# Authenticated Garbling and Efficient Maliciously Secure Multi-Party Computation

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### Abstract

In this paper, we extend the recent work by Wang et al., who proposed a new framework for secure two-party computation in the preprocessing model that can be instantiated efficiently using TinyOT. We show that their protocol can be generalized to the multi-party setting, where the preprocessing functionality is based on the multi-party TinyOT-like protocol. Assuming there are n parties where at most n-1 parties are corrupted, the function-dependent phase has a total communication complexity of  $O(\kappa n^2)$  bits per AND gate; the online phase has a total communication complexity of  $O(\kappa n^2)$  bits per input bit.

In the second part of this paper, we propose a new multi-party TinyOT protocol. The new protocol uses a set of new techniques that allow parties to distributively check the correctness without the need for cut-and-choose. The resulting protocol is much more efficient compared to previous protocols: with statistical security parameter  $\rho$ , the complexity to generate one AND triple is  $O(\frac{\rho}{\log |\mathcal{C}|}n^2)$ , where  $|\mathcal{C}|$  is the circuit size. The best previous multi-party TinyOT protocol hydrarity at all has a complexity of  $O(-\frac{\rho^2}{2}-\pi^2)$  per AND triple

protocol by Frederiksen et al. has a complexity of  $O(\frac{\rho^2}{\log^2 |\mathcal{C}|} n^2)$  per AND triple.

The resulting protocol enjoys extremely high efficiency, compared to the state-of-the-art protocol by Lindell et al. that combines the BMR protocol with the SPDZ protocol.

## 1 Introduction

Secure multi-party computation (MPC) allows a set of parties to privately compute a function on their joint inputs. The protocol ensures that an adversary corrupting a set of parties cannot learn anything more than the output of the function.

Most works on MPC [KOS16, FKOS15, BDOZ11, DPSZ12, FLNW17] suffer from one huge drawback: the protocol requires a number of round-trips proportional to the depth of the circuit being evaluated. When the parties are geographically separated, or when the number of parties becomes high, such round-trip time can be overwhelming, compared to the time required for the other parts of the protocol. For example, the AES circuit has a depth of around 50. If parties are located in the U.S. and Europe, round-trip time is 75 ms even with dedicated networks provided by Amazon EC2. This means a total of 3750 ms is spent on round-trips, not to mentioned the time to perform cryptographic operations and to send messages. Most of these works are based on secret sharing: for each AND/Mult gate, they require at least one round-trip.

Another completely different approach that constructs constant-round MPC protocol is by Beaver, Micali, and Rogaway [BMR90]. Their protocol uses any interactive MPC protocol to jointly garble a circuit, which can be then evaluated. This approach was regarded as only a theoretical

	Complexity
Choi et al. [CKMZ14] Lindell et al. [LPSY15] + Keller et al. [KOS16]	$O\left( \mathcal{C} \frac{\rho^2}{\log \mathcal{C} }\right)\\O\left( \mathcal{C} \kappa n^2\right)$
Section $4 +$ Frederiksen et al. [FKOS15] Section $4 +$ Section $6$	$\begin{array}{c} O\left( \mathcal{C} \frac{\rho^2}{\log^2 \mathcal{C} }n^2\right)\\ O\left( \mathcal{C} \frac{\rho}{\log \mathcal{C} }n^2\right) \end{array}$

Table 1: Constant-round Multi-party protocol secure against n-1 corruption. Choi et al. is only for three party.

solution until recently: Damgard and Ishai [DI05] applied this idea to a setting with honest majority; Choi et al. [CKMZ14] applied to a setting with three parties and dishonest majority; Lindell et al. [LPSY15, LSS16] uses the SPDZ protocol and Somewhat Homomorphic Encryption to garble a circuit achieving constant round MPC protocol with all-but-one corruption.

Authenticated Garbling. A recent work by Wang et al. shows that in the two-party setting, BMR protocol can be made practical. In particular, the paper discusses two techniques: 1) how to use the TinyOT protocol to distributively garble a single circuit efficiently. The distributed garbled circuit is "authenticated" such that an adversary cannot arbitrarily change it; 2) how to use ideas from zero-knowledge garbled circuit [JKO13] to, in turn, construct an improved TinyOT protocol.

**Contribution.** In this paper, we fully extend the authenticated garbling in the multi-party setting:

- 1. We present an extension of the main protocol by Wang et al. to the multi-party setting. The resulting protocol is in the (TinyOT-like) preprocessing model, with communication  $O(\kappa n^2 |\mathcal{C}|)$  bits and only has a constant number of rounds.
- 2. The above preprocessing functionality can be instantiated using existing work. However, we design a new protocol that generalizes TinyOT for the multi-party setting. The cost to preprocess a single AND gate is  $O(Bn^2)$  where  $B = \frac{\rho}{\log |\mathcal{C}|}$ , while the best previous work [FKOS15] requires  $O(B^2n^2)$ .
- 3. The resulting protocol is very simple, and we intend to implement it to test its practical performance.

**Outline.** In the next section, we will provide some high-level intuition on how our main protocol in the preprocessing model works. In Section 4, we provide complete description of the protocol, with proof in Section 5. Finally in Section 6, we discuss an efficient instantiation of the preprocessing functionality.

## 2 Notations and Preliminaries

We use  $\kappa$  to denote the computational security parameter and  $\rho$  to denote the statistical security parameter. We also use = to denote equality and := to denote assignment.

We represent a circuit as a list of gates. Each gate is represented as  $(\alpha, \beta, \gamma, T)$ , which means a gate with input-wire indices as  $\alpha$  and  $\beta$ ; output wire index as  $\gamma$  and gate type as  $T \in \{\oplus, \wedge\}$ . Furthermore, we use  $\mathcal{I}_i$  to denote the set of all input wire indices for  $P_i$ 's input;  $\mathcal{W}$  to denote the set of output wire indices for all AND gates,  $\mathcal{O}$  to denote the set of output wire indices of the circuit. Parties are denoted as  $P_1, ..., P_n$ . Since our main protocol is based on garbled circuits, we designate  $P_1$  as the circuit evaluator.  $\mathcal{M}$  is used to denote the set of parties that are corrupted and  $\mathcal{H}$  is used to denote the set of honest parties, which means  $\mathcal{M} \cup \mathcal{H} = [n]$ .

Information-theoretic MAC (IT-MAC). We use a multi-party variant of the informationtheoretic message authentication code originally used by Nielsen et al. [NNOB12]. We follow the description from Wang et al. [WRK17]. Each player holds a global key  $\Delta_i$ . To allow the player  $P_i$  to hold a MAC tag for the value *b* towards player  $P_j$ , we give a  $\kappa$ -bit long random key  $\mathsf{K}_j[b]$ to  $P_j$  and give  $\mathsf{M}_j[b] := \mathsf{K}_j[b] \oplus b\Delta_j$  to player  $P_i$ . We also allow a player  $P_i$  to authenticate a single value *x* towards all other players: for each  $j \in [n], j \neq i$ , we give,  $P_j$  a random key  $\mathsf{K}_j[x]$ and give  $\mathsf{M}_j[b] := \mathsf{K}_j[b] \oplus b\Delta_j$  to  $P_i$ . This is equivalent to authenticating the same bit to all other parties. (We use  $\mathcal{F}^n_{\mathsf{aBit}}$  to model this as an ideal functionality and discuss an efficient instantiation in Section 6.1.)

We will use  $[x]^i$  to denote a multi-party IT-MAC for a bit x held by  $P_i$ .  $[x]^i$  therefore means  $(x, \{\mathsf{M}_k[x]\}_{k\neq i})$  for  $P_i$ , and  $[x]^i$  means  $\mathsf{K}_j[x]$  for  $P_j$  with  $j \neq i$ . Note that  $[x]^i$  is XOR-homomorphic: given two authenticated bits  $[x]^i, [y]^i$ , it is possible to generate an authenticated bit  $[z]^i$  whose value is the XOR of the two authenticated bits by doing the following:

1.  $z := x \oplus y$ 2.  $\mathsf{K}_j[z] := \mathsf{K}_j[x] \oplus \mathsf{K}_j[y], \forall j \neq i$ 3.  $\mathsf{M}_j[z] := \mathsf{M}_j[x] \oplus \mathsf{M}_j[y], \forall j \neq i$ 

It is also possible to negate  $[x]^i$  resulting in  $[y]^i$ :

1. 
$$y := x \oplus 1$$
  
2.  $\mathsf{K}_j[y] := \mathsf{K}_j[x] \oplus \Delta_j, \forall j \neq i$   
3.  $\mathsf{M}_j[y] := \mathsf{M}_j[x], \forall j \neq i$ 

In the above construction, x is known to one party. To generate a distributed authenticated bit x, where the value is not known to any party, we generate shares for x, namely  $\bigoplus_i x^i = x$ . For each  $x^i$ , parties also obtain  $[x^i]^i$ , that is, multi-party MACs on  $x^i$  with  $P_i$  holding  $x^i$ . We also use  $[x]^i$  to denote  $[x^i]^i$  as a simplified notation when it is not ambiguous. It is easy to see that such distributed authenticated bit is also XOR-homomorphic.

Note that, we use the notation  $[x]^i$  to denote an multi-party authenticated bit  $x^i$  where the global key are  $\Delta$ 's. In the case where global keys are some G's, we explicitly add a subscript to the representation:  $[x]^i_G$  denotes an authenticated bit  $x^i$  under global keys G's. Similar, when the global key is some  $G_i$ , we then use  $M_i[x]_{G_i}$ ,  $K_i[x]_{G_i}$  to represent the MAC and keys. That is  $M_i[x]_{G_i} = K_i[x]_{G_i} \oplus xG_i$ .

**Related functionalities.** The MPC functionality that our main protocol instantiates is shown in Figure 1. We focus on a simplified version where only  $P_1$  gets the output. Our main protocol works in the  $\mathcal{F}_{\mathsf{Pre}}$ -hybrid model. The detailed ideal functionality  $\mathcal{F}_{\mathsf{Pre}}$  is shown in Figure 2. From a high level view,  $\mathcal{F}_{\mathsf{Pre}}$  generates multi-party IT-MAC on some value x, y, z such that  $z = x \wedge y$ . In the later section, we also refer to this set of multi-party IT-MACs as a AND triple.

#### Functionality $\mathcal{F}_{mpc}$

**Private inputs:**  $P_i$  has input  $x^i \in \{0, 1\}^{n_i}$ .

1. Upon receiving (input,  $x^i$ ) from  $P_i$ , store the message  $(i, x^i)$  if no message of the form  $(i, \cdot)$  is present in memory. If  $(i, x^i)$  is present in memory for all  $i \in [n]$ , the box computes  $z := f(x_1, ..., x_n)$  and sends z to  $P_1$ .

### Figure 1: Functionality $\mathcal{F}_{mpc}$ for multi-party computation.

### Functionality $\mathcal{F}_{\mathsf{Pre}}$

- 1. Upon receiving init from all  $P_i$ 's, sample  $\{\Delta_i \in \{0,1\}^\kappa\}_{i \in [n]}$  and send  $\Delta_i$  to  $P_i$ . Corrupted parties can choose their own  $\Delta_i$ .
- 2. Upon receiving random from all  $P_i$ , sample a random bit r and a random multi-party IT-MAC, namely  $\{(r_i, \{\mathsf{M}_j[r_i], \mathsf{K}_j[r_i]\}_{j \neq i})\}_{i \in [n]}$ . The box sends  $(r_i, \{\mathsf{M}_j[r_i], \mathsf{K}_i[r_j]\}_{j \neq i})$  to  $P_i$ . Corrupted parties can choose their own randomness.
- 3. Upon receiving (AND,  $(r_i, \{M_j[r_i], K_i[r_j]\}_{j \neq i}), (s_i, \{M_j[s_i], K_i[s_j]\}_{j \neq i})$  from  $P_i$ , the box checks that each IT-MAC is valid, picks random  $\{t_i\}_{i \in [n]}$ , such that  $\bigoplus_{i \in [n]} t_i = (\bigoplus_{i \in [n]} r_i) \land (\bigoplus_{i \in [n]} s_i)$  and random IT-MACs  $\{(t_i, \{M_j[t_i], K_j[t_i]\}_{j \neq i})\}_{i \in [n]}$  on them, and sends  $(r_i, \{M_j[r_i], K_i[r_j]\}_{j \neq i})$  to  $P_i$ . Corrupted party gets to choose its own randomness.

Figure 2: The multi-party preprocessing Functionality.

## **3** Protocol Intuition

Our main protocol can be viewed as a (non-trivial) extension of a recent work by Wang et al. that proposed an authenticated garbling protocol for maliciously-secure two-party computation. From a high-level view, their protocol constructs shares of a garbled table where permutation bits are authenticated in the following way.

$x\oplus\lambda_lpha$	$y\oplus\lambda_eta$	$P_2$ 's share of Garbled Table	$P_1$ 's share of Garbled Table
0	0	$H(L_{lpha,0},L_{eta,0},\gamma,00)\oplus(r_{00}^2,M_1[r_{00}^2],R_{00}\oplusL_{\gamma,ar{z}_{00}})$	$(r_{00}^1 = \bar{z}_{00} \oplus r_{00}^2, K_1[r_{00}^2], R_{00})$
0	1	$H(L_{lpha,0},L_{eta,1},\gamma,01)\oplus(r_{01}^2,M_1[r_{01}^2],R_{01}\oplusL_{\gamma,ar{z}_{01}})$	$(r_{01}^1 = \bar{z}_{01} \oplus r_{01}^2, K_1[r_{10}^2], R_{01})$
1	0	$H(L_{\alpha,1},L_{\beta,0},\gamma,10)\oplus(r_{10}^2,M_1[r_{10}^2],R_{10}\oplusL_{\gamma,\bar{z}_{10}})$	$(r_{10}^1 = \bar{z}_{10} \oplus r_{10}^2, K_1[r_{01}^2], R_{10})$
1	1	$H(L_{\alpha,1},L_{\beta,1},\gamma,11)\oplus(r_{11}^2,M_1[r_{11}^2],R_{11}\oplusL_{\gamma,\bar{z}_{11}})$	$(r_{11}^1 = \bar{z}_{11} \oplus r_{11}^2, K_1[r_{11}^2], R_{11})$

With an appropriate choice of the preprocessing functionality, each row of the garbled table can easily be computed as follows.

$x\oplus\lambda_lpha$	$y\oplus\lambda_eta$	$P_1$ 's share of Garbled Table	$P_2$ 's share of Garbled Table
0	0	$H(L_{\alpha,0},L_{\beta,0},\gamma,00)\oplus(r_{00},M[r_{00}],L_{\gamma,0}\oplus r_{00}\Delta_{1}\oplusK[s_{00}])$	$(s_{00} = \bar{z}_{00} \oplus r_{00}, K[r_{00}], M[s_{00}])$
0	1	$H(L_{\alpha,0},L_{\beta,1},\gamma,01)\oplus(r_{01},M[r_{01}],L_{\gamma,0}\oplus r_{01}\Delta_1\oplusK[s_{01}])$	$(s_{01} = \bar{z}_{01} \oplus r_{01}, K[r_{01}], M[s_{01}])$
1	0	$H(L_{\alpha,1},L_{\beta,0},\gamma,10)\oplus(r_{10},M[r_{10}],L_{\gamma,0}\oplus r_{10}\Delta_1\oplusK[s_{10}])$	$(s_{10} = \bar{z}_{10} \oplus r_{10}, K[r_{10}], M[s_{10}])$
1	1	$H(L_{\alpha,1},L_{\beta,1},\gamma,11)\oplus(r_{11},M[r_{11}],L_{\gamma,0}\oplus r_{11}\Delta_1\oplusK[s_{11}])$	$(s_{11} = \bar{z}_{11} \oplus r_{11}, K[r_{11}], M[s_{11}])$

Our main goal is to generalize these ideas to n > 2 parties where n - 1 parties jointly garble and then let the excluded party evaluate the garbled circuit. Since up to n - 1 parties can be malicious, the garbled circuit and associated permutation bits need to be shared among all parties such that no subset of the parties can recover the garbled circuit. Similar to the original 2PC protocol, permutation bits also need to be authenticated.

In the following example, we will restrict ourselves to the three-party setting. The first step is to extend the garbled table without considering how to construct the authenticated garbling.

$P_3$ 's share of Garbled Table	$P_2$ 's share of Garbled Table
$ \begin{array}{l} H(L^{3}_{\alpha,0},L^{3}_{\beta,0},\gamma,00)\oplus(r^{3}_{00},M_{1}[r^{3}_{00}],R^{2}_{00}\oplus R^{1}_{00}\oplusL^{3}_{\gamma,\bar{z}_{00}},S^{3}_{00})\\ H(L^{3}_{\alpha,0},L^{3}_{\beta,1},\gamma,01)\oplus(r^{3}_{01},M_{1}[r^{3}_{01}],R^{2}_{01}\oplus R^{1}_{01}\oplusL^{3}_{\gamma,\bar{z}_{01}},S^{3}_{01})\\ H(L^{3}_{\alpha,1},L^{3}_{\beta,0},\gamma,10)\oplus(r^{3}_{10},M_{1}[r^{3}_{10}],R^{2}_{10}\oplus R^{1}_{10}\oplusL^{3}_{\gamma,\bar{z}_{10}},S^{3}_{10})\\ H(L^{3}_{\alpha,1},L^{3}_{\beta,1},\gamma,11)\oplus(r^{3}_{11},M_{1}[r^{3}_{11}],R^{2}_{11}\oplus R^{1}_{11}\oplusL^{3}_{\gamma,\bar{z}_{11}},S^{3}_{11}) \end{array}$	$ \begin{split} & H(L^2_{\alpha,0},L^2_{\beta,0},\gamma,00)\oplus(r^2_{00},M_1[r^2_{00}],S^3_{00}\oplus S^1_{00}\oplusL^2_{\gamma,\bar{z}_{00}},R^2_{00}) \\ & H(L^2_{\alpha,0},L^2_{\beta,1},\gamma,01)\oplus(r^2_{01},M_1[r^2_{01}],S^3_{01}\oplus S^1_{01}\oplusL^2_{\gamma,\bar{z}_{01}},R^2_{01}) \\ & H(L^2_{\alpha,1},L^2_{\beta,0},\gamma,10)\oplus(r^2_{10},M_1[r^2_{10}],S^3_{10}\oplus S^1_{10}\oplusL^2_{\gamma,\bar{z}_{10}},R^2_{10}) \\ & H(L^2_{\alpha,1},L^2_{\beta,1},\gamma,11)\oplus(r^2_{11},M_1[r^2_{11}],S^3_{11}\oplus S^1_{11}\oplusL^2_{\gamma,\bar{z}_{11}},R^2_{11}) \end{split} $
$ \begin{array}{c} \hline P_{1}\text{'s share of Garbled Table} \\ \hline \\ \hline (r_{00}^{1} = \bar{z}_{00} \oplus r_{00}^{2} \oplus r_{00}^{2}, K_{1}[r_{00}^{3}], K_{1}[r_{00}^{2}], R_{00}^{1}, S_{00}^{1}) \\ (r_{01}^{1} = \bar{z}_{01} \oplus r_{01}^{3} \oplus r_{01}^{2}, K_{1}[r_{01}^{3}], K_{1}[r_{01}^{2}], R_{01}^{1}, S_{01}^{1}) \\ (r_{10}^{1} = \bar{z}_{10} \oplus r_{10}^{3} \oplus r_{10}^{2}, K_{1}[r_{10}^{3}], K_{1}[r_{10}^{2}], R_{10}^{1}, S_{10}^{1}) \\ (r_{11}^{1} = \bar{z}_{11} \oplus r_{11}^{3} \oplus r_{11}^{2}, K_{1}[r_{11}^{3}], K_{1}[r_{11}^{2}], R_{11}^{1}, S_{11}^{1}) \\ \end{array}$	

In the above example,  $r_{uv}^i$ 's are random bits while  $R_{uv}^i, S_{uv}^i$  are random  $\kappa$ -bit strings. As can be noticed, there are two sets of garbled labels used by  $P_2$  and  $P_3$  respectively. Furthermore, both of these sets are shared among the three parties such that the garbled circuit remains private even when the adversary corrupts all-but-one parties. The last ingredient that we need is a protocol for constructing these "shared and permuted garbled labels" distributively. Observe that

$$\begin{split} \mathsf{L}^{3}_{\gamma,\bar{z}_{00}} &= \mathsf{L}^{3}_{\gamma,0} \oplus \bar{z}_{00} \Delta_{3} \\ &= \mathsf{L}^{3}_{\gamma,0} \oplus (r^{1}_{00} \oplus r^{2}_{00} \oplus r^{3}_{00}) \Delta_{3} \\ &= (\mathsf{L}^{3}_{\gamma,0} \oplus r^{3}_{00} \Delta_{3} \oplus \mathsf{K}_{3}[r^{1}_{00}] \oplus \mathsf{K}_{3}[r^{2}_{00}]) \oplus (\mathsf{K}_{3}[r^{1}_{00}] \oplus r^{1}_{00} \Delta_{3}) \oplus (\mathsf{K}_{3}[r^{2}_{00}] \oplus r^{2}_{00} \Delta_{3}) \\ &= (\mathsf{L}^{3}_{\gamma,0} \oplus r^{3}_{00} \Delta_{3} \oplus \mathsf{K}_{3}[r^{1}_{00}] \oplus \mathsf{K}_{3}[r^{2}_{00}]) \oplus \mathsf{M}_{3}[r^{1}_{00}] \oplus \mathsf{M}_{3}[r^{2}_{00}] \end{split}$$

Applying this to the construction above, with the  $\mathcal{F}_{\mathsf{Pre}}$  functionality described in Section 2:

$P_3$ 's share of Garbled Table		
$ \begin{split} & H(L^{3}_{\alpha,0},L^{3}_{\beta,0},\gamma,00) \oplus (r^{3}_{00},M_{1}[r^{3}_{00}],L^{3}_{\gamma,0} \oplus r^{3}_{00}\Delta_{3} \oplus K_{3}[r^{1}_{00}] \oplus K_{3}[r^{2}_{00}],M_{2}[r^{3}_{00}]) \\ & H(L^{3}_{\alpha,0},L^{3}_{\beta,1},\gamma,01) \oplus (r^{3}_{01},M_{1}[r^{3}_{01}],L^{3}_{\gamma,0} \oplus r^{3}_{10}\Delta_{3} \oplus K_{3}[r^{1}_{10}] \oplus K_{3}[r^{2}_{10}],M_{2}[r^{3}_{01}]) \\ & H(L^{3}_{\alpha,1},L^{3}_{\beta,0},\gamma,10) \oplus (r^{3}_{10},M_{1}[r^{3}_{10}],L^{3}_{\gamma,0} \oplus r^{3}_{01}\Delta_{3} \oplus K_{3}[r^{1}_{01}] \oplus K_{3}[r^{2}_{01}],M_{2}[r^{3}_{10}]) \\ & H(L^{3}_{\alpha,1},L^{3}_{\beta,1},\gamma,11) \oplus (r^{3}_{11},M_{1}[r^{3}_{11}],L^{3}_{\gamma,0} \oplus r^{3}_{11}\Delta_{3} \oplus K_{3}[r^{1}_{11}] \oplus K_{3}[r^{2}_{11}],M_{2}[r^{3}_{11}]) \end{split} $		
$\begin{split} & P_2 \text{'s share of Garbled Table} \\ & H(L^2_{\alpha,0},L^2_{\beta,0},\gamma,00) \oplus (r^2_{00},M_1[r^2_{00}],L^2_{\gamma,0}\oplus r^2_{00}\Delta_2 \oplus K_2[r^1_{00}] \oplus K_2[r^3_{00}],M_3[r^2_{00}]) \\ & H(L^2_{\alpha,0},L^2_{\beta,1},\gamma,01) \oplus (r^2_{01},M_1[r^2_{01}],L^2_{\gamma,0}\oplus r^2_{10}\Delta_2 \oplus K_2[r^1_{10}] \oplus K_2[r^3_{10}],M_3[r^2_{01}]) \\ & H(L^2_{\alpha,1},L^2_{\beta,0},\gamma,10) \oplus (r^2_{10},M_1[r^2_{10}],L^2_{\gamma,0}\oplus r^2_{01}\Delta_2 \oplus K_2[r^1_{01}] \oplus K_2[r^3_{01}],M_3[r^2_{10}]) \\ & H(L^2_{\alpha,1},L^2_{\beta,1},\gamma,11) \oplus (r^2_{11},M_1[r^2_{11}],L^2_{\gamma,0}\oplus r^2_{11}\Delta_2 \oplus K_2[r^1_{11}] \oplus K_2[r^3_{11}],M_3[r^2_{11}]) \end{split}$		
$P_1$ 's share of Garbled Table		
$ \begin{split} & (r_{00}^1 = \bar{z}_{00} \oplus r_{00}^3 \oplus r_{00}^2, K_1[r_{00}^3], K_1[r_{00}^2], M_3[r_{00}^1], M_2[r_{00}^1]) \\ & (r_{01}^1 = \bar{z}_{01} \oplus r_{01}^3 \oplus r_{01}^2, K_1[r_{01}^3], K_1[r_{01}^2], M_3[r_{01}^1], M_2[r_{01}^1]) \\ & (r_{10}^1 = \bar{z}_{10} \oplus r_{10}^3 \oplus r_{10}^2, K_1[r_{10}^3], K_1[r_{10}^2], M_3[r_{11}^1], M_2[r_{10}^1]) \\ & (r_{11}^1 = \bar{z}_{11} \oplus r_{11}^3 \oplus r_{11}^2, K_1[r_{11}^3], K_1[r_{11}^2], M_3[r_{11}^1], M_2[r_{11}^1]) \end{split} $		

## 4 The Main Scheme

In Figure 3 and Figure 4, we present the complete MPC protocol in the  $\mathcal{F}_{\mathsf{Pre}}$ -hybrid model. In Section 6, we will introduce an efficient instantiation of  $\mathcal{F}_{\mathsf{Pre}}$ , which extends two-party TinyOT protocol.

## 5 Proof

**Theorem 5.1.** The protocol in Figure 3 and Figure 4, where H is modeled as a random oracle, securely instantiates  $\mathcal{F}_{mpc}$  in the  $\mathcal{F}_{Pre}$ -hybrid model with security  $negl(\kappa)$  against an adversary corrupting up to n-1 parties.

*Proof.* We will consider separately the case where  $P_1 \in \mathcal{H}$  and the case where  $P_1 \in \mathcal{M}$  and  $P_2 \in \mathcal{H}$ . The case when  $P_1 \in \mathcal{M}$  and  $P_i \in \mathcal{H}$  for some  $i \geq 3$  is similar to the second case. This covers all cases.

**Honest**  $P_1$ . Let  $\mathcal{A}$  be an adversary corrupting  $\{P_i\}_{i \in \mathcal{M}}$ . We construct a simulator  $\mathcal{S}$  that runs  $\mathcal{A}$  as a subroutine and plays the role of  $\{P_i\}_{i \in \mathcal{M}}$  in the ideal world involving an ideal functionality  $\mathcal{F}_{mpc}$  evaluating f.  $\mathcal{S}$  is defined as follows.

- 1-4 S acts as honest  $\{P_i\}_{i \in \mathcal{H}}$  and plays the functionality of  $\mathcal{F}_{\mathsf{Pre}}$ , recording all outputs. If any honest party or  $\mathcal{F}_{\mathsf{Pre}}$  would abort, S outputs whatever  $\mathcal{A}$  outputs and then aborts.
  - 5 S interacts with A acting as an honest  $\{P_i\}_{i\in\mathcal{H}}$ , using input  $\{x^i := 0\}^{i\in\mathcal{H}}$ . For each  $i\in\mathcal{M}, w\in\mathcal{I}_i, S$  receives  $\hat{x}^i_w$  and computes  $x^i_w := \hat{x}^i_w \oplus \bigoplus_{i\in[n]} r^i_w$ . If any honest party would abort, S outputs whatever A outputs and aborts.
  - 6 S interacts with A acting as honest  $\{P_i\}_{i \in \mathcal{H}}$ , using input  $x^1 := 0$ .
- 7-8 S interacts with A acting as honest  $\{P_i\}_{i \in \mathcal{H}}$ . If an honest  $P_1$  would abort, S outputs whatever A outputs and aborts; otherwise for each  $i \in \mathcal{M}$ , S sends (input,  $x^i$ ) on behalf of  $P_i$  to  $\mathcal{F}_{mpc}$ .

We now show that the joint distribution over the outputs of  $\mathcal{A}$  and the honest parties in the real world is indistinguishable from the joint distribution over the outputs of  $\mathcal{S}$  and the parties in the ideal world.

- **Hybrid**<sub>1</sub>. Same as the hybrid-world protocol, where S plays the role of honest  $\{P_i\}_{i \in \mathcal{H}}$ , using the actual inputs  $\{x^i\}^{i \in \mathcal{H}}$ .
- **Hybrid**<sub>2</sub>. Same as **Hybrid**<sub>1</sub>, except that in step 5, for each  $i \in \mathcal{M}, w \in \mathcal{I}_i, \mathcal{S}$  receives  $\hat{x}_w^i$  and computes  $x_w^i := \hat{x}_w^i \oplus \bigoplus_{i \in [n]} r_w^i$ . If any honest party would abort,  $\mathcal{S}$  outputs whatever  $\mathcal{A}$  outputs; otherwise for each  $i \in \mathcal{M}, \mathcal{S}$  sends (input,  $x^i$ ) on behalf of  $P_i$  to  $\mathcal{F}_{mpc}$ .

The views produced by the two Hybrids are exactly the same. According to Lemma 5.1,  $P_1$  will learn the same output in both Hybrids with all but negligible probability.

**Hybrid**<sub>3</sub>. Same as **Hybrid**<sub>2</sub>, except that, for each  $i \in \mathcal{H}$ ,  $\mathcal{S}$  computes  $\{r_w^i\}_{w \in \mathcal{I}_i}$  as follows:  $\mathcal{S}$  first randomly pick  $\{u_w^i\}_{w \in \mathcal{I}_i}$ , and then computes  $r_w^i := u_w^i \oplus x_w^i$ .

The two Hybrids produce exactly the same view.

#### $\mathbf{Protocol} \ \Pi_{\mathsf{mpc}}$

**Inputs:** In the function-independent phase, parties know  $|\mathcal{C}|$  and  $|\mathcal{I}|$ ; in the function-dependent phase, parties get a circuit representing function  $f : \{0,1\}^{|\mathcal{I}_1|} \times ... \times \{0,1\}^{|\mathcal{I}_n|} \to \{0,1\}^{|\mathcal{O}|}$ ; in the input-processing phase,  $P_i$  holds  $x_i \in \{0,1\}^{|\mathcal{I}_i|}$ .

#### Function-independent phase:

- 1.  $P_i$  sends init to  $\mathcal{F}_{\mathsf{Pre}}$ , which sends  $\Delta_i$  to  $P_i$ .
- 2. For each wire  $w \in \mathcal{I} \cup \mathcal{W}, i \in [n], P_i$  sends random to  $\mathcal{F}_{\mathsf{Pre}}$ , which sends  $\left(r_w^i, \left\{\mathsf{M}_j[r_w^i], \mathsf{K}_i[r_w^j]\right\}_{j \neq i}\right)$  to  $P_i$ , where  $\bigoplus_{i \in [n]} r_w^i = \lambda_w$ . For each  $i \neq 1, P_i$  also picks a random  $\kappa$ -bit string  $\mathsf{L}_{w,0}^i$ .

### Function-dependent phase:

3. For each gate  $\mathcal{G} = (\alpha, \beta, \gamma, \oplus)$ , each  $i \in [n]$ ,  $P_i$  computes  $\left(r_{\gamma}^i, \left\{\mathsf{M}_j[r_{\gamma}^i], \mathsf{K}_i[r_{\gamma}^j]\right\}_{i \neq i}\right) :=$  $\left(r_{\alpha}^{i}\oplus r_{\beta}^{i}, \left\{\mathsf{M}_{j}[r_{\alpha}^{i}]\oplus\mathsf{M}_{j}[r_{\beta}^{i}], \mathsf{K}_{i}[r_{\alpha}^{j}]\oplus\mathsf{K}_{i}[r_{\beta}^{j}]\right\}_{i\neq i}\right). \text{ For each } i\neq 1, P_{i} \text{ also computes } \mathsf{L}_{\gamma,0}^{i}:=\mathsf{L}_{\alpha,0}^{i}\oplus\mathsf{L}_{\beta,0}^{i}.$ 4. For each gate  $\mathcal{G} = (\alpha, \beta, \gamma, \wedge)$ : (a) For each  $i \in [n]$ ,  $P_i$  sends  $\left( \operatorname{and}, \left( r_{\alpha}^i, \left\{ \mathsf{M}_j[r_{\alpha}^i], \mathsf{K}_i[r_{\alpha}^j] \right\}_{j \neq i} \right), \left( r_{\beta}^i, \left\{ \mathsf{M}_j[r_{\beta}^i], \mathsf{K}_i[r_{\beta}^j] \right\}_{i \neq i} \right) \right)$  to  $\mathcal{F}_{\mathsf{Pre}}$ , which sends  $\left(r_{\sigma}^{i}, \left\{\mathsf{M}_{j}[r_{\sigma}^{i}], \mathsf{K}_{i}[r_{\sigma}^{j}]\right\}_{j \neq i}\right)$  to  $P_{i}$ , where  $\bigoplus_{i \in [n]} r_{\sigma}^{i} = \left(\bigoplus_{i \in [n]} r_{\alpha}^{i}\right) \wedge \left(\bigoplus_{i \in [n]} r_{\beta}^{i}\right)$ . (b) For each  $i \neq 1$ ,  $P_i$  computes the following locally.  $\begin{pmatrix} r_{\gamma,0}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,0}^{i}], \mathsf{K}_{i}[r_{\gamma,0}^{j}]\right\}_{j\neq i} \end{pmatrix} := \begin{pmatrix} r_{\sigma}^{i} \oplus r_{\gamma}^{i}, \left\{\mathsf{M}_{j}[r_{\sigma}^{i}] \oplus \mathsf{M}_{j}[r_{\gamma}^{i}], \mathsf{K}_{i}[r_{\sigma}^{j}] \oplus \mathsf{K}_{i}[r_{\gamma}^{j}]\right\}_{j\neq i} \end{pmatrix} \\ \begin{pmatrix} r_{\gamma,1}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,1}^{i}], \mathsf{K}_{i}[r_{\gamma,1}^{j}]\right\}_{j\neq i} \end{pmatrix} := \begin{pmatrix} r_{\gamma,0}^{i} \oplus r_{\alpha}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,0}^{i}] \oplus \mathsf{M}_{j}[r_{\alpha}^{i}], \mathsf{K}_{i}[r_{\gamma,0}^{j}] \oplus \mathsf{K}_{i}[r_{\alpha}^{j}]\right\}_{j\neq i} \end{pmatrix} \\ \begin{pmatrix} r_{\gamma,2}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,2}^{i}], \mathsf{K}_{i}[r_{\gamma,2}^{j}]\right\}_{j\neq i} \end{pmatrix} := \begin{pmatrix} r_{\gamma,0}^{i} \oplus r_{\beta}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,0}^{i}] \oplus \mathsf{M}_{j}[r_{\beta}^{i}], \mathsf{K}_{i}[r_{\gamma,0}^{j}] \oplus \mathsf{K}_{i}[r_{\beta}^{j}]\right\}_{j\neq i} \end{pmatrix} \\ \end{pmatrix}$  $\left(r_{\gamma,3}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,3}^{i}], \mathsf{K}_{i}[r_{\gamma,3}^{j}]\right\}_{j\neq i}\right) := \left(r_{\gamma,1}^{i} \oplus r_{\beta}^{i}, \left\{\mathsf{M}_{1}[r_{\gamma,1}^{i}] \oplus \mathsf{M}_{1}[r_{\beta}^{i}], \quad \mathsf{K}_{i}[r_{\gamma,1}^{1}] \oplus \mathsf{K}_{i}[r_{\beta}^{1}] \oplus \Delta_{i}\right\}\right)$  $\bigcup_{i=1}^{\mathsf{C}} \left\{ \mathsf{M}_{j}[r_{\gamma,1}^{i}] \oplus \mathsf{M}_{j}[r_{\beta}^{i}], \mathsf{K}_{i}[r_{\gamma,1}^{j}] \oplus \mathsf{K}_{i}[r_{\beta}^{j}] \right\}_{i \neq i} \prod_{j=1}^{\mathsf{C}} \left\{ \mathsf{M}_{j}[r_{\beta}^{j}] \right\}_{i \neq j} \left\{ \mathsf{M}$ (c)  $P_1$  computes the following locally.  $\begin{pmatrix} r_{\gamma,0}^{1} \{\mathsf{M}_{j}[r_{\gamma,0}^{1}],\mathsf{K}_{1}[r_{\gamma,0}^{j}]\}_{j\neq i} \end{pmatrix} := \begin{pmatrix} r_{\sigma}^{1} \oplus r_{\gamma}^{1}, & \left\{\mathsf{M}_{j}[r_{\sigma}^{1}] \oplus \mathsf{M}_{j}[r_{\gamma}^{1}], & \mathsf{K}_{1}[r_{\sigma}^{j}] \oplus \mathsf{K}_{1}[r_{\gamma}^{j}] \right\}_{j\neq i} \end{pmatrix} \\ \begin{pmatrix} r_{\gamma,1}^{1}, \left\{\mathsf{M}_{j}[r_{\gamma,1}^{1}],\mathsf{K}_{1}[r_{\gamma,1}^{j}]\right\}_{j\neq i} \end{pmatrix} := \begin{pmatrix} r_{\gamma,0}^{1} \oplus r_{\alpha}^{1}, & \left\{\mathsf{M}_{j}[r_{\gamma,0}^{1}] \oplus \mathsf{M}_{j}[r_{\alpha}^{1}], & \mathsf{K}_{1}[r_{\gamma,0}^{j}] \oplus \mathsf{K}_{1}[r_{\alpha}^{j}] \right\}_{j\neq i} \end{pmatrix} \\ \begin{pmatrix} r_{\gamma,2}^{1}, \left\{\mathsf{M}_{j}[r_{\gamma,2}^{1}],\mathsf{K}_{1}[r_{\gamma,2}^{j}]\right\}_{j\neq i} \end{pmatrix} := \begin{pmatrix} r_{\gamma,0}^{1} \oplus r_{\beta}^{1}, & \left\{\mathsf{M}_{j}[r_{\gamma,0}^{1}] \oplus \mathsf{M}_{j}[r_{\beta}^{1}], & \mathsf{K}_{1}[r_{\gamma,0}^{j}] \oplus \mathsf{K}_{1}[r_{\beta}^{j}] \right\}_{j\neq i} \end{pmatrix} \\ \end{pmatrix}$  $\left(r_{\gamma,3}^{1},\left\{\mathsf{M}_{j}[r_{\gamma,3}^{1}],\mathsf{K}_{1}[r_{\gamma,3}^{j}]\right\}_{i\neq i}^{j}\right):=\left(r_{\gamma,1}^{1}\oplus r_{\beta}^{1}\oplus 1,\left\{\mathsf{M}_{j}[r_{\gamma,1}^{1}]\oplus\mathsf{M}_{j}[r_{\beta}^{1}],\mathsf{K}_{1}[r_{\gamma,1}^{j}]\oplus\mathsf{K}_{1}[r_{\beta}^{j}]\right\}_{i\neq i}^{j}\right)$ (d) For each  $i \neq 1$ ,  $P_i$  computes  $\mathsf{L}^i_{\alpha,1} := \mathsf{L}^i_{\alpha,0} \oplus \Delta_i$  and  $\mathsf{L}^i_{\beta,1} := \mathsf{L}^i_{\beta,0} \oplus \Delta_i$ , and sends the following to  $P_1$ .  $G_{\gamma,0}^{i} := H\left(\mathsf{L}_{\alpha,0}^{i},\mathsf{L}_{\beta,0}^{i},\gamma,0\right) \oplus \left(r_{\gamma,0}^{i},\left\{\mathsf{M}_{j}[r_{\gamma,0}^{i}]\right\}_{j\neq i},\mathsf{L}_{\gamma,0}^{i} \oplus \left(\bigoplus_{j\neq i}\mathsf{K}_{i}[r_{\gamma,0}^{j}]\right) \oplus r_{\gamma,0}^{i}\Delta_{i}\right)$  $G_{\gamma,1}^{i} := H\left(\mathsf{L}_{\alpha,0}^{i}, \mathsf{L}_{\beta,1}^{i}, \gamma, 1\right) \oplus \left(r_{\gamma,1}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,1}^{i}]\right\}_{j \neq i}, \mathsf{L}_{\gamma,0}^{i} \oplus \left(\bigoplus_{j \neq i} \mathsf{K}_{i}[r_{\gamma,1}^{j}]\right) \oplus r_{\gamma,1}^{i}\Delta_{i}\right)$  $G_{\gamma,2}^{i} := H\left(\mathsf{L}_{\alpha,1}^{i}, \mathsf{L}_{\beta,0}^{i}, \gamma, 2\right) \oplus \left(r_{\gamma,2}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,2}^{i}]\right\}_{i\neq i}, \mathsf{L}_{\gamma,0}^{i} \oplus \left(\bigoplus_{j\neq i}\mathsf{K}_{i}[r_{\gamma,2}^{j}]\right) \oplus r_{\gamma,2}^{i}\Delta_{i}\right)$  $G_{\gamma,3}^{i} := H\left(\mathsf{L}_{\alpha,1}^{i}, \mathsf{L}_{\beta,1}^{i}, \gamma, 3\right) \oplus \left(r_{\gamma,3}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,3}^{i}]\right\}_{i \neq i}, \mathsf{L}_{\gamma,0}^{i} \oplus \left(\bigoplus_{j \neq i} \mathsf{K}_{i}[r_{\gamma,3}^{j}]\right) \oplus r_{\gamma,3}^{i} \Delta_{i}\right)$ 

Figure 3: Our main protocol instantiating  $\mathcal{F}_{mpc}$ .

**Hybrid**<sub>4</sub>. Same as **Hybrid**<sub>3</sub>, except that S uses  $\{x^i = 0\}^{i \in \mathcal{H}}$  as input in step 5 and step 6. Note that although the distribution of  $\{x^i\}^{i \in \mathcal{H}}$  in **Hybrid**<sub>3</sub> and **Hybrid**<sub>4</sub> are different, the

#### **Protocol** $\Pi_{mpc}$ , continued

#### Input Processing:

- 5. For each  $i \neq 1, w \in \mathcal{I}_i$ , for each  $j \neq i, P_j$  sends  $(r_w^j, \mathsf{M}_i[r_w^j])$  to  $P_i$ , who checks that  $(r_w^j, \mathsf{M}_i[r_w^j], \mathsf{K}_i[r_w^j])$  is valid, and computes  $x_w^i \oplus \lambda_w := x_w^i \left(\bigoplus_{i \in [n]} r_w^i\right)$ .  $P_i$  broadcasts the value  $x_w^i \oplus \lambda_w$ . For each  $j \neq 1, P_j$  sends  $\mathsf{L}_{x^i \oplus \lambda_w}^j$  to  $P_1$ .
- 6. For each  $w \in \mathcal{I}_1, i \neq 1$ ,  $P_i$  sends  $(r_w^i, \mathsf{M}_1[r_w^i])$  to  $P_1$ , who checks that  $(r_w^i, \mathsf{M}_1[r_w^i], \mathsf{K}_1[r_w^i])$  are valid, and computes  $x_w^1 \oplus \lambda_w := x_w^1 \oplus \left(\bigoplus_{i \in [n]} r_w^i\right)$ .  $P_1$  sends  $x_w^1 \oplus \lambda_w$  to  $P_i$ , who sends  $\mathsf{L}_{w,x_w^1 \oplus \lambda_w}^i$  to  $P_1$ .

### **Circuit Evaluation:**

7.  $P_1$  evaluates the circuit following the topological order. For each gate  $\mathcal{G} = (\alpha, \beta, \gamma, T)$ ,  $P_1$  holds  $\left(z_{\alpha} \oplus \lambda_{\alpha}, \left\{\mathsf{L}^{i}_{\alpha, z_{\alpha} \oplus \lambda_{\alpha}}\right\}_{i \neq 1}\right)$  and  $\left(z_{\beta} \oplus \lambda_{\beta}, \left\{\mathsf{L}^{i}_{\beta, z_{\beta} \oplus \lambda_{\beta}}\right\}_{i \neq 1}\right)$ , where  $z_{\alpha}, z_{\beta}$  are the underlying values of the wire.

(a) If 
$$T = \oplus$$
,  $P_1$  computes  $z_{\gamma} \oplus \lambda_{\gamma} := (z_{\alpha} \oplus \lambda_{\alpha}) \oplus (z_{\beta} \oplus \lambda_{\beta})$  and  $\left\{ \mathsf{L}^i_{\gamma, z_{\gamma} \oplus \lambda_{\gamma}} := \mathsf{L}^i_{\alpha, z_{\alpha} \oplus \lambda_{\alpha}} \oplus \mathsf{L}^i_{\beta, z_{\beta} \oplus \lambda_{\beta}} \right\}_{i \neq 1}$ 

(b) If  $T = \wedge$ ,  $P_1$  computes  $\ell := 2(z_\alpha \oplus \lambda_\alpha) + (z_\beta \oplus \lambda_\beta)$ . For  $i \neq 1$ ,  $P_1$  computes

$$\left(r_{\gamma,\ell}^{i}, \left\{\mathsf{M}_{j}[r_{\gamma,\ell}^{i}]\right\}_{j\neq i}, \mathsf{L}_{\gamma}^{i}\right) := G_{\gamma,\ell}^{i} \oplus H\left(\mathsf{L}_{\alpha,z_{\alpha}\oplus\lambda_{\alpha}}^{i}, \mathsf{L}_{\beta,z_{\beta}\oplus\lambda_{\beta}}^{i}, \gamma, \ell\right)$$

 $P_{1} \text{ checks that } \left\{ \left( r_{\gamma,\ell}^{i}, \mathsf{M}_{1}[r_{\gamma,\ell}^{i}], \mathsf{K}_{1}[r_{\gamma,\ell}^{i}] \right) \right\}_{i \neq 1} \text{ are valid and aborts if fails. } P_{1} \text{ computes } z_{\gamma} \oplus \lambda_{\gamma} := \bigoplus_{i \in [n]} r_{\gamma,\ell}^{i}, \text{ and } \left\{ \mathsf{L}_{\gamma,z_{\gamma} \oplus \lambda_{\gamma}}^{i} := \mathsf{L}_{\gamma}^{i} \oplus \left( \bigoplus_{j \neq i} \mathsf{M}_{i}[r_{\gamma,\ell}^{j}] \right) \right\}_{i \neq 1}$ 

### **Output Processing:**

8. For each  $w \in \mathcal{O}, i \neq 1$ ,  $P_i$  sends  $(r_w^i, \mathsf{M}_1[r_w^i])$  to  $P_1$ , who checks that  $(r_w^i, \mathsf{M}_1[r_w^i], \mathsf{K}_1[r_w^i])$  is valid.  $P_1$  computes  $z_w := (\lambda_w \oplus z_w) \oplus \left(\bigoplus_{i \in [n]} r_w^i\right)$ .

Figure 4: Our main protocol instantiating  $\mathcal{F}_{mpc}$ , continued.

distribution of  $\{x_w^i \oplus r_w^i\}^{i \in \mathcal{H}}$  are exactly the same. The views produced by the two Hybrids are therefore the same, we will show that  $P_1$  aborts with the same probability in both Hybrids.

Observe that the only place where  $P_1$ 's abort can possibly depends on  $\{x^i\}^{i \in \mathcal{H}}$  is in step 7(b). However, this abort depends on which row is selected to decrypt, that is the value of  $\lambda_{\alpha} \oplus z_{\alpha}$  and  $\lambda_{\beta} \oplus z_{\beta}$ , which are chosen independently random in both Hybrids.

As  $Hybrid_4$  is the ideal-world execution, this completes the proof when  $P_1$  is honest.

Malicious  $P_1$  and honest  $P_2$ . Let  $\mathcal{A}$  be an adversary corrupting  $\{P_i\}_{i \in \mathcal{M}}$ . We construct a simulator  $\mathcal{S}$  that runs  $\mathcal{A}$  as a subroutine and plays the role of  $\{P_i\}_{i \in \mathcal{M}}$  in the ideal world involving an ideal functionality  $\mathcal{F}_{mpc}$  evaluating f.  $\mathcal{S}$  is defined as follows.

- 1-4 S acts as honest  $\{P_i\}_{i \in \mathcal{H}}$  and plays the functionality of  $\mathcal{F}_{\mathsf{Pre}}$ , recording all outputs. If any honest party would abort, S output whatever  $\mathcal{A}$  outputs and aborts.
- 5-6 S interacts with A acting as honest  $\{P_i\}_{i \in \mathcal{H}}$ , using input  $\{x^i := 0\}^{i \in \mathcal{H}}$ . For each  $i \in \mathcal{M}, w \in \mathcal{I}_i$ , S receives  $\hat{x}^i_w$  and computes  $x^i_w := \hat{x}^i_w \oplus \bigoplus_{i \in [n]} r^i_w$ . If any honest party would abort, S output whatever A outputs and aborts.

8 For each  $i \in \mathcal{M}$ ,  $\mathcal{S}$  sends (input,  $x^i$ ) on behalf of  $P_i$  to  $\mathcal{F}_{mpc}$ . If  $\mathcal{F}_{mpc}$  abort,  $\mathcal{S}$  aborts, outputting whatever  $\mathcal{A}$  outputs. Otherwise, if  $\mathcal{S}$  receives z as the output,  $\mathcal{S}$  computes  $z' := f(y^1, ..., y^n)$ , where  $\{y^i := 0\}^{i \in \mathcal{H}}$ , and  $\{y^i := x^i\}^{i \in \mathcal{M}}$ . For each  $i \in \mathcal{H}, w \in \mathcal{O}$ , if  $z'_w = z_w$ ,  $\mathcal{S}$  sends  $(r^i_w, \mathsf{M}_1[r^i_w])$  on behalf of  $P_i$  to  $\mathcal{A}$ ; otherwise,  $\mathcal{S}$  sends  $(r^i_w \oplus 1, \mathsf{M}_1[r^i_w] \oplus \Delta_1)$ .

We now show that the joint distribution over the outputs of  $\mathcal{A}$  and honest parties in the real world is indistinguishable from the joint distribution over the outputs of  $\mathcal{S}$  and honest parties in the ideal world.

- **Hybrid**<sub>1</sub>. Same as the hybrid-world protocol, where S plays the role of honest  $\{P_i\}_{i \in \mathcal{H}}$  using the actual inputs  $\{x^i\}^{i \in \mathcal{H}}$ .
- **Hybrid**<sub>2</sub>. Same as **Hybrid**<sub>1</sub>, except that in step 5 and step 6, for each  $i \in \mathcal{M}, w \in \mathcal{I}_i, \mathcal{S}$  receives  $\hat{x}^i_w$  and computes  $x^i_w := \hat{x}^i_w \oplus \bigoplus_{i \in [n]} r^i_w$ . If any honest party would abort,  $\mathcal{S}$  outputs whatever  $\mathcal{A}$  outputs; otherwise for each  $i \in \mathcal{M}, \mathcal{S}$  sends (input,  $x^i$ ) on behalf of  $P_i$  to  $\mathcal{F}_{mpc}$ .

 $P_1$  does not have output; furthermore the view of  $\mathcal{A}$  does not change between the two Hybrids.

**Hybrid**<sub>3</sub>. Same as **Hybrid**<sub>2</sub>, except that in step 5 and step 6, S uses  $\{x^i := 0\}^{i \in \mathcal{H}}$  as input and in step 8, S computes z' as defined. For each  $w \in \mathcal{O}$ , if  $z'_w = z_w$ , S sends  $(r^i_w, \mathsf{M}_1[r^i_w])$ ; otherwise, S sends  $(r^i_w \oplus 1, \mathsf{M}_1[r^i_w] \oplus \Delta_1)$ .

 $\mathcal{A}$  has no knowledge of  $r_w^i$ , therefore  $r_w^i$  and  $r_w^i \oplus 1$  are indistinguishable.

Note that since S uses different values for x between the two Hybrids, we also need to show that the distribution of garbled rows opened by  $P_1$  are indistinguishable for the two Hybrids. According to Lemma 5.2,  $P_1$  is able to open only one garble rows in each garbled table  $G_{\gamma,i}$ . Therefore, given that  $\{\lambda_w\}_{w \in \mathcal{I}_1 \cup W}$  values are not known to  $P_1$ , masked values and garbled keys are indistinguishable between two Hybrids.

As  $Hybrid_3$  is the ideal-world execution, the proof is complete.

**Lemma 5.1.** Consider an  $\mathcal{A}$  corrupting parties  $\{P_i\}_{i \in \mathcal{M}}$  such that  $P_1 \in \mathcal{H}$ , and denote  $x_w^i := \hat{x}_w^i \oplus \bigoplus_{i=1}^n r_w^i$ , where  $\hat{x}_w$  is the value  $\mathcal{A}$  sent,  $r_w^i$  are the values from  $\mathcal{F}_{\mathsf{Pre}}$ . With probability all but negligible,  $P_1$  either aborts or learns  $z = f(x^1, ..., x^n)$ .

*Proof.* Define  $z_w^*$  as the correct wire values computed using x defined above and y,  $z_w$  as the actually wire values  $P_1$  holds in the evaluation.

We will first show that  $P_1$  learns  $\{z^w \oplus \lambda_w = z_w^* \oplus \lambda_w\}_{w \in \mathcal{O}}$  by induction on topology of the circuit.

**Base step:** It is obvious that  $\{z_w^* \oplus \lambda_w = z_w \oplus \lambda_w\}_{w \in \mathcal{I}_1 \cup \mathcal{I}_2}$ , unless  $\mathcal{A}$  is able to forge an IT-MAC. **Induction step:** Now we show that for a gate  $(\alpha, \beta, \gamma, T)$ , if  $P_1$  has  $\{z_w^* \oplus \lambda_w = z_w \oplus \lambda_w\}_{w \in \{\alpha, \beta\}}$ , then  $P_1$  also obtains  $z_{\gamma}^* \oplus \lambda_{\gamma} = z_{\gamma} \oplus \lambda_{\gamma}$ .

- $T = \oplus$ : It is true according to the following:  $z_{\gamma}^* \oplus \lambda_{\gamma} = (z_{\alpha}^* \oplus \lambda_{\alpha}) \oplus (z_{\beta}^* \oplus \lambda_{\beta}) = (z_{\alpha} \oplus \lambda_{\alpha}) \oplus (z_{\beta} \oplus \lambda_{\beta}) z_{\gamma} \oplus \lambda_{\gamma}$
- $T = \wedge$ : According to the protocol,  $P_1$  will open the garbled row defined by  $i := 2(z_\alpha \oplus \lambda_\alpha) + (z_\beta \oplus \lambda_\beta)$ . If  $P_1$  learns  $z_\gamma \oplus \lambda_\gamma \neq z_\gamma^* \oplus \lambda_\gamma$ , then it means that  $P_1$  learns  $r_{\gamma,i}^* \neq r_{\gamma,i}$ . However, this would mean that  $\mathcal{A}$  forge a valid IT-MAC, happening with negligible probability.

Now we know that  $P_1$  learns correct masked output.  $P_1$  can therefore learn correct output f(x, y) unless  $\mathcal{A}$  is able to flip  $\{r_w\}_{w \in \mathcal{O}}$ , which, again, happens with negligible probability.  $\Box$ 

**Lemma 5.2.** Consider an  $\mathcal{A}$  corrupting  $\{P_i\}_{i \in \mathcal{M}}$  and that  $P_1 \in \mathcal{M}$ , with negligible probability,  $P_1$  learns both garbled labels for some wire generated by an honest party.

*Proof.* The proof is very similar to the proof of semi-honest garbled circuit protocol by Lindell and Pinkas [LP09]. Let's use  $z_w^*$ 's to denote the correct value on all input wire and internal wires if x and y defined above are used to evaluate the circuit, and use  $z_w$  to denote the actual wire values when  $P_1$  is malicious.

We will show that  $z_w^* \oplus \lambda_w = z_w \oplus \lambda_w$ , and  $\mathsf{L}_{w, z_w^* \oplus \lambda_w} = \mathsf{L}_{w, z_w \oplus \lambda_w}$ , and that  $P_1$  does not learn  $\mathsf{L}_{w, z_w \oplus \lambda_w \oplus 1}$  for all  $w \in \mathcal{O}$ .

**Base step:** Honest  $P_i$  only sends one garbled labels to  $P_1$ , and  $\Delta_i$  is hidden from  $\mathcal{A}$ , therefore the base step is true.

**Induction step:** It is obvious that  $P_1$  cannot learn the other label for an XOR gate and we will focus on AND gates.

Note that  $P_1$  only learns one garbled keys for input wire  $\alpha$  and  $\beta$ . However, each row is encrypted using different combinations of  $L_{\alpha,b}$  and  $L_{\beta,b}$ . In order for  $P_1$  to open two rows in the garbled table,  $P_1$  needs to learn both garbled keys for some input wire, which contradict with assumptions in the induction step.

## 6 Instantiation of the Preprocessing Functionality

In this section, we describe an efficient instantiation of  $\mathcal{F}_{Pre}$ . All previous protocols [LOS14, BLN<sup>+</sup>15, FKOS15] for multi-party TinyOT relies on cut-and-choose with bucketing to ensure correctness and at least an additional round of bucketing to ensure the privacy, resulting a complexity at least  $O(B^2n^2)$  per AND triple, where B is the bucket size. In order to achieve better performance, we instead propose a new distributed checking protocol that allows parties to distributively check the correctness of *each* triple, where the probability of being caught is at least one-half. We then used bucketing to eliminate such leakage. Overall our protocol has complexity  $O(Bn^2)$ .

## 6.1 Multi-party Authenticated Bit

The first step of our protocol is to design a multi-party variant of authenticated bit [NNOB12]. One naive solution for  $P_i$  to obtain an authenticated bit is to let  $P_i$  to run a two-party authenticated bit protocol ( $\mathcal{F}^2_{aBit}$ ) with every other party using the same input x. This solution does not work, since a malicious  $P_i$  can potentially use inconsistent values when running  $\mathcal{F}^2_{aBit}$  with other parties. In our protocol shown in Figure 6, we use this general idea and in addition, we also perform checks to ensure that the values are consistent. The check is similar to the recent malicious OT extension protocol by Keller et al. [KOS15], where parties perform some random linear check, which reveals some linear relationship of the input. To eliminate such leakage, a small number of additional random authenticated bits are computed and checked together. They are later discarded to break the linear dependency.

#### Functionality $\mathcal{F}_{aBit}^n$

**Honest Parties:** The box receives (input,  $i, \ell$ ) from all parties and picks random bit-string  $x \in \{0, 1\}^{\ell}$ . For each  $j \in [\ell], k \neq i$ , the box picks random  $\mathsf{K}_k[x_j]$ , and computes  $\{\mathsf{M}_k[x_j] := \mathsf{K}_k[x_j] \oplus x_j \Delta_k\}_{k \neq i}$ , and sends them to parties. That is, for each  $j \in [\ell]$ , it sends  $\{\mathsf{M}_k[x_j]\}_{k \neq i}$  to  $P_i$  and sends  $\mathsf{K}_k[x_j]$  to  $P_k$  for each  $k \neq i$ .

Malicious Party: Corrupted parties can choose their output from the protocol.

**Global Key Queries:** The adversary at any point can send some  $(p, \Delta')$  and told if  $\Delta' = \Delta_p$ .

Figure 5: Functionality  $\mathcal{F}_{\mathsf{aBit}}^n$  for multi-party authenticated bit.

### Protocol $\Pi^n_{aBit}$

- 1. Set  $\ell' := \ell + 2\rho$ .  $P_i$  picks random bit-string  $x \in \{0, 1\}^{\ell'}$ .
- 2. For each  $k \neq i$ ,  $P_i$  and  $P_k$  runs  $\mathcal{F}^2_{aBit}$ , where  $P_i$  sends  $\{x_j\}_{j \in [\ell']}$  to  $\mathcal{F}^2_{aBit}$ . From the functionality,  $P_i$  gets  $\{\mathsf{M}_k[x_j]\}_{j \in [\ell']}$ ,  $P_k$  gets  $\{\mathsf{K}_k[x_j]\}_{j \in [\ell']}$ .
- 3. For  $j \in [2\rho]$ , all parties perform the following:
  - (a) All parties sample a random  $\ell'$ -bit strings r.
  - (b)  $P_i$  computes  $\mathcal{X}_j = \bigoplus_{m=1}^{\ell'} r_m x_m$ , and broadcast  $\mathcal{X}_j$ , and computes  $\left\{\mathsf{M}_k[\mathcal{X}_j] = \bigoplus_{m=1}^{\ell'} r_m \mathsf{M}_k[x_m]\right\}_{k \neq i}$ .
  - (c)  $P_k$  computes  $\mathsf{K}_k[\mathcal{X}_j] = \bigoplus_{m=1}^{\ell'} r_m \mathsf{K}_k[x_m].$
  - (d)  $P_i$  sends  $M_k[\mathcal{X}_j]$  to  $P_k$  who check the validity.
- 4. All parties return the first  $\ell$  objects.

Figure 6: The protocol  $\Pi^n_{\mathsf{aBit}}$  instantiating  $\mathcal{F}^n_{\mathsf{aBit}}$ .

Note that in the later sections of the protocol, we need "dual global key" of abit, where some bits are authenticated with two different sets of global keys. This can be easily achieved by running this protocol with  $2\kappa$  key length, and split each into two MAC/Keys.

**Theorem 6.1.** The protocol in Figure 6 securely instantiates the  $\mathcal{F}_{aBit}^n$  functionality with statistical security  $2^{-\rho}$  in the  $\mathcal{F}_{aBit}^2$ -hybrid model.

*Proof.* Case 1:  $P_i \in \mathcal{H}$ . Note that in this case, the only way malicious parties can break the protocol is to learn some information about  $\{x_i\}_{i \in [\ell]}$  in the checking step. However, we will show that, because we "throw out" the last  $2\rho$  authenticated bits, the adversary can learn nothing about x's.

Using  $s_j$  to denote the last  $2\rho$  bits of r in the j-th check. According to Lemma 6.1 and the parameters we chose, the probability that any subset of  $\{s_j\}_{j\in[2\rho]}$  is linearly independent is  $1-2^{-\rho}$ . Now we will show that if linear independence holds then the adversary cannot learn anything.

For the *j*-checking,  $\mathcal{X} = \left(\bigoplus_{m=1}^{\ell} r_m x_m\right) \oplus \left(\bigoplus_{m=1}^{2\rho} s_m x_{\ell+m}\right)$ . Note that  $\bigoplus_{m=1}^{2\rho} s_m x_{\ell+m}$  from each checking are independent random bits, where  $\{x_m\}_{m=\ell}^{\ell'}$  is random. This is true because the  $s_i$ 's are linearly independent. Therefore,  $\bigoplus_{m=1}^{2\rho} s_m x_{\ell+m}$  acts as one-time pad to  $\bigoplus_{m=1}^{\ell} r_m x_m$ . Given

the above, the simulation is straightforward. Note that for all global key queries, S can send the query to  $\mathcal{F}^2_{\mathsf{aBit}}$  and send the answer from  $\mathcal{F}^2_{\mathsf{aBit}}$  to  $\mathcal{A}$ .

**Case 2:**  $P_i \in \mathcal{M}$ . The simulation is straightforward if we could show that for any  $\mathcal{A}$  who uses inconsistent x's can pass all  $2\rho$  checks with at most negligible probability. This is what we will proceed to show.

Suppose that  $\mathcal{A}$  sends  $x^1$  to  $\mathcal{F}^2_{\mathsf{aBit}}$  when interacting with one honest party, and uses a different  $x^2$  with another honest party, where  $x^1 \neq x^2$ . We also assume that  $\mathcal{A}$  passes all checks. Note that for the *j*-th checking, if  $\mathcal{A}$  is not able to forge a MAC, then the probability that the checking passes is the probability that  $\mathcal{X}_j = \bigoplus_m r_m x_m^1$  and that  $\mathcal{X}_j = \bigoplus_m r_m x_m^2$ .

$$\Pr\left\{\bigoplus_{m} r_m x_m^1 = \bigoplus_{m} r_m x_m^2\right\} = \Pr\left\{\bigoplus_{m} r_m (x_m^1 \oplus x_m^2) = 0\right\}$$
$$= \Pr\left\{\bigoplus_{m \in I} r_m = 0 : I \text{ is the set of indices where } x_m^1 \neq x_m^2\right\}$$
$$= 1/2$$

Each checking is independent as long as r is selected independently. Therefore,  $\mathcal{A}$  can pass all checks with probability at most  $2^{-2\rho}$ .

**Lemma 6.1.** Let  $r_1, ..., r_l$  be random bit vectors of length k. With probability at most  $2^{l-k}$ , there exists some subset  $I \subset [l]$ , such that

$$\bigoplus_{i\in I} r_i = 0$$

*Proof.* Note that given a fixed interval  $I \subset [l]$ , the probability that  $\bigoplus_{i \in I} r_i = 0$  is  $2^{-k}$ . According to the union bound, the probability that any subset  $I \subset [l]$  has  $\bigoplus_{i \in I} r_i = 0$  is  $2^{-k} \times 2^l = 2^{l-k}$ .  $\Box$ 

### 6.2 Multi-party Leaky Authenticated AND triple

Once we have multi-party version of authenticated bit, our next step is to compute leaky authenticated AND triples. The adversary can perform selective failure attacks where he gets caught with some probability.

The first step is to compute the AND triples, such that the triples will be correct if every party behaves honestly without revealing any party's share. This is done in our protocol by letting every distinct pair of parties, namely  $P_i$ ,  $P_j$ , compute XOR-shares of  $x^i y^j \oplus x^j y^i$ . Similar to the improved TinyOT protocol [WRK17], each pair of the computation only requires 4 bits of communication. The next step is to check the correctness of the computation. Note that this is main challenge. In existing protocols, they follow the cut-and-choose with a sacrifice and merge step. Cut-and-choose ensures that only small number of triples that are not checked are incorrect; bucketing is used twice to gain correctness and privacy, leading to a  $B^2n^2$  term.

Our checking phase differs substantially from existing works. We design an efficient checking protocol, that always ensures the correctness of the triple (if no party aborts) which allows malicious parties to learn k bits of some specific information with probability  $2^{-k}$ . This leakage can be easily eliminated using bucketing discussed later. In the two-party protocol, one party construct "checking tables" and lets the other party to evaluate/check. In the multi-party protocol here, we instead let

## Functionality $\mathcal{F}_{LaAND}^n$

Honest parties: For each  $i \in [n]$ , the box picks random  $[x]^i, [y]^i, [z]^i$  such that  $(\bigoplus x^i) \land (\bigoplus y^i) = \bigoplus z^i$ . Corrupted parties:

1. Corrupted parties can choose all their randomness. Furthermore, adversary can send  $(R, \{Q_i\}_{i \in [n]}, D)$  to the box and perform a linear combination test. The box will check

$$R \oplus \bigoplus_{i} x^{i} Q_{i} \in \{0, D\}$$

If the check is incorrect, the box outputs fail and terminates, otherwise the box proceeds as normal. **Global Key Queries:** The adversary at any point can send some  $(p, \Delta')$  and will be told if  $\Delta' = \Delta_p$ .

Figure 7: Functionality  $\mathcal{F}_{LaAND}^n$  for leaky AND triple generation.

all parties distributively construct the "checking tables". Interestingly, distributively constructing these checks is inspired by the main protocol where parties distributively construct garbled tables. In the distributive checking, all parties compute the checking as if  $\bigoplus_i x^i = 0$  and  $\bigoplus_i x^i = 1$ , in a way such that each party obtains some share  $H_i$  and  $D_i$ . If  $\bigoplus_i x^i = 0$  and the correctness holds, then  $\bigoplus_i H_i = 0$ ; if  $\bigoplus_i x^i = 1$  and the correctness holds, then  $\bigoplus_i H_i \oplus D_i = 0$ . Then all parties will jointly perform an oblivious comparison to check if one of the above equation is correct.

In more detail, the correctness proof proceeds as follows: First, each value will be given new MACs under fresh random global keys. This will be done by using the MACs and keys under  $\Omega$  and then using these keys as garbled labels. We will then use these fresh values to produce  $H_i$ ,  $D_i$ ,  $D := \bigoplus_i D_i$  with two properties. The first property is:

- 1. if  $\bigoplus_i x_i = 0$  and  $\bigoplus_i z_i = 0$  then  $\bigoplus_i H_i = 0$
- 2. if  $\bigoplus_i x_i = 1$  and  $\bigoplus_i y_i \oplus z_i = 0$  then  $\bigoplus_i H_i = D$

If on the other hand none of these conditions are met and we reveal D to the adversary then it should be infeasible for the adversary to influence the  $H_i$  held by honest parties such that the adversary can select  $H_i$  for the malicious parties such that  $\bigoplus_i H_i \in \{0, D\}$ .

Given such a construction for  $H_i$  and  $D_i$ , it seems that all we need to do is open up the  $H_i$  and verify that  $\bigoplus_i H_i \in \{0, D\}$ . However revealing  $H_i$  does not work since it would reveal  $\bigoplus_i x_i$  which needs to remain secret. However by having each player random sample a bit  $b_i \in \{0, 1\}$  and then by having each player reveal  $T_i := H_i \oplus b_i D$  instead of  $H_i$ , then we can verify that  $(\bigoplus_i x_i) \wedge (\bigoplus_i y_i) = \bigoplus_i z_i$  without revealing information. As noted before, this protocol is vulnerable to selective failure attacks. The full description of this protocol is presented in Figure 8.

#### 6.2.1 Correctness of the protocol

We want to show first that if all parties behave honestly, then the protocol outputs correct AND triples. Defining  $c = \bigoplus_i x^i$ , we would like to show that  $\bigoplus_i H_i \in \{0, D\}$ .

#### Protocol $\Pi^n_{LaAND}$

Compute the triple with semi-honest security

- 1. For each  $i \in [n]$  each party calls  $\mathcal{F}^n_{\mathsf{aBit}}$  and obtains random authenticated bits  $\{[y]^i, [r]^i\}$ ; They also obtains random authenticated bits  $\{[x]^i, [x]^i_{\Omega_i}\}$  that are the same bit authenticated on different global keys.
- 2. For each  $i, j \in [n]$  such that i < j,  $P_i$  computes and sends the following values to  $P_j$ :

 $\begin{array}{ll} G_{0,0} := \mathsf{Lsb}(H(\mathsf{K}_i[x^j], & \mathsf{K}_i[y^j] & )) \oplus (0 \oplus x^i) \wedge (0 \oplus y^i) \oplus r^i \\ G_{1,0} := \mathsf{Lsb}(H(\mathsf{K}_i[x^j] \oplus \Delta_i, & \mathsf{K}_i[y^j] & )) \oplus (1 \oplus x^i) \wedge (0 \oplus y^i) \oplus r^i \\ G_{0,1} := \mathsf{Lsb}(H(\mathsf{K}_i[x^j], & \mathsf{K}_i[y^j] \oplus \Delta_i & )) \oplus (0 \oplus x^i) \wedge (1 \oplus y^i) \oplus r^i \\ G_{1,1} := \mathsf{Lsb}(H(\mathsf{K}_i[x^j] \oplus \Delta_i, & \mathsf{K}_i[y^j] \oplus \Delta_i & )) \oplus (1 \oplus x^i) \wedge (1 \oplus y^i) \oplus r^i \\ P_i \text{ computes } s_j := r^i \oplus x^i y^i; P_j \text{ computes } s_i := \mathsf{Lsb}(H(\mathsf{M}_i[x^j], \mathsf{M}_i[y^j])) \oplus G_{x^j, y^j} \oplus x^j y^j. \end{array}$ 

3. For each  $i \in [n]$ ,  $P_i$  computes  $z^i := x^i y^i \oplus \left(\bigoplus_{k \neq i} s_k\right)$ .  $P_i$  also broadcasts  $e^i := z^i \oplus r^i$  to all other parties. All parties computes  $[z]^i := [r]^i \oplus e^i$ .

#### Check the correctness

4. For each i ∈ [n], P<sub>i</sub> randomly sample a Φ<sub>i</sub>. For every pair of i, j ∈ [n], P<sub>i</sub> compute and sends the following to P<sub>j</sub>:
U<sub>i</sub> i<sub>0</sub> := H(K<sub>i</sub>[x<sup>j</sup>]<sub>Ω<sub>i</sub></sub>) ⊕ K<sub>i</sub>[x<sup>j</sup>]<sub>Φ<sub>i</sub></sub>

$$\begin{split} U_{i,j,0} &:= H(\mathsf{K}_i[x^j]_{\Omega_i}) \oplus \mathsf{K}_i[x^j]_{\Phi_i} \\ U_{i,j,1} &:= H(\mathsf{K}_i[x^j]_{\Omega_i} \oplus \Omega_i) \oplus \mathsf{K}_i[x^j]_{\Phi_i} \oplus \Phi_i \\ P_j \text{ computes } \mathsf{M}_i[x^j]_{\Phi_i} &:= U_{i,j,x^j} \oplus H(\mathsf{M}_i[x^j]_{\Omega_i}) \end{split}$$

- 5. For  $i \in [n]$ ,  $P_i$  computes the followings  $H_i := x^i \Phi_i \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_i[x^k]_{\Phi_i} \oplus \mathsf{M}_k[x^i]_{\Phi_k} \right) \oplus z^i \Delta_i \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_i[z^k] \oplus \mathsf{M}_k[z^i] \right)$   $D_i := \Phi_i \oplus y^i \Delta_i \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_i[y^k] \oplus \mathsf{M}_k[y^i] \right)$ and broadcast  $D^i$ . All parties computes  $D := \bigoplus_i D^i$ .
- 6.  $P_i$  picks a random bit b, compute and simultaneously broadcast  $T_i := H_i \oplus bD$ . All parties compute  $T := \bigoplus_i T_i$  and check if  $T \in \{0^{\kappa}, D\}$  or not.

## Figure 8: The protocol $\Pi_{\mathsf{LaAND}}^n$ .

**Case 1:** c = 0. In this case, the relationship we would like to check is  $\bigoplus_i z^i = 0$ .

$$\begin{split} \bigoplus_{i} H_{i} &= \bigoplus_{i} \left( x^{i} \Phi_{i} \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_{i} [x^{k}]_{\Phi_{i}} \oplus \mathsf{M}_{k} [x^{i}]_{\Phi_{k}} \right) \oplus z^{i} \Delta_{i} \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_{i} [z^{k}] \oplus \mathsf{M}_{k} [z^{i}] \right) \right) \\ &= \bigoplus_{i} \left( x^{i} \Phi_{i} \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_{i} [x^{k}]_{\Phi_{i}} \oplus \mathsf{M}_{k} [x^{i}]_{\Phi_{k}} \right) \right) \oplus \bigoplus_{i} \left( z^{i} \Delta_{i} \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_{i} [z^{k}] \oplus \mathsf{M}_{k} [z^{i}] \right) \right) \\ &= \bigoplus_{i} \left( x^{i} \Phi_{i} \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_{i} [x^{k}]_{\Phi_{i}} \oplus \mathsf{M}_{i} [x^{k}]_{\Phi_{k}} \right) \right) \oplus \bigoplus_{i} \left( z^{i} \Delta_{i} \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_{i} [z^{k}] \oplus \mathsf{M}_{i} [z^{k}] \right) \right) \\ &= \bigoplus_{i} \left( x^{i} \Phi_{i} \oplus \left( \bigoplus_{k \neq i} x^{k} \Phi_{i} \right) \right) \oplus \bigoplus_{i} \left( z^{i} \Delta_{i} \oplus \left( \bigoplus_{k \neq i} z^{k} \Delta_{i} \right) \right) \\ &= \left( \bigoplus_{i} x^{i} \right) \cdot \left( \bigoplus_{i} \Phi_{i} \right) \oplus \left( \bigoplus_{i} z^{i} \right) \cdot \left( \bigoplus_{i} \Delta_{i} \right) = 0 \end{split}$$

**Case 2:** c = 1. In this case, the relationship we would like to check is  $\bigoplus_i (z^i \oplus y^i) = 0$ , because  $\bigoplus_i x^i = 1$ . We would like to show that  $\bigoplus_i H_i = D$ , which means that  $\bigoplus_i (H_i \oplus D^i) = 0$ .

$$\begin{split} &\bigoplus_{i} \left(H_{i} \oplus D^{i}\right) \\ &= \bigoplus_{i} \left(\Phi_{i} \oplus x^{i} \Phi_{i} \oplus \left(\bigoplus_{k \neq i} \mathsf{K}_{i}[x^{k}]_{\Phi_{i}} \oplus \mathsf{M}_{k}[x^{i}]_{\Phi_{k}}\right) \oplus (z^{i} \oplus y^{i}) \Delta_{i} \oplus \left(\bigoplus_{k \neq i} \mathsf{K}_{i}[z^{k}] \oplus \mathsf{M}_{k}[z^{i}] \oplus \mathsf{M}_{k}[y^{i}]\right)\right) \\ &= \bigoplus_{i} \left(\Phi_{i} \oplus x^{i} \Phi_{i} \oplus \left(\bigoplus_{k \neq i} \mathsf{K}_{i}[x^{k}]_{\Phi_{i}} \oplus \mathsf{M}_{k}[x^{i}]_{\Phi_{k}}\right)\right) \oplus \bigoplus_{i} \left((z^{i} \oplus y^{i}) \Delta_{i} \oplus \left(\bigoplus_{k \neq i} \mathsf{K}_{i}[z^{k}] \oplus \mathsf{M}_{k}[z^{i}] \oplus \mathsf{M}_{k}[y^{i}]\right)\right) \\ &= \bigoplus_{i} \left(\Phi_{i} \oplus x^{i} \Phi_{i} \oplus \left(\bigoplus_{k \neq i} \mathsf{K}_{i}[x^{k}]_{\Phi_{i}} \oplus \mathsf{M}_{i}[x^{k}]_{\Phi_{k}}\right)\right) \oplus \bigoplus_{i} \left((z^{i} \oplus y^{i}) \Delta_{i} \oplus \left(\bigoplus_{k \neq i} \mathsf{K}_{i}[z^{k}] \oplus \mathsf{M}_{i}[z^{k}] \oplus \mathsf{M}_{i}[y^{k}]\right)\right) \\ &= \bigoplus_{i} \left(\Phi_{i} \oplus x^{i} \Phi_{i} \oplus \left(\bigoplus_{k \neq i} \mathsf{K}^{k} \Phi_{i}\right)\right) \oplus \bigoplus_{i} \left((z^{i} \oplus y^{i}) \Delta_{i} \oplus \left(\bigoplus_{k \neq i} (z^{k} \oplus y^{k}) \Delta_{i}\right)\right) \\ &= \bigoplus_{i} \Phi_{i} \oplus \left(\bigoplus_{i} x^{i}\right) \cdot \left(\bigoplus_{i} \Phi_{i}\right) \oplus \left(\bigoplus_{i} (z^{i} \oplus y^{i})\right) \cdot \left(\bigoplus_{i} \Delta_{i}\right) = 0 \end{split}$$

### 6.2.2 Unforgeability

**Lemma 6.2.** If  $(\bigoplus_i x_i) \land (\bigoplus_i y_i) \neq \bigoplus_i z_i$  then the protocol results in an abort except with negligible probability.

We Define  $c = \bigoplus_i x^i$ . We define  $\mathsf{K}_i[x^j]_{\Phi_i}$  from  $U_0$  and define  $\Phi_i$  from  $D^i$ . We denote  $Q_{i,j} := U_1 \oplus U_1^*$ , where  $U_1^*$  is what an honest party would compute based on values defined above. We further use  $H_i^*$  to denote the value that an honest  $P_i$  would have computed. For  $i \in \mathcal{M}$ , we define  $R_i := T_i \oplus H_i^*$  For  $i \in \mathcal{H}$ , honest parties computes  $H_i$  affected by the malicious parties:  $H_i = H_i^* \oplus \left(\bigoplus_{k \neq i} x^k Q_{k,i}\right)$ .

**Case 1:** c = 0. We will prove by contradiction, and assume that the equation does not hold, meaning that  $\bigoplus_i z^i = 1$ . We also assume that the check goes through, meaning that  $\bigoplus_i T_i \in \{0, D\}$ . In the following, we will derive a contradiction. Note that

$$\bigoplus_{i} H_{i}^{*} = \left(\bigoplus_{i} x^{i}\right) \cdot \left(\bigoplus_{i} \Phi_{i}\right) \oplus \left(\bigoplus_{i} z^{i}\right) \cdot \left(\bigoplus_{i} \Delta_{i}\right) = \bigoplus_{i} \Delta_{i}$$

Therefore, we know that

$$\begin{split} \bigoplus_{i}^{} T_{i} &= \bigoplus_{i}^{} \left(H_{i} \oplus b_{i}D\right) \\ &= \bigoplus_{i \in \mathcal{M}}^{} \left(H_{i} \oplus b_{i}D\right) \oplus \bigoplus_{i \in \mathcal{H}}^{} \left(H_{i} \oplus b_{i}D\right) \\ &= \bigoplus_{i \in \mathcal{M}}^{} \left(H_{i}^{*} \oplus b_{i}D \oplus R_{i}\right) \oplus \bigoplus_{i \in \mathcal{H}}^{} \left(H_{i}^{*} \oplus b_{i}D \oplus \left(\bigoplus_{k \neq i}^{} x^{k}Q_{k,i}\right)\right) \right) \\ &= \bigoplus_{i}^{} H_{i}^{*} \oplus \bigoplus_{i}^{} b_{i}D \oplus \bigoplus_{i \in \mathcal{M}}^{} R_{i} \oplus \bigoplus_{i \in \mathcal{H}}^{} \left(\bigoplus_{k \neq i}^{} x^{k}Q_{k,i}\right) \\ &= \bigoplus_{i}^{} \Delta_{i} \oplus \bigoplus_{i}^{} b_{i}D \oplus \bigoplus_{i \in \mathcal{M}}^{} R_{i} \oplus \bigoplus_{i \in \mathcal{H}}^{} \left(\bigoplus_{k \neq i}^{} x^{k}Q_{k,i}\right) \end{split}$$

In order to make  $\bigoplus_i T_i$  to be in the set  $\{0, D\}$ , the adversary needs to find paddings such that

$$\bigoplus_{i \in \mathcal{M}} R_i \oplus \bigoplus_{i \in \mathcal{H}} \left( \bigoplus_{k \neq i} x^k Q_{k,i} \right) \in \left\{ \bigoplus_i \Delta_i, \bigoplus_i \Delta_i \oplus D \right\}$$

The above happens with at most negligible probability.

**Case 2:** c = 1. We will prove by contradiction, and assume that the equation does not hold, meaning that  $\bigoplus_i (z^i \oplus y^i) = 1$ . We also assume hat the check goes through, meaning that  $\bigoplus_i T_i \in \{0, D\}$ . In the following, we will derive a contradiction. Note that

$$\begin{split} \bigoplus_{i} H_{i}^{*} &= \bigoplus_{i} \Phi_{i} \oplus \left(\bigoplus_{i} x^{i}\right) \cdot \left(\bigoplus_{i} \Phi_{i}\right) \oplus \left(\bigoplus_{i} (z^{i} \oplus y^{i})\right) \cdot \left(\bigoplus_{i} \Delta_{i}\right) \oplus \bigoplus_{i} D_{i} \\ &= \left(\bigoplus_{i} \Delta_{i}\right) \oplus D \end{split}$$

Similar to the above,

$$\begin{split} \bigoplus_{i}^{\leftarrow} T_{i} &= \bigoplus_{i}^{\leftarrow} (H_{i} \oplus b_{i}D) \\ &= \bigoplus_{i \in \mathcal{M}}^{\leftarrow} (H_{i} \oplus b_{i}D) \oplus \bigoplus_{i \in \mathcal{H}}^{\leftarrow} (H_{i} \oplus b_{i}D) \\ &= \bigoplus_{i \in \mathcal{M}}^{\leftarrow} (H_{i}^{*} \oplus b_{i}D \oplus R_{i}) \oplus \bigoplus_{i \in \mathcal{H}}^{\leftarrow} \left(H_{i}^{*} \oplus b_{i}D \oplus \left(\bigoplus_{k \neq i}^{\leftarrow} x^{k}Q_{k,i}\right)\right) \\ &= \bigoplus_{i}^{\leftarrow} H_{i}^{*} \oplus \bigoplus_{i}^{\leftarrow} b_{i}D \oplus \bigoplus_{i \in \mathcal{M}}^{\leftarrow} R_{i} \oplus \bigoplus_{i \in \mathcal{H}}^{\leftarrow} \left(\bigoplus_{k \neq i}^{\leftarrow} x^{k}Q_{k,i}\right) \\ &= \bigoplus_{i}^{\leftarrow} \Delta_{i} \oplus D \oplus \bigoplus_{i}^{\leftarrow} b_{i}D \oplus \bigoplus_{i \in \mathcal{M}}^{\leftarrow} R_{i} \oplus \bigoplus_{i \in \mathcal{H}}^{\leftarrow} \left(\bigoplus_{k \neq i}^{\leftarrow} x^{k}Q_{k,i}\right) \end{split}$$

In order to make  $\bigoplus_i T_i$  to be in the set  $\{0, D\}$ , the adversary needs to find paddings such that

$$\bigoplus_{i \in \mathcal{M}} R_i \oplus \bigoplus_{i \in \mathcal{H}} \left( \bigoplus_{k \neq i} x^k Q_{k,i} \right) \in \left\{ \bigoplus_i \Delta_i, \bigoplus_i \Delta_i \oplus D \right\}$$

The above happens with at most negligible probability.

### 6.2.3 Proof

**Theorem 6.2.** The protocol in Figure 8, where H is modeled as a random oracle, securely instantiates  $\mathcal{F}_{LaAND}^n$  functionality in the  $\mathcal{F}_{aBit}^n$ -hybrid model.

*Proof.* We constructor a simulator in the following. For all global key queries, S redirect them to  $\mathcal{F}_{\mathsf{aBit}}^n$  and redirect the answer to  $\mathcal{A}$ .

- 1. S plays the role of  $\mathcal{F}_{aBit}^{n}$  storing all information sent to parties.
- 2. For each  $i \in \mathcal{H}$ ,  $\mathcal{S}$  simulates  $P_i$  as follows: When  $P_i$  interacts with  $P_j$  with i < j,  $P_i$  sends four random bits to  $P_j$ .

- 3. S simulate each honest  $P_i$  by broadcasting a random bit.
- 4. For each  $i \in \mathcal{M}$ ,  $\mathcal{S}$  receives  $\{U_{i,j,b}\}_{j \in \mathcal{H}, b \in \{0,1\}}$  from  $P_i$ .  $\mathcal{S}$  picks random  $\{U_{j,i,b}\}_{j \in \mathcal{H}, b \in \{0,1\}}$  and sends them to  $P_i$  playing the role of  $P_j$  for each  $j \in \mathcal{H}$ .
- 5. For each  $i \in \mathcal{H}$ , S acts an honest  $P_i$ , using some random  $D_i$ , and awaits for  $\{D_i\}_{i \in \mathcal{M}}$  broadcast from malicious parties.
- 6. For each  $i \in \mathcal{M}, \mathcal{S}$  defines  $\Phi_i$  as

$$\Phi_i := D_i \oplus y^i \Delta_i \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_i[y^k] \oplus \mathsf{M}_k[y^i] \right)$$

using values when S plays the role of  $\mathcal{F}_{aBit}^n$ . S computes  $z^i := e^i \oplus r^i$ , where  $e^i$  is the value broadcast by the malicious parties,  $r^i$  is the value when S used to play the role of  $\mathcal{F}_{aBit}^n$ . If  $(\bigoplus_i x^i) \land (\bigoplus_i y^i) \neq (\bigoplus_i z^i)$ , S acts as honest parties until the protocol aborts, outputting whatever  $\mathcal{A}$  outputs. In detail, S can use values that S used when playing the role of  $\mathcal{F}_{aBit}^n$ . If the equation hold, S will perform the following to check if  $\mathcal{A}$  launched a selective failure attack:

 $\mathcal{S}$  computes  $c = \bigoplus_i x^i$ , and  $\mathsf{K}_i[x^j]_{\Phi_i} := U_{i,j,0} \oplus H(\mathsf{K}_i[x^j]_{\Omega_i})$ , and computes  $\Phi_i := D_i \oplus y^i \Delta_i \oplus (\bigoplus_{k \neq i} \mathsf{K}_i[y^k] \oplus \mathsf{M}_k[y^i])$ .  $\mathcal{S}$  then computes  $Q_{i,j} := U_{i,j,1} \oplus U^*_{i,j,1}$ , where  $U^*_{i,j,1}$  is what an honest  $P_i$  would have sent based on values defined above. We further use  $H^*_i$  to denote the value that an honest  $P_i$  would have computed. For  $i \in \mathcal{M}$ , we define  $R_i := T_i \oplus H^*_i$ . For  $i \in \mathcal{H}$ , honest parties computes  $H_i$  affected by the malicious parties:  $H_i = H^*_i \oplus (\bigoplus_{k \neq i} x^k Q_{k,i})$ .  $\mathcal{S}$  defines  $Q_k = \bigoplus_{i \neq k, i \in \mathcal{H}} Q_{k,i}$ .  $\mathcal{S}$  sends  $(\bigoplus_i R_i, \{Q_i\}_{i \in [n]}, D)$  to  $\mathcal{F}_{\mathsf{L}\mathsf{a}\mathsf{AND}}$ . If  $\mathcal{F}_{\mathsf{L}\mathsf{a}\mathsf{AND}}$  terminates,  $\mathcal{S}$  aborts outputting whatever  $\mathcal{A}$  outputs; otherwise,  $\mathcal{S}$  obtains  $\{T_i\}_{i \in \mathcal{M}}$  and picks random  $\{T_i\}_{i \in \mathcal{H}}$  such that  $\bigoplus_i T_i = rD$  for some random bit r and follow the protocol using these values.

Note that the first five steps are perfectly indistinguishable given that H is a random oracle. We will focus on the last step. If in step 6, it is the case that  $(\bigoplus_i x^i) (\bigoplus_i y^i) \neq (\bigoplus_i z^i)$ , then it is easy to see that the views are indistinguishable: all parties behave the same between hybrids. According to the unforgeability lemma, the protocol will abort with all but negligible probability. In the following, we will focus on the case when the equation holds.

First, given definition in step 6, we can express an honest parties'  $T_i$  as  $T_i := H_i^* \oplus (\bigoplus_i x^k Q_{k,i})$ , where  $Q_{k,i}$  are values defined based on  $\mathcal{A}$ 's message. Note that  $\bigoplus_{i \in \mathcal{H}} H_i^*$  is already defined, since  $\bigoplus_i H_i^* = 0$ . Now we will show that for any proper subset  $S \subset \mathcal{H}$ ,  $\bigoplus_{i \in S} H_i^*$  is indistinguishable from random to the  $\mathcal{A}$ . It is easy to see: we use e to denote an honest party such that  $e \in \mathcal{H}, e \notin \S$ . Such e always exists, since S is a proper subset of  $\mathcal{H}$ . Observe that in the computation of  $H^*$ :

$$H_i^* := x^i \Phi_i \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_i[x^k]_{\Phi_i} \oplus \mathsf{M}_k[x^i]_{\Phi_k} \right) \oplus z^i \Delta_i \oplus \left( \bigoplus_{k \neq i} \mathsf{K}_i[z^k] \oplus \mathsf{M}_k[z^i] \right)$$

The value  $F_i^* = \left(\bigoplus_{k \neq i} \mathsf{K}_i[x^k]_{\Phi_i} \oplus \mathsf{M}_k[x^i]_{\Phi_k}\right)$  is independent of the remaining part. Therefore we

## Functionality $\mathcal{F}_{aAND}^n$

Honest parties: For each  $i \in [n]$ , the box picks random  $[x]^i, [y]^i, [z]^i$  such that  $(\bigoplus x^i) \land (\bigoplus y^i) = \bigoplus z^i$ . Corrupted parties: Corrupted parties get to choose all of their randomness. Global Key Queries: The adversary at any point can send some  $(p, \Delta')$  and will be told if  $\Delta' = \Delta_p$ .

## Figure 9: Functionality $\mathcal{F}_{\mathsf{aAND}}^n$ for generating AND triples

## **Protocol** $\Pi_{aAND}^{n}$

- 1.  $P_i$  call  $\mathcal{F}_{\mathsf{LaAND}}^n \ell' = \ell B$  times and obtains  $\{[x_j]^i, [y_j]^i, [z_j]^i\}_{j \in [\ell']}$ .
- 2. All parties randomly partition all objects into  $\ell$  buckets, each with B objects.
- 3. For each bucket, parties combine *B* leaky ANDs into one non-leaky AND. To combine two leaky ANDs, namely  $([x_1]^i, [y_1]^i, [z_1]^i)$  and  $([x_2]^i, [y_2]^i, [z_2]^i)$ :
  - (a) Each party  $P_i$  reveals  $d^i := y_1^i \oplus y_2^i$  with MAC checked, All parties compute  $d := \bigoplus_i d^i$ .
  - (b) Each party  $P_i$  sets  $[x]^i := [x_1]^i \oplus [x_2]^i, [y]^i := [y_1]^i, [z]^i := [z_1]^i \oplus [z_2]^i \oplus d[x_2]^i.$

Parties iterate all B leaky objects, by taking the resulted object and combine with the next element.

Figure 10: Protocol  $\Pi_{\mathsf{aAND}}^n$  instantiating  $\mathcal{F}_{\mathsf{aAND}}^n$ .

will show  $\bigoplus_{i \in S} F_i^*$  is indistinguishable from random.

$$\begin{split} \bigoplus_{i\in S} F_i^* &= \bigoplus_{i\in S} \bigoplus_{k\neq i} \left( \mathsf{K}_i[x^k]_{\Phi_i} \oplus \mathsf{M}_k[x^i]_{\Phi_k} \right) \\ &= \bigoplus_{i\in S} \bigoplus_{k\neq i} \left( \mathsf{K}_i[x^k]_{\Phi_i} \right) \oplus \bigoplus_{i\in S} \bigoplus_{k\neq i} \left( \mathsf{M}_k[x^i]_{\Phi_k} \right) \\ &= \bigoplus_{i\in S} \bigoplus_{k\neq i} \left( \mathsf{K}_i[x^k]_{\Phi_i} \right) \oplus \bigoplus_{k\in S} \bigoplus_{i\neq k} \left( \mathsf{M}_i[x^k]_{\Phi_k} \right) \\ &= \bigoplus_{i\in S} \bigoplus_{k\neq i} \left( \mathsf{K}_i[x^k]_{\Phi_i} \right) \oplus \bigoplus_{i\in [n]} \bigoplus_{k\in S, k\neq i} \left( \mathsf{M}_i[x^k]_{\Phi_k} \right) \end{split}$$

From the equation, it is clear that for  $i \in S$ ,  $\mathsf{K}_e[x^i]$  is not in the computation, while  $\mathsf{M}_e[x^i]$  is. Since  $\mathsf{K}_e[x^i]$  is randomly picked by  $P_e$ ,  $\bigoplus_{i \in S} F_i^*$  is random. Therefore we can see that for any proper subset  $S \subset \mathcal{H}$ ,  $\bigoplus_{i \in S} T_i$  is indistinguishable from random, which concludes the proof.  $\Box$ 

## 6.3 Multi-party Authenticated AND triple

Once we have a protocol for leaky authenticated AND triple, it is straightforward to obtain an non-leaky authenticated AND triple, using the combine protocol in [WRK17]. We show the details of the protocol in Figure 10.

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