People Who Live in Glass Houses Should not Throw Stones: Targeted Opening Message Franking Schemes

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Abstract. Message franking enables a receiver to report a potential abuse in a secure messaging system which employs an end to end encryption. Such mechanism is crucial for accountability and is already widely adopted in real world products such as the Facebook messenger. Grubs et al [5] initiated a systematic study of such a new primitive, and Dodis et al [2] gave a more efficient construction. We observe that in all existing message franking schemes, the receiver has to reveal the whole communication for a session in order to report one abuse. This is highly undesirable in many settings where revealing other non-abusive part of the communication leaks too much information; what is worse, a foxy adversary may intentionally mixing private information of the receiver with the abusive message so that the receiver will be reluctant to report. This essentially renders the abuse reporting mechanism ineffective.

To tackle this problem, we propose a new primitive called targeted opening compactly committing AEAD (TOCE for short). In a TOCE, the receiver can select arbitrary subset of bits from the plaintext to reveal during opening, while keep all the rest still secure as in an authenticated encryption. We gave a careful formulation, together with a generic construction which allowing a bit level targeted opening. While the generic construction may require a substantial number of passes of symmetric key ciphers when encrypting a large message such as a picture, we thus further set forth and give a more efficient non-black-box construction allowing a block-level (e.g., 256 bit) opening. We also propose a privacy-efficiency trade off if we can relax the security of non-opened messages to be one way secure after the abusive reporting (they are still semantically secure if no opening).

1 Introduction

End-to-end encryption enables users to securely communicate with each other, without worrying the message to be seen to any third party including the platform that hosts the secure messaging service. Multiple large scale secure messaging systems such as WhatsApp, Signal, and Facebook Messenger have already been deployed to serve more than a billion users across the globe. On the other hand, confidentiality also brings new challenges of other security goals.

Most notably, when one user spreads misinformation such as harassing messages, phishing links and/or any other improper contents, the recipients should be allowed to report the malicious behavior to the service provider, so that the sender could be penalized (e.g., blocked). On the same time, no dishonest reporter should be able to fabricate any fake message to frame an innocent sender. To address this pressing challenge, Facebook Messenger [3, 4] recently introduced the concept of *message franking* for such verifiable abuse reporting in encrypted systems. Also, a new cryptographic primitive called compactly committing authenticated encryption with associated data (ccAEAD) was proposed in recent cryptography literature [5, 2] to provide formal investigations.

A ccAEAD first is a standard authenticated encryption, but with the extra property that enables a receiver to open the plaintext if he chooses to. Two natural properties arise: a malicious sender could not deny the opening of an honest receiver, and a malicious receiver cannot arbitrarily open the message to frame an honest sender. Besides these two, in practice, it is preferable to add a short tag to enable these two properties whose size is independent of the message size (this property refers to compactness).

Intuitively, in a message franking system, some short tag served as a proof will be attached to the ciphertext so that a later "opening" of the ciphertext can be verified with this tag. Imagine a user Bob receives a ciphertext which is "stamped" by the server from a user Alice, (server signs or even stores the tag ensuring the ciphertext is indeed sent from Alice to Bob). If Bob decodes the ciphertext, validates the tag, and obtains an improper message, he will then reveal either the message or the secret key, so that the service provider can check the reported abuse. Existing methods including the one deployed in Facebook Messenger and the constructions in [5, 2] all follow this pattern.

The undesirability of "all or nothing" abuse reporting. However, revealing the whole piece of the plaintext transmitted during a session when reporting an abusive message in many cases is undesirable to the recipient, as some parts of the plaintext (or the existence of the conversation itself) could contain private information. Consider the following exemplary scenarios: a doctor or a pharmacist is communicating with one patient about the situation of some diseases the patient is suffering from or the medicine the patient is taking; two members of a cult group are discussing or debating on some issue regarding their special interests; a merchant on Ebay is explaining to a customer about the product (which could be for some special hobby and the customer would prefer to keep private) he is selling. In all those scenarios, the conversations contain some private information of the recipient, if improper messages such as harassing messages are generated during those conversations, the recipients may feel reluctant to reveal his name or the other personal information, thus not reporting the abuse.

What's worse, having this in mind, a malicious sender would intentionally insert some kind of personal information of the receiver when sending improper messages. Given current all-or-nothing type of opening in ccAEAD schemes, the attacker can simply concatenate some piece of receiver personal information with the abusive message and send over together via the secure messaging sys-

tem. Doing this essentially renders abuse reporting in message franking as an ineffective deterrence towards resolving the misinformation problem in secure messaging. Such potential threat of existing message franking schemes calls for a formal study that whether the abuse reporting can be done in a way that the receiver can choose flexibly which part to reveal. In this paper, we are seeking to answer the following question:

Can we design a message franking scheme that enables the receiver to selectively report the abusing message, without revealing any information about other parts of the plaintext?

Our contributions. To defend against the above attack to message franking, we strengthen the ccAEAD notion to enable a targeted opening. In more details:

Targeted opening ccAEAD: modeling. It turns out that adding a targeted opening property influences all security properties. We formally define the targeted opening property for ccAEAD, such that a recipient could reveal any part of the message of his choice, while other parts remain as secure as in an authenticated encryption. This means for both confidentiality and ciphertext integrity, we need to allow the attacker an extra query about opening of a targeted part of the plaintext. Furthermore, the two binding properties also need to be revised accordingly. More specifically, it means that the sender must not be able to provide a valid ciphertext which can be decrypted successfully but can not be targeted opened correctly for some positions. Also the receiver can not maliciously open any targeted part of the ciphertext to a abusive message.

Targeted opening ccAEAD: a generic construction. Unfortunately, none of existing constructions of ccAEAD satisfies targeted opening, since their opening algorithm will reveal the whole information about the message. To follow the generic commit-then-encrypt methodology in [5] to construct a ccAEAD and also to support targeted opening, we propose a modular approach. We first introduce a cryptographic notion of targeted opening commitment scheme (TOC for short). TOC is similiar to some more advanced notions like a functional commitment [7] or vector commitment [1], since it allows one to open any part of the message while the rest remain hidden, and to confirm that the partial message is indeed extracted from the exact bit positions of the original message. However, different the previous notions, TOC additionally requires a property named efficiently checkable, which intuitively means if a commitment can be opened respect to the entire message, it can be successfully targeted opened respect to any positions. This property is important to guarantee sender binding of the TOCE scheme, which requires that the decryption algorithm of the TOCE scheme can make sure that the commitment can be successfully targeted opened according to the decrypted message. But in the reality the decryption algorithm can not check all kinds of targeted opening, since the number of selecting partial positions is exponentially large. We provide a very simple initiation of TOC that only utilizes collision resistant hash. We then give a generic construction of TOCE from a TOC scheme and an AEAD scheme, together with a detailed security analysis.

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Targeted opening ccAEAD: more efficient constructions. Our generic construction leverages bitwise operations thus incurs large overhead for encryption, which makes the scheme only applicable when encrypting short messages such as texts. To also consider the applicability in the setting of encrypting large messages such as pictures, and even videos, we set forth to consider more efficient constructions. We first consider a block-wise targeted opening. However, straightforward instantiation of our generic construction, yields an encryption algorithm that needs four passes of block cipher operations for a message string. We observe that, if we reuse some intermediate results of the encryption part to the commitment part, we can construct a nonce based block wise TOCE with three passes in the random oracle model. Furthermore, if we weaker the confidentiality definition and allow the unopened message part to be one-way secure instead of semantic secure, we can get a construction of TOCE with only two passes. Note that even for our latter weaker version construction, its security is still strictly stronger than previous ccAEAD constructions in [5, 2].

Scheme	Without Opening	Targeted Opening	Pass
CtE1/CtE2[5]	Semantic	No	2
CEP [5]	Semantic	No	2
HFC [2]	Semantic	No	1
CEP2 [6]	Semantic	No	2
CEP-AOP1/2 [6]	Semantic	Semantic	4
TOCE	Semantic	Semantic	4
bTOCE	Semantic	Semantic	3
wbTOCE	Semantic	One-Way	2

Table 1. Comparison for existing schemes. **Without Opening** and **Targeted Opening** denote the security level of the confidentiality without opening and targeted opening respectively. **Pass** denotes the complexity of encryption and decryption.

Related work and Comparisons. Grubs et al. [5] initiated a systematic formal study of message franking, and formalized a cryptographic scheme called compactly committing authenticated encryption with associated data (ccAEAD). The authors did a thorough examination of existing concrete AEAD schemes and generic constructions in use. Finally, they also provided a nonce based construction for ccAEAD with two passes, which is as efficient as our weaker confidentiality TOCE. Dodis et al. [2] demonstrated a concrete attack that the Facebook message franking scheme is actually insecure. They also gave an efficient construction of ccAEAD that only involves a one-pass of symmetric key ciphers. We stress that all constructions do not support a selective opening of only a part of the plaintext.

Concurrent work. Recently Leontiadis and Vaudeny [6] considered a similar security definition for the message franking scheme, named after opening privacy.

This property allows only the abusive blocks are opened while the rest non-abusive blocks of the message remain private. In our paper, we further consider other properties, such as integrity, sender binding and receiver binding under the targeted open capability. Leontiadis and Vaudeny also gave two constructions to show feasibility, thus their constructions at least need four passes block cipher operations, while our efficient construction reduces it to three and even fewer when taking the privacy-efficiency trade off.

2 Preliminary and Background

In this section, we explain several definitions of cryptographic primitives necessary as our preliminary.

2.1 Classical cryptographic primitives

Let $\{0,1\}^n$ denote the bit string with length n. Specifically, $\{0,1\}^*$ denote the bit string with arbitrary length.

Nonce-based pseudorandom generator. a nonce based pseudo random generator (PRG) $\mathcal{G}$ is a deterministic algorithm that takes as input a key K, a nonce N, and an output length l. It outputs a string of length l bits. The PRG advantage of an adverary $\mathcal{A}$ against $\mathcal{G}$ is defined by

$$\mathbf{Adv}_G^{prg}(\mathcal{A}) = \left| \Pr_{K \leftarrow \{0,1\}^k} \left[\mathcal{A}^{G(K,\cdot,\cdot)} = 1 \right] - \Pr \left[\mathcal{A}^{R(\cdot,\cdot)} = 1 \right] \right|$$

where R works as follows. On query N, l it checks if a previous query N,l' was submitted. If $l' < l$ it picks a new random string of length $l - l'$, appends it to the previous returned string for N, records it in a table indexed by N, and returns the concatenated random string. If no previous query exists, then it picks a random string of length l, records and then returns it. We call a PRG adversary $\mathcal{A}$ nonce-respecting if all its queries use a unique nonce N. One can build a nonce-based pseudorandom generator from a block cipher in CTR mode.

Commitment scheme. A commitment scheme with verification $\mathsf{CS} = (\mathsf{Com}, \mathsf{VerC})$ consist of two algorithms. Associated to any commitment scheme is an opening space $\mathcal{K}_f \subseteq \{0,1\}^*$, and a commitment space $\mathcal{C} \subseteq \{0,1\}^*$. The algorithm Com is randomized and takes as input a $M \in \{0,1\}^*$ and outputs a pair $(K,C) \in \mathcal{K}_f \times \mathcal{C}$ or an error symbol $\perp$. We assume that Com return $\perp$ with probability one if $M \notin \mathcal{M}$. The algorithm VerC is deterministic. It takes input a tuple $(K,C,M) \in \{0,1\}^*$ and outputs a bit. We assume that VerC returns 0 if its input $(K,C,M) \notin \mathcal{K}_f \times \mathcal{C} \times \mathcal{M}$.

- *Correctness.* A commitment is correct if for all $M \in \mathcal{M}$, $\Pr[\mathsf{VerC}(\mathsf{Com}(M), M) = 1]$ where the probability is over the coins used by Com

- *Binding.* A commitment is binding if no (computational or unbounded) adversary can output a tuple (K_c, M, K'_c, M', C) where both (K_c, M, C) and (K'_c, M', C) can pass the verification.
- *Hiding.* A commitment is hiding if a commitment is indistinguishable from a random bit string while the opening remaining secret.

Merkle Tree. A Merkle tree is a (binary) tree in which every leaf node is labelled with the hash of a data block and every non-leaf node is labelled with the cryptographic hash of the labels of its child nodes. Merkle trees allow efficient and secure verification of the contents of large data structures. To prove whether a value c_i is one of leafs corresponding to a root R, we just need to provide all the siblings of all the nodes on the path from the leaf c_i to the root R. We call all these values are a Merkle proof for c_i, which can be denoted as π_i in the following. This proof π_i not only show that c_i is indeed one of the leafs, but also proved c_i is in the ith position of the string of all leafs $c_1, \ldots, c_l$. Note that the size of π is logarithmic to the number of the leafs.

Authenticated encryption with associated data. The AEAD is a variant of authenticated encryption (AE) where the data to be encrypted needs both authentication and integrity as opposed to just integrity. It is required, for example, by network packets. The header needs integrity, but must be visible; payload, instead, needs integrity and also confidentiality. Both need authenticity. Similar to AE, AEAD consist of three algorithms (AEAD.KeyGen, AEAD.Enc, AEAD.Dec).

- AEAD.KeyGen(1^λ): Given the security parameter λ, output a security key K.
- AEAD.Enc(K, H, M): Given the secret key K, the header H, the message M, output the ciphertext C.
- AEAD.Dec(K, H, M): Given the secret key K, the header H, the ciphertext C, output the message M or a error symbol $\perp$.
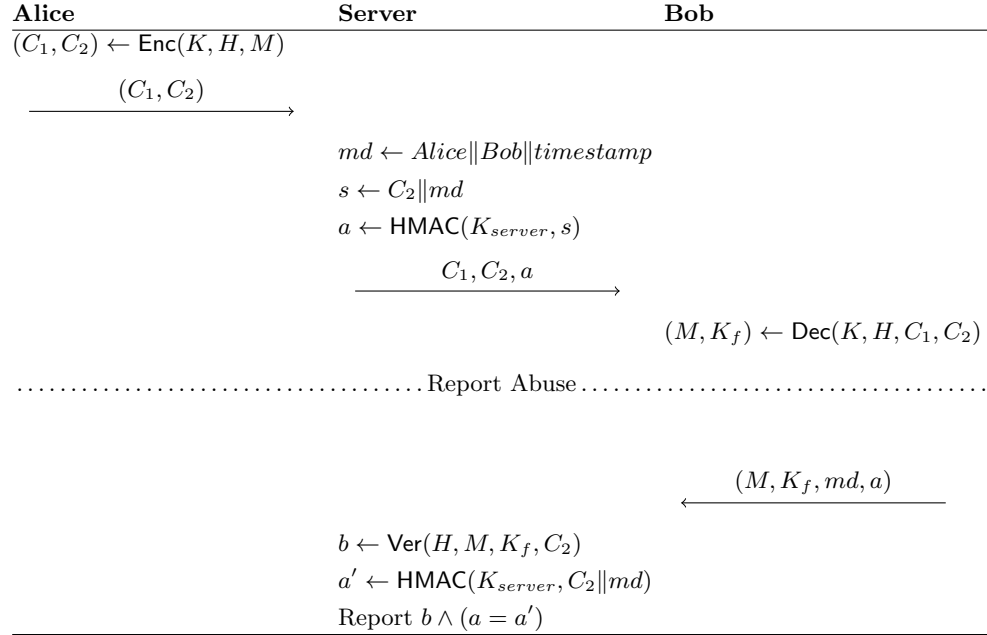
2.2 ccAEAD and message franking

In this section, we will revisit the definition of ccAEAD in [5], and how the kidnapping attack works.

Definition of ccAEAD A committing AEAD scheme CE consists of four algorithms (KeyGen, Enc, Dec, Ver). Let us represent the key space as $\mathcal{K} \subseteq \{0,1\}^*$, the header space as $\mathcal{H} \subseteq \{0,1\}^*$, the message space as $\mathcal{M} \subseteq \{0,1\}^*$, the ciphertext space as $\mathcal{C} \subseteq \{0,1\}^*$, the opening space as $\mathcal{K}_f \subseteq \{0,1\}^*$, and the franking tag space $\mathcal{T} \subseteq \{0,1\}^*$.

- KeyGen: The randomized key generation algorithm KeyGen outputs a secret key $K \in \mathcal{K}$.
- Enc: The randomized algorithm Enc takes a triple $(K, H, M) \in \mathcal{K} \times \mathcal{H} \times \mathcal{M}$ as input and outputs a pair $(C_1, C_2) \in \mathcal{C} \times \mathcal{T}$. Here C_1 is the ciphertext and C_2 is the franking tag.

- Dec: The deterministic algorithm Dec takes a tuple $(K, H, C_1, C_2) \in \mathcal{K} \times \mathcal{H} \times \mathcal{C} \times \mathcal{T}$ as input and outputs a message, opening value pair $(M, K_f) \in \mathcal{M} \times \mathcal{K}_f$ or a distinguished error symbol $\perp$.
- Verify: The deterministic algorithm Ver takes a tuple $(H, M, K_f, C_2) \in \mathcal{H} \times \mathcal{M} \times \mathcal{K}_f \times \mathcal{T}$ as input and output a bit b. Specifically, we assume that Ver outputs 0 for $(H, M, K_f, C_2) \notin \mathcal{H} \times \mathcal{M} \times \mathcal{K}_f \times \mathcal{T}$.

Definition of nessage franking. We notice that in the verification algorithm, the input includes the entire message.

Alice	Server	Bob
$(C_1, C_2) \leftarrow \mathsf{Enc}(K, H, M)$		

$\xrightarrow{\quad (C_1, C_2) \quad}$

$md \leftarrow Alice\|Bob\|timestamp$
$s \leftarrow C_2\|md$
$a \leftarrow \mathsf{HMAC}(K_{server}, s)$

$\xrightarrow{\quad C_1, C_2, a \quad}$

$(M, K_f) \leftarrow \mathsf{Dec}(K, H, C_1, C_2)$

....Report Abuse.......................................

$\xleftarrow{\quad (M, K_f, md, a) \quad}$

$b \leftarrow \mathsf{Ver}(H, M, K_f, C_2)$
$a' \leftarrow \mathsf{HMAC}(K_{server}, C_2\|md)$
Report $b \wedge (a = a')$

Since in the report phase, Bob will provide the whole message to the server, otherwise the server can not proceed the correct verification.

Security definition of ccAEAD. For a secure CE scheme, we require that it can satisfies the following properties: confidentially, ciphertext integrity, sender binding and receiver binding.

Specifically, the confidentially can be defined as the difference between the probability of returning 1 in the game $\mathrm{REAL}_{CE}^{\mathcal{A}}$ and $\mathrm{RAND}_{CE}^{\mathcal{A}}$ in Figure 2.2 is negligible, while the integrity is defined as the probability of returning 1 in the game $\mathrm{RAND}_{CE}^{\mathcal{A}}$ is negligible.

The CE scheme not only require confidentially and ciphertext binding, but also the sender binding security and the receiver binding security. Sender binding ensures the sender of a message is bound to the message it actually sent. This property can prevent the sender to generate a bogus commitment that does not give the receiver the ability to report the message. It is formal defined as that the

$\text{REAL}_{CE}^{\mathcal{A}}$
$K \leftarrow \mathsf{KeyGen}$
$b \leftarrow \mathcal{A}^{\mathbf{Enc},\mathbf{Dec},\mathbf{ChalReal}}$
Return b

$\text{RAND}_{CE}^{\mathcal{A}}$
$K \leftarrow \mathsf{KeyGen}$
$b \leftarrow \mathcal{A}^{\mathbf{Enc},\mathbf{Dec},\mathbf{ChalRand}}$
Return b

$\text{CTXT}_{CE}^{\mathcal{A}}$
$K \leftarrow \mathsf{KeyGen}; \; win \leftarrow 0$
$\mathcal{A}^{\mathbf{Enc},\mathbf{Dec},\mathbf{ChalDec}}$
Return win

Oracle $\mathbf{Enc}(H, M)$
$(C_1, C_2) \leftarrow \mathsf{Enc}_K(H, M)$
$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{(H, C_1, C_2)\}$
Return (C_1, C_2)

Oracle $\mathbf{Dec}(H, C_1, C_2)$
If $(H, C_1, C_2) \notin \mathcal{Y}_1$
    then Return $\bot$
$(M, K_f) \leftarrow \mathsf{Dec}_K(H, C_1, C_2)$

Oracle $\mathbf{Dec}^*(H, C_1, C_2)$
Return $\mathsf{Dec}_K(H, C_1, C_2)$

Oracle $\mathbf{ChalReal}(H, M)$
$(C_1, C_2) \leftarrow \mathsf{Enc}_K(H, M)$
Return (C_1, C_2)

Oracle $\mathbf{ChalRand}(H, M)$
$(C_1, C_2) \leftarrow \mathcal{C} \times \mathcal{T}$
Return (C_1, C_2)

Oracle $\mathbf{ChalDec}^*(H, C_1, C_2)$
If $(H, C_1, C_2) \in \mathcal{Y}$
    Return $\bot$
$(M, K_f) \leftarrow \mathsf{Dec}_K(H, C_1, C_2)$
If $M \neq \bot$
    then $win \leftarrow 1$
Return (M, K_f)

Fig. 1. Security Games for confidentially and integrity for ccAEAD

probability of the game s-$\text{BIND}_{CE}^{\mathcal{A}}$ on the left column of returning ture of Figure 2 is negligible. The receiver binding is adopted from the traditional binding notions for the commitment. It formalizes the intuition that a malicious receiver should not be able to accuse a non-abusive sender of having said something malicious, which can be defined as the probability of the game r-$\text{BIND}_{CE}^{\mathcal{A}}$ return 1 on the right column of Figure 2 is negligible.

$s - BIND_{CE}^{\mathcal{A}}$
$(K, H, C_1, C_2) \leftarrow_{\$} \mathcal{A}$
$(M', K_f) \leftarrow \mathsf{Dec}(K, H, C_1, C_2)$
If $M' = \bot$ then Return false
$b \leftarrow \mathsf{Ver}(H, M', K_f, C_2)$
If $b = 0$ then
    Return true
Return false

$r - BIND_{CE}^{\mathcal{A}}$
$((H, M, K_f), (H', M', K_f'), C_2) \leftarrow_{\$} \mathcal{A}$
$b \leftarrow \mathsf{Ver}(H, M, K_f, C_2)$
$b' \leftarrow \mathsf{Ver}(H', M', K_f', C_2)$
If $(H, M) = (H', M')$ then
    Return false
Return$(b = b' = 1)$

Fig. 2. The security games for the binding properties for ccAEAD.

3   Targeted Opening Compactly Committing AEAD

As briefly discussed in the introduction, a foxy attacker in a message franking scheme (or the underlying ccAEAD scheme) could leverage the fact that recip-

ients may be reluctant to report an abusive message if his private information is contained in the session plaintext, when the opening requires the recipient to reveal the whole piece of the plaintext. The attacker could intentionally embed private information about the recipient to make abuse reporting functionality essentially nullified. For this reason, we initiate a systematic study about targeted opening property in a ccAEAD scheme. The targeted opening property allows a recipient to pick exclusively the abusive message from the plaintext, only revealing the abusive message to the server as evidence, while keep all other plaintext still confidential.

A TOCE scheme consists of five algorithms, i.e., $\mathsf{TOCE} = (\mathsf{KG}, \mathsf{Enc}, \mathsf{Dec}, \mathsf{TOpen}, \mathsf{TVer})$. Let us represent the key space as $\mathcal{K} \subseteq \{0,1\}^*$, the header space as $\mathcal{H} \subseteq \{0,1\}^*$, the message space as $\mathcal{M} \subseteq \{0,1\}^*$, the ciphertext space as $\mathcal{C} \subseteq \{0,1\}^*$, the opening space as $\mathcal{K}_f \subseteq \{0,1\}^*$, the targeted opening space as $\mathcal{S} \subseteq \{0,1\}^*$ and the franking tag space $\mathcal{T} \subseteq \{0,1\}^*$.
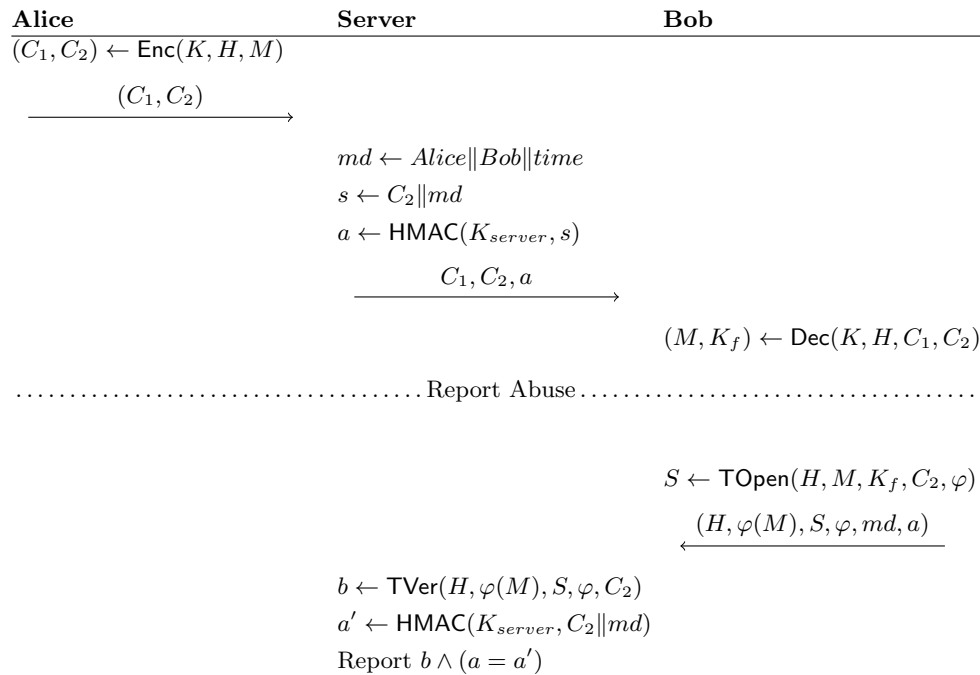
Before we describe the syntax, we first define the position function φ as follows. If M is a bit string with length n, φ is a function that take as input the message M, picks the bits of M with the indices $\{i_1, i_2, \ldots, i_j\}$, (for each index chosen from $\{1, \ldots, n\}$) depending on φ's definition. Without loss of generality, we denote the identity function I as choosing all the positions from $\{1, \ldots, n\}$, i.e., $I(M) = M$. We define the space of all position functions as Φ.

- **Key generation**: The randomized algorithm KeyGen outputs a secret key $K \in \mathcal{K}$.

- **Encryption**: The randomized algorithm Enc takes a triple $(K, H, M) \in \mathcal{K} \times \mathcal{H} \times \mathcal{M}$ as input and outputs a pair $(C_1, C_2) \in \mathcal{C} \times \mathcal{T}$. Here C_1 is the ciphertext that carries the payload and C_2 is the franking tag, and H is the associated data.

- **Decryption**: The deterministic algorithm Dec takes a tuple $(K, H, C_1, C_2) \in \mathcal{K} \times \mathcal{H} \times \mathcal{C} \times \mathcal{T}$ as input and outputs a message and opening value pair $(M, K_f) \in \mathcal{M} \times \mathcal{K}_f$ or the error symbol $\perp$.

- **Targeted open**: The deterministic algorithm TOpen takes as input a tuple $(H, M, K_f, C_2, \varphi) \in \mathcal{H} \times \mathcal{M} \times \mathcal{K}_f \times \mathcal{T} \times \Phi$, and outputs the targeted value represented as $\varphi(M)$ and the corresponding targeted opening S.

- **Verification**: The deterministic algorithm TVer takes as input a tuple values of $(H, \varphi(M), S, \varphi, C_2)$ and output a bit b. Specifically, we assume that Ver outputs 0 if the targeted opening is not valid.

Compactness. Similarly to previous work [5, 2], we also require the tocc-AEAD scheme to be compact, which means the length of the tag part of the ciphertext is independent with the message length. This is important for the server to authenticate the tag and even store the short tag.

With the revised syntax, the message franking protocol would now be modified correspondingly as follows.

Correctness. We say a TOCE scheme has decryption correctness if for all $(K, H, M) \in \mathcal{K} \times \mathcal{H} \times \mathcal{M}$ it holds that $\Pr[\mathsf{Dec}(K, H, C_1, C_2) = M] = 1$ where

Alice	Server	Bob
$(C_1, C_2) \leftarrow \mathsf{Enc}(K, H, M)$		

$$\xrightarrow{\quad (C_1, C_2) \quad}$$

$md \leftarrow Alice\|Bob\|time$

$s \leftarrow C_2\|md$

$a \leftarrow \mathsf{HMAC}(K_{server}, s)$

$$\xrightarrow{\quad C_1, C_2, a \quad}$$

$(M, K_f) \leftarrow \mathsf{Dec}(K, H, C_1, C_2)$

.........................Report Abuse.........................

$S \leftarrow \mathsf{TOpen}(H, M, K_f, C_2, \varphi)$

$$\xleftarrow{\quad (H, \varphi(M), S, \varphi, md, a) \quad}$$

$b \leftarrow \mathsf{TVer}(H, \varphi(M), S, \varphi, C_2)$

$a' \leftarrow \mathsf{HMAC}(K_{server}, C_2\|md)$

Report $b \wedge (a = a')$

Fig. 3. Message franking supporting targeted opening

the probability is taken over the coins in the key generation Kg and the encryption Enc. We say a target commitment ccAEAD scheme has targeted open commitment correctness if for all $(H, M, S, \varphi) \in \mathcal{H} \times \mathcal{M} \times \mathcal{S} \times \varPhi$ it holds that

$$\Pr[\mathsf{TVer}(\varphi(M), S, \varphi, C_2) = 1] = 1$$

where the probability is taken over the random variables in the following procedure:

1. $K \leftarrow_\$ \mathsf{KeyGen}$;
2. $(C_1, C_2) \leftarrow_\$ \mathsf{Enc}_K(H, M)$;
3. $(M, K_f) \leftarrow \mathsf{Dec}_K(H, C_1, C_2)$;
4. $S \leftarrow \mathsf{TOpen}(H, M, K_f, C_2, \varphi)$.

3.1 Security definitions

In this subsection, we will give a detailed characterization of the security notions in the new setting allowing targeted opening (which could be multiple times for the same plaintext). We note that a TOCE would still satisfy the confidentiality, ciphertext integrity, sender binding, and receiver binding, but all of them are influenced by the targeted opening functionality thus we need to adapt carefully.

Message confidentiality. In a TOCE scheme, we require that the messages bits that have not been opened, remain semantically secure. This requires no single bit of information will be leaked except the explicitly revealed part. In the TO-IND game defined in Fig 4 below, we further allow the adversary to have access to **TOpen** oracle. To avoid trivial impossibility, we require that for the two challenge messages, the opened part to be identical. It is straightforward that if the recipient does not open any bits, the standard IND-CPA security will apply.

Ciphertext integrity. We also require that any adversary without the secret key can not generate new valid ciphertexts from existing ciphertexts. Thus we define the TO-CTXT game in Fig 4. Similarly, we allow the adversary to query the **TOpen** oracle.

Sender binding ensures the sender of a message is bound to the message it actually sent. So we define the TO-s-BIND game in Fig 4. In this game, we require that a valid ciphertext which is decrypted to M' can be successfully targeted opened according to *any* position function φ and pass the verification algorithm for the opening S, the partial message $\varphi(M')$ and the position function φ. Previously, a CE scheme can generically meet sender binding by running the verification algorithm during the decryption and return $\perp$ if the verification returns 0 [2]. However, since the space of the position function $\varPhi$ is exponentially large, we can not add the verification step for all φ in the decryption algorithm. The proof for the sender binding property for TOCE scheme is highly non-trivial.

Receiver binding ensures the receive can not maliciously open the ciphertext to two different message. This is shown in the TO-r-BIND game in Fig 4. Different with the previous CE scheme, we do not require the adversary to output two whole messages, but simply two partial messages and a position function. Besides, we also provide the **TOpen** oracle to the adversary.

3.2 A generic construction of toccAEAD

In this subsection, we introduce a generic construction for the desired toccAEAD scheme. This construction follows the commitment-then-encrypt mythology. To satisfy the targeted opening property, we propose the notion of *targeted opening commitment* (TOC) and provide a candidate construction for TOC. Follow the strategy of TOC-then-encrypt, we can easily obtain the construction of toccAEAD.

Targeted opening commitment scheme is a new primitive that allows to commit an bit string with length ℓ in such a way that one can later open the commitment of certain segments at specific positions (or arbitrary non-consecutive substring), so it can open in a way that m_i is the i-th bit of the committed message[1]. Specifically, TOC can be formalized as following four algorithms.

- TOC.Setup(1^λ): Given the security parameter λ, the key generation outputs some public parameters pp.
- TOC.Com(pp, M): On input a bit string M and the public parameters pp, the committing algorithm outputs a commitment string C and the commit key K.
- TOC.TOpen (pp, C, K, φ, M) : On input the public parameter pp, the commitment C, the commitment key K, the position function φ and the message M. This target opening algorithm is to produce a opening S which prove that $\varphi(M)$ consists of the certain bits according to the position function φ.
- TOC.TVer(pp, C, S, m, φ): The verification algorithm accepts (i.e., it outputs 1) only if S is a valid proof that C was created to a bit string M such that $\varphi(M) = m$.

In the most settings, we can assume that the TOC.Setup all ready exists, and one takes the public parameter pp as implicit input for other tree algorithms. So we usually can omit them in scheme descriptions. A TOC scheme must satisfy the correctness, i.e., if Com(M) = C and S = TOC.TOpen(C, K, φ, M) for any φ, the probability $\Pr(\text{TOC.TVer}(C, S, m, \varphi) = 0)$ is negligible.

The target opening commitment meets an attractive security requirement named position binding. Informally, this says that it should be infeasible, for any polynomially bounded adversary having knowledge of pp, to come up with

---

[1] We may view a TOC as a special case of the more general notion of vector commitment [1] or functional commitment [7]. Both of them rely on algebraic structure and public key operations. We formulate the notion of ToC simply for the sake of potential efficient constructions that are more suitable for secure messaging.

TO-IND$_{CE}^{\mathcal{A}}$
$K \leftarrow_\$ \mathsf{KeyGen}$
$state \leftarrow \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}$
$\{H^*, (M_0, M_1)\} \leftarrow_\$ \mathcal{A}(st)$
$b \leftarrow_\$ \{0, 1\}$
$(C_1^*, C_2^*) \leftarrow \mathsf{Enc}_K(H^*, M_b)$
$b' \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}(C_1^*, C_2^*, st)$
Return $b = b'$

TO-CTXT$_{CE}^{\mathcal{A}}$
$K \leftarrow_\$ Kg$
win $\leftarrow$ false
$\mathcal{A}^{\mathbf{Enc,Dec^*,TOpen,ChalDec}}$
Return win

TO-r-BIND$_{CE}^{\mathcal{A}}$
$((m, S), (m', S'), C_2, \varphi) \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}$
$b \leftarrow \mathsf{TVer}(m, S, C_2, \varphi)$
$b' \leftarrow \mathsf{TVer}(m, S', C_2, \varphi)$
If $m = m'$ then
$\qquad$ Return false
Return$(b = b' = 1)$

TO-s-BIND$_{CE}^{\mathcal{A}}$
$(K, H, C_1, C_2, \varphi) \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}$
$(M', K_f) \leftarrow \mathsf{Dec}(K, H, C_1, C_2)$
If $M' = \bot$ then Return false
$S \leftarrow \mathsf{TOpen}(H, M', K_f, C_2, \varphi)$
$b \leftarrow \mathsf{TVer}(H, \varphi(M'), S, C_2)$
If $b = 0$ then Return true
Else Return false

Oracle $\mathbf{Enc}(H, M)$
$(C_1, C_2) \leftarrow \mathsf{Enc}_K(H, M)$
$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{(H, C_1, C_2)\}$
Return (C_1, C_2)

Oracle $\mathbf{Dec}(H, C_1, C_2)$
If $(H, C_1, C_2) \notin \mathcal{Y}_1$
$\quad$ then Return $\bot$
If $(H, C_1, C_2) = (H^*, C_1^*, C_2^*)$
$\quad$ then Return $\bot$
$(M, K_f) \leftarrow \mathsf{Dec}_K(H, C_1, C_2)$
Return (M, K_f)

Oracle $\mathbf{TOpen}(H, C_1, C_2, \varphi)$
If $(H^*, C_1^*, C_2^*) = (H, C_1, C_2)$ then
$\quad$ If $\varphi(M_0) \neq \varphi(M_1)$ then
$\qquad$ Return $\bot$
If $(H, C_1, C_2) \notin \mathcal{Y}_1$ then
$\quad$ Return $\bot$
$(M, K_f) \leftarrow \mathsf{Dec}_K(H, C_1, C_2)$
$(\varphi(M), S) \leftarrow \mathsf{TOpen}_K(M, K_f, \varphi)$
Return $(m = \varphi(M), S)$

Oracle $\mathbf{Dec}^*(H, C_1, C_2)$
Return $\mathsf{Dec}_K(H, C_1, C_2)$

Oracle $\mathbf{ChalDec}(H, C_1, C_2)$
If $(H, C_1, C_2) \in \mathcal{Y}_1$ then
$\quad$ Return $\bot$
$(M, K_f) \leftarrow \mathsf{Dec}_K(H, C_1, C_2)$
If $M \notin \bot$ then
$\quad$ win $\leftarrow$ true

Fig. 4. Security games for TOCE

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a commitment C and two different valid openings for the same position i. More formally:

Definition 1 (Position Binding). *A TOC scheme satisfies position binding if for every PPT adversary $\mathcal{A}$ and position function φ the following probability (which is taken over all honestly generated parameters) is at most negligible in λ, i.e.,*

$$\Pr[(C, m, m', S, S', \varphi) \leftarrow_\$ \mathcal{A}] \leq \mathsf{negl}(\lambda)$$

where $\mathsf{TOC.TVer}(C, m, S, \varphi) = 1$, $\mathsf{TOC.TVer}(C, m', S', \varphi) = 1$ and $m \neq m'$.

A TOC scheme also requires the targeted hiding property, i.e., the bits that have not been opened will remain semantically secure. Informally, a TOC scheme is targeted hiding if an adversary cannot distinguish whether a commitment was created to a bit string M or to M', even after seeing some openings at certain bit positions where the two bit strings agree.

Definition 2 (Targeted Hiding). *A TOC scheme satisfies targeted hiding if for every PPT adversary $\mathcal{A}$ and position function φ,*

$$\left| \Pr(\textit{T-HIDE}^{\mathcal{A}} \Rightarrow 1) - 1/2 \right| \leq \mathsf{negl}(\lambda),$$

where the T-HIDE game is defined in Fig 5 and the probability is taken over all honestly generated parameters.

T-HIDE$^{\mathcal{A}}$	Oracle **TOpen**(C, φ)
$1:$ $b \leftarrow_\$ \{0, 1\}$	$1:$ **if** $C = C^*$
$2:$ $pp \leftarrow_\$ \mathsf{KeyGen}$	$2:$ **if** $\varphi(M_0) \neq \varphi(M_1)$
$3:$ $(M_0, M_1) \leftarrow_\$ \mathcal{A}(pp)$	$3:$ **return** $\perp$
$4:$ $(C^*, K_f) \leftarrow_\$ \mathsf{TOC.Com}(pp, M_b)$	$4:$ **else** $S \leftarrow \mathsf{TOC.TOpen}(pp, C, K_f, \varphi, M)$
$5:$ $b' \leftarrow_\$ \mathcal{A}^{\textbf{TOpen}}(1^n, pp, C)$	$5:$ **return** $(S, \varphi(M))$
$6:$ **return** $b = b'$	

Fig. 5. The security game for targeted hiding

Another important property we need is named *efficient checkable*. Intuitively, this property guarantees that the no adversary can generate a malicious commitment which successful targeted verified according to the identity function I, but can not be successful verified according to some other position function φ. This property is important for the proof of sender binding property for the following generic construction of TOCE scheme. Formally, we have

Definition 3 (Efficient Checkable). *A TOC scheme satisfies efficient checkable if for every PPT adversary $\mathcal{A}$, the probability of outputting a commitment C, a position function ϕ and a message M, which satisfy*

- *$S_1 = \mathsf{TOC.TOpen}(C, K, I, M)$ and $\mathsf{TOC.TVer}(C, M, S, I) = 1$;*
- *$S_2 = \mathsf{TOC.TOpen}(C, K, \varphi, M)$ and $\mathsf{TOC.TVer}(C, \varphi(M), S_2, \varphi) = 0$,*

is negligible.

A simple instantiation of TOC. We can give a very simply construction of TOC that only involves the collision resistant hash function. Intuitively, this construction is obtained by using bit commitment scheme to commit each bit of the message, and then hash all the commitment value together.

- $\mathsf{TOC.Com}(M)$: On input a bit string $M = m_1 m_2 \ldots m_\ell$ with length ℓ, and the public parameters pp, the committing algorithm first commits each bit running the bit commitment algorithm $\mathsf{bCom}(m_i, pp)$ and outputs a commitment c_i and the opening r_i. In particular, bCom can be instantiated simply with a collision resistant hash. Then apply a collision resistant hash H on the commitments of the message bit to build a Merkle tree using $c_1, \ldots, c_\ell$ as leaves, and the resulting root is denoted as C. The algorithm outputs commitment C and openings (or commitment key) $K := r_1, \ldots, r_\ell$.

- $\mathsf{TOC.TOpen}\ (C, K, \varphi, M)$: On input the public parameter pp, the commitment C, the commitment key K, the position function ϕ and the message M. This target opening algorithm first evaluates $\varphi(M)$, suppose $\varphi(M) := \{m_{i_j}\}$, where i_j is the index that the corresponding bit to be opened. For each i_j, the algorithm first reveals c_{i_j} and the corresponding Merkle proof π_{i_j}, and the corresponding openings r_{i_j}

- $\mathsf{TOC.TVer}(C, S, m, \varphi)$: For each i_j, the verification algorithm first checks whether the Merkle proof π_{i_j} is correctly formed, and then checks whether $h(m_{i_j}, r_{i_j}) = c_{i_j}$. If all passes, the algorithm outputs 1, otherwise outputs 0.

Security sketch. The above construction is fairly simple, we only briefly explain the security here and defer a detailed proof to the full version. Regarding position binding, it is fairly easy to see. For an index i, supposed it is opened, the actual commitment c_i with its Merkle proof can be verified. Then following the property of the underlying bit commitment , the opening of c_i can be ensured by the binding property (or simply the collision resistance of the hash). Regarding targeted hiding, in the first step, the revealed contains only information about commitments of the unopened message bits, which are simulatable with nothing, thus the remaining bits are still semantically secure.

A generic construction of toccAEAD. Here we will provide a generic construction TOCtE of toccAEAD from a TOC scheme TOC=($\mathsf{TOC.Com}$,$\mathsf{TOC.TOpen}$, $\mathsf{TOC.TVer}$) and any AEAD scheme AEAD=(AEAD.KeyGen, AEAD.Enc, AEAD.Dec).

- TOCtE.KeyGen(1^λ): On input the security parameter λ, use AEAD.KeyGen to generate the secret key K, and output K as the secret key for the TOCE scheme.

- TOCtE.Enc(K, H, M): On input the secret key K, the header H and the message m, firstly one commits the message M and the header under the TOC scheme and get $(C_2, K_f) = $ TOC.Com($M\|H$) where C_2 is the commitment and K_f is the commit key. Secondly, one takes C_2 as the header of AEAD, encrypts the concatenation of the message M and the commitment key K_f, and get $C_1 = $ AEAD,Enc($K, C_2, M\|K_f$). Finally, the algorithm outputs the ciphertext (C_1, C_2).

- TOCtE.Dec(K, H, C_1, C_2): On input the secret key K, the header H and the ciphertext (C_1, C_2), firstly if $\perp \leftarrow$ AEAD.Dec(K, C_2, C_1) then return $\perp$; otherwise parse the result of AEAD.Dec(K, C_2, C_1) as M and K_f. Secondly, compute $S_I \leftarrow$ TOC.TOpen(C_2, M, K_f, I) for the identity position function I. If TOC.TVer(S_I, K_f, M, I) $= 0$, abort; otherwise return (M, K_f).

- TOCtE.TOpen(H, M, K_f, C_2, φ): On input the header H, the message M, the commit key K_f and the position function φ, suppose the lengths of H and M are l_1 and l_2 respectively, one can define a new position function $\varphi'(\cdot)$ for a bit string with length $l_1 + l_2$ as inputting the first l_1 bits to φ and concatenating the output of φ with next l_2 input bits as it is, i.e., $\varphi'(M\|H) = \varphi(M)\|H$. Then use the target opening algorithm $S \leftarrow$ TOC.TOpen($C_2, M\|H, K_f, \varphi'$) for the extended position function φ'.

- TOCtE.TVer($H, \varphi(M), S, \varphi, C_2$): On input the header H, the partial message $\varphi(M)$, the targeted opening S, the position function φ and the tag C_2, one can get the extended position function φ' just as above. If

$$\text{TOC.TVer}(C_2, S, \varphi(M)\|H, \varphi') = 0,$$

output 0, otherwise output 1.

3.3 Security analysis

In this subsection, we will prove the TOCtE scheme satisfy the confidentiality, integrity, sender binding and receiver binding properties defined in Fig 4.

Theorem 1 (Confidentiality). *Let $TOCtE$ be the generic TOCE scheme described as above, which is based the AEAD scheme and the TOC scheme. Let $\mathcal{A}$ be an adversary for the game TO-IND in Fig 4. Then we give the adversary $\mathcal{B}$ against the hiding property of TOC scheme and the adversary $\mathcal{C}$ against the AEAD scheme, which satisfy*

$$Adv_{\mathcal{A}}^{TOCtE} \leq Adv_{\mathcal{C}}^{AEAD} + Adv_{\mathcal{B}}^{TOC}$$

Proof. We start from the Game 1 in the left column of Fig 6, which is the real game that the adversary faces. According to the confidentiality of the AEAD,

we can replace the encryption result of the AEAD to the encryption of random message, then we get the Game 2.

Next, we will reduce the hiding property of the target opening commitment to Game 2. Precisely, given the adversary $\mathcal{A}$ to attack the Game 2, we can construct an adversary $\mathcal{B}$ to attack the hiding property of the TOC scheme. $\mathcal{B}$ works as follows. He first generates the secret key K for AEAD, provide public parameter for $\mathcal{A}$, then answer the oracles for $\mathcal{A}$. Note that $\mathcal{B}$ can easily answer the Enc oracle by generate the commitment by himself as C_1 and encrypt a random message by K as C_2. $\mathcal{B}$ answer the decryption oracle by search (H, M_1, M_2) in the list $\mathcal{Y}_1$ and find the corresponding (M, K_f). When $\mathcal{A}$ output the message pair (M_1, M_2), $\mathcal{B}$ provide same message pair to the challenger. When the challenger reply the commitment C^*, $\mathcal{B}$ output the challenge ciphertext (C_1^*, C_2^*) to adv where C_1^* is the AEAD encryption of H and a random message M and C_2^* is the commitment.

To answer the oracle **TOpen**, given (H, C_1, C_2, ϕ), if (H, C_1, C_2) is the challenge ciphertext, $\mathcal{B}$ first check whether $\varphi(M_0) \neq \varphi(M_1)$, then use the (C_2, φ) to ask the **TOC.TOpen** oracle and output $S, \varphi(M)$, otherwise return $\bot$. If (H, C_1, C_2) is not the challenge ciphertext, $\mathcal{B}$ first check whether (H, C_1, C_2) is in $\mathcal{Y}_1$. If not, return $\bot$. Otherwise $\mathcal{B}$ can find corresponding (M, K_f) and compute the **TOC.TOpen** by himself.

Finally, we get the result

$$\mathsf{Adv}_{\mathcal{A}}^{TOCtE} \leq \mathsf{Adv}_{\mathcal{C}}^{AEAD} + \mathsf{Adv}_{\mathcal{B}}^{TOC}$$
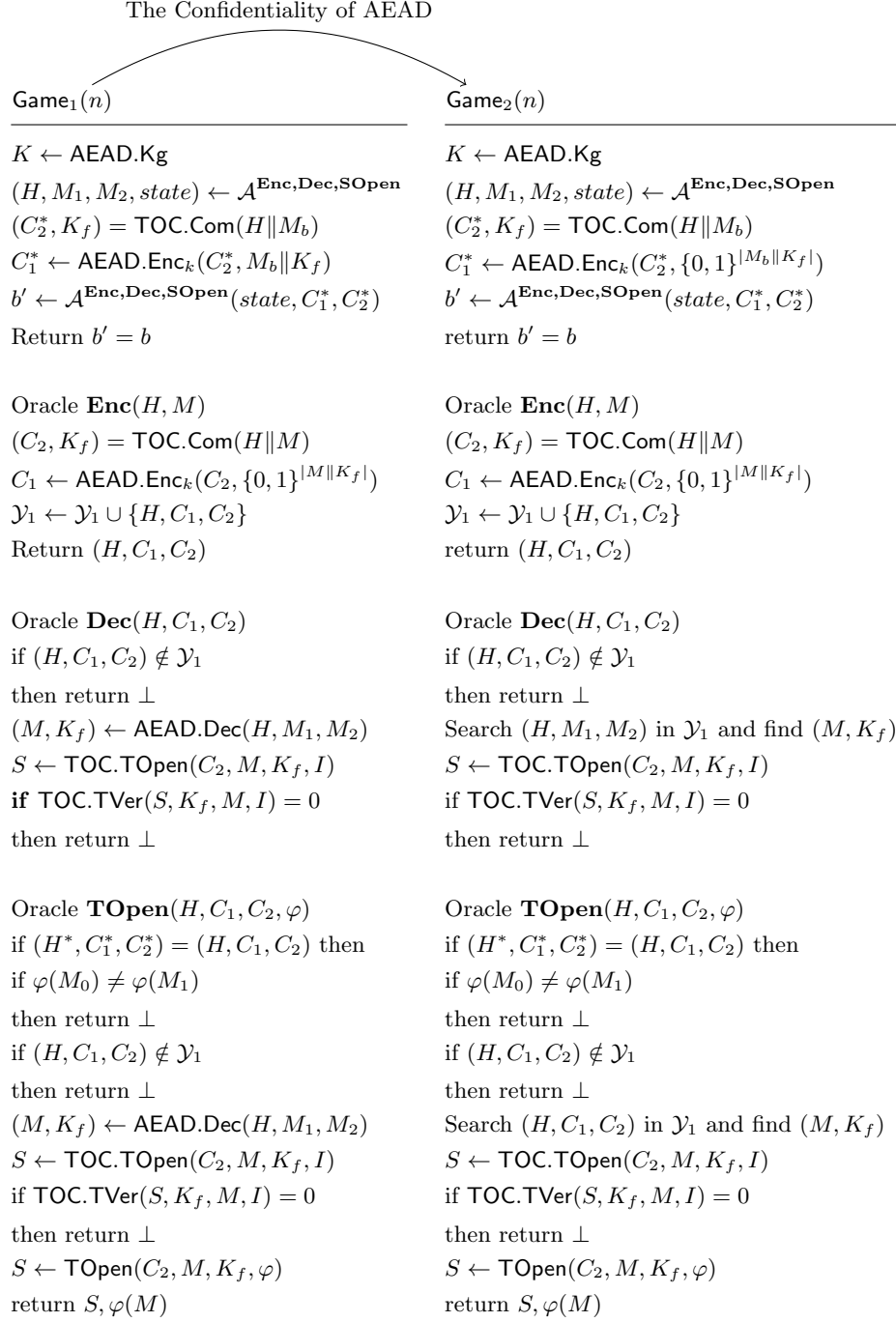
$\square$

Theorem 2 (Integrity). *Let TOCtE be the generic TOCE scheme described as above, which is based the AEAD scheme and the TOC scheme. Let $\mathcal{A}$ be an adversary for the game TO-CTXT in Fig 4. Then we can give adversaries $\mathcal{B}$ against the integrity of the AEAD scheme and $\mathcal{C}$ against the the targeted binding of the TOC scheme, which satisfy*

$$\mathit{Adv}_{\mathcal{A}, TO-CTXT}^{TOCtE} \leq \mathit{Adv}_{\mathcal{C}, CTXT}^{AEAD} + \mathit{Adv}_{\mathcal{B}, BIND}^{TOC}$$

.

Proof.

We have the TO-CTXT game as Fig 7. First of all, we can transform the TO-CTXT game to the game G_1 in Fig 8. The only difference between the TO-CTXT game and the game G_1 is that we replace the oracle **Dec*** and **TOpen** with the oracle **Dec**$'$ and **TOpen**$'$. For the **Dec**$'$ oracle and **TOpen**$'$, the challenger first looks up the existing table to answer the decryption query. If the queried ciphertext does not exist in the table but it still can pass the validity check, the flag win will be setted to true. Then we have that

$$\mathbf{Adv}_{TOCtE}^{TO-CTXT}(\mathcal{A}) \leq \Pr[G_1^{\mathcal{A}} \Rightarrow \mathsf{true}]$$

The Confidentiality of AEAD

$\mathsf{Game}_1(n)$	$\mathsf{Game}_2(n)$

$K \leftarrow \mathsf{AEAD.Kg}$

$(H, M_1, M_2, state) \leftarrow \mathcal{A}^{\mathbf{Enc,Dec,SOpen}}$

$(C_2^*, K_f) = \mathsf{TOC.Com}(H\|M_b)$

$C_1^* \leftarrow \mathsf{AEAD.Enc}_k(C_2^*, M_b\|K_f)$

$b' \leftarrow \mathcal{A}^{\mathbf{Enc,Dec,SOpen}}(state, C_1^*, C_2^*)$

Return $b' = b$

$K \leftarrow \mathsf{AEAD.Kg}$

$(H, M_1, M_2, state) \leftarrow \mathcal{A}^{\mathbf{Enc,Dec,SOpen}}$

$(C_2^*, K_f) = \mathsf{TOC.Com}(H\|M_b)$

$C_1^* \leftarrow \mathsf{AEAD.Enc}_k(C_2^*, \{0,1\}^{|M_b\|K_f|})$

$b' \leftarrow \mathcal{A}^{\mathbf{Enc,Dec,SOpen}}(state, C_1^*, C_2^*)$

return $b' = b$

Oracle $\mathbf{Enc}(H, M)$

$(C_2, K_f) = \mathsf{TOC.Com}(H\|M)$

$C_1 \leftarrow \mathsf{AEAD.Enc}_k(C_2, \{0,1\}^{|M\|K_f|})$

$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{H, C_1, C_2\}$

Return (H, C_1, C_2)

Oracle $\mathbf{Enc}(H, M)$

$(C_2, K_f) = \mathsf{TOC.Com}(H\|M)$

$C_1 \leftarrow \mathsf{AEAD.Enc}_k(C_2, \{0,1\}^{|M\|K_f|})$

$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{H, C_1, C_2\}$

return (H, C_1, C_2)

Oracle $\mathbf{Dec}(H, C_1, C_2)$

if $(H, C_1, C_2) \notin \mathcal{Y}_1$

then return $\bot$

$(M, K_f) \leftarrow \mathsf{AEAD.Dec}(H, M_1, M_2)$

$S \leftarrow \mathsf{TOC.TOpen}(C_2, M, K_f, I)$

if $\mathsf{TOC.TVer}(S, K_f, M, I) = 0$

then return $\bot$

Oracle $\mathbf{Dec}(H, C_1, C_2)$

if $(H, C_1, C_2) \notin \mathcal{Y}_1$

then return $\bot$

Search (H, M_1, M_2) in $\mathcal{Y}_1$ and find (M, K_f)

$S \leftarrow \mathsf{TOC.TOpen}(C_2, M, K_f, I)$

if $\mathsf{TOC.TVer}(S, K_f, M, I) = 0$

then return $\bot$

Oracle $\mathbf{TOpen}(H, C_1, C_2, \varphi)$

if $(H^*, C_1^*, C_2^*) = (H, C_1, C_2)$ then

if $\varphi(M_0) \neq \varphi(M_1)$

then return $\bot$

if $(H, C_1, C_2) \notin \mathcal{Y}_1$

then return $\bot$

$(M, K_f) \leftarrow \mathsf{AEAD.Dec}(H, M_1, M_2)$

$S \leftarrow \mathsf{TOC.TOpen}(C_2, M, K_f, I)$

if $\mathsf{TOC.TVer}(S, K_f, M, I) = 0$

then return $\bot$

$S \leftarrow \mathsf{TOpen}(C_2, M, K_f, \varphi)$

return $S, \varphi(M)$

Oracle $\mathbf{TOpen}(H, C_1, C_2, \varphi)$

if $(H^*, C_1^*, C_2^*) = (H, C_1, C_2)$ then

if $\varphi(M_0) \neq \varphi(M_1)$

then return $\bot$

if $(H, C_1, C_2) \notin \mathcal{Y}_1$

then return $\bot$

Search (H, C_1, C_2) in $\mathcal{Y}_1$ and find (M, K_f)

$S \leftarrow \mathsf{TOC.TOpen}(C_2, M, K_f, I)$

if $\mathsf{TOC.TVer}(S, K_f, M, I) = 0$

then return $\bot$

$S \leftarrow \mathsf{TOpen}(C_2, M, K_f, \varphi)$

return $S, \varphi(M)$

Fig. 6. Security games for the proof for confidentiality.

TO-CTXT

$K \leftarrow \mathsf{AEAD.Kg}$

$\mathsf{win} \leftarrow \mathsf{false}$

$\mathcal{A}^{\mathbf{Enc,Dec,SOpen}}$

return win

Oracle $\mathbf{Enc}(H, M)$

$(C_2, K_f) = \mathsf{TOC.Com}(H\|M)$

$C_1 \leftarrow \mathsf{AEAD.Enc}_k(C_2, M\|K_f)$

$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{H, C_1, C_2\}$

Return (H, C_1, C_2)

Oracle $\mathbf{Dec}^*(H, C_1, C_2)$

if $\perp \leftarrow \mathsf{AEAD.Dec}(H, M_1, M_2)$

  return $\perp$

else $(M, K_f) \leftarrow \mathsf{AEAD.Dec}(H, M_1, M_2)$

    $S \leftarrow \mathsf{TOC.TOpen}(C_2, M, K_f, I)$

    if $\mathsf{TOC.TVer}(S, K_f, M, I) = 0$

      return $\perp$

    else return (M, K_f)

Oracle $\mathbf{TOpen}(H, C_1, C_2, \varphi)$

if $\perp \leftarrow \mathsf{AEAD.Dec}(H, M_1, M_2)$ **then**

  return $\perp$

else $(M, K_f) \leftarrow \mathsf{AEAD.Dec}(H, M_1, M_2)$

  $S \leftarrow \mathsf{TOC.TOpen}(C_2, M, K_f, I)$

  if $\mathsf{TOC.TVer}(S, K_f, M, I) = 0$ **then**

    return $\perp$

    $S \leftarrow \mathsf{TOpen}(C_2, M, K_f, \varphi)$

return $(S, \varphi(M))$

Oracle $\mathbf{ChalDec}^*(H, C_1, C_2)$

if $(H, C_1, C_2) \in \mathcal{Y}_1$

  return $\perp$

if $\perp \leftarrow \mathsf{AEAD.Dec}(H, M_1, M_2)$

  return $\perp$

else $(M, K_f) \leftarrow \mathsf{AEAD.Dec}(H, M_1, M_2)$

    $S \leftarrow \mathsf{TOC.TOpen}(C_2, M, K_f, I)$

    if $\mathsf{TOC.TVer}(S, K_f, M, I) = 0$

      return $\perp$

if $M \neq \perp$

  $\mathsf{win} \leftarrow \mathsf{true}$

    else return (M, K_f)

Fig. 7. The TO-CTXT game for TOCtE

Note that for win to be set with a query (H, C_1, C_2) in Game G_1, it must be that no previous encryption query (H, M) for some M returned (C_1, C_2). Let the winning query be on the values (H^*, C_1^*, C_2^*). We partition the probability of setting win into two cases, either (C_1^*, C_2^*) is distinct from all encryption outputs, or (C_1^*, C_2^*) is one of the encryption outputs and H^* is not the header for the encryption query that returned C_1^*, C_2^*. Let win_H be the event that $\mathcal{A}$ wins with a query where H^* is a different header, and win_C be the event that $\mathcal{A}$ wins with a query where (C_1^*, C_2^*) is distinct. Then $\Pr[G_0^{\mathcal{A}} \Rightarrow \mathsf{true}] \leq \Pr[\mathsf{win}_H] + \Pr[\mathsf{win}_C]$.

We will first bound $\Pr[\mathsf{win}_C]$. In this case we will construct an adversary $\mathcal{B}$ in the CTXT game of AEAD. This adversary simulates G_0 for $\mathcal{A}$, as follows. When $\mathcal{A}$ queries (H, M) to **Enc**, $\mathcal{B}$ first generates a targeted opening commitment and opening K_f, C_2 though $\mathsf{TOC.Com}(M \| H)$. Then, $\mathcal{B}$ queries **Enc** oracle of the CTXT game for AEAD with $(C_2, M \| K_f)$. It stores the result in a table, then outputs C_1, C_2 to $\mathcal{A}$. It simulates $\mathbf{Dec}^*$, $\mathbf{TOpen}'$ and $\mathbf{ChalDec}$ queries that are outputs of previous **Enc** queries by consulting its table and outputting either the proper value (for **Dec** and **TOpen**) or $\perp$ (for **ChalDec**). When $\mathcal{A}$ queries $\mathbf{Dec}^*$, $\mathbf{TOpen}'$ and $\mathbf{ChalDec}$ with a value not in the table, $\mathcal{B}$ submits (C_2, C_1) as a forgery to its decryption oracle, and use the returned results in the further calculations. Our $\mathcal{B}$ perfectly simulates G_1 for $\mathcal{A}$. Since $\mathcal{A}$'s query must be a successful forgery and $\mathcal{B}$ will break CTXT of AEAD in this reduction with probability at least $\Pr[\mathsf{win}_C]$, i.e., $\Pr[\mathsf{win}_C] \leq \mathbf{Adv}_{AEAD}^{CTXT}(\mathcal{B})$.

To bound $\Pr[\mathsf{win}_H]$ and complete the proof we can build another reduction using an adversary $\mathcal{C}$ against the targeted binding property of the TOC scheme. The adversary $\mathcal{C}$ simulates $\mathcal{A}$'s view of G_1 as $\mathcal{B}$ did, except $\mathcal{C}$ generates a random encryption key and computes $\mathsf{AEAD.Enc}$ and $\mathsf{AEAD.Dec}$ internally. When $\mathcal{A}$ makes a query (H, C_1, C_2) to $\mathbf{Dec}^*$, $\mathbf{TOpen}$ or $\mathbf{ChalDec}$ where H is not the header input to the encryption query that output C_1, C_2, $\mathcal{C}$ fetches from its stored values the message M and opening K_f corresponding to C_2, as well as H_0, the header part of the encryption query that produced C_1, C_2. In the TOC binding game $\mathcal{C}$ outputs $((M \| H, S, I), (M \| H_0, S', I), C_2)$ for S and S' are both targeted opening respecting to the identity function I. The environment of G_1 is perfectly simulated by $\mathcal{C}$. Since in the winning case for (H, C_1, C_2), $\mathsf{TOC.Ver}(M \| H, S, I)$ must output 1. In this case, $\mathcal{A}$ has broken binding property of the commitment.

Theorem 3 (Sender Binding). *Let TOCtE be the generic TOCE scheme described as above, which is based the AEAD scheme and the TOC scheme. Let $\mathcal{A}$ be an adversary for the game TO-s-BIND in Fig 4. Then we can give adversaries $\mathcal{B}$ against the efficient checkable property of the*

$$\mathsf{Adv}_{\mathcal{A}, TO\text{-}s\text{-}BIND}^{TOCtE} \leq \mathsf{Adv}_{\mathcal{B}, CHECK}^{TOC}.$$

Proof. In the decryption algorithm of our TOCtE scheme, one need to targeted open the commitment part C_2 according the identity function I and check whether the verification can be passed. So if a ciphertext can be successfully decrypted but can not pass the verification when it is opened according to some position function φ, the efficient checkable property can be broken.

Game G_1

$K \leftarrow$ AEAD.Kg

win $\leftarrow$ false

$\mathcal{A}^{\mathbf{Enc,Dec,SOpen}}$

return win

Oracle $\mathbf{Enc}(H, M)$

$(C_2, K_f) =$ TOC.Com(H, M)

$C_1 \leftarrow$ AEAD.Enc$_k(C_2, M \| K_f)$

$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{H, C_1, C_2\}$

$D[H, C_1, C_2] \leftarrow (M, K_f)$

Return (H, C_1, C_2)

Oracle $\mathbf{Dec}'(H, C_1, C_2)$

if $D[H, C_1, C_2] \neq \perp$ **then**

   return $D[H, C_1, C_2]$

else if $\perp \leftarrow$ AEAD.Dec(H, C_1, C_2) **then**

     return $\perp$

  else $(M, K_f) \leftarrow$ AEAD.Dec(H, C_1, C_2)

     $S \leftarrow$ TOC.TOpen(C_2, M, K_f, I)

     if TOC.TVer$(S, K_f, M, I) = 0$

     return $\perp$

     else win $\leftarrow$ true

     return (M, K_f)

Oracle $\mathbf{TOpen}'(H, C_1, C_2, \varphi)$

if $D(H, C_1, C_2) \neq \perp$

   return $(M, K_f) \leftarrow D(H, C_1, C_2)$

else $(M, K_f) \leftarrow$ AEAD.Dec$_K(H, M_1, M_2)$

   $S \leftarrow$ TOC.TOpen(C_2, M, K_f, I)

   if TOC.TVer$(S, K_f, M, I) = 0$ **then**

     return $\perp$

   else $S \leftarrow$ TOpen(C_2, M, K_f, φ)

     win $\leftarrow$ true

     return $(S, \varphi(M))$

Oracle $\mathbf{ChalDec}(H, C_1, C_2)$

if $(H, C_1, C_2) \in \mathcal{Y}_1$

   return $\perp$

if $\perp \leftarrow$ AEAD.Dec(H, M_1, M_2)

   return $\perp$

else $(M, K_f) \leftarrow$ AEAD.Dec(H, M_1, M_2)

    $S \leftarrow$ TOC.TOpen(C_2, M, K_f, I)

    if TOC.TVer$(S, K_f, M, I) = 0$

      return $\perp$

   if $M \neq \perp$

  win $\leftarrow$ true

   else return (M, K_f)

Fig. 8. The game for the integrity proof.

Theorem 4 (Receiver Binding). *Let TOCtE be the generic TOCE scheme described as above, which is based the AEAD scheme and the TOC scheme. Let $\mathcal{A}$ be an adversary for the game TO-r-BIND in Fig 4. Then we can give adversaries $\mathcal{B}$ against the efficient checkable property of the*

$$Adv_{\mathcal{A}, TO\text{-}r\text{-}BIND}^{TOCtE} \leq Adv_{\mathcal{B}, BIND}^{TOC}.$$

3.4 An efficient instantiation

In this section, we will provide an efficient instantiation for our targeted open commitment. Here we use the pseudo-random function $\mathcal{G}$ and the cryptographic hash function $\mathcal{H}$ as primitives.

– TOC.Com(M) : Given the message M as the input, parse M into a sequence of bits $m_1, \ldots, m_l$. Then use the pseudo-random generator $\mathcal{G}$ with seed sd to generate a sequence of $r_1, \ldots, r_l \in \{0,1\}^\lambda$, and compute $h_i = \mathcal{H}(r_i, m_i)$ for $i = 1, \ldots, l$. Then use the Merkle tree to hash all h_i together and get the final commitment C. The corresponding opening is $K_f = sd$.
– TOC.TOpen(M, sd, φ): Given the seed sd, we can generate the random number $r_1, \ldots, r_l$. Then we can easily compute each h_i from r_i and m_i . Suppose that the position function φ denotes to targeted open the bits $m_{i_1}, m_{i_2}, \ldots, m_{i_k}$ while conceal the rest bits $m_{j_1}, \ldots, m_{j_{k'}}$, so the targeted opening S should be the values h_j for $j \in \{j_1, \ldots, j_{k'}\}$ and (r_i, m_i) for $i \in \{i_1, \ldots, i_k\}$.
– TOC.TVer($C, S, \varphi(M)$): Given the targeted opening S as h_j for $j \in \{j_1, \ldots, j_{k'}\}$ and (r_i, m_i) for $i \in \{i_1, \ldots, i_k\}$, the verifier compute $h_i = \mathcal{H}(r_i, m_i)$ and gather all h_i for $i = 1, \ldots, l$. Then verifier checks whether $\mathcal{H}(h_1, \ldots, h_l) = C$.

The targeted hiding property can easily obtain if we model the hash function as the random oracle. Also, the targeted binding property and the efficient checkable property can easily obtain from the collision resistance of the function $\mathcal{H}$.

4 More Efficient TOCE

Our generic construction above can achieve targeted opening in an ideal case, i.e., the receiver can choose arbitrary bit to open, thus requires cryptographic operations such as committing, to be called on each bit of the message. Such kind of selective capability is unnecessarily strong. For example, when the abusive message is an improper picture, the revealed message would not need the precision to bit. Even the abusive message is simply some texts, a meaningful sentence is also composed of multiple consecutive characters which are at least hundreds of bits. Moreover, such a method incurs large overhead when the message size is large, for instance, when one user is sending a picture, or a short video via secure messaging, applying the above construction may require a large number of hash operations.

In this section, we seek for more efficient constructions of toccAEAD with a slightly weaker targeted open capability which is still useful in many settings. In particular, as all AEAD schemes apply some ciphers on message blocks with size λ bits (λ could be 256 for example), we will restrict the targeted opening at the block level: plaintext M is now divided into $m_1, \ldots, m_\ell$, each m_i is with length λ. During the opening phase, the receiver will reveal the message blocks according to the indices, i.e., $\{m_j\} = \varphi(M, \lambda)$, now the selection function φ takes an extra input of message block size λ, and the indices are chosen by the recipient from $\{1, \ldots, \ell\}$, and $\ell = |M|/\lambda$.

There are two reasons to explore in depth such a block-wise targeted opening: (1) the recipient would still be able to choose some of the blocks to reveal to report abusive messages. If a block of 256 bits (just 32 English characters) already contains substantial amount of personal information, there won't be much room for abusive messages; even if the recipient chooses not to reveal this block, the missing tiny piece of information in this hidden block would not influence the abuse reporting much. To put it another way, in a revealed block of 256 bits chosen by the recipient, the leaked information excluding the abusive message would be insignificant to him. (2) trivial application of the generic construction to message blocks still has an large overhead, thus more specially designed constructions are needed.

To be more precise about the overhead, one efficiency metric we consider is the *pass* defined in [2], which characterizes the ratio of the number of calls of symmetric key cryptographic building block such as a cipher (or hash) needed for a ccAEAD over the number of calls for a regular AEAD scheme. In particular, in [2], the authors gave an elegant construction of ccAEAD that only requires one pass! The intuition is to chain the ciphertext together so that the binding properties are generated along the way of encryption.

Inefficiency of toccAEAD constructions. The toccAEAD of the previous generic construction can be bit-wise targeted opening. Essentially, it can also be trivially extended to blockwise targeted open. However, since the pseudo random generator need at least one path to generate enough randomness, the TOC scheme need at least two pass to compute the commitment and the AEAD scheme need at least one pass to encrypt, the generic construction of toccAEAD need at least four pass to compute encryption. Obviously, it is far from one desires for practical use, and we need to design more efficient specific constructions for block wise targeted opening.

4.1 Block-wise targeted open ccAEAD definitions

Now let us define the block-wise toccAEAD. The syntax is essentially the same as regular toccAEAD, with the only exception that each message bit now becomes a message block with length λ.

Targeted opening, compactness, and using few passes seem to be antagonistic to each other. The cascaded construction in [2] achieved both compactness and using only one pass; however, the messages are all chained together, verifying m_i

requires knowledge of m_{-1}, thus inherently difficult to enable targeted opening. On the other hand, processing each data block separately to enable targeted opening, then different randomness seems required for each message block. Generating those randomness already somehow requires one pass of crypto calls. Together with the encryption itself, and the commitment, this already causes three passes. (If we need further compress all the commitments for compactness, requires one more pass such as the trivial instantiation of our generic construction). Those attempts motivate us to consider a potential weaker notion, and seek for a non-black box construction to reduce the number of passes needed.

Nonce-based scheme. The above generic construction of targeted opening committing AEAD is randomized. However, cryptographers have advocated that modern AEAD schemes should be designed as nonce-based instead. Thus the internal randomness during the encryption should be replaced with an input nonce, and the security should hold as long as the nonce never repeats throughout the course of encrypting messages with a particular key.

Formally, a nonce-based block-wise targeted opening committing AEAD is a following tuple of algorithms (KeyGen, Enc, Dec, TOpen, TVer), which is similar to the previous definition. In addition to the other sets, we associate to any nbTOCE scheme a nonce space $\mathcal{N} \in \{0,1\}^*$. We also define the block-wise position function φ as follows. If message M is a bit string with length n, φ_t is a function that divides M into $l = n/t$ blocks $m_1, \ldots, m_l$ of size t,[2] then picks a subset of the blocks m_i with the indices $i_1, i_2, \ldots, i_k$ depending on φ_t's definition. The space of all the block-wise position functions is Φ_t.

- **Key generation**: The randomized algorithm KeyGen outputs a secret key $K \in \mathcal{K}$.
- **Encryption**: The deterministic algorithm Enc takes a triple $(K, N, H, M) \in \mathcal{K} \times \mathcal{N} \times \mathcal{H} \times \mathcal{M}$ as input and outputs a pair $(C_1, C_2) \in \mathcal{C} \times \mathcal{T}$. Here C_1 is the ciphertext that carries the payload and C_2 is the franking tag.
- **Decryption**: The deterministic algorithm Dec takes a tuple $(K, N, H, C_1, C_2) \in \mathcal{K} \times \mathcal{N} \times \mathcal{H} \times \mathcal{C} \times \mathcal{T}$ as input and outputs a message and opening value pair $(M, K_f) \in \mathcal{M} \times \mathcal{K}_f$.
- **Targeted open**: The deterministic algorithm TOpen takes as input a tuple $(H, M, K_f, C_2, \varphi_t) \in \mathcal{H} \times \mathcal{M} \times \mathcal{K}_f \times \mathcal{T} \times \Phi_t$, the targeted value represented as $\varphi_t(M)$, and the corresponding opening S.
- **Verification**: The deterministic algorithm TVer takes as input a tuple values of $(H, \varphi_t(M), S, C_2, , \varphi_t) \in \mathcal{H} \times \varphi_t(\mathcal{M}) \times \mathcal{S} \times \mathcal{T} \times \Phi_t$ and output a bit b. Specifically, we assume that TVer outputs 0 if the targeted opening is not valid.

Blockwise TOCE security definitions. We weaken the confidentiality after opening part of the message blocks of a TOCE, which enables us to search for a more efficient construction that uses fewer passes. There are multiple ways

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[2] For simplicity, we assume that n can be divided by t, otherwise we can pad M with bits zeros.

of weakening on confidentiality of the remaining message blocks. The first one requires that a message block that has not been opened, will remain semantically secure, if the message block is unpredictable, i.e., generated from a distribution that has sufficient entropy. The second one requires that a message block that has not been opened, will remain one way secure, i.e., adversary who sees the opening of some other message blocks, cannot recover the remaining unopened ones. Clearly, the first definition is strictly stronger, so we adopt the first weakened definition. We emphasize here that all messages satisfy the standard semantic security if no message blocks are revealed by the receiver.

Formally, we define the security games for the nonce based block wise targeted opening ccAEAD in Figure 9. Note that the adversary never repeat the same N across a pair of encryption queries, and the challenge nonce N^* also will not be queried for the **Enc** oracle. To achieve more efficient construction, we also provide a more weaker notion of confidentiality as follows:

4.2 Block wise TOCE construction

We now proceed to describe our nonce based block-wise targeted open ccAEAD construction. This structure is directly modified from the Committing Encrypt-and-PRF structure in [5], except that our construction supports select opening.

Let $\mathcal{G}$ is a nonce-based pseudo-random generator. $\mathcal{H}$ is a collision resistant hash function which can be modelized as a random oracle. Integer t denotes the block size of the message (e.g., 256 for popular ciphers). So the scheme is as follows.

- bTOCE.KeyGen(1^λ): Generate a seed sd for the pseudo random generator $\mathcal{G}$. The secret key K is sd.
- bTOCE.Enc(N, H, K, M): Given the nonce N, the secret key $K = sd$ and the message $M \in \{0,1\}^{lt}$, do the following steps:
  1. Use the pseudorandom generator $\mathcal{G}$ with the seed sd and the nonce N to generate bits strings R with the size of lt, i.e., $R = (r_0, r_1, \ldots, r_\ell) \leftarrow \mathcal{G}(sd, N, lt)$ where each $r_i \in \{0,1\}^t$.
  2. Divide each M into ℓ blocks $m_1, \ldots, m_\ell$, and every block has t bits. Then use one time pad to encrypt each message m_i, i.e., $C_1^i = r_i \oplus m_i$, for $i = 1, \ldots, \ell$;
  3. Hash each r_i together with m_i and get $h_i = \mathcal{H}(r_i, m_i)$;
  4. Compute the final tag $C_2 = \mathcal{H}(H, h_1, \ldots, h_l)$;
  5. Compute the MAC $T = \mathcal{H}(r_0, C_2)$ respect to the key r_0;

  The final output ciphertext is (C_1, C_2) where $C_1 = \big(\{C_1^i\}_{i=1}^l, T\big)$.
- bTOCE.Dec($K, N, H, (C_1, C_2)$): Firstly, use seed $K = sd$ to recover r_0 and $R = (r_1, \ldots, r_\ell)$. Then one can get $m_i = C_1^i \oplus r_i$ and $h_i = \mathcal{H}(m_i, r_i)$ for $i = 1, \ldots, l$. If $C_2 = \mathcal{H}(H, h_1, \ldots, h_l)$ and $T = \mathcal{H}(r_0, C_2)$, output the message $M = \{m_1, \ldots, m_l\}$ and the opening $K_f = R = \{r_1, \ldots, r_l\}$, otherwise output $\perp$.

$TO - nIND_{nTOCE}^{\mathcal{A}}$

$K \leftarrow_\$ \mathsf{KeyGen}$
$st_1 \leftarrow \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}$
$\{N^*, H^*, (M_0, M_1), st_2\} \leftarrow_\$ \mathcal{A}(st_1)$
$b \leftarrow_\$ \{0, 1\}$
$(C_1^*, C_2^*) \leftarrow \mathsf{Enc}(K, N^*, H^*, M_b)$
$b \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}(C_1^*, C_2^*, st_2)$
Return b

$TO - nCTXT_{CE}^{\mathcal{A}}$

$K \leftarrow_\$ \mathsf{KeyGen}$
win $\leftarrow$ false
$\mathcal{A}^{\mathbf{Enc,Dec^*,TOpen,ChalDec}}$
Return win

Oracle $\mathbf{Enc}(N, H, M)$
$(C_1, C_2) \leftarrow \mathsf{Enc}(K, N, H, M)$
$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{(N, H, C_1, C_2)\}$
Return (C_1, C_2)

Oracle $\mathbf{TOpen}(N, H, C_1, C_2, \varphi)$
If $(H^*, C_1^*, C_2^*) = (H, C_1, C_2)$ then
    If $\varphi(M_0) \neq \varphi(M_1)$ then
        Return $\perp$
If $(N, H, C_1, C_2) \notin \mathcal{Y}_1$ then
        Return $\perp$
$(M, K_f) \leftarrow \mathsf{Dec}(K, N, H, C_1, C_2)$
$(\varphi(M), S) \leftarrow \mathsf{TOpen}(H, M, K_f, C_2, \varphi)$
Return $(m = \varphi(M), S)$

$TO - r - nBIND_{nTOCE}^{\mathcal{A}}$

$((m, S), (m', S'), C_2, \varphi) \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}$
$b \leftarrow \mathsf{TVer}(m, S, C_2, \varphi)$
$b' \leftarrow \mathsf{TVer}(m, S', C_2, \varphi)$
If $m = m'$ then
    Return false
Return$(b = b' = 1)$

$TO - s - nBIND_{CE}^{\mathcal{A}}$

$(K, H, C_1, C_2, \varphi) \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}$
$(M', K_f) \leftarrow \mathsf{Dec}(K, N, H, C_1, C_2)$
If $M' = \perp$ then Return false
$S \leftarrow \mathsf{TOpen}(H, M', K_f, C_2, \varphi)$
$b \leftarrow \mathsf{TVer}(H, \varphi(M'), S, C_2)$
If $b = 0$ then Return true
Else Return false

Oracle $\mathbf{Dec}(N, H, C_1, C_2)$
If $(N, H, C_1, C_2) \notin \mathcal{Y}_1$
    then Return $\perp$
If $(N, H, C_1, C_2) = (N^*, H^*, C_1^*, C_2^*)$
    then Return $\perp$
$(M, K_f) \leftarrow \mathsf{Dec}(K, N, H, C_1, C_2)$
Return (M, K_f)

Oracle $\mathbf{Dec}^*(N, H, C_1, C_2)$
Return $\mathsf{Dec}(K, N, H, C_1, C_2)$

Oracle $\mathbf{ChalDec}(N, H, C_1, C_2)$
If $(N, H, C_1, C_2) \in \mathcal{Y}_1$ then
    Return $\perp$
$(M, K_f) \leftarrow \mathsf{Dec}(K, N, H, C_1, C_2)$
If $M \notin \perp$ then
    win $\leftarrow$ true
    Return (M, K_f)

Fig. 9. The security games for the nonce based block wise TOCE.

- bTOCE.TOpen(H, M, R, φ_t): If the position function φ_t denotes to open the blocks with index $i_1, \ldots, i_j$, one just compute each $h_i = \mathcal{H}(r_i, m_i)$ and output the targeted opening $S = \big\{\{h_i\}_{i \notin \{i_1, \ldots, i_j\}}, \{r_i\}_{i \in \{i_1, \ldots, i_j\}}\big\}$ and the opened messages $\varphi_t(M) = \{m_i\}_{i \in \{i_1, \ldots, i_j\}}$.
- bTOCE.TVer($H, \varphi_t(M), S, C_2, \varphi_t$): If the position function φ_t denotes to open the blocks with index $i_1, \ldots, i_j$, one parse the targeted opening S as $\{h_i\}_{i \notin \{i_1, \ldots, i_j\}}$ and $\{r_i\}_{i \in \{i_1, \ldots, i_j\}}$ and $\varphi_t(M)$ as $\{m_i\}_{i \in \{i_1, \ldots, i_j\}}$. Then compute $h_i = \mathcal{H}(r_i, m_i)$ for $i \in \{i_1, \ldots, i_j\}$ and check whether $C_2 = \mathcal{H}(H, h_1, \ldots, h_l)$. If the check is passed, output 1 otherwise output 0.

Comparison. The main advantage of bTOCE is efficiency. Note that bTOCE only need tree pass, while the generic construction need at least four passes.

4.3 Security Analysis

Next we will provide a security analysis for our bTOCE scheme.

Confidentiality. The confidentiality of the scheme can be seen from the following theorem.

Theorem 5 (Confidentiality). *Let $\mathcal{G}$ is a nonce-based pseudo-random generator. $\mathcal{H}$ is a collision resistant hash function which can be modelized as a random oracle. Let $\mathcal{A}$ be the TO-nIND adversary, and $\mathcal{B}$ be the adversary against the pseudo random generator $\mathcal{G}$.*

$$\boldsymbol{Adv}^{\mathcal{A}}_{TO\text{-}nIND} \leq \mathsf{negl}(n) + \boldsymbol{Adv}^{\mathcal{B}}_{\mathcal{G}}$$

Proof. Let $G_0 = \text{TO-nIND}^{\mathcal{A}}_{bTOCE}$. Firstly, we replace the pseudo random strings $r_0, r_1, \ldots, r_l$ with truly random strings and obtain game G_1 in Figure 10. So the challenger answers the **Dec** and **TOpen** oracles by retrieving the stored plaintext-ciphertext table instead of decrypting the ciphertext with the secret key. Hence we have

$$\mathbf{Adv}^{\mathcal{A}}_{\text{TO-nIND}} \leq \mathbf{Adv}^{\mathcal{A}}_{G_1} + \mathbf{Adv}^{\mathcal{B}}_{\mathcal{G}}$$

where $\mathcal{B}$ is the adversary to attack the PRG $\mathcal{G}$.

Secondly, we replace each h_i in game G_1 with newly generated random string according to the random oracle model and get Game G_2. Hence we have

$$\mathbf{Adv}^{\mathcal{A}}_{G_1} \leq \mathbf{Adv}^{\mathcal{A}}_{G_2}.$$

Since C_1 and C_2 in Game G_2 are both independent of the message M_b, we have

$$\mathbf{Adv}^{\mathcal{A}}_{G_2} \leq \mathsf{negl}(n)$$

$\square$

Game G_1

$K \leftarrow_\$ \mathsf{KeyGen}$
$st_1 \leftarrow \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}(1^\lambda)$
$\{N^*, H^*, (M_0, M_1), st_2\} \leftarrow_\$ \mathcal{A}(st_1)$
$b \leftarrow_\$ \{0,1\}$
$(H^*, C_1^*, C_2^*) \leftarrow \mathsf{Enc}_K(N^*, H^*, M_b)$
$b' \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec,TOpen}}(C_1^*, C_2^*, st_2)$
return $b = b'$

Oracle $\mathbf{Enc}(N, H, M)$
$(r_0, r_1, \ldots, r_l) \leftarrow_\$ \{0,1\}^{lt}$
for i from 1 to n
$\quad C_1^i = m_i \oplus r_i$
$\quad h_i = \mathcal{H}(r_i, m_i)$
$C_2 = \mathcal{H}(H, h_1, \ldots, h_l)$
$T = \mathcal{H}(r_0, C_2)$
$C_1 = (\{C_1^i\}_{i=1}^n, T)$
$K_f = (r_1, \ldots, r_l)$
$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{N, H, C_1, C_2\}$
$D[N, H, C_1, C_2] \leftarrow (M, K_f)$
Return (N, H, C_1, C_2)

Oracle $\mathbf{Dec}(N, H, C_1, C_2)$
if $D[N, H, C_1, C_2] \neq \bot$ **then**
$\quad$ **return** $D[N, H, C_1, C_2]$
else return $\bot$

Oracle $\mathbf{TOpen}(N, H, C_1, C_2, \varphi_t)$
if $D[N, H, C_1, C_2] = \bot$ **then**
$\quad$ **return** $\bot$
else $(M, R) \leftarrow D[N, H, C_1, C_2]$
parse M as $(m_1, \ldots, m_l)$
parse R as $(r_1, \ldots, r_l)$
φ_t corresponds to positions $(i_1, \ldots, i_j)$
for j from 1 to s
$\quad h_{i_j} = \mathcal{H}(r_{i_j}, m_{i_j})$
$S = \left(\{h_i\}_{i \in \{l\}/\{i_1, \ldots, i_j\}}, \{r_i\}_{i \in \{i_1, \ldots, i_j\}}\right)$
return $(S, \varphi_t(M))$

Fig. 10. Game G_1 for confidentiality proof

Integrity. Next we will show the integrity of our bTOCE scheme.

Lemma 1. *Let $\mathcal{H}$ be a collision resistant hash function. $M = (m_1, \ldots, m_l) \in \{0,1\}^{l\lambda}$ and $R = (r_1, \ldots, r_l) \in \{0,1\}^{l\lambda}$. So the function*

$$\mathcal{F}(H, M, R) = \mathcal{H}\left(H, \mathcal{H}(r_1, m_1), \ldots, \mathcal{H}(r_l, m_l)\right) \tag{1}$$

is collision resistance.

Lemma 2. *Let $\mathcal{H}$ be a collision resistant hash function. The function*

$$\mathsf{MAC}_r(*) = \mathcal{H}(r, *) \tag{2}$$

is a MAC scheme with respect to the key r. We can define the algorithms Tag_r and Ver_r accordingly. Specifically, it is multi-user unforgeable under chosen-message attack.

Theorem 6 (Integrity). *Let $\mathcal{A}$ be the TO-nCTXT adversary, $\mathcal{B}$ be the adversary against the collision resistance of $\mathcal{F}$ defined in (1), $\mathcal{C}$ be the multi-user unforgeability under chosen-message attack (MU-UF-CMA) for MAC in (2).*

$$\boldsymbol{Adv}_{TO\text{-}nCTXT}^{bTOCE}(\mathcal{A}) \leq \boldsymbol{Adv}_{\mathcal{F}}^{CR}(\mathcal{B}) + \boldsymbol{Adv}_{\mathsf{MAC}}^{MU-UF-CMA}(\mathcal{C})$$

Proof. Let $G_0 = \text{TO-nCTXT}_{bTOCE}^{\mathcal{A}}$. By the random oracle model, we can transition to a game G_1 in which $\mathcal{G}$ are replaced by a random oracle $\mathcal{G}'$ and r_0 is randomly chosen from $\{0,1\}^{\lambda}$. Here $\mathcal{G}'$ takes a secret key sd and a nonce N, and outputs a random string from $\{0,1\}^{l\lambda}$. We modify game G_1 to obtain game G_2 in Figure 11. The differences are that:

1. queries to $\mathbf{Dec}^*$ on tuples (N, H, C_1, C_2) for which there was a previous query to $\mathbf{Enc}(N, H, M)$ that returned C_1, C_2 simply reply with (M, K_f) without bothering to do decryption;
2. we set win to true if any other query to $\mathbf{Dec}$ successfully decrypts.

The first difference is without loss, since the $\mathbf{Dec}^*$ in G_2 would have anyway returned (M, K_f). The second difference only increases the adversary's probability of success. Thus

$$\Pr[G_1^{\mathcal{A}} \Rightarrow 1] \leq \Pr[G_2^{\mathcal{A}} \Rightarrow 1].$$

We now bound $\mathcal{A}$'s probability of success in G_2 by its ability to forge against the MAC in the equation (2). The MU-UF-CMA adversary $\mathcal{C}$ can simulate the environment of $\mathcal{A}$ by using the $\mathbf{Tag}$ and $\mathbf{Ver}$ oracles to perform tagging and verification via MAC.

We need to show that anytime win would have been set in G_2 for ciphertext (N^*, H^*, C_1^*, C_2^*), the corresponding query to $\mathbf{Ver}(C_2^*, T^*)$ is a successful forgery for the MAC scheme $\mathcal{F}$, i.e., C_2^* is not generated from the oracle $\mathbf{Tag}$. To proof this claim, we need to consider two scenarios. The first scenario is that T^* did not exist in previous answers of $\mathbf{Enc}$ queries, so obviously the T^* can not be the answer of the $\mathbf{Tag}$ oracle and (C_2^*, T^*) is a successful MAC forgery. The second

scenario is that T^* is included in previous answers of **Enc** which corresponding input is (N, H, M). Let the return from the corresponding **Enc** query on inputs (N, H, M) be the pair (N, H, C_1, C_2^*) where $C_1 = \left(\{C_1^i\}_{i=1}^n, T^*\right)$ and corresponding randomness is R. Let the ciphertext (N^*, H^*, C_1^*, C_2^*) is decrypted to the message M^* and the corresponding randomness is R^*. According to the collision resistance of $\mathcal{F}$, $(H, R, M) = (H^*, R^*, M^*)$ with the probability $1 - Adv_{\mathcal{F}}^{CR}$. Then since each C_1^i is computed from XOR strings m_i and r_i, $C_1^i = {C_1^i}^*$ due to the same R^* and M^*. According to the property of random oracle $\mathcal{G}'$, the probability of $N \neq N^*$ but $R = R^*$ is less than $2^{-l\lambda}$. If $(N^*, H^*, C_1^*, C_2^*) = (N, H, C_1, C_2^*)$, it is contradict to our assumption which states (N^*, H^*, C_1^*, C_2^*) is not generate from **Enc** oracle, because in the second scenario the $\mathcal{A}$ have queried the **Enc** oracle with the point $(N, H, M) = (N^*, H^*, M^*)$. Hence we have

$$\Pr[G_1^{\mathcal{A}} \Rightarrow 1] \leq \mathbf{Adv}_{\mathcal{F}}^{CR}(\mathcal{B}) + \mathbf{Adv}_{\mathsf{MAC}}^{MU-UF-CMA}(\mathcal{C}) + 2^{-l\lambda}$$

$\square$

Sender Binding property can be easily verified, since the targeted opening is just a subset of all $\{r_1, \ldots, r_l\}$, while all r_i are already checked in the decryption algorithm.

Receiver Binding. We have the following theorem.

Theorem 7. *Let $\mathcal{A}$ be the TO-nCTXT adversary. There is an adversary against the collision resistance of the hash function $\mathcal{H}$.*

$$\mathbf{Adv}_{TO\text{-}nCTXT}^{bTOCE}(\mathcal{A}) \leq l \cdot \mathbf{Adv}_{\mathcal{H}}^{CR}(\mathcal{B})$$

4.4 Construction with weaker confidentiality after opening

Definition 4 (Weak confidentiality after opening). *We define two security games for weaker confidentiality as Figure 12, where the oracle **Enc** and **Dec** are as same as that in the previous games in Figure 9. Formally, We say a nonce based block wise targeted opening ccAEAD scheme satisfies weaker confidentiality if it satisfies:*

- *the standard IND-CPA security without opening, i.e.,*

$$\Pr[\text{IND-CPA}_{nTOCE}^{\mathcal{A}} \Rightarrow 1] \leq \mathsf{negl}(\lambda);$$

- *the targeted opening one-way security, i.e.,*

$$\Pr[One\text{-}Way_{nTOCE}^{\mathcal{A}} \Rightarrow 1] \leq \mathsf{negl}(\lambda).$$

Next we will introduce a more efficient construction but with weaker confidentiality. Similarly, $\mathcal{H}$ is a hash function and $\mathcal{G}$ is a pseudo random generator.

Game G_1

$K \leftarrow \mathsf{KeyGen}$

$\mathsf{win} \leftarrow \mathsf{false}$

$\mathcal{A}^{\mathbf{Enc,Dec,ChalDec,TOpen}}$

return win

Oracle $\mathbf{Enc}(N, H, M)$

$R = (r_1, \ldots, r_l) \leftarrow_\$ \mathcal{G}'(sd, N)$

$r_0 \leftarrow_\$ \{0,1\}^\lambda$

for i from 1 to n

    $C_1^i = m_i \oplus r_i$

    $h_i = \mathcal{H}(r_i, m_i)$

$C_2 = \mathcal{H}(H, h_1, \ldots, h_l)$

$T = \mathsf{Tag}_{r_0}(C_2)$

$C_1 = \left(\{C_1^i\}_{i=1}^l, T\right)$

$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{N, H, C_1, C_2\}$

$D[N, H, C_1, C_2] \leftarrow (M, R)$

Return (H, C_1, C_2)

Oracle $\mathbf{Dec}^*(N, H, C_1, C_2)$

if $D[N, H, C_1, C_2] \neq \bot$ **then**

    return $D[N, H, C_1, C_2]$

else $R = (r_1, \ldots, r_l) \leftarrow \mathcal{G}(sd, N, l\lambda)$

    for i from 1 to n

        $m_i = C_i^i \oplus r_i$

        $h_i = \mathcal{H}(r_i, m_i)$

if $C_2 \neq \mathcal{H}(H, h_1, \ldots, h_l)$

    return $\bot$

if $0 \leftarrow_\$ \mathsf{Ver}_{r_0}(T, C_2)$

    return $\bot$

else $win \leftarrow true$

        return $M = (m_1, \ldots, m_l)$ and R

Oracle $\mathbf{TOpen}(N, H, C_1, C_2, \varphi)$

if $D[N, H, C_1, C_2] \neq \bot$ **then**

    $(M, R) \leftarrow D[N, H, C_1, C_2]$

else $R = (r_1, \ldots, r_l) \leftarrow \mathcal{G}(sd, N, l\lambda)$

    for i from 1 to n

        $m_i = C_i^i \oplus r_i$

        $h_i = \mathcal{H}(r_i, m_i)$

    if $C_2 \neq \mathcal{H}(H, h_1, \ldots, h_l)$

        return $\bot$

    φ corresponds to positions $(i_1, \ldots, i_s)$

    else win $\leftarrow$ true

    $S = \left(\{h_i\}_{i \in \{l\}/\{i_1, \ldots, i_j\}}, \{r_i\}_{i \in \{i_1, \ldots, i_j\}}\right)$

    return $(S, \varphi(M))$

Oracle $\mathbf{ChalDec}(H, C_1, C_2)$

if $(H, C_1, C_2) \in \mathcal{Y}_1$

    return $\bot$

$r_1, \ldots, r_l \leftarrow \mathcal{G}(sd, N, l\lambda)$

for i from 1 to n

    $m_i = C_i^i \oplus r_i$

    $h_i = \mathcal{H}(r_i, m_i)$

if $C_2 \neq \mathcal{H}(H, h_1, \ldots, h_l)$

    return $\bot$

if $0 \leftarrow_\$ \mathsf{Ver}_{r_0}(C_2, T)$

    return $\bot$

else win $\leftarrow$ true

    return (M, sd)

Fig. 11. Game G_1 for integrity proof

$C^{\mathbf{Tag,Ver}}$

$sd \leftarrow \{0,1\}^\lambda$
win $\leftarrow$ false
$\mathcal{A}^{\mathbf{Enc,Dec^*,ChalDec,TOpen}}$
return win

Oracle $\mathbf{Enc}_K(N,H,M)$
$R = (r_1, \ldots, r_l) \leftarrow_\$ \mathcal{G}(sd, N, l \cdot t)$
for i from 1 to l
$\quad C_1^i = m_i \oplus r_i$
$\quad h_i = \mathcal{H}(r_i, m_i)$
$C_2 = \mathcal{H}(H, h_1, \ldots, h_l)$
$T = \mathbf{Tag}(C_2)$
$C_1 = \left(\{C_1^i\}_{i=1}^n, T\right)$
$\mathcal{Y}_1 \leftarrow \mathcal{Y}_1 \cup \{N, H, C_1, C_2\}$
$D[N, H, C_1, C_2] \leftarrow (M, R)$
Return (N, H, C_1, C_2)

Oracle $\mathbf{Dec}^*(N, H, C_1, C_2)$
if $D[N, H, C_1, C_2] \neq \bot$ **then**
$\quad$ **return** $D[N, H, C_1, C_2]$
$R = (r_1, \ldots, r_l) \leftarrow \mathcal{G}(sd, N, l \cdot t)$
for i from 1 to n
$\quad m_i = C_i^i \oplus r_i$
if $C_2 \neq \mathcal{H}(H, h_1, \ldots, h_l)$
$\quad$ **return** $\bot$
if $0 \leftarrow_\$ \mathbf{Ver}(C_2, T)$
$\quad$ **return** $\bot$
else win $\leftarrow$ true
return $M = (m_1, \ldots, m_l)$ and R

Oracle $\mathbf{TOpen}(N, H, C_1, C_2, \varphi_t)$
if $D[N, H, C_1, C_2] \neq \bot$ **then**
$\quad (M, R) \leftarrow D[N, H, C_1, C_2]$
$R = (r_1, \ldots, r_l) \leftarrow \mathcal{G}(sd, N, l \cdot t)$
φ_t corresponds to positions $(i_1, \ldots, i_s)$
for j from 1 to s
$\quad h_{i_j} = \mathcal{H}(r_{i_j}, m_{i_j})$
$S = \left(\{h_i\}_{i \in \{l\}/\{i_1, \ldots, i_j\}}, \{r_i\}_{i \in \{i_1, \ldots, i_j\}}\right)$
return $(S, \varphi_t(M))$

Oracle $\mathbf{ChalDec}(sd, N, H, C_1, C_2)$
if $(N, H, C_1, C_2) \in \mathcal{Y}_1$
$\quad$ **return** $\bot$
$R = (r_1, \ldots, r_l) \leftarrow \mathcal{G}(sd, N, lt)$
for i from 1 to n
$\quad m_i = C_i^i \oplus r_i$
if $C_2 \neq \mathcal{H}(H, h_1, \ldots, h_l)$
$\quad$ **return** $\bot$
if $0 \leftarrow_\$ \mathbf{Ver}(C_2, T)$
$\quad$ **return** $\bot$
else win $\leftarrow$ true
$\quad$ **return** (M, R)

$$\underline{\text{IND-CPA}_{nTOCE}^{\mathcal{A}}} \qquad\qquad \underline{\text{One-Way}_{nTOCE}^{\mathcal{A}}}$$

$K \leftarrow_\$ \mathsf{KeyGen}$ $K \leftarrow_\$ \mathsf{KeyGen}$

$st_1 \leftarrow \mathcal{A}^{\mathbf{Enc,Dec}}(1^\lambda)$ $(N^*, H^*, M^*) \leftarrow_\$ \mathcal{N} \times \mathcal{H} \times \mathcal{M}$

$\{N^*, H^*, (M_0, M_1), st_2\} \leftarrow_\$ \mathcal{A}(st_1)$ $(N^*, H^*, C_1^*, C_2^*) \leftarrow \mathsf{Enc}(K, N^*, H^*, M^*)$

$b \leftarrow_\$ \{0,1\}$ $M' \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec,TOpen}^*}(N^*, H^*, C_1^*, C_2^*)$

$(H^*, C_1^*, C_2^*) \leftarrow \mathsf{Enc}_K(N^*, H^*, M_b)$ $\mathbf{return}\ M = M'$

$b' \leftarrow_\$ \mathcal{A}^{\mathbf{Enc,Dec}}(C_1^*, C_2^*, st_2)$

$\mathbf{return}\ b = b'$ $Oracle \quad \mathbf{TOpen}^*(N, H, C_1, C_2, \varphi)$

                                   $\mathbf{if}\ (N, H, M) = (N^*, H^*, M^*)$

                                      $\mathbf{if}\ \varphi = I \quad \mathbf{return}\ \bot$

                                 $\mathbf{if}\ (N, H, C_1, C_2) \in \mathcal{Y}_1 \quad \mathbf{return}\ \bot$

                                 $(M, K_f) \leftarrow \mathsf{Dec}(K, N, H, C_1, C_2)$

                                 $(\varphi(M), S) \leftarrow \mathsf{TOpen}(H, M, K_f, C_2, \varphi)$

                                 $\mathbf{return}\ (m = \varphi(M), S)$

Fig. 12. The security games for weaker confidentiality

- bTOCE.KeyGen(1^λ): Generate a seed sd for the pseudo random generator $\mathcal{G}$. The secret key K is sd.
- bTOCE.Enc(N, H, K, M): Given the nonce N, the secret key $K = sd$ and the message $M \in \{0,1\}^{lt}$, do the following steps:
  1. Use the pseudorandom generator $\mathcal{G}$ with the seed sd and the nonce N to generate bits strings R with the size of lt, i.e.,$R = (r_0, r_1, \ldots, r_\ell) \leftarrow \mathcal{G}(sd, N, (l+1)t)$ where each $r_i \in \{0,1\}^t$.
  2. Divide each M into ℓ blocks $m_1, \ldots, m_\ell$, and every block has t bits. Then use one time pad to encrypt each message m_i, i.e., $C_1^i = r_i \oplus m_i$, for $i = 1, \ldots, \ell$;
  3. Hash each r_i together with m_i and get $h_i = \mathcal{H}(m_i)$;
  4. Compute the final tag $C_2 = \mathcal{H}(H, h_1, \ldots, h_l)$.
  5. Compute the MAC $T = \mathcal{H}(r_0, C_2)$

  The finally output ciphertext is $C_1 = \left(\{C_1^i\}_{i=1}^l, T\right)$ and the tag C_2.
- bTOCE.Dec($K, N, H, (C_1, C_2)$): Firstly, use seed $K = sd$ to recover $R = (r_1, \ldots, r_\ell)$. Then one can get $m_i = C_1^i \oplus r_i$ and $h_i = \mathcal{H}(m_i)$ for $i = 1, \ldots, l$. If $C_2 = \mathcal{H}(H, h_1, \ldots, h_l, r_0)$, output the message $M = \{m_1, \ldots, m_l\}$ and the opening $K_f = R = \{r_1, \ldots, r_l\}$, otherwise output $\bot$.
- bTOCE.TOpen(H, M, R, φ_t): If the position function φ_t denotes to open the blocks with index $i_1, \ldots, i_j$, one just compute each $h_i = \mathcal{H}(m_i)$ and output the targeted opening $S = \left\{\{h_i\}_{i \notin \{i_1, \ldots, i_j\}}, r_0\right\}$ and the opened messages $\varphi_t(M) = \{m_i\}_{i \in \{i_1, \ldots, i_j\}}$.
- bTOCE.TVer($H, \varphi_t(M), S, C_2, \varphi_t$): If the position function φ_t denotes to open the blocks with index $i_1, \ldots, i_j$, one parses the targeted opening S as $\{h_i\}_{i \notin \{i_1, \ldots, i_j\}}$ and r_0, and $\varphi_t(M)$ as $\{m_i\}_{i \in \{i_1, \ldots, i_j\}}$. Then compute $h_i = \mathcal{H}(m_i)$ for $i \in$

$\{i_1, \ldots, i_j\}$ and check whether $C_2 = \mathcal{H}(H, h_1, \ldots, h_l, r_0)$. If the check is passed, output 1 otherwise output 0.

Security Analysis. One can easily prove that the wbTOCE scheme satisfies the weak confidentially in Definition 4 in the random oracle model.

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