Neeva: A Lightweight Hash Function

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Abstract

RFID technology is one of the major applications of lightweight cryptography where security and cost both are equally essential or we may say that cost friendly cryptographic tools have given more weightage. In this paper, we propose a lightweight hash, *Neeva-hash* satisfying the very basic idea of lightweight cryptography. Neeva-hash is based on sponge mode of iteration with software friendly permutation which provides great efficiency and required security in RFID technology. The proposed hash can be used for many application based purposes.

Keywords: Hash function, Lightweight cryptography, Present, Quark, Sponge construction, Spongent

1 Introduction

When we think about the advancement of today's world, the very first thing comes into our mind is the 'Internet' and with it, 'how secure it is'. One of the important tasks in front of cryptographers is to preserve the privacy, authentication as well as integrity of the messages which we want to send through insecure channel like internet. Hash functions have a significant role in cryptography. It maps messages of arbitrary length into a fixed length digest. They were used to check the integrity of message initially but now they have been used in each and every field of online world. They are the building blocks of today's digital world. The online banking transactions would not be that secured without hash functions, password protected systems would not exist without it, even the android phones would have lost its charm without that extra feature of pattern lock which is an application of hash functions (SHA-1). In the mentioned examples, we just don't need to manage privacy and integrity but also sometimes authentication (keyed hash) and many

other features and this is done by standard dedicated hash functions such as SHA-224, SHA-256, SHA-384, SHA-512 (collectively called SHA-2 [SS]) and now SHA-3 [RPCK] can also be counted in this list. MD5 [Ber] and SHA-1 [CMR] are outdated due to its low security and SHA-2 are excessively used worldwide for data integrity, privacy, digital signatures and for many more purposes. SHA-3 has just standardised in Aug, 2015 by NIST and now can be used in the applications of hash function. Dedicated hash functions usually need more memory size hence cost to achieve the normal efficiency and required security. A decent trade-off between efficiency and security is what we are looking in a standard hash function.

Size plays an important role in today's world as it can be seen in many small computing devices that are used in day-to-day life. These small embedded devices like barcodes, biometrics, smart cards, RFIDs (Radio frequency identification) which play a very prominent part of today's modern world where integrity, authentication and compactness are needed. The "Internet of Things" which comprises a network of physically small things needed in electronics, software, sensors for exchanging data between the objects. The compactness can be understood by the limitation on size or battery power and here comes lightweight cryptography. As the name suggests, it would be light in the sense that the memory part is restricted, i.e., low cost in the hardware but performance doesn't get halted. In this case, we need to have a good trade-off between storage and security. Lightweight cryptography ensures that the algorithm would be efficient and secured (majorly preimage resistant) at the lower cost. Its main aim is to achieve "low cost" subjected to good efficiency in hardware as well as software and security of algorithm. We don't want to keep the information secret forever, hence low-embedded devices do not need security more than what is required. Many lightweight ciphers have been proposed since then which includes many block cipher as well as stream cipher like HIGHT [HSH], IDEA [WPS], NEOKEON [DPR], PRESENT [BKLP], Grain-128a [HJM] and many more can be added in the list. Most of them are not a novel design, instead constructed on the existed designs to assure their security and performance are upto the mark.

Lightweight hash functions are integral part of lightweight cryptography. It has vast applications in smart cards technology, RFID tags [Fin] not just for tracking the shipping materials but also for every grocery item and many others. There excess demand in every sector, viz., industries, education, services etc. says it all. These hash functions target on low cost of implementation without compromising much on efficiency and provides necessary security. We have sponge based lightweight hash like QUARK [Aum], PHOTON [GPP], SPONGENT [BKL] which provide good trade-off between efficiency and security. There are few designs of lightweight hash functions which are based on stream cipher, i.e., BEAN [KOJ] which could be used as random number generators and have been successfully used in many applications.

Lightweight cryptography is still under exploring phase. We don't have proper standard lightweight hash or lightweight block ciphers but as already mentioned many have been introduced lately. A lot of research and analysis are going on for their betterment so that it can be used for further applications and providing an upcoming area of research.

In this paper we propose a lightweight hash function, $Neeva-hash^1$. From now onwards we call this hash as Neeva-hash. This paper is organised in the following manner: In section 2, lightweight cryptography is briefly discussed, we describe our proposed lightweight hash scheme in section 3 and its analysis is shown in section 4.

2 Lightweight Cryptography

Cost, security, and efficiency are the three major dimensions of lightweight cryptography. The standardization of lightweight ciphers has not taken place yet, so any design whether it's a conventional one or unconventional novel structure is welcomed with keeping in mind its related cost, power consumption and cryptographic security and performance needed in today's world. Few of the lightweight ciphers have been designed initially like Crypto1 is a stream cipher with 48-bit key designed for RFID tags [Sol], Cryptomeria cipher is a Feistel based block cipher used in encryption on DVD audio discs, Kindle is a stream cipher with 128-bit key and used in Amazon kindle. Because of their specified use and low cost they are used very much but been broken recently [BLR]. In the last decade, massive designs been introduced in lightweight ciphers. Many lightweight block ciphers and stream ciphers are there in the usage. Present, is one of the important ultra lightweight block cipher and been extensively used in many lightweight block cipher based hash. After SHA-3 competition many sponge based hash functions, for example Quark – sponge construction based hash with non-linear Boolean functions available in the digest size of 256-bit, 176-bit and 136-bit, Photon – sponge like construction and AES like primitive as internal permutation available in the digest size 256-bit and 160-bit, Spongent – sponge construction with Present permutations and counter available in the digest size 88-bit, 128-bit, 160-bit 224-bit and 256-bit, even Keccak (small) can be used as lightweight hash with r=40, c = 160 and digest size is 160-bit where r is the rate and c is capacity, are designed and used extensively for their good efficiency and software friendly designs.

The security of sponge based designs depends on their capacity. A sponge function is been found indifferentiable from a random oracle upto $2^{c/2}$ computation. For n-bit sponge based hash function and $n \ge c$, the security bound for collision resistant is $2^{c/2}$ and for second preimage resistant, it has been reduced to $2^{c/2}$. If the sponge construction is hermetic (underlying permutation doesn't have structural distinguishes) and has a reasonable small rate (r) then security bound for preimage resistant has been reduced to 2^{n-r} [BKL].

3 Proposed Scheme

The scheme proposed in this paper is based on sponge construction. Here initial register is of b-bit and b = r + c where r is rate and c is capacity of the state b. The state b is of 256-bit. The rate and capacity is 32-bit and 224-bit respectively, viz.,

¹ "Neeva" is a Punjabi word which literally means "low". Here we are using Neeva to explain the small memory size required for this hash hence the low cost

r=32, c=224. As in sponge construction, message block will be xored to the most significant 32-bit of the initial register. Message is padded so it can be divided into the blocks of 32-bit. The initial state s_0 is of all zeroes i.e., $s_0 = 0^r || 0^c$, first message block is xored and initial register is updated. Here we have sixteen 16-bit words in the updated register. We apply Present S-box (4×4) on these sixteen words in parallel for confusion. Then first, second and third word is updated by xoring with fourth word and keeping fourth word unchanged. This unbalanced Feistal structure is applied in parallel on four 64-bit strings of the register to provide word wise diffusion but this alone would not be enough. For overall diffusion throughout the 256-bit register, there is a 8-bit left rotation of the register and then we add round constants to it. Addition is done as addition modulo 2^{16} . The register is updated and this whole comprises to one round. So here we have three basic operations for confusion and diffusion, i.e., S-Box layer for confusion, xoring and rotation will provide overall diffusion and modular addition will remove fixed patterns. The whole process will be repeated for 31 more rounds i.e., in total 32 rounds. So, every message block will go through these 32 rounds.

The sponge construction processed in three phases as follows:

(i) Initialization Phase

The message can be of arbitrary length. The padded message should be a multiple of 32-bit. For that we need an unambiguous padding rule. Given an input message M of length ℓ bits, append the bit 1 to end of M, and then append $(-\ell-2) \equiv k \mod 32$ '0' bits and 1 at the end of it. For sponge based hash function, we need to have a message blocks of size of rate.

$$M||Pad(M) = M_1||M_2|| \cdots ||M_t|$$

where each M_i is a 32-bit block.

(ii) Absorbing Phase

The first message block is xored with most significant 32-bit of initial register, s_0 (i.e. 256-bit register of all zeroes) and then permutation f applies on it. In the processing of one block, 32 times the same permutation acts on it. This keep happens till all message blocks are absorbed. In the absorbing phase, the initial register as_i is updated by the following manner:

$$as_i = f(as_{i-1} \oplus M_i||0^c),$$

for $1 \le i \le t$ and $as_0 = s_0$ is initial register.

(iii) Squeezing Phase

The most significant 32-bit are taken as an output after first round of squeezing phase by just applying f on final register of absorbing phase. Then again the permutation applied on register in the same manner and every time most significant 32-bit are taken. These bits then concatenated and continues till we get 224-bit required digest i.e., we need to have 7 rounds of squeezing

phase to get a digest size of 224-bit. In the squeezing phase, ss_i is updated by the following manner:

$$ss_i = f(ss_{i-1})$$
 for $1 \le i \le 7$ and $ss_0 = as_t$.

Figure 1 describes the phases of sponge construction [BDPA].

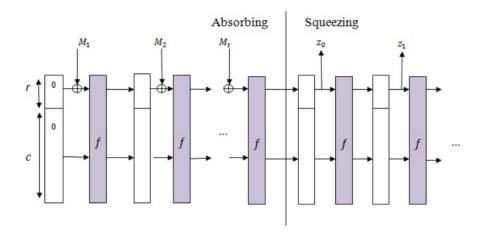


Figure 1: Three Stages of sponge construction

3.1 The Compression Function

The compression function of proposed scheme is based on sponge construction [BDPA]. Suppose we want to compute Neeva-hash of a message M. Message M is padded and divided into the 32-bit blocks and then the first message block M_1 is xored to the state. After applying the Present S-box in parallel, the updated register is divided in sixteen 16-bit words on which we apply Feistel structure on every 64-bit parallely. After a 8-bit left rotation, it is added to a round constant. The updated register after modular addition is the output of first round. Its keep feeding to the next round till 32 rounds. This is the absorbing phase of compression function as message is getting absorbed here. If we have more than one message block, then after the first block absorption, its output will be taken as an updated register and the next message block will be xored to updated register and again whole of the steps would be repeated for this message block. We keep processing all the message blocks in this manner till they get exhausted and this would end absorption phase. In squeezing phase, most significant 32-bit is taken out. Then we apply permutation f on the updated register and every time we take out the most significant 32-bit. This is done for seven times and all these seven 32-bit are concatenated to get the output of 224-bit. Hash digest of 224-bit would usually provide security of 2^{112} and here c=224 which implies that collision security would be 2^{112} which is good with respect to today's security requirement.

3.2 Mode of Operation

After initialization, all the message blocks are first absorbed on which we apply the permutations. Each message block is processed in 32 rounds by these permutations.

Once message blocks are exhausted then we start taking first 32-bit after every f application, to have a digest of 224-bit. This would need application of f seven times. The following figure describes the processing of one message block with Neeva-hash.

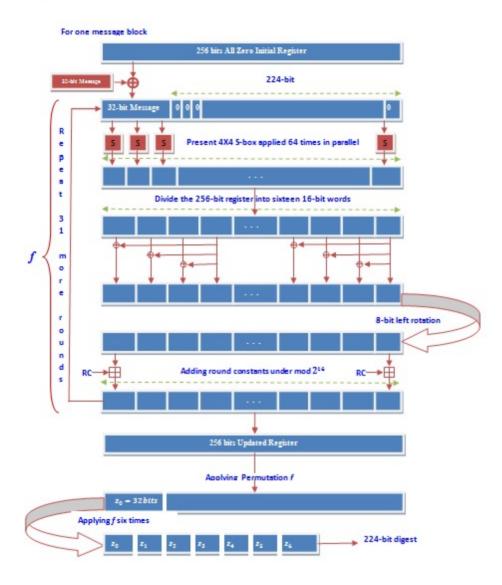


Figure 2: Neeva-hash function

4 Analysis of Neeva-hash

In this section we will discuss the analysis of Neeva-hash. The test values have been given in the end of the paper.

4.1 Efficiency of Neeva-hash Function

In this subsection we are analysing the efficiency of Neeva-hash with one of the popular lightweight hash functions, Spongent-224. The following table provides

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 \begin{aligned} & \text{input} \ : M_1, M_2, \dots, M_t \\ & \text{for} \ i = 1 \ to \ t \ \text{do} \\ & A_i \leftarrow CV_{i-1} \oplus M_i, \ CV_0 = 0^{32} || 0^{224} \\ & \text{for} \ j = 0 \ to \ 31 \ \text{do} \\ & \left| \ B_i^{(j)} \leftarrow S^{(j)}(A_i) \ \text{Apply S-box } 64 \ \text{times in parallel} \right| \\ & B_i^{(j)} = b_0^{(j)} || b_1^{(j)} || \cdots || b_{15}^{(j)}, \ b_m^{(j)} \rightarrow 16 \text{-bit words}, \ 0 \leq m \leq 15 \\ & \text{for} \ k = 0 \ to \ 3 \ \text{do} \\ & \left| \ b_i^{(j)} = 0 \ to \ 2 \ \text{do} \right| \\ & \left| \ b_{4k+l}^{(j)} \leftarrow b_{4k+l}^{(j)} \oplus b_{4k+3}^{(j)} \right| \\ & \text{end} \\ & B_i^{(j)} \leftarrow b_0^{(j)} || b_1^{(j)} || \cdots || b_{15}^{(j)} \\ & \text{end} \\ & B_i^{(j)} \leftarrow rotl_8(B_i^{(j)}) \\ & B_i^{(j)} \leftarrow B_i^{(j)} \boxplus_{2^{16}} RC_j \\ & \text{end} \\ & CV_i \leftarrow B_i^{(31)} \\ & \text{end} \\ & return \ A_t \leftarrow B_t^{(31)}; \\ & r = 0, 1 \dots, 6; \\ & z_r \leftarrow MSB_{32}(f^r(A^t)) \\ & H = z_0 || z_1 || z_2 || z_3 || z_4 || z_5 || z_6 \end{aligned}
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Algorithm 1: Neeva-hash Function

the comparison in the efficiency of Neeva-hash with Spongent-224 on an Intel core 2 duo 32-bit OS E8400 @ 3 Ghz processor with 1 GB RAM.

File Size	Spongent-224	Neeva-hash
(in MB)	(in Sec)	(in Sec)
1	1.44	0.65
5	3.06	2.53
10	5.87	4.99

This shows that the efficiency of Neeva-hash is better than Spongent-224 which makes it really software friendly.

The speed of this hash algorithm has been calculated as almost 12067 cycles/bytes which seems fairly good in context to hardware.

4.2 Avalanche Effect

A message M of length 1024-bit is taken and its Neeva-hash(M) is calculated. While calculating Neeva-hash it will be padded before dividing it into the blocks of 32-bit which means we would have 33 message blocks. Now change in the i^{th} bit in message M will generate M_i files where $1 \le i \le 1024$. The hamming distance of M_i from M exactly 1. We then calculate Neeva-hash (M_i) , thus compute the hamming distance d_i , between Neeva-hash (M_i) and Neeva-hash(M) for $1 \le i \le 1024$ and finally the hamming distances in the corresponding 32-bit words of the hash values are computed.

The results have been shown in the following table with the maximum, the minimum, the mode and the average value of distances mentioned above.

Changes	W_1	W_2	W_3	W_4	W_5	W_6	W_7	Spongent-224	Neeva-hash
Max	24	24	24	25	25	26	23	136	137
Min	8	7	5	7	7	8	8	89	89
Mode	16	15	17	16	16	16	18	113	113
Mean	16.03	15.77	16.03	16.06	15.97	16.07	15.98	111.84	111.91

Table 1: Hamming Distances

The following figure shows the hamming distances range of 1024 files which is coming out to be almost uniform i.e change in one bit of the input brings $\approx 50\%$ change in output digest of hash.

4.3 Differential Characteristics

Differential attack was presented by Biham and Shamir in 1990 on DES block cipher [BS]. This attack exploits the high probability differences in input and output of an encryption scheme. High probability input and output differences of the non-linear components (e.g., S-box in this case, as modular addition is not counted here because we try to apply differential cryptanalysis of the modified version of our proposed hash function by replacing modular addition of constants with xor operation with the round constants) are used to form differential trail of the sponge

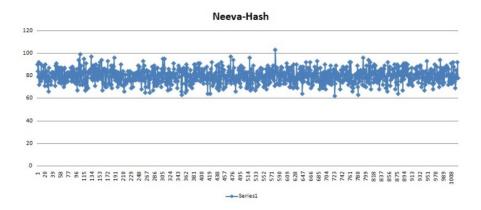


Figure 3: Hamming Distances range of the 1024 files

f function by joining 1 round high probability differentials trails. The modified f function uses a 4×4 Present S-box as its only non-linear component now. Maximum differential probability for arbitrary input difference producing a output difference in a single S-box application is $\frac{4}{16} = 2^{-2}$ [Wan]. This value ensures that even if there is only one active S-box in each round, still differential attack will require 2^{64} chosen plaintexts to distinguish the first 32-bit of Neeva-hash.

Now, we see whether differential cryptanalysis is applicable on Neeva-hash. This hash function is using PRESENT S-box in their construction. In the modified version of Neeva-hash, at least one bit input difference causes an active S-box after one round and 1 more active S-box after second round if it occurs in the most significant byte of the word of updated register. The number of active S-boxes is 12 after 9-rounds. If we keep continuing in this way till all 32-rounds, the number of active S-boxes would reach to 50. Then, the minimum number of active S-boxes is 50 (Here we have taken the input difference in the first sixteen most significant bits). Hence the maximal probability of finding a differential characteristic is $(2^{-2})^{50}$, i.e., 2^{-100} . This means we require 2^{100} chosen plaintexts to distinguish the most significant 32-bit of the output whereas by birthday paradox this chosen plaintexts is 2^{16} (for most significant 32-bit of the output) which is comparatively very small as compared to 2^{100} . It shows that differential cryptanalysis is not applicable to modified version of Neeva-hash hence Neeva-hash.

4.4 Bit-Variance Test

Bit Variance is one of the statistical tests for the randomness of the hash digest. It basically tests the change in the hash output when input bits are changed. It measures the uniformity in each bit of the output. Given an input message, all the changes in the input are accounted and output is calculated for each of the change. Then, for each digest bit the probabilities of taking on the values of 1 and 0 are measured considering all the outputs produced by applying input message bit changes. If the probability, $P_i(1) = P_i(0) = 1/2$ for all digest bits i = 1, ..., 224 then, the Neeva-hash function has attained maximum performance in view of bit variance test [KZ]. Since it is computationally infeasible to consider all input message bit changes, we have evaluated the results for only up to 1024

files, viz. $M, M_1, M_2, \ldots, M_{1024}$ which we have generated for conducting avalanche effect, and found the following results:

The experiments were performed on 1024 different messages (which we have taken in avalanche test). This hash function passes the bit-variance test. Plotting the probability (Figure 4) of each of the bits (224-bit), we see that the average probability is approximately 0.50.

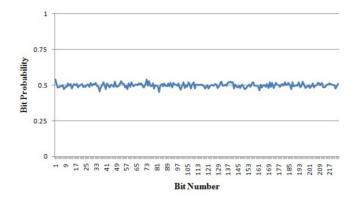


Figure 4: The probability of the bit position

4.5 Near-collision resistant

A hash function is called near-collision resistant if it is computationally infeasible to find two inputs with hash output differ in small number of bits i.e.,for two different messages M and M', their Neeva-hash value is almost same (differ in small number of bits), which means hamming weight of $(H(M) \oplus H(M'))$ is relatively small (upto 16-bit). To check the near-collision resistance we have taken 100,000 files and checked xor of hamming distance of Neeva-hash of two random files from the lot. So, we need to choose two files out of 100,000 files that would be $\binom{100000}{2}$ which is 4,999,950,000 files. After analyzing, it shows the minimum and maximum hamming weight of the hash of these files comes as 66 and 162 respectively. The hamming weight 113 comes maximum number of times i.e. 266,272,292.

No. of files having the difference between 92 and 132

$$(92 \le \#files \le 132) = 4,967,495,075(i.e.,99.35\%)$$

That means more than 99% of files give hamming distance between 112 ± 20 which is good with respect to the fact that they won't give any near-collision attack as for near-collision the hamming distance of two files needs to be really small viz. upto 16-bit. Hence by the analysis results *Neeva-hash* shows resistant to near-collision attack.

5 Conclusion

In this paper we have proposed a lightweight hash function, Neeva-hash based on sponge construction with a software friendly permutation. It gives the collision resistance 2¹¹² which is good with respect to today's security requirements. Analysis of this hash function includes avalanche effect, a heuristic proof of differential characteristics, bit variance test and near-collision resistant test. It satisfies all the properties needed for an RFID tag and pseudo random number generator. It seems a good option for lightweight hash and can be used in many of its applications.

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Test Vectors

Test values of the three inputs are given below:

Neeva- $hash(a)$	=	52ca54ca	ad4617dc	b051b2c4	cc6c1c9e
		92753d16	47a22405	aa912c08	
Neeva-hash(ab)	=	0a163ca8	02692371	b2d1a303	5da3bb8f
		5e9b08ee	82e2d5f4	1e532c1a	
Neeva-hash(abc)	=	b0c8be3d	fcbc3886	439256e1	fe568253
		5d58c7dd	9124dbc3	6cc37c91	

Round Constants

 RC_0 c7b119402be75b5fe34230e1c6de7511503b802a96a7f546fd02a80d8cb27863 RC_1 6990c02e24cf9ab94c057e4e08726162dccb97ca280e1ccb6db961615a126f97 RC_2 = ff223911f7f604c272d7ec72db58b760669de33dee6be0202550c439d270f05e RC_3 = f5a6c2820cac1ab3b263f3f68b1d3c53118bb9d52521bd520eb7a1e5a3cb9e5b RC_4 = 1612115e8201b0311ea4d23d2bb3f906832a60191b4181d9f3f2a22b9671f3ba RC_5 = d299ae33da1d4ed5ed9c5c77047b758fe01bb24d4801a33b8050013fbb396b14 RC_6 1d18fe11cd6aa678cfe053451418e7dbb8b382220290ebd42291a6ff6c4c1743 RC_7 = 4afc5e1277a7355ec0b5a2231a9e2ccc02f555d4739836567bcdef91d914cfe2 RC_8 = ece8b0d3361a8b569fe8cecb31b9ecd7e730d51ab9f94b620357d728fdbeda72 RC_{9} 1e5d2b7bfca2f0cce303b2bf33be3dc4ce60882398bb64f60b7adb092bface29 RC_{10} = 89a2a6a2baf87b8705ead75447d16334479ad1f87a467e1245e036f2119df0eb RC_{11} = 96b970981eb889eb988a96bf01fc1dd13a0c119519ffe34590a0fe36c225749e $RC_{12} =$ 10f20d64be3da2783114fe4dfaef826db18e6e25cf42ff6f22a604a3496878d6 RC_{13} 104d1cdde66f47312729c321e0ca3b99d39b754672e3910d6a4ddc204a7989f6 = RC_{14} = 3b346ce05703de7eb2719130af1b426660aac3243e43b2234b95c10d28d13528 RC_{15} = 786d780921f9490b94476162609fd9e100c2fdb347fe2208086b1d8fc2459661 $RC_{16} =$ 888460b5299cee14e2095e0676c4ee73aef17819767cd8ee9223162928c83763 RC_{17} e80f465c9f7cfc78a49539b737812cbcdcd37347cf4d4025ac70a24356ef05d3 RC_{18} ce366bd878a9218786f4fddef33e2ad51012edbde19085f0ebcee84638fa7126 RC_{19} 76a45e9feb2c4123370448278054b494b62d481b5c8403a1cab5529bea62b745 RC_{20} adf6d3e93166a6f892b0a9d59d55a1a51ca11b9cb530d7f5d50946dd9ceeda2c RC_{21} 3246b10c987b174fd9f598444a5c42e9ea390cf5c4c5a5fdba7e0a08f59d2f10 RC_{22} 9f3903e5338b6415d92b4707462d4ef82844f7897dcf8f702e131c062682a99a RC_{23} 70ff29c4c11f18008dd533acd7248c9b0a642ebaf42b4fb20898288b394e5f33 RC_{24} = cb8befdfdf5b238b1c730c0bf30855bbc7a0bfa5ae3516ab7edd326f5611ae48 $RC_{25} = dfeb28672f6bcfc1afb3d11a97bbe65fc0ffb97d526913fca74d7e995ba9a3a6$ $RC_{26} =$ 9f7f4896467352c824c941af49866c11246f4529d55c0b1110b9047575249533 $RC_{27} = 79990702621c531145378996444dc267629c221a9d6fc3d75be71d704ae1bac2$ $RC_{28} = 5$ f6731bf692923f1b6d1dce74905c7ca504acba3d0b95bc79d7787025783e5cf RC_{29} ec1d0d8ddd6b5d8dcf1c5a759fae7dc0c206489bc8f14d8d9e4a6bcb2287c7c3 RC_{30} = fc2d8fd04b8f582fadd6205ca979b648a2c6fc9b00ca8b389cd94a3ef90ad435 RC_{31} = 40e308b38501c4273130a587906a0ccc5461f947f201759b50b61dd32adedb9a