-1}$ , instead of  $\pm 2^{-2}$  by the piling-up lemma [7]. The invalid application of the piling-up lemma is due to the dependence of the two S-boxes, namely both of them take  $L^r[j+8]$  as input. We should take the dependence seriously as it may invalidate a linear characteristic by correlation 0. In the following, we scritinize the relationship between the input variables of active S-boxes and the correlation of the corresponding expression.

Firstly, the input masks  $(I_1^r, I_8^r)$  of  $f^N$  determine whether the correlation of an approximation is zero or not. For non-zero cases, the output mask determines the absolute value of the correlation. This property comes from a fact on quadratic Boolean functions as follows.

Consider a Boolean function

$$f: \mathbb{F}_2 \times \mathbb{F}_2 \times \cdots \mathbb{F}_2 \to \mathbb{F}_2$$
$$(x_1, x_2, \cdots, x_n) \to L_x(x_1, x_2, \cdots, x_n) + B_x(x_1, x_2, \cdots, x_n),$$

where  $L_x(x_1, x_2, \dots, x_n)$  is linear and  $B_x(x_1, x_2, \dots, x_n)$  is sum of quadratic terms  $x_i \cdot x_j$  and  $x_i, x_j \in GF(2)$ . A new quadratic form

$$g: \mathbb{F}_2 \times \mathbb{F}_2 \times \cdots \times \mathbb{F}_2 \to \mathbb{F}_2$$
$$(y_1, y_2, \cdots, y_n) \to L_y(y_1, y_2, \cdots, y_n) + B_y(y_1, y_2, \cdots, y_n),$$

retaining the same correlation is obtained from  $f(x_1, x_2, \dots, x_n)$  by a nonsingular linear transform y = A \* x, where  $L_y(y_1, y_2, \dots, y_n) = y_{j_1} + y_{j_2} + \dots + y_{j_t}$  and  $B_y(y_1, y_2, \dots, y_n) = y_{i_1} \cdot y_{i_2} + y_{i_3} \cdot y_{i_4} + \dots + y_{i_{2s-1}} \cdot y_{i_{2s}}$  with all subscripts  $i_1, i_2, \dots, i_{2s}$  not coincident. The absolute value of the correlation of the linear approximation of g is 0 if  $\{j_1, j_2, \dots, j_t\} \setminus \{i_1, i_2, \dots, i_{2s}\}$  is non-empty or  $2^{-s}$  if  $\{j_1, j_2, \dots, j_t\} \subseteq \{i_1, i_2, \dots, i_{2s}\}$ . In the latter case, therefore, less variables involved in quadratic terms result in greater absolute value of correlation.

The linear approximation of S-box layer in the r-th round of SIMON is

 $G: \mathbb{F}_2 \times \mathbb{F}_2 \times \cdots \times \mathbb{F}_2 \to \mathbb{F}_2$  $(L^r[1], L^r[2], \cdots, L^r[n]) \to L_G(L^r[1], L^r[2], \cdots, L^r[n]) + B_G(L^r[1], L^r[2], \cdots, L^r[n]),$ where

$$L_G(L^r[1], L^r[2], \cdots, L^r[n]) = \sum_{j=1}^n (I_1^r[j] \cdot L^r[j+1] + I_8^r[j] \cdot L^r[j+8])$$
$$B_G(L^r[1], L^r[2], \cdots, L^r[n]) = \sum_{j=1}^n O^r[j] \cdot (L^r[j+1] \cdot L^r[j+8]).$$

and its correlation should be calculated following the above rules.

## 3.3 Description of automatic enumeration of characteristics with MILP

Automatic search of differential characteristic for bit-oriented block ciphers by Mixed-integer Linear Programming (MILP) modelling was investigated by Sun *et al.* [11], which extended the method to automatic search linear characteristic and linear hull in [10]. This kind of methods denotes each mask bit as a 0-1 variable and describes their propagation through the cipher as linear inequalities (constraints) subjected to which an optimized value of number of active S-boxes is returned. Specifically, the MILP model is as follows.

#### Constraints for linear operation.

These three constraints for linear operation can be directly obtained from paper [6, 10].

1. For each bitwise XOR operation,  $(\alpha_1, \alpha_2)$  and  $\beta$  denote the input masks and output mask of  $\oplus$ . The constraints of these mask bits are:

$$\alpha_1 = \alpha_2 = \alpha_3. \tag{3}$$

2. For each branching in the cipher structre, let  $(\alpha_1, \alpha_2, \alpha_3)$  denote the masks on three branches. The constraints of the masks are:

$$\begin{cases} \tau \ge \alpha_1, \tau \ge \alpha_2, \tau \ge \alpha_3; \\ \alpha_1 + \alpha_2 + \alpha_3 \ge 2\tau; \\ \alpha_1 + \alpha_2 + \alpha_3 \le 2. \end{cases}$$

$$\tag{4}$$

where  $\tau$  is a dummy variable.

3. For operation of left circular shift by i bits, let  $\mu = (\mu[1], \mu[2], \dots, \mu[n])$  and  $\nu = (\nu[1], \nu[2], \dots, \nu[n])$  be the input and output masks. The constraints of the masks are:

$$\nu[j] = \mu[j+i], j \in \{1, 2, \cdots, n\}$$
(5)

#### Constraints for S-box.

The S-box in SIMON is bitwise AND and to get valid linear characteristics we only allow the active S-boxes with non-zero output masks and inactive S-boxes with all zero masks. This rule can be described as:

$$\begin{cases} O^{r}[j] \ge I_{1}^{r}[j], \\ O^{r}[j] \ge I_{8}^{r}[j], \end{cases}$$

$$\tag{6}$$

where the symbols are as mentioned earlier. The constraint (6) also means that the output mask must be non-zero if the input mask is non-zero.

#### Constraints dealing with dependences of S-boxes.

As presented in Section 3.2, given the masks  $(I_1^r, I_8^r), O^r$  for the S-box layer in one round, a smaller number of variables involved in quadratic terms leads to a bigger absolute value of the correlation of G. In this paper, we want to find the masks that lead to the least number of variables appearing in quadratic terms. To indicate the number of variables in quadratic terms of the linear approximation of  $f^N$ , n new 0-1 variables  $V^r[j]$  ( $j \in \{1, 2, \dots, n\}$ ) indicating whether  $L^r[j]$  exists in the quadratic terms are introduced in each round for SIMON. The constraints are

$$\begin{cases} V^{r}[j] \ge O^{r}[j-1], \\ V^{r}[j] \ge O^{r}[j-8], \\ V^{r}[j] \le O^{r}[j-1] + O^{r}[j-8]. \end{cases}$$
(7)

Thus,  $\sum_{j=1}^{n} V^{r}[j]$  is the number of variables appearing in quadratic terms of the

linear approximation for one round and  $\sum_{r} \sum_{j=1}^{n} V^{r}[j]$  is the number of variables appearing in the linear approximation of SIMON. Note that linear characteristics with the same number of active S-boxes may have different correlations due to different cases of dependences of active S-boxes.

## Objective function.

To get the minimum number of linearly active S-boxes, the objective function is set to be the sum of all output mask bits of S-box layers in [10]. However, it is the correlation of the linear characteristics that determines the effectiveness of the linear cryptanalysis. Therefore, considering the influence of the dependence of active S-boxes on correlation, we set the objective function to be  $\sum_{r} \sum_{j=1}^{n} V^{r}[j]$ .

With the constraints and the objective function defined above, we try to find better linear characteristics and linear hulls for SIMON with Gurobi, a solver for MILP models. The linear characteristics found may has correlation value 0 due to the dependence of active S-boxes. It is imperative to test whether the linear characteristic has correlation 0.

## Constraints for linear hulls.

To get linear hulls, we set the input and output mask bits as the ones in a known linear characterisitc and get an amount of linear characteristics that form a linear hull.

## 4 Results

For each linear characteristic, we obtain the accurate absolute value of the correlation of the linear approximation for each round by nonsingular transform method shown in Section 3.2. After getting the correlation in each round, apply the piling-up lemma to obtain the absolute value of the correlation of the whole cipher since S-boxes from different rounds can be seen as independent ones with the effect of round keys. The results are as follows.

#### 4.1 Linear characteristic

Experiments have been done on SIMON128. A 34-round linear characteristic of SIMON128 with bias  $2^{-62}$  for a key recovery attack has been found. To the best of our knowledge, the best 34-round characteristic of SIMON128 known previously is presented in [3] and has the bias  $2^{-64}$ . What is more, all active S-boxes in this characteristic are independent according to our test. Besides, this characteristic of SIMON128 with bias  $2^{-62}$  is the linear characteristic that covers most rounds and simultaneously meets the condition of  $\delta \geq 2^{-n+2}$ , which indicates that the probability of success for key recovery is 0.997 [9]. The previous best result that satisfies the condition is a 33-round characteristic with bias  $2^{-60}$  in [3]. The linear mask (separated into left and right parts) is presented in Tables 5 and 6 in Appendix.

Our characteristic can be used to attack 36-round SIMON128 with data complexity  $2^{124}$  and time complexity  $2^{124}$  by Matsui's algorithm 1 [7], and can be further extended to attack 43 rounds with data complexity  $2^{127}$  with probability of success 0.997 by Matsui's algorithm 2 [7,9]. The latter is demonstrated in Figure 1 where the 60 bits of subkeys numbered in black need to be guessed and the red ones not.

For SIMON64, a 18-round linear characteristic with bias  $2^{-32}$  is listed in Table 7 and Table 8 in Appendix. The longest linear characteristic known previously with absolute value of bias no less than  $2^{-32}$  is a 17-round linear characteristic with bias  $2^{-29}$  presented in [3]. The comparison between our results and the results presented in [3] is in Table 3. Characteristics for SIMON32, SIMON48 are listed in Tables 9-12 in Appendix.

ſ	Version	# Rounds	Bias	Reference
ſ	SIMON64	17	$2^{-29}$	[3]
SIMO	511/10/1/04	18	$2^{-32}$	This paper
ſ	SIMON198	34	$2^{-64}$	[3]
ľ	5111/01/120	34	$2^{-62}$	This paper

Table 3. The comparion between this paper and others.

## 4.2 Linear hull

By setting the input and output masks same as the characteristic in Table 9 and Table 10 with an added constraint  $\sum_{r} \sum_{j=1}^{n} V^{r}[j] \leq 45$ , we find a 13-round linear hull with *potential* 2<sup>-28.99</sup> for SIMON32. To our knowledge, the best previously found linear hull for SIMON32 was a 13-round linear hull presented in paper

<sup>#</sup> Rounds: Number of rounds for linear characteristic.

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Fig. 1. Linear cryptanalysis of SIMON128/192

[3] with *potential*  $2^{-31.69}$ . Actually, 412206 linear characteristics are returned in our model, among which only 196474 have non-zero correlation while others are zero due to the dependence of active S-boxes. Dependence of active S-boxes also exerts influence on valid characteristics. For example, the linear characteristic presented in Table 9 and Table 10 is with correlation  $2^{-18}$  but with 19 active S-boxes. Further, this linear hull can be used to attack 21 rounds for SIMON32/64 as Figure 2 shows with success probability 97%. The number of the bits guessed for the key is 32.

A 15-round linear hull with *potential*  $2^{-42.28}$  for SIMON48 is obtained by setting input and output masks same as the characteristic shown in Table 11 and Table 12, with an additional constraint  $\sum_{r} \sum_{j=1}^{n} V^{r}[j] \leq 59$ . As we know, the best previously found linear hull for SIMON48 was a 15-round linear hull presented in paper [3] with *potential*  $2^{-44.11}$ . Actually, 50432 linear characteristics are returned among which only 43524 are valid. This linear hull can be used to attack 21 rounds for SIMON48/96 with success probability 97% as Figure 3 shows. The number of the bits guessed for the key is 51.

A 21-round linear hull with *potential*  $2^{-60.72}$  for SIMON64 is obtained whereas the previous best linear hull for this version is a 21-round linear characteristic with *potential*  $2^{-62.53}$  [3]. Among the 115199 linear characteristics found with additional constraint  $\sum_{r} \sum_{j=1}^{n} V^{r}[j] \leq 78$ , 63996 have non-zero bias. This linear hull can be used to attack 29 rounds for SIMON64/128 demonstrated in Figure 4 achieving success probability 97%. The number of the guessed bits of key is 63. The masks listed in Table 13 and Table 14 in Appendix is a linear characteristic with bias  $2^{-36}$ . Besides, a 22-round linear hull with *potential*  $2^{-63.83}$  for SIMON64 is found in this paper, with the input and output masks same with the linear characteristic listed in Table 15 and Table 16 in Appendix.

Summary of the results about linear hulls in this paper is presented in Table 4.

Version	# Rounds	potential	# Returned	# Valid	# Attacked	Reference
SIMON32/64	13	$2^{-31.69}$	-	-	20	[3]
51101032/04	13	$2^{-28.99}$	412206	196474	21	This paper
SIMON48/96	15	$2^{-44.11}$	-	-	20	[3]
	15	$2^{-42.28}$	50432	43524	21	This paper
	21	$2^{-62.53}$	-	-	28	[3]
SIMON64/128	21	$2^{-60.72}$	115199	63996	29	This paper
	22	$2^{-63.83}$	52840	28590		This paper

 Table 4. Summary of results with linear hull.

# Rounds: Number of rounds for linear hull.

# Returned: Number of characteristics returned by the model.

# Valid: Number of characteristics with non-zero correlation.

# Attacked: Number of attacked rounds.



Fig. 2. Linear hull cryptanalysis of SIMON32/62



Fig. 3. Linear hull cryptanalysis of SIMON48/96



Fig. 4. Linear hull cryptanalysis of SIMON64/128

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 $\mathbf{K}^{28}$ [1, 2, 3, 4, 5, 6, 7, 8, 10, 11, 12,

14, 18, **26**, 28, 29, **30**, 32]

 $\begin{array}{c} K^{29} [1,2,3,4,5,6,7,8,9,10,11,12\\ ,13,14,15,16,18,19,20,22,26\\ ,27,28,29,30,31,32 ] \end{array}$ 

[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12]

, 13, 14, 15, 16, 18, 19, 20, 22, 26

, 27, 28, 29, 30, 31, 32]

## 5 Conclusion

In this paper, we considered the dependence of S-boxes in the evaluation of correlation of a linear approximation. With an automatic enumeration of the differential and linear characteristic, improved results on the linear (hull) crypt-analysis on SIMON were obtained. Simply, the 34-round linear characteristic with correlation  $2^{-61}$  on SIMON128 presented in this paper is the best linear characteristic as we know. Besides, a 13-round linear hull with *potential*  $2^{-30.19}$  for SIMON32, a 15-round linear hull with *potential*  $2^{-42.28}$  for SIMON48, a 21-round linear hull with *potential*  $2^{-63.83}$  for SIMON64 were presented in this paper.

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## 6 Appendix

Rounds	The input linear mask of the left half
0	000000000000000000000000000000000000000
1	000000000000000000000000000000000000000
2	000000000000000000000000000000000000000
3	000000000000000000000000000000000000000
4	000000000000000000000000000000000000000
5	000000000000000000000000000000000000000
6	0100000000000000000000000000000000000
7	000100000000000000000000000000000000000
8	0100110000000000000000000000000000000
9	0110000100000000000000000000000000000
10	010001000000000000000000000000000000000
11	000100000000000000000000000000000000000
12	010000000000000000000000000000000000000
13	000000000000000000000000000000000000000
14	000000000000000000000000000000000000000
15	000000000000000000000000000000000000000
16	000000000000000000000000000000000000000
17	000000000000000000000000000000000000000
18	000000000000000000000000000000000000000
19	000000000000000000000000000000000000000
20	000000000000000000000000000000000000000
21	000000000000000000000000000000000000000
22	010000000000000000000000000000000000000
23	000100000000000000000000000000000000000
24	010001000000000000000000000000000000000
25	0110000100000000000000000000000000000
26	0100110000000000000000000000000000000
27	000100000000000000000000000000000000000
28	0100000000000000000000000000000000000
29	000000000000000000000000000000000000
30	000000000000000000000000000000000000000
31	000000000000000000000000000000000000000
32	000000000000000000000000000000000000000
33	000000000000000000000000000000000000000
34	000000000000000000000000000000000000000

 Table 5. The left mask of 34-round linear characteristic for SIMON128

Rounds	The input linear mask of the right half
0	000000000000000000000000000000000000000
1	000000000000000000000000000000000000000
2	000000000000000000000000000000000000000
3	000000000000000000000000000000000000000
4	000000000000000000000000000000000000000
5	010000000000000000000000000000000000000
6	000100000000000000000000000000000000000
7	0100110000000000000000000000000000000
8	011000010000000000000000000000000000000
9	010001000000000000000000000000000000000
10	000100000000000000000000000000000000000
11	010000000000000000000000000000000000000
12	000000000000000000000000000000000000000
13	000000000000000000000000000000000000000
14	000000000000000000000000000000000000000
15	000000000000000000000000000000000000000
16	000000000000000000000000000000000000000
17	000000000000000000000000000000000000000
18	000000000000000000000000000000000000000
19	000000000000000000000000000000000000000
20	000000000000000000000000000000000000000
21	0100000000000000000000000000000000000
22	000100000000000000000000000000000000000
23	010001000000000000000000000000000000000
24	0110000100000000000000000000000000000
25	0100110000000000000000000000000000000
26	000100000000000000000000000000000000000
27	010000000000000000000000000000000000000
28	000000000000000000000000000000000000000
29	000000000000000000000000000000000000000
30	000000000000000000000000000000000000000
31	000000000000000000000000000000000000000
32	000000000000000000000000000000000000000
33	000000000000000000000000000000000000000
34	000000000000000000000000000000000000000

Table 6. The right mask of 34-round linear characteristic for SIMON128

Rounds	The input linear mask of the left half
0	100000000000000000000000000000000000000
1	000000000000000000000000000000000000000
2	000000000000000000000000000000000000000
3	000000000000000000000000000000000000000
4	100000000000000000000000000000000000000
5	001000000000000000000000000000000000000
6	000010000000000000000000000000000000000
7	001000100000000000000000000000000000000
8	100000010000000000000000000000000000000
9	000000100110000000000000000000000000000
10	000000110000100000000000000000000000000
11	000000100010000000000000000000000000000
12	100000010000000000000000000000000000000
13	001000100000000000000000000000000000000
14	000010000000000000000000000000000000000
15	001000000000000000000000000000000000000
16	100000000000000000000000000000000000000
17	000000000000000000000000000000000000000
18	000000000000000000000000000000000000000

 Table 7. The left mask of 18 rounds linear characteristic for SIMON64

 Table 8. The right mask of 18-round linear characteristic for SIMON64

Rounds	The input linear mask of the right half
0	000000000000000000000000000000000000000
1	000000000000000000000000000000000000000
2	000000000000000000000000000000000000000
3	100000000000000000000000000000000000000
4	001000000000000000000000000000000000000
5	000010000000000000000000000000000000000
6	001000100000000000000000000000000000000
7	100000010000000000000000000000000000000
8	000000100110000000000000000000000000000
9	000000110000100000000000000000000000000
10	000001000100000000000000000000000000000
11	100000010000000000000000000000000000000
12	001000100000000000000000000000000000000
13	000010000000000000000000000000000000000
14	001000000000000000000000000000000000000
15	100000000000000000000000000000000000000
16	000000000000000000000000000000000000000
17	000000000000000000000000000000000000000
18	000000000000000000000000000000000000000

Rounds	The input linear mask of the left	half
0	000000000100000	
1	0000000000000000	
2	000000000100000	
3	000000000001000	
4	000000000100010	
5	1000000000000000	
6	001000000100010	
7	0000100000011000	
8	0010001000100000	
9	00000001000000	
10	0010001000000000	
11	000010000000000	
12	0010000000000000	
13	0000000000000000	

 Table 9. The left mask of 13-round linear characteristic for SIMON32

Table 10. The right mask of 13-round linear characteristic for SIMON32  $\,$ 

Rounds	The input linear mask of the right half
0	0000000000000000
1	000000000100000
2	000000000001000
3	000000000100010
4	1000000000000000
5	001000000100010
6	0000100000011000
7	0010001000100000
8	000000010000000
9	001000100000000
10	000010000000000
11	001000000000000
12	000000000000000
13	001000000000000

Rounds	The input linear mask of the left half
0	01000100010000001000000
1	00000010000000000000000
2	010001000000000001000000
3	000100000000000000000000000000000000000
4	0100000000000000001000100
5	000000000000000000000000000000000000000
6	0000000000000000001000100
7	000000000000000000000000000000000000000
8	000000000000000000000000000000000000000
9	000000000000000000000000000000000000000
10	000000000000000000000000000000000000000
11	000000000000000000000000000000000000000
12	000000000000000000000000000000000000000
13	000000000000000000000000000000000000000
14	0100000000000000001000100
15	000100000000000000000000000000000000000

 Table 11. The left mask of 15-round linear characteristic for SIMON48

 Table 12. The right mask of 15-round linear characteristic for SIMON48

Rounds	The input linear mask of the right hal
0	00000010000000000000000
1	01000100000000001000000
2	000100000000000000000000000000000000000
3	010000000000000000000000000000000000000
4	000000000000000000000000000000000000000
5	000000000000000000000000000000000000000
6	000000000000000000000000000000000000000
7	000000000000000000000000000000000000000
8	000000000000000000000000000000000000000
9	000000000000000000000000000000000000000
10	000000000000000000000000000000000000000
11	000000000000000000000000000000000000000
12	000000000000000000000000000000000000000
13	010000000000000000000000000000000000000
14	000100000000000000000000000000000000000
15	010101000000000001000000

 Table 13. The left mask of 21-round linear characteristic for SIMON64

Rounds	The input linear mask of the left half
0	000000000000000000000000000000000000000
1	000000000000000000000000000000000000000
2	000000000000000000000000000000000000000
3	000000000000000000000000000000000000000
4	000000000000000000000000000000000000000
5	000000000000000000000000000000000000000
6	010000000000000000000000000000000000000
7	000100000000000000000000000000000000000
8	010011000000000000000000000000000000000
9	011000010000000000000000000000000000000
10	010001000000000000000000000000000000000
11	000100000000000000000000000000000000000
12	010000000000000000000000000000000000000
13	000000000000000000000000000000000000000
14	000000000000000000000000000000000000000
15	000000000000000000000000000000000000000
16	000000000000000000000000000000000000000
17	000000000000000000000000000000000000000
18	000000000000000000000000000000000000000
19	000000000000000000000000000000000000000
20	000000000000000000000000000000000000000
21	000000000000000000000000000000000000000

Table 14. The right mask of 21-round linear characteristic for SIMON64

Rounds	The input linear mask of the right half
0	000000000000000000000000000000000000000
1	000000000000000000000000000000000000000
2	000000000000000000000000000000000000000
3	000000000000000000000000000000000000000
4	000000000000000000000000000000000000000
5	010000000000000000000000000000000000000
6	000100000000000000000000000000000000000
7	010011000000000000000000000000000000000
8	011000010000000000000000000000000000000
9	010001000000000000000000000000000000000
10	000100000000000000000000000000000000000
11	010000000000000000000000000000000000000
12	000000000000000000000000000000000000000
13	000000000000000000000000000000000000000
14	000000000000000000000000000000000000000
15	000000000000000000000000000000000000000
16	000000000000000000000000000000000000000
17	000000000000000000000000000000000000000
18	000000000000000000000000000000000000000
19	000000000000000000000000000000000000000
20	000000000000000000000000000000000000000
21	010000000000000000000000000000000000000

Rounds	The input linear mask of the left half
0	100010000000000000000000000000000000000
1	001000000000000000000000000000000000000
2	100000000000000000000000000000000000000
3	000000000000000000000000000000000000000
4	000000000000000000000000000000000000000
5	000000000000000000000000000000000000000
6	000000000000000000000000000000000000000
7	000000000000000000000000000000000000000
8	100000000000000000000000000000000000000
9	001000000000000000000000000000000000000
10	100010000000000000000000000000000000000
11	000000100000000000000000000000000000000
12	000010011000000000000000000000000000000
13	000011000010000000000000000000000000000
14	000010001000000000000000000000000000000
15	000000100000000000000000000000000000000
16	100010000000000000000000000000000000000
17	001000000000000000000000000000000000000
18	100000000000000000000000000000000000000
19	000000000000000000000000000000000000000
20	000000000000000000000000000000000000000
21	000000000000000000000000000000000000000
22	000000000000000000000000000000000000000

 Table 15. The left mask of 22-round linear characteristic for SIMON64

Table 16. The right mask of 22-round linear characteristic for SIMON64

Rounds	The input linear mask of the right half
0	001000000000000000000000000000000000000
1	100000000000000000000000000000000000000
2	000000000000000000000000000000000000000
3	000000000000000000000000000000000000000
4	000000000000000000000000000000000000000
5	000000000000000000000000000000000000000
6	000000000000000000000000000000000000000
7	100000000000000000000000000000000000000
8	001000000000000000000000000000000000000
9	100010000000000000000000000000000000000
10	000001000000000000000000000000000000000
11	000010011000000000000000000000000000000
12	000011000010000000000000000000000000000
13	000010001000000000000000000000000000000
14	000001000000000000000000000000000000000
15	100010000000000000000000000000000000000
16	001000000000000000000000000000000000000
17	100000000000000000000000000000000000000
18	000000000000000000000000000000000000000
19	000000000000000000000000000000000000000
20	000000000000000000000000000000000000000
21	000000000000000000000000000000000000000
22	00000000000000000000000000000000110
	$\begin{array}{r} \mbox{Rounds} \\ \hline 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \\ 16 \\ 17 \\ 18 \\ 19 \\ 20 \\ 21 \\ 22 \\ \end{array}$