

# Encrypted Distributed Hash Tables

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## Abstract

Distributed hash tables (DHT) are a fundamental building block in the design of distributed systems with applications ranging from content distribution networks to off-chain storage networks for blockchains and smart contracts. When DHTs are used to store sensitive information, system designers use end-to-end encryption in order to guarantee the confidentiality of their data. A prominent example is Ethereum’s off-chain network Swarm.

In this work, we initiate the study of end-to-end encryption in DHTs and the many systems they support. We introduce the notion of an *encrypted DHT* and provide simulation-based security definitions that capture the security properties one would desire from such a system. Using our definitions, we then analyze the security of a standard approach to storing encrypted data in DHTs. Interestingly, we show that this “standard scheme” leaks information *probabilistically*, where the probability is a function of how well the underlying DHT load balances its data. We also show that, in order to be securely used with the standard scheme, a DHT needs to satisfy a form of equivocation with respect to its overlay. To show that these properties are indeed achievable in practice, we study the balancing properties of the Chord DHT—arguably one of the most influential DHT—and show that it is equivocal with respect to its overlay in the random oracle model. Finally, we consider the problem of encrypted DHTs in the context of transient networks, where nodes are allowed to leave and join.

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# 1 Introduction

In the early 2000’s, the field of distributed systems was revolutionized in large part by the performance and scalability requirements of large Internet companies like Akamai, Amazon, Google and Facebook. The operational requirements of these companies—which include running services at Internet scale using commodity hardware in data centers distributed across the world—motivated the design of highly influential systems like Chord [28], Dynamo [12] and BigTable [8]. These advances in distributed systems are what enable companies like Amazon to handle over a billion purchases a year and Facebook to support two billion users worldwide.

**Distributed hash tables.** The most fundamental building block in the design of highly scalable and reliable systems are *distributed hash tables* (DHT). DHTs are decentralized and distributed systems that store data items associated to a label. Roughly speaking, a DHT is a distributed dictionary data structure that stores label/value pairs  $(\ell, v)$  and that supports get and put operations. The former takes as input a label  $\ell$  and returns the associated value  $v$ . The latter takes as input a pair  $(\ell, v)$  and stores it. DHTs are distributed in the sense that the pairs are stored by a set of  $n$  nodes  $N_1, \dots, N_n$ . To communicate and route messages to and from nodes, DHTs rely on (1) a randomly generated *overlay network* which, intuitively, arranges nodes in a chosen network topology (e.g., star topology, tree topology) and (2) a distributed routing protocol that routes messages between nodes. DHTs provide many useful properties but the most important are load balancing and fast data retrieval and storage even in highly-transient networks (i.e., where storage nodes join and leave at high rates). In this work, we focus on the perpetual setting where nodes do not leave and join the network. The formalization and analysis in this setting is complicated enough and therefore we address the transient setting in our future work.

**Classic applications of DHTs.** It is hard to overstate the impact that DHTs have had on system design and listing all their possible applications is not feasible so we will recall just a few. One of the first applications of DHTs was to the design of content distribution networks (CDNs). In 1997, Karger et al. introduced the notion of consistent hashing [18] which was adopted as a core component of Akamai’s CDN. Since then, many academic and industry CDNs have used DHTs for fast content delivery [14, 27]. DHTs are also used by many P2P systems like BitTorrent [1] and its many trackerless clients including Vuze, rTorrent, Ktorrent and  $\mu$ Torrent. Many distributed file systems are built on top of DHTs, including CFS [11], Ivy [22], Pond [24], PAST [13]. DHTs are also the main component of distributed key-value stores like Amazon’s Dynamo [12] which underlies the Amazon cart, LinkedIn’s Voldemort [29] and Riak [30]. Finally, many wide column NoSQL databases like Facebook’s Cassandra [20], Google’s BigTable [8] and Amazon’s DynamoDB [26] make use of DHTs.

**Off-chain storage.** Currently, the field of distributed systems is going through another revolution brought about by the introduction of blockchains [23]. Roughly speaking, blockchains are distributed and decentralized storage networks with integrity and probabilistic eventual consistency. Blockchains have many interesting properties and have fueled an unprecedented amount of interest in distributed systems and cryptography. For all their appeal, blockchains have several shortcomings; the most important of which are limited storage capacity and lack of confidentiality. To address this, a lot of effort in recent years has turned to the design of distributed and/or decentralized *off-chain* storage networks whose primary purpose is to store large amounts of data while supporting fast retrieval and storage in highly transient networks. In fact, many influential

blockchain projects, including Ethereum [31, 2], Enigma [32], Storj [25] and Filecoin [19] rely on off-chain storage: Ethereum, Enigma and Storj on their own custom networks and Filecoin on IPFS [3]. Due to the storage and scalability requirements of these blockchains, these off-chain storage networks often use DHTs as a core building block.

**DHTs and end-to-end encryption.** As discussed, DHTs are a fundamental building block in distributed systems with applications ranging from CDNs to blockchains. DHTs were originally designed for applications that mostly dealt with public data: for example, web caching or P2P file sharing. The more recent applications of DHTs, however, also need to handle *private* data. This is the case, for example, for off-chain storage networks, many of which aim to support decentralized apps for medical records, IoT data, tax information, customer records and insurance data, just to name a few. Indeed, most of these networks (e.g., Ethereum’s Swarm, IPFS, Storj and Enigma) explicitly implement some form of end-to-end encryption.

The specific designs are varied but, as far as we know, none of them have been formally analyzed. This is not surprising, however, since the problem of end-to-end encryption in the context of DHTs has never been properly studied. In this work, we address this by formalizing the goals of encryption in DHTs. In particular, we introduce the notion of an *encrypted DHT* (EDHT) and propose formal syntax and security definitions for these objects. Due to the ubiquity of DHTs and the recent interest in using them to store sensitive data, we believe that a formal study of confidentiality in DHTs is a well-motivated problem of practical importance.

**The standard scheme.** The simplest approach to storing sensitive data on a DHT—and the one we will study in this work—is to store a label/value pair  $(\ell, v)$  as  $(F_{K_1}(\ell), \text{Enc}_{K_2}(v))$  on a standard DHT. Here,  $F$  is a pseudo-random function and  $\text{Enc}$  is a symmetric-key encryption scheme. Throughout we will refer to this as the *standard scheme*. The underlying DHT will then assign this pair to a storage node in a load balanced manner, handle routing and will move pairs around the network if a node leaves or joins. This scheme is simple and easy to implement and is, roughly speaking, what most systems implement. Ethereum’s Swarm, for example, stores pairs as  $(H(\text{ct}), \text{ct})$ , where  $\text{ct} \leftarrow \text{Enc}_K(v)$  and  $H$  is a hash function. But is this secure? Answering this question is not simple as it is not even clear what we mean by security. But even if we were equipped with a meaningful notion of security, we will see that the answer is not straightforward. The reason is because, as we will see, the security of the standard scheme is tightly coupled with how the the underlying DHT is designed.

**Information leakage in EDHTs.** To illustrate this point, suppose a subset of nodes are corrupted and collude. During the operation of this DHT, what information can they learn about a client’s data and/or queries? A-priori, it might seem that the only information they can learn is related to what they collectively hold (i.e., the union of the data they store). For example, they might learn that there are at least  $m$  pairs stored in the DHT, where  $m$  is the sum of the number of pairs held by each corrupted node. With respect to the client’s queries they might learn, for any label handled by a corrupted node, when a query repeats. While this intuition might seem correct, it is not true. In fact, the corrupted nodes can infer additional information about data they do not hold. For example, they can infer a good approximation on the *total* number of pairs in the system even if they collectively hold a small fraction of it. Here, the problem is that DHTs are load balanced in the sense that, with high probability, each node will receive approximately the same number of pairs. Because of this, the corrupted nodes can guess that, with high probability, the total number of pairs in the system is about  $mn/t$ , where  $t$  is the number of corrupted nodes and

$n$  is the total number of nodes.

While this may seem benign, this is just one example to highlight the fact that finding and analyzing information leakage in distributed systems can be non-trivial. In fact, some of the very properties which we aim for in the context of distributed systems (e.g., load balancing) can have subtle effects on security.

## 1.1 Our Contributions

In this work, we aim to formalize the use of end-to-end encryption in DHTs and the many systems they support. As an increasing number of applications wish to store sensitive data on DHT-based systems, the use of end-to-end encryption in DHTs should be raised from a technique to a cryptographic primitive with formal syntax and security definitions. Equipped with these definitions, our goal will be to understand and study the security guarantees of the simple EDHT described above. As we will see, analyzing and proving the security of even this simple scheme is complex enough. We make several contributions.

**Formalizing DHTs.** To better understand EDHTs and their security properties, we aim for a modular treatment. In particular, we want to isolate the properties of the underlying DHTs that have an effect on security and decouple the components of the system that have to do with the DHT from the cryptographic primitives we use like encryption and PRFs. This is in line with how systems designers use encryption in DHTs; as far as we know, all DHT-based systems that support end-to-end encryption add encryption on top of an “unmodified” DHT. Our first step, therefore, is to formally define DHTs. This includes a formal syntax but, more interestingly, a useful abstraction of the core components of a DHT including, their network overlays, their allocations (i.e., how they map label/value pairs to nodes) and their routing components.

**Properties of DHTs.** As mentioned above, we found that the security of the standard EDHT scheme is tightly coupled with two main properties of DHTs. More precisely, we discovered that the former’s leakage is affected by a property we call *balance* which, roughly speaking, means that with probability at least  $1 - \delta$  over the choice of overlays, the DHT allocates any label  $\ell$  to any  $\theta$ -sized set of nodes with probability at most  $\varepsilon$  (over the choice of allocation).

Another interesting finding we made was that if the standard scheme is to satisfy our simulation-based definition, then the underlying DHT has to satisfy a form of equivocation. Intuitively, the DHT must be designed in such a way that, for any fixed overlay within a (large) class of overlays, it is possible to “program” the allocation so that it maps a given label to a given node. We found the appearance of equivocation in the context of DHTs quite surprising as it is usually a property that comes up in the context of cryptographic primitives.

**Chord in the perpetual setting.** Having isolated the properties we need from a DHT in order to prove the security of the standard scheme, it is natural to ask whether there are any known DHTs that satisfy them. Interestingly, we not only found that such DHTs exist but that Chord [18]—which is arguably the most influential DHT—is both balanced and non-committing in the sense that it supports the kind of equivocation discussed above. Without getting into details of how this DHT works, we mention here that it make use of two hash functions: one to map names to addresses and a second to map labels to addresses. We show that both the DHTs are non-committing if the second hash function is modeled as a random oracle.

**Security of EDHTs.** Another contribution we make is a simulation-based definition of security for EDHTs. The definition is in the real/ideal-world paradigm commonly used to formalize the security of multi-party computation [5]. Formulating security in this way allows for definitions that are modular and intuitive. Furthermore, this seems to be a natural way to define security since DHTs are distributed objects. In our definition, we compare a real-world execution between  $n$  nodes, an honest client and an adversary, where the latter can corrupt a subset of the nodes. Roughly speaking, we say that an EDHT is secure if this experiment is indistinguishable from an ideal-world execution between the nodes, the honest client, an ideal adversary (i.e., a simulator) and an functionality that captures the ideal security properties of EDHTs. As discussed above, for any EDHT scheme, including the standard construction, there can be subtle ways in which some information about the dataset is leaked (e.g., its total size). To formally capture this, we parameterize our definition with (stateful) leakage functions that capture exactly what is or is not being revealed to the adversary. We note that our definitions handle static corruptions and are in the standalone setting.

**EDHTs and structured encryption.** The notion of an EDHT can be viewed and understood from the perspective of structured encryption (STE). STE schemes are encryption schemes that encrypt data structures in such a way that they can be privately queried. From this perspective, EDHTs are a form of distributed encrypted dictionaries and, in fact, one recovers the latter from the former when the network consists of only one node. We note that this connection is not just syntactical, but also holds with respect to the security definitions of both objects and to their leakage profiles. Indeed the standard scheme’s leakage profile on a single-node network reduces to the leakage profile of common dictionary encryption schemes [9, 7]. This leakage, however, represents the “worst-case” leakage of the standard EDHT. This suggests that distributed STE schemes can leak less than non-distributed STE schemes which makes sense intuitively since, in the distributed setting, the adversary can only corrupt a subset of the nodes whereas in the non-distributed setting the adversary corrupts the only existing node and, therefore, all the nodes.

With this in mind, one can view our results as another approach to the recent efforts to suppress the leakage of STE schemes [17, 16]. That is, instead of (or in addition to) compiling STE schemes as in [17] or of transforming the underlying data structures as in [16], one could *distribute* the encrypted data structure.

**Probabilistic leakage.** Our security definition allows us to formally study any leakage produced by EDHT schemes. Interestingly, our analysis of the standard scheme will show that it achieves a very novel kind of leakage profile. Now, this leakage profile is itself quite interesting. First, it is *probabilistic* in the sense that it leaks only with some probability  $p \leq 1$ . As far as we know, this is the first time such a leakage profile has been encountered. Here, the information it leaks (when it does leak) is the query equality pattern (see [17] for a discussion of various leakage patterns) which reveals if and when a query was made in the past. This is not surprising as labels are passed as  $F_K(\ell)$  to the underlying DHT, which are deterministic. This leakage profile is also interesting because the probability  $p$  with which it leaks is determined by properties of the underlying DHT and, in particular, to its load balancing properties. Specifically, the better the DHT load balances its data the smaller the probability that the EDHT will leak the query equality.

**Worst-case vs. expected leakage.** A-priori one might think that the adversary should only learn information related to pairs that are stored on corrupted nodes and that, since DHTs are load balanced, the total number of pairs visible to the adversary will be roughly  $mt/n$ . But there is a

slight technical problem with this intuition: a DHT’s allocation of labels depends on its overlay and, for any set of corrupted nodes, there are many overlays that can induce an allocation where, say, a very large fraction of labels are mapped to corrupted nodes. The problem then is that, in the *worst-case*, the adversary could see *all* the (encrypted) pairs. We will show, however, that the intuition above is still correct because the worst-case is unlikely to occur. More precisely, we show that with probability at least  $1 - \delta$  over the choice of overlay, the standard scheme achieves a certain leakage profile  $\mathcal{L}$  which is a function of  $\delta$  (and other parameters). As far as we know, this is the first example of a leakage analysis that is not worst-case but that, instead, considers the expected leakage (with high probability) of a construction. We believe this new kind of leakage analysis is of independent interest and that the idea of expected leakage may be a fruitful direction in the design of low- or even zero-leakage schemes.

**Transient EDHTs.** All the analysis discussed above was for what we call the *perpetual* setting where nodes never leave the network.<sup>1</sup> Note that the perpetual setting is realistic and interesting in itself. It captures, for example, how DHTs are used by many large companies who run nodes in their own data centers, e.g., Amazon, Google, LinkedIn. Nevertheless, we also consider the *transient* setting where nodes are allowed to leave and join the network arbitrarily. We extend our syntax and security definitions to this setting and prove that the standard scheme—equipped with certain join and leave protocols—achieves another probabilistic leakage profile. Our leakage analysis in the transient setting relies on a new and stronger property of the underlying DHT we call *stability* which, roughly speaking, means that with probability at least  $1 - \delta$  over the choice of overlay parameter  $\omega$ , for all large enough overlays, the DHT allocates any label to any  $\theta$ -sized set with probability at most  $\varepsilon$ .

**Chord in the transient setting.** Having analyzed the standard EDHT in the transient setting, we study its properties when it is instantiated with a transient variant of Chord. Our analysis of Chord’s stability is non-trivial. At a very high level the main challenge is that, in the transient setting, Chord’s overlay changes with every leave or join. To handle this, we introduce a series of (probabilistic) bounds to handle “dynamic” overlays that may be of independent interest.

## 2 Preliminaries

**Notation.** The set of all binary strings of length  $n$  is denoted as  $\{0, 1\}^n$ , and the set of all finite binary strings as  $\{0, 1\}^*$ .  $[n]$  is the set of integers  $\{1, \dots, n\}$ , and  $2^{[n]}$  is the corresponding power set. We write  $x \leftarrow \chi$  to represent an element  $x$  being sampled from a distribution  $\chi$ , and  $x \stackrel{\$}{\leftarrow} X$  to represent an element  $x$  being sampled uniformly at random from a set  $X$ . The output  $x$  of an algorithm  $\mathcal{A}$  is denoted by  $x \leftarrow \mathcal{A}$ . Given a sequence  $\mathbf{v}$  of  $n$  elements, we refer to its  $i^{\text{th}}$  element as  $v_i$  or  $\mathbf{v}[i]$ . If  $S$  is a set then  $|S|$  refers to its cardinality. If  $s$  is a string then  $|s|_2$  refers to its bit length. We denote by  $\text{Ber}(p)$  the Bernoulli distribution with parameter  $p$ .

**Dictionaries.** A dictionary structure  $\text{DX}$  of capacity  $n$  holds a collection of  $n$  label/value pairs  $\{(\ell_i, v_i)\}_{i \leq n}$  and supports get and put operations. We write  $v_i := \text{DX}[\ell_i]$  to denote getting the value associated with label  $\ell_i$  and  $\text{DX}[\ell_i] := v_i$  to denote the operation of associating the value  $v_i$  in  $\text{DX}$  with label  $\ell_i$ . A multi-map structure  $\text{MM}$  with capacity  $n$  is a collection of  $n$  label/tuple pairs  $\{(\ell_i, \mathbf{v}_i)\}_{i \leq n}$  that supports get and put operations. Similar to dictionaries, we write  $\mathbf{v}_i := \text{MM}[\ell_i]$  to

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<sup>1</sup>Note that in this setting we allow nodes to fail as long as they come back up in a bounded amount of time.



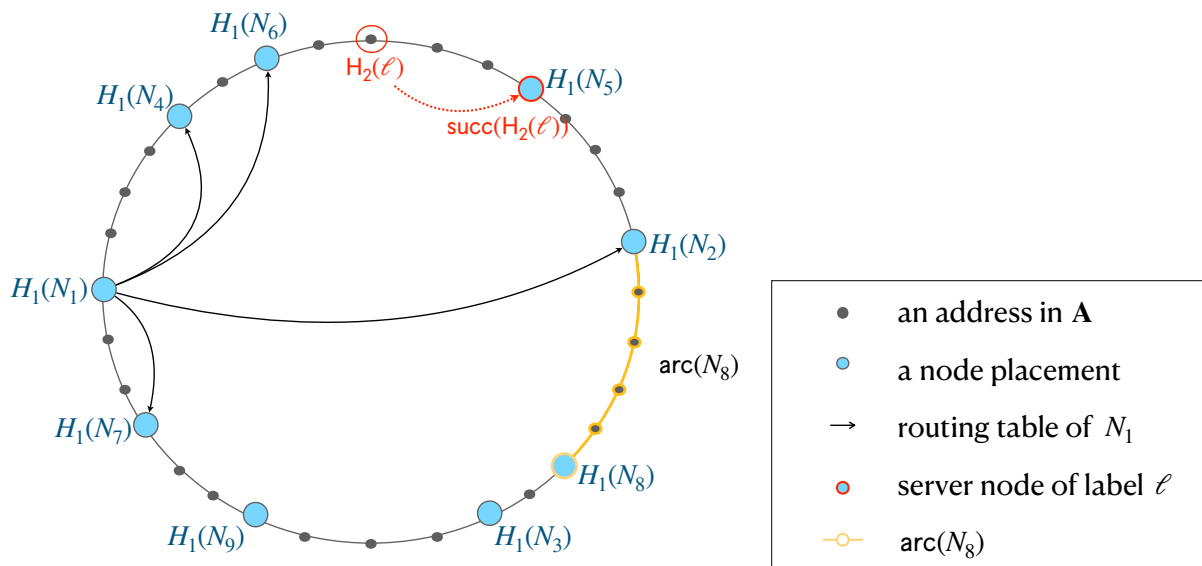


Figure 1: Chord DHT

denote getting the tuple associated with label  $\ell_i$  and  $\text{MM}[\ell_i] := \mathbf{v}_i$  to denote operation of associating the tuple  $\mathbf{v}_i$  to label  $\ell_i$ .

### 3 Distributed Hash Tables

A distributed hash table is a distributed storage system that instantiates a dictionary data structure. It is distributed in the sense that the data is stored by a set of  $n$  nodes  $N_1, \dots, N_n$  and it instantiates a dictionary in the sense that it stores label/value pairs and supports Get and Put operations. Because they are distributed, DHTs rely on an overlay network which, intuitively, consists of a set of node addresses and a distributed routing protocol. As discussed in Section 1, DHTs are a fundamental primitive in distributed systems and have many applications. In this work, we consider perpetual DHTs, which are composed of a fixed set of nodes that are all known at setup time. They can handle nodes going down (e.g., due to failure) and coming back online but such unresponsive nodes are expected to come back online after some period of time.

We now formalize DHTs and abstract their core components out. We use Chord as a running example to make the exposition easier to understand.

#### 3.1 Chord DHT

**Setting up Chord.** Chord works in a logical  $m$ -bit address space  $\mathbf{A} = \{0, \dots, 2^m - 1\}$ . It views the set of addresses to be arranged in a ring (see Fig 1). At the time of setup, it samples two hash functions,  $H_1$  and  $H_2$ , where  $H_1$  assigns each node  $N$  an address  $H_1(N)$  and  $H_2$  assigns each label  $\ell$  an address  $H_2(\ell)$ . We call the set  $\chi = \{H_1(N_1), \dots, H_1(N_n)\}$  of addresses assigned to nodes a *configuration*. Intuitively, a configuration denotes the placement of nodes on the ring of addresses.



Given a configuration  $\chi$ , Chord defines the “successor” of an address  $a$  as the node that follows  $a$  on the address ring in clockwise direction. The first successor of  $a$  is the first node that follows  $a$ , the second successor is the second node that follows  $a$ , and so on. The predecessors of an address/node are defined in the same way. We use the notation  $\text{succ}_\chi(a)$  to denote the first successor of address  $a$ , and  $\text{pred}_\chi(a)$  to denote its first predecessor. For visual clarity, we sometimes drop  $\chi$  from the subscript when its clear from context.

**Routing in Chord.** At the time of setup, each node also constructs a routing table where they store the addresses of their  $2^i$ th successor where  $0 \leq i \leq \log n$ . Note that a routing table contains at most  $\log n$  other nodes. The Chord routing protocol is fairly simple: given a message destined to a node  $N_d$ , a node  $N$  checks if  $N = N_d$ . If not, the node forwards the message to the node  $N'$  in its routing table with an address closest to  $N_d$ . Note that given a configuration  $\chi$ , the route between any two nodes is fixed. Moreover, the structure of routing tables ensures that the route lengths are at most  $\log n$  long [28].

**Storing and retrieving.** Once the DHT is instantiated, each node instantiates an empty dictionary data structure  $\text{DX}_i$ . When a client executes a Put operation on a label/value pair  $(\ell, v)$ , it chooses a node  $N_s$  (called the front-end node) and forwards the Put request to  $N_s$ .  $N_s$  then computes  $N_d = \text{succ}(H_2(\ell))$  and uses the Chord routing protocol to send the pair  $(\ell, v)$  to the node  $N_d$  who stores it in its local dictionary  $\text{DX}_i$ . When executing a Get query on a label  $\ell$ , the client again chooses and forwards its get request to a node  $N_s$ . The front-end node  $N_s$  again computes  $N_d = \text{succ}(H_2(\ell))$  and, again, uses the Chord routing protocol to send the label  $\ell$  to  $N_d$ . The latter looks up  $\ell$  in its local dictionary  $\text{DX}_i$  and return the associated value  $v$  to  $N_s$ , which in turn returns  $v$  to the client. We note that Chord allows its clients to choose any node as the front-end node. Moreover, it does not restrict them to connect to the same node everytime the client wants to query the same  $\ell$ .

### 3.2 Formalizing DHTs

**Syntax.** We now formalize DHTs as a collection of six algorithms  $\text{DHT} = (\text{Overlay}, \text{Alloc}, \text{FrontEnd}, \text{Daemon}, \text{Put}, \text{Get})$ . The first three algorithms, **Overlay**, **Alloc** and **FrontEnd** are executed only once by the entity responsible for setting up the system. They all take as input an integer  $n \geq 1$ . **Overlay** outputs a parameter  $\omega$  from a space  $\Omega$ , **Alloc** outputs a parameter  $\psi$  from a space  $\Psi$ , and **FrontEnd** outputs a parameter  $\phi$  from space  $\Phi$ . We refer to these parameters as the *DHT parameters* and represent them by  $\Gamma = (\omega, \psi, \phi)$ . Each DHT has an address space  $\mathbf{A}$  and the DHT parameters in  $\Gamma$  define different components of the DHT over this address space. For example,  $\omega$  maps node names to addresses in  $\mathbf{A}$ ,  $\psi$  maps labels to addresses in  $\mathbf{A}$ ,  $\phi$  maps operation requests to the address of a front-end node (or starting node). The fourth algorithm, **Daemon**, takes  $\Gamma$  and  $n$  as input and is executed by every node in the network. **Daemon** is halted only when a node wishes to leave the network and it is responsible for setting up its calling node’s state for routing messages and for storing and retrieving label/value pairs from the node’s local storage when a node receives a get/put request. The fifth algorithm, **Put**, is executed by a client to store a label/value pair on the network. **Put** takes as input  $\Gamma$  and a label/value pair  $\ell$  and  $v$ , and outputs nothing. The sixth algorithm, **Get**, is executed by a client to retrieve the value associated to a given label from the network. **Get** takes as input  $\Gamma$  and a label  $\ell$  and outputs a value  $v$ . Since all DHT algorithms take  $\Gamma$  as input we sometimes omit it for visual clarity.

**Abstracting DHTs.** We now abstract the core components of DHTs out. These abstractions will be helpful in our security analysis. Given  $\Gamma$ , we can describe a DHT using a tuple of function families  $(\text{addr}, \text{server}, \text{route}, \text{fe})$  that are all parameterized by subset of parameters in  $\Gamma$ . These functions are defined as

$$\begin{aligned} \text{addr}_\omega : \mathbf{N} &\rightarrow \mathbf{A}, & \text{server}_{\omega, \psi} : \mathbf{L} &\rightarrow \mathbf{N}, \\ \text{route}_\omega : \mathbf{N} \times \mathbf{N} &\rightarrow 2^{\mathbf{N}}, & \text{fe}_\phi : \mathbf{L} &\rightarrow \mathbf{N} \end{aligned}$$

where  $\text{addr}_\omega$  maps names from a name space  $\mathbf{N}$  to addresses from an address space  $\mathbf{A}$ ,  $\text{server}_{\omega, \psi}$  maps labels from a label space  $\mathbf{L}$  to the node that stores it,  $\text{route}_\omega$  maps two nodes to the set of nodes on the route between them, and  $\text{fe}_\phi$  maps labels to node addresses who forward client requests to the rest of the network. For visual clarity we abuse notation and represent the path between two addresses by a *set* of addresses instead of as a sequence of addresses, but we stress that paths are sequences. Note that this is an abstract representation of a DHT that will be particularly useful for our analysis but, in practice, these are implemented by the six algorithms defined in the last section.

We also note that at any time, a DHT only has a subset  $\mathbf{C} \subseteq \mathbf{N}$  of active nodes (i.e., the nodes currently in the network); e.g., one can think of  $\mathbf{N}$  as the set of all IPv4 addresses but only a subset would join the DHT network. Together  $\omega$  and  $\mathbf{C}$  create an overlay, and henceforth we refer to  $(\omega, \mathbf{C})$  as an overlay.

**Instantiating abstractions for Chord.** For Chord,  $\omega = H_1$  and  $\psi = H_2$ , where  $H_1$  and  $H_2$  are modeled as random oracles. Then the overlay  $(\omega, \mathbf{C})$  is equivalent to a configuration  $\chi = \{H_1(N_1), \dots, H_1(N_n)\}$ . The map  $\text{addr}_\omega$  is  $H_1$  which assigns to each active node  $N \in \mathbf{C}$  an address  $H_1(N)$  in  $\mathbf{A}$ . The map  $\text{server}_{\omega, \psi}$  is the function  $\text{succ} \circ H_2$ , that stores a label  $\ell$  at the successor of  $H_2(\ell)$ . Recall that given a configuration  $\chi$ , the route between any two nodes is fixed. Therefore, the  $\text{route}_\omega$  map for Chord is deterministic and well defined.

Further recall that Chord allows its clients to choose any node as the front-end node to issue its operations. Moreover, it does not restrict them to connect to the same node  $\text{fe}_\phi(\ell)$ , time the client wants to query the same  $\ell$ . This means that for Chord,  $\text{fe}_\phi$  is not necessarily a function but can be a one-to-many relation. Unfortunately we will later see that we cannot prove that an EDHT based on Chord is “secure” for arbitrary  $\text{fe}_\phi$ ’s. We therefore modify Chord and let  $\phi$  be a third hash function  $H_3$  that maps labels to nodes currently active. Then,  $\text{fe}_\phi$  is the hash function  $H_3$  itself that assigns a front-end node  $H_3(\ell)$  to each request for  $\ell$ .

**Visible addresses.** An important notion for our purposes will be that of the set of *visible addresses* to a node. Intuitively, we say that an address  $a$  is visible to a node  $N$ , if labels mapped to  $a$  are either stored by  $N$  or are routed by it. Notice that whether or not addresses mapped to  $a$  are routed by  $N$  depend on the node where the request for the label originates. Changing the frontend node, changes the route, even if the destination node remains the same. Therefore, instead of simply defining the visibility of a node, we define what we call a node’s  $N_s$ -visibility, where  $N_s$  is the starting node of the routes. Throughout we assume the set of visible addresses to be efficiently computable.

**Definition 3.1** ( $N_s$ -visibility). *Let  $(\omega, \mathbf{C})$  be an overlay,  $\psi$  be an allocation parameter and  $N_s \in \mathbf{C}$  be an active node. Then we say an address  $a \in \mathbf{A}$  is  $N_s$ -visible to a node  $N \in \mathbf{C}$  if there exists a label  $\ell \in \mathbf{L}$  such that if  $\psi$  allocates  $\ell$  to  $a$ , then either: (1)  $N = \text{server}_{\omega, \psi}(\ell)$ ; or (2)  $N \in \text{route}_\omega(N_s, \text{server}_{\omega, \psi}(\ell))$ . We denote the set of  $N_s$ -visible addresses to  $N$  by  $\text{Vis}(N_s, N)$ .*

Since the set of  $N_s$ -visible addresses depends on  $\omega$  and the set  $\mathbf{C}$  of nodes that are currently active, we subscript  $\text{Vis}_{\omega, \mathbf{C}}(N_s, N)$  with all these parameters. Finally, we extend the notion of visibility of a single node to the visibility of a set of nodes  $S \subseteq \mathbf{C}$ . It is defined simply as the union of visibilities of individual nodes, i.e., for  $S \subseteq \mathbf{C}$ ,  $\text{Vis}_{\omega, \mathbf{C}}(N_s, S) = \cup_{N \in S} \text{Vis}_{\omega, \mathbf{C}}(N_s, N)$ . Again, for visual clarity, we will drop the subscripts wherever they are clear from the context.

**Visibility in Chord.** Given a configuration  $\chi$ , let *arc* of a node  $N$  is the set of addresses in  $\mathbf{A}$  between  $N$  and its predecessor in  $\chi$  (see Figure 1). More formally, we write  $\text{arc}_{\chi}(N) = (\text{pred}_{\chi}(H_1(N)), \dots, H_1(N)]$ , where  $\text{pred}_{\chi}(N)$  is the *predecessor* function defined earlier.

Recall that an address  $a$  is visible to a node  $N$ , if (1)  $N$  stores the labels hashed to  $a$  or, (2)  $N$  routes the labels hashed to  $a$  (starting from  $N_s$ ). In Chord, a node  $N$  stores all the labels that are hashed to its arc. Therefore, due to (1), all the addresses in  $N$ 's arc are visible to it. Moreover, due to (2), addresses in the arcs of any other node  $N'$  are also  $N_s$ -visible to  $N$ , if  $N$  falls on the route between  $N_s$  and  $N'$ . This is because, all the labels hashed in the arc of  $N'$  will be routed by  $N$ . In summary, given a fixed configuration  $\chi$ , and two distinct nodes  $N_s, N \in \mathbf{C}$ :

$$\text{Vis}_{\chi \mathbf{C}}(N_s, N) = \text{arc}_{\chi \mathbf{C}}(N) \cup \left\{ \text{arc}_{\chi \mathbf{C}}(N') : N \in \text{route}_{\chi \mathbf{C}}(N_s, N') \right\}$$

**Allocation distribution.** The next important notion in our analysis is what we refer to as a label's *allocation distribution* which is the probability distribution that governs the address at which a label is allocated. More precisely, this is captured by the random variable  $\psi(\ell)$ , where  $\psi$  is sampled by the algorithm `Alloc`. We therefore simply refer to this distribution as the DHT's allocation distribution.

Given a DHT's allocation distribution, we also consider a distribution  $\Delta(S)$  that is parameterized by a set of addresses  $S \subseteq \mathbf{A}$ . This distribution is over  $S$  and has probability mass function

$$f_{\Delta(S)}(a) = \frac{\Pr[\psi(\ell) = a]}{\Pr[\psi(\ell) \in S]}.$$

We assume that given a subset  $S \subseteq \mathbf{A}$ ,  $\Delta(S)$  is efficiently computable.

For the case of Chord, recall that it assigns labels to addresses using a random oracle  $H_2$ . Therefore it follows that for all configurations  $\chi$ , all labels  $\ell \in \mathbf{L}$  and all subsets  $S \subseteq \mathbf{A}$ , and all  $a \in S$ ,

$$f_{\Delta(S)}(a) = \frac{\Pr[H_2(\ell) = a]}{\Pr[H_2(\ell) \in S]} = \frac{\frac{1}{|\mathbf{A}|}}{\frac{|S|}{|\mathbf{A}|}} = \frac{1}{|S|}.$$

**Non-committing allocations.** As we will see in Section 4.2, our EDHT construction can be based on any DHT but the security of the resulting scheme will depend on certain properties of the underlying DHT. We describe these properties here. The first property that we require of a DHT is that the allocations it produces be non-committing in the sense that it supports a form of equivocation. More precisely, for some fixed overlay  $(\omega, \mathbf{C})$  and allocation parameter  $\psi$ , there should exist some efficient mechanism to arbitrarily change/program  $\psi$ . In other words, there should exist a polynomial-time algorithm `Program` such that, for all  $(\omega, \mathbf{C})$  and  $\psi$ , given a label  $\ell \in \mathbf{L}$  and address  $a \in \mathbf{A}$ , `Program`( $\ell, a$ ) modifies the DHT so that  $\psi(\ell) = a$ .

For the special case of Chord, given a label  $\ell$  and an address  $a$ , the allocation parameter  $H_2$  can be changed by programming the random oracle  $H_2$  to output  $a$  when it is queried on  $\ell^2$ .

<sup>2</sup>This is also true for every DHT we are aware of [21, 15, 28, 13].

**Balanced overlays.** The second property is related to how well the DHT load balances the label/value pairs it stores. While load balancing is clearly important for storage efficiency we will see, perhaps surprisingly, that it also has an impact on security. Intuitively, we say that an overlay  $(\omega, \mathbf{C})$  is balanced if for all labels  $\ell$ , the probability that any set of  $\theta$  nodes “sees”  $\ell$  is small.

**Definition 3.2** (Balanced overlays). *Let  $\omega \in \Omega$  be an overlay parameter and let  $\mathbf{C} \subseteq \mathbf{N}$  be a set of active nodes. We say that an overlay  $(\omega, \mathbf{C})$  is  $(\varepsilon, \theta)$ -balanced if for all  $\ell \in \mathbf{L}$  and for all  $S \subseteq \mathbf{C}$  with  $|S| = \theta$ ,*

$$\Pr \left[ S \cap \text{route}_\omega \left( \text{fe}_\phi(\ell), \text{server}_{\omega, \psi}(\ell) \right) \neq \emptyset \right] \leq \varepsilon$$

where the probability is over the coins of `Alloc` and `FrontEnd` and where  $\varepsilon$  can depend on  $\theta$  and  $|\mathbf{C}|$ .

We will later see that the better the balance, the better the security guarantee of the standard EDHT. The reason is that, intuitively, if an adversary sees a label with low probability, then it learns information about it with low probability.

**Definition 3.3** (Balanced DHT). *We say that a distributed hash table  $\text{DHT} = (\text{Overlay}, \text{Alloc}, \text{FrontEnd}, \text{Daemon}, \text{Put}, \text{Get})$  is  $(\varepsilon, \delta, \theta)$ -balanced if for all  $\mathbf{C} \subseteq \mathbf{N}$ , the probability that an overlay  $(\omega, \mathbf{C})$  is  $(\varepsilon, \theta)$ -balanced is at least  $1 - \delta$  over the coins of `Overlay` and where  $\varepsilon$  and  $\delta$  can depend on  $\mathbf{C}$  and  $\theta$ .*

**Balance of Chord.** We now analyze the balance of Chord. We show that with high probability, Chord samples an  $H_1$  (i.e., a configuration  $\chi$ ) such that the visibility of any  $\theta$  nodes is not too large. Showing this is non-trivial and requires us to bound the total lengths of  $\theta$  (possibly non-contiguous) arcs in  $\chi$ . Let  $\text{sumarcs}(\chi_{\mathbf{C}}, x)$  be the random variable denoting the total lengths of *any*  $x$  arcs in configuration  $\chi$ .

One way to bound  $\text{sumarcs}(\chi_{\mathbf{C}}, x)$  is to bound the length of the largest arc, and then use a union bound on it for  $x$  arcs. Precisely, if the length of the largest arc is at most  $\lambda$ , then the total length of any  $\theta$  arcs can be at most  $\theta\lambda$ . Unfortunately, this is a very weak bound, and we improve it by noticing that there cannot be a lot of very large arcs in a configuration. Intuitively, if one arc is on the larger side, then others will be on the smaller side. Formally speaking, the arc lengths are negatively dependent on each other, and we use the following result from [4]. We adapt their theorem in our notation.

**Theorem 3.4** ([4]). *Let  $\chi_{\mathbf{C}}$  be a configuration chosen uniformly at random. Then for  $\theta \leq 4ne^{-2}$ ,*

$$\Pr \left[ \text{sumarcs}(\chi_{\mathbf{C}}, \theta) \leq \frac{6\theta|\mathbf{A}|}{n} \log \left( \frac{n}{\theta} \right) \right] \geq 1 - o \left( \frac{1}{n} \right)$$

Notice that this bound is only  $O(\log \frac{n}{\theta})$  away from the optimal: in the best case, all the arcs are of average length  $|\mathbf{A}|/n$ , setting a lower bound of  $\theta|\mathbf{A}|/n$  on  $\text{sumarcs}(\chi_{\mathbf{C}}, \theta)$ .

Also notice that this theorem in some sense bounds the probability that a label will be stored at one of the  $\theta$  adversarial nodes. This is because, Chord maps labels to addresses with uniform probability, and Theorem 3.4 bounds the fraction of the address space that the adversary holds in

its arcs. Formally, for a set of nodes  $I$  such that  $|I| = \theta < 4ne^{-2}$ , with probability at least  $1 - o(\frac{1}{n})$ ,

$$\begin{aligned}
\Pr \left[ \text{server}(\ell) \in I \right] &= \Pr \left[ H_2(\ell) \in \bigcup_{N \in I} \text{arc}(N) \right] \\
&= \frac{|\bigcup_{N \in I} \text{arc}_\chi(N)|}{|\mathbf{A}|} \\
&\leq \frac{\text{sumarcs}(\chi, |I|)}{|\mathbf{A}|} \\
&\leq \frac{6\theta}{n} \log \left( \frac{n}{\theta} \right) \tag{1}
\end{aligned}$$

Finally, we bound the probability that a label is routed by an adversarial node. The main idea is the following: for all labels  $\ell$ , given a random front end node (due to  $H_3$ ), and an (almost) random destination node (due to  $H_2$ ), the adversary cannot place itself on  $\ell$ 's route with very high probability, especially when Chord ensures that routes are at most  $\log n$  long. Formally, we show the following:

**Theorem 3.5.** *Let  $\chi_{\mathbf{C}}$  be a configuration chosen uniformly at random. Then for all labels  $\ell$ , and for all  $I \subseteq \mathbf{C} \setminus \{\text{fe}(\ell), \text{server}(\ell)\}$ , with  $|I| = \theta \leq n/\log n$ ,*

$$\Pr \left[ I \cap \text{route}(\text{fe}(\ell), \text{server}(\ell)) \neq \emptyset \right] \leq \frac{\theta \log n}{n}. \tag{2}$$

*Proof.* For all  $\ell \in \mathbf{L}$ , let  $\mathcal{E}$  be the event that at least one of the nodes in  $I$  is on the path to the server of  $\ell$ . Precisely,

$$\mathcal{E} = \{I \cap \text{route}(\text{fe}(\ell), \text{server}(\ell)) \neq \emptyset\}$$

By the union bound and the law of total probability, we have that,

$$\begin{aligned}
\Pr[\mathcal{E}] &= \Pr[I \cap \text{route}(\text{fe}(\ell), \text{server}(\ell)) \neq \emptyset] \\
&\leq \sum_{N \in I} \Pr[N \in \text{route}(\text{fe}(\ell), \text{server}(\ell))] \\
&= \sum_{N \in I} \sum_{N_s \in \mathbf{C}} \sum_{N_d \in \mathbf{C}} \Pr[N \in \text{route}(N_s, N_d) \mid \text{server}(\ell) = N_d \wedge \text{fe}(\ell) = N_s] \cdot \\
&\quad \Pr[\text{fe}(\ell) = N_s \mid \text{server}(\ell) = N_d] \cdot \Pr[\text{server}(\ell) = N_d] \\
&= \sum_{N \in I} \sum_{N_s \in \mathbf{C}} \sum_{N_d \in \mathbf{C}} \Pr[N \in \text{route}(N_s, N_d) \mid \text{server}(\ell) = N_d \wedge \text{fe}(\ell) = N_s] \cdot \\
&\quad \Pr[\text{fe}(\ell) = N_s] \cdot \Pr[\text{server}(\ell) = N_d] \tag{3}
\end{aligned}$$

where, the last equality follows from the fact that  $\text{fe}(\ell)$  and  $\text{server}(\ell)$  are chosen independently. But note that,

$$\Pr[N \in \text{route}(N_s, N_d) \mid \text{server}(\ell) = N_d \wedge \text{fe}(\ell) = N_s] \leq \frac{\log n}{n}$$

which follows from the fact that path lengths in Chord are at most  $\log n$ . Substituting this in Eq.

(3) we get,

$$\begin{aligned}
\Pr[\mathcal{E}] &\leq \sum_{N \in I} \sum_{N_s \in \mathbf{C}} \sum_{N_d \in \mathbf{C}} \frac{\log n}{n} \cdot \Pr[\text{fe}(\ell) = N_s] \cdot \Pr[\text{server}(\ell) = N_d] \\
&\leq \sum_{N \in I} \frac{\log n}{n} \sum_{N_s \in \mathbf{C}} \sum_{N_d \in \mathbf{C}} \Pr[\text{fe}(\ell) = N_s] \cdot \Pr[\text{server}(\ell) = N_d] \\
&= \sum_{N \in I} \frac{\log n}{n} \\
&= \frac{\theta \log n}{n}
\end{aligned}$$

□

We now use Equations 1 and 2 to show that Chord is balanced.

**Theorem 3.6.** *Chord, is  $(\varepsilon, \delta, \theta)$  balanced for:*

$$\varepsilon = \frac{8\theta \log n}{n} \quad \text{and} \quad \theta \leq \frac{n}{8 \log n} \quad \text{and} \quad \delta = 1 - o\left(\frac{1}{n}\right)$$

*Proof.* Given a  $\chi$ , we bound the probability that for a label  $\ell$ , an adversarial node is on the route from  $\text{fe}(\ell)$  to  $\text{server}(\ell)$ . There are three ways in which this can happen: (1) front end node is corrupted, or (2) the storage node is corrupted, or (3) one of the nodes on the route (excluding  $\text{fe}(\ell)$  and  $\text{server}(\ell)$ ) are corrupted. Therefore, we have that:

$$\begin{aligned}
&\Pr\left[I \cap \text{route}(\text{fe}(\ell), \text{server}(\ell)) \neq \emptyset\right] \\
&= \Pr\left[\text{fe}(\ell) \in I\right] + \Pr\left[\text{server}(\ell) \in I\right] + \Pr\left[I \cap \text{route}(\text{fe}(\ell), \text{server}(\ell)) \neq \emptyset \mid \text{fe}(\ell) \notin I \wedge \text{server}(\ell) \notin I\right] \\
&= \Pr\left[H_3(\ell) \in I\right] + \frac{6\theta}{n} \log\left(\frac{n}{\theta}\right) + \Pr\left[I \cap \text{route}(H_3(\ell), \text{server}(\ell)) \neq \emptyset \mid H_3(\ell) \notin I \wedge \text{server}(\ell) \notin I\right] \\
&\leq \frac{\theta}{n} + \frac{6\theta}{n} \log\left(\frac{n}{\theta}\right) + \frac{\theta \log n}{n} \\
&\leq \frac{8\theta \log n}{n}
\end{aligned} \tag{4}$$

where the second and third inequalities follow from Equations 1 and 2. Note that the bound above only makes sense for  $\theta < n/8 \log n$ . Finally, we know that Equation 1 holds with probability  $1 - o(\frac{1}{n})$ , therefore, we conclude that Chord is balanced for the given values of  $\varepsilon$ ,  $\delta$  and  $\theta$ . □

Note that assigning labels uniformly at random to nodes would achieve  $\varepsilon = \theta/n$ , whereas Theorem 3.6 achieves  $\varepsilon = O(\theta \log n/n)$ . This shows that the balance of Chord is only  $\log n$  factor away from optimal balance which is very good given that the optimal balance is achieved with no routing at all.

## 4 Encrypted Distributed Hash Tables in the Perpetual Setting

In this Section, we formally define encrypted distributed hash tables. An EDHT is an end-to-end encrypted distributed system that instantiates a dictionary data structure.

**Functionality  $\mathcal{F}_{\text{DHT}}^{\mathcal{L}}$**

$\mathcal{F}_{\text{DHT}}^{\mathcal{L}}$  stores a dictionary  $\text{DX}$  initialized to empty and proceeds as follows, running with client  $\mathcal{C}$ ,  $n$  nodes  $N_1, \dots, N_n$  and a simulator  $\text{Sim}$ :

- **Put**( $\ell, v$ ): Upon receiving a label/value pair  $(\ell, v)$  from client  $\mathcal{C}$ , it sets  $\text{DX}[\ell] := v$ , and sends the leakage  $\mathcal{L}(\text{DX}, (\text{put}, \ell, v))$  to the simulator  $\text{Sim}$ .
- **Get**( $\ell$ ): Upon receiving a label  $\ell$  from client  $\mathcal{C}$ , it returns  $\text{DX}[\ell]$  to the client  $\mathcal{C}$  and the leakage  $\mathcal{L}(\text{DX}, (\text{get}, \ell, \perp))$  to the simulator  $\text{Sim}$ .

Figure 2:  $\mathcal{F}_{\text{DHT}}^{\mathcal{L}}$ : The DHT functionality parameterized with leakage function  $\mathcal{L}$ .

#### 4.1 Syntax and Security Definitions

**Syntax.** We formalize symmetric EDHTs as a collection of seven algorithms  $\text{EDHT} = (\text{Gen}, \text{Overlay}, \text{Alloc}, \text{FrontEnd}, \text{Daemon}, \text{Put}, \text{Get})$ . The first algorithm  $\text{Gen}$  is executed by a client and takes as input a security parameter  $1^k$  and outputs a secret key  $K$ . All the other algorithms have the same syntax as before (See Section 3), with the difference that  $\text{Get}$  and  $\text{Put}$  also take the secret key  $K$  as input.

**Security.** We now turn to formalizing the security of an EDHT. We do this by combining the definitional approaches used in secure multi-party computation [5] and in structured encryption [10, 9]. The security of multi-party protocols is generally formalized using the Real/Ideal-world paradigm. This approach consists of defining two probabilistic experiments **Real** and **Ideal** where the former represents a real-world execution of the protocol where the parties are in the presence of an adversary, and the latter represents an ideal-world execution where the parties interact with a trusted functionality. The protocol is secure if no environment can distinguish between the outputs of these two experiments. Below, we will describe both these experiments more formally.

Before doing so, we discuss an extension to the standard definitions. To capture the fact that a protocol could leak information to the adversary, we parameterize the definition with a leakage profile that consists of a leakage function  $\mathcal{L}$  that captures the information leaked by the  $\text{Put}$  and  $\text{Get}$  operations. Our motivation for making the leakage explicit is to highlight its presence.

**The real-world experiment.** The experiment is executed between a trusted party  $\mathcal{T}$ , a client  $\mathcal{C}$ , a set  $\mathbf{C} \subseteq \mathbf{N}$  of  $n$  nodes  $N_1, \dots, N_n$ , an environment  $\mathcal{Z}$  and an adversary  $\mathcal{A}$ . The trusted party  $\mathcal{T}$  runs  $\text{Overlay}(n)$  and  $\text{Alloc}(n)$  and  $\text{FrontEnd}(n)$ , and sends  $\Gamma = (\omega, \psi, \phi)$  to all parties, i.e., the nodes, the client, the environment and the adversary. Given  $z \in \{0, 1\}^*$ , the environment  $\mathcal{Z}$  sends to the adversary  $\mathcal{A}$ , a subset  $I \subseteq \mathbf{C}$  of nodes to corrupt. The client  $\mathcal{C}$  generates a secret key  $K \leftarrow \text{Gen}(1^k)$ . The nodes execute  $\text{EDHT.Daemon}(\Gamma, n)$ .  $\mathcal{Z}$  then adaptively chooses a polynomial number of operations  $\text{op}_j$ , where  $\text{op}_j \in \{\text{get}, \text{put}\} \times \mathbf{L} \times \{\mathbf{V}, \perp\}$  and sends it to  $\mathcal{C}$ . If  $\text{op}_j = (\text{get}, \ell)$ , the client  $\mathcal{C}$  executes  $\text{EDHT.Get}(K, \ell)$ . If  $\text{op}_j = (\text{put}, \ell, v)$ ,  $\mathcal{C}$  initiates  $\text{EDHT.Put}(K, \ell, v)$ . The client forwards its output from running the get/put operations to  $\mathcal{Z}$ .  $\mathcal{A}$  computes a message  $m$  from its view and sends it to  $\mathcal{Z}$ . Finally,  $\mathcal{Z}$  returns a bit that is output by the experiment. We let  $\text{Real}_{\mathcal{A}, \mathcal{Z}}(k)$  be a random variable denoting  $\mathcal{Z}$ 's output bit.

**The ideal-world experiment.** The experiment is executed between a client  $\mathcal{C}$ , a set  $\mathbf{C} \subseteq \mathbf{N}$  of  $n$  nodes  $N_1, \dots, N_n$ , an environment  $\mathcal{Z}$  and a simulator  $\text{Sim}$ . Each party also has access to the ideal functionality  $\mathcal{F}_{\text{DHT}}^{\mathcal{L}}$ . Given  $z \in \{0, 1\}^*$ , the environment  $\mathcal{Z}$  sends to the simulator



Sim, a subset  $I \subseteq \mathbf{C}$  of nodes to corrupt.  $\mathcal{Z}$  then adaptively chooses a polynomial number of operations  $\text{op}_j$ , where  $\text{op}_j \in \{\text{get}, \text{put}\} \times \mathbf{L} \times \{\mathbf{V}, \perp\}$ , and sends it to the client  $\mathcal{C}$  which, in turn, forwards it to  $\mathcal{F}_{\text{DHT}}^{\mathcal{L}}$ . If  $\text{op}_j = (\text{get}, \ell)$ , the functionality executes  $\mathcal{F}_{\text{DHT}}^{\mathcal{L}}.\text{Get}(\ell)$ . Otherwise, if  $\text{op}_j = (\text{put}, \ell, v)$  the functionality executes  $\mathcal{F}_{\text{DHT}}^{\mathcal{L}}.\text{Put}(\ell, v)$ .  $\mathcal{C}$  forwards its outputs to  $\mathcal{Z}$  whereas Sim sends  $\mathcal{Z}$  some arbitrary message  $m$ . Finally,  $\mathcal{Z}$  returns a bit that is output by the experiment. We let  $\mathbf{Ideal}_{\text{Sim}, \mathcal{Z}}(k)$  be a random variable denoting  $\mathcal{Z}$ 's output bit.

**Definition 4.1** ( $\mathcal{L}$ -security). *We say that an encrypted distributed hash table  $\text{EDHT} = (\text{Gen}, \text{Overlay}, \text{Alloc}, \text{FrontEnd}, \text{Daemon}, \text{Put}, \text{Get})$  is  $\mathcal{L}$ -secure, if for all PPT adversaries  $\mathcal{A}$  and all PPT environments  $\mathcal{Z}$ , there exists a PPT simulator Sim such that for all  $z \in \{0, 1\}^*$ ,*

$$|\Pr[\mathbf{Real}_{\mathcal{A}, \mathcal{Z}}(k) = 1] - \Pr[\mathbf{Ideal}_{\text{Sim}, \mathcal{Z}}(k) = 1]| \leq \text{negl}(k).$$

## 4.2 The Standard EDHT in the Perpetual Setting

We now describe the standard approach to storing sensitive data on a DHT. This approach relies on simple cryptographic primitives and a non-committing and balanced DHT.

**Overview.** The scheme  $\text{EDHT} = (\text{Gen}, \text{Overlay}, \text{Alloc}, \text{Daemon}, \text{Put}, \text{Get})$  is described in detail in Figure 3 and, at a high level, works as follows. It makes black-box use of a distributed hash table  $\text{DHT} = (\text{Overlay}, \text{Alloc}, \text{Daemon}, \text{Put}, \text{Get})$ , a pseudo-random function  $F$  and a symmetric-key encryption scheme  $\text{SKE} = (\text{Gen}, \text{Enc}, \text{Dec})$ .

The **Gen** algorithm takes as input a security parameter  $1^k$  and uses it to generate a key  $K_1$  for the pseudo-random function  $F$  and a key  $K_2$  for the symmetric encryption scheme **SKE**. It then outputs a key  $K = (K_1, K_2)$ . The **Overlay**, **Alloc**, **FrontEnd** and **Daemon** algorithms respectively execute  $\text{DHT.Overlay}$ ,  $\text{DHT.Alloc}$ ,  $\text{DHT.FrontEnd}$  and  $\text{DHT.Daemon}$  to generate and output the parameters  $\omega$ ,  $\psi$  and  $\phi$ . The **Put** algorithm takes as input the secret key  $K$  and a label/value pair  $(\ell, v)$ . It first computes  $t := F_{K_1}(\ell)$  and  $e \leftarrow \text{Enc}(K_2, v)$  and then executes  $\text{DHT.Put}(t, e)$ . The **Get** algorithm takes as input the secret key  $K$  and a label  $\ell$ . It computes  $t := F_{K_1}(\ell)$  and executes  $e \leftarrow \text{DHT.Get}(t)$ . It then outputs  $\text{SKE.Dec}(K, e)$ .

**Security.** We now describe the leakage of EDHT. Intuitively, it reveals to the adversary the times at which a label is stored or retrieved with some probability. More formally, it is defined with the following *stateful* leakage function

- $\mathcal{L}_\varepsilon(\text{DX}, (\text{op}, \ell, v))$  :
  1. if  $\ell$  has never been seen
    - (a) sample and store  $b_\ell \leftarrow \text{Ber}(\varepsilon)$
  2. if  $b_\ell = 1$ 
    - (a) if  $\text{op} = \text{put}$ , output  $(\text{put}, \text{oqeq}(\ell))$
    - (b) else if  $\text{op} = \text{get}$ , output  $(\text{get}, \text{oqeq}(\ell))$
  3. else if  $b_\ell = 0$ 
    - (a) output  $\perp$

where **oqeq** is the *operation equality pattern* which reveals if and when a label was queried or put in the past. Note that when  $\varepsilon = 1$  (for some  $\theta$ ),  $\mathcal{L}_\varepsilon$  reduces to the leakage profile achieved by standard encrypted dictionary constructions [9, 7]. On the other hand, when  $\varepsilon < 1$ , this leakage profile is “better” than the profile of known constructions.

Let  $\text{DHT} = (\text{Overlay}, \text{Alloc}, \text{Daemon}, \text{Put}, \text{Get})$  be a distributed hash table,  $\text{SKE} = (\text{Gen}, \text{Enc}, \text{Dec})$  be a symmetric-key encryption scheme and  $F$  be a pseudo-random function. Consider the encrypted distributed hash table  $\text{EDHT} = (\text{Gen}, \text{Overlay}, \text{Alloc}, \text{Daemon}, \text{Put}, \text{Get})$  that works as follows:

- $\text{Gen}(1^k)$ :
  1. sample  $K_1 \xleftarrow{\$} \{0, 1\}^k$  and compute  $K_2 \leftarrow \text{SKE.Gen}(1^k)$
  2. output  $K = (K_1, K_2)$
- $\text{Overlay}(n)$ :
  1. compute and output  $\omega \leftarrow \text{DHT.Overlay}(n)$
- $\text{Alloc}(n)$ :
  1. compute and output  $\psi \leftarrow \text{DHT.Alloc}(n)$
- $\text{FrontEnd}(n)$ :
  1. compute and output  $\phi \leftarrow \text{DHT.FrontEnd}(n)$
- $\text{Daemon}(\omega, \psi, \phi, n)$  :
  1. Execute  $\text{DHT.Daemon}(\omega, \psi, \phi, n)$
- $\text{Put}(K, \ell, v)$  :
  1. Parse  $K$  as  $(K_1, K_2)$
  2. compute  $t := F_{K_1}(\ell)$
  3. compute  $e \leftarrow \text{SKE.Enc}(K_2, v)$
  4. execute  $\text{DHT.Put}(t, e)$
- $\text{Get}(K, \ell)$ :
  1. Parse  $K$  as  $(K_1, K_2)$
  2. Initialise  $v := \perp$
  3. compute  $t := F_{K_1}(\ell)$
  4. execute  $e \leftarrow \text{DHT.Get}(t)$
  5. if  $e \neq \perp$ , compute and output  $v \leftarrow \text{SKE.Dec}(K_2, e)$

Figure 3: The Standard EDHT Scheme

**Discussion.** We now explain why the leakage function is probabilistic and why it depends on the balance of the underlying DHT. Intuitively, one expects that the adversary’s view is only affected by get and put operations on labels that are either: (1) allocated to a corrupted node; (2) start at a corrupted front end node; or (3) allocated to an uncorrupted node whose path (starting from the client) includes a corrupted node. In such a case, the adversary’s view would not be affected by all operations but only a subset of them. Our leakage function captures this intuition precisely and it is probabilistic because, in the real world, the subset of operations that affect the adversary’s view is determined probabilistically because it depends on the choice of overlay and allocation—both of which are chosen at random. The way this is handled in the leakage function is by sampling a bit  $b$  with some probability and revealing leakage on the current operation if  $b = 1$ . This determines the subset of operations whose leakage will be visible to the adversary.

Now, for the simulation to go through, the operations simulated by the simulator need to be

visible to the adversary with the same probability as in the real execution. But these probabilities depend on DHT parameters  $\Gamma = (\omega, \psi, \phi)$ , which are not known to the leakage function. Note that this implies a rather strong definition in the sense that the scheme hides information about the overlay and the allocation of the DHT.

Since  $\omega$ ,  $\psi$  and  $\phi$  are unknown to the leakage function, the leakage function can only guess as to what they could be. But because the DHT is guaranteed to be  $(\varepsilon, \delta, \theta)$ -balanced, the leakage function can assume that, with probability at least  $1 - \delta$ , the overlay will be  $(\varepsilon, \theta)$ -balanced which, in turn, guarantees that the probability that a label is visible to any adversary with at most  $\theta$  corruptions is at most  $\varepsilon$ . Therefore, in our leakage function, we can set the probability that  $b = 1$  to be  $\varepsilon$  in the hope that simulator can “adjust” the probability internally to be in accordance to the  $\omega$  that it sampled. Note that the simulator can adjust the probability only if for its own chosen  $\omega$ , the probability that a query is visible to the adversary is less than  $\varepsilon$ . But this will happen with probability at least  $1 - \delta$  so the simulation will work with probability at least  $1 - \delta$ .

We are now ready to state our main security Theorem which proves that the standard EDHT construction is  $\mathcal{L}_\varepsilon$ -secure with probability that is negligibly close to  $1 - \delta$  when its underlying DHT is  $(\varepsilon, \delta, \theta)$ -balanced.

**Theorem 4.2.** *If  $|I| \leq \theta$  and if DHT is  $(\varepsilon, \delta, \theta)$ -balanced and has non-committing allocation, then EDHT is  $\mathcal{L}_\varepsilon$ -secure with probability at least  $1 - \delta - \text{negl}(k)$ .*

*Proof.* Consider the simulator  $\text{Sim}$  that works as follows. Given a set of corrupted nodes  $I \subseteq \mathbf{C}$ , it computes  $\omega \leftarrow \text{DHT.Overlay}(n)$ ,  $\phi \leftarrow \text{DHT.FrontEnd}(n)$ , initializes  $n$  nodes  $N_1, \dots, N_n$  in  $\mathbf{C}$ , simulates the adversary  $\mathcal{A}$  with  $I$  as input, and generates a symmetric key  $K \leftarrow \text{SKE.Gen}(1^k)$ . When a put/get operation is executed,  $\text{Sim}$  receives from  $F_{\text{DHT}}$  the leakage

$$\lambda \in \left\{ \left( \text{put}, \text{oqeq}(\ell) \right), \left( \text{get}, \text{oqeq}(\ell) \right), \perp \right\}.$$

If  $\lambda = \perp$  then  $\text{Sim}$  does nothing. If  $\lambda \neq \perp$ , then  $\text{Sim}$  checks the operation equality to see if the label has been seen in the past. There are two cases:

1. **Label was not seen in the past:** If the label was not seen in the past (as deduced from operation equality), it sets  $t \xleftarrow{\$} \{0, 1\}^d$ , and samples and stores a bit

$$b' \leftarrow \text{Ber} \left( \frac{p'}{\varepsilon} \right).$$

where,  $p' \stackrel{\text{def}}{=} \Pr [\psi(t) \in \text{Vis}(\text{fe}_\phi(t), I)]$ . Note that, this is indeed a valid Bernoulli distribution since

$$p' = \Pr [\psi(t) \in \text{Vis}(\text{fe}(t), I)] \leq \varepsilon,$$

where the last inequality follows from  $|I| \leq \theta$  and  $(\omega, \mathbf{C})$  being  $(\varepsilon, \theta)$ -balanced.

If  $b' = 0$ , it does nothing, but if  $b' = 1$ , it computes  $e \leftarrow \text{SKE.Enc}(K, 0)$ , sets the front-end node  $N_s \leftarrow \text{fe}(t)$ , samples an address  $a \leftarrow \Delta(\text{Vis}(\text{fe}(t), I))$ . It then programs  $\psi$  to map  $t$  to  $a$ . Finally, if the operation was a put, it executes  $\text{DHT.Put}(t, e)$ , otherwise it executes  $\text{DHT.Get}(t)$ .

2. **Label was seen in the past:** If the label was seen in the past (as deduced from operation equality), **Sim** retrieves the bit  $b'$  that was previously sampled. If  $b' = 0$ , then it does nothing, but if  $b' = 1$  it sets  $t$  to the  $d$ -bit value previously used, and computes  $e \leftarrow \text{SKE.Enc}(K, 0)$ . Finally, if the operation was a put, it executes  $\text{DHT.Put}(t, e)$ , otherwise it executes  $\text{DHT.Get}(t)$ .

Once all of the environment's operations are processed, the simulator returns whatever the adversary outputs.

It remains to show that the view of the adversary  $\mathcal{A}$  during the simulation is indistinguishable from its view in a **Real** experiment. We do this using a sequence of games.

**Game<sub>0</sub>** : is the same as a  $\text{Real}_{\mathcal{A}, \mathcal{Z}}(k)$  experiment.

**Game<sub>1</sub>** : is the same as **Game<sub>0</sub>** except that the encryption of the value  $v$  during a **Put** is replaced by  $\text{SKE.Enc}(K_2, 0)$ .

**Game<sub>2</sub>** : is the same as **Game<sub>1</sub>** except that output of the PRF  $F$  is replaced by a truly random string of  $d$  bits.

**Game<sub>3</sub>** : is the same as **Game<sub>2</sub>** except that for each operation  $(\text{op}, \ell, v)$  (where  $v$  can be null), we check if  $\ell$  has been seen before. If not, we sample a bit  $b_\ell \leftarrow \text{Ber}(\varepsilon)$ , else we set  $b_\ell$  to the bit previously sampled. If  $b_\ell = 1$  and  $\text{op} = (\text{put}, \ell, v)$ , we replace the **Put** operation with  $\text{Sim}(\text{put}, \text{oqq}(\ell))$ , and if  $b_\ell = 1$  and  $\text{op} = (\text{get}, \ell)$ , we replace the **Get** operation with  $\text{Sim}(\text{get}, \text{oqq}(\ell))$ . If  $b_\ell = 0$ , we do nothing.

**Game<sub>1</sub>** is indistinguishable from **Game<sub>0</sub>**, otherwise the encryption scheme is not semantically secure. **Game<sub>2</sub>** is indistinguishable from **Game<sub>1</sub>** because the outputs of pseudorandom functions are indistinguishable from random strings.

We now show that the adversary's views in **Game<sub>2</sub>** and **Game<sub>3</sub>** are indistinguishable. We denote these views by  $\text{view}_2(I)$  and  $\text{view}_3(I)$ , respectively, and consider the  $i$ th "sub-views"  $\text{view}_2^i(I)$  and  $\text{view}_3^i(I)$  which include the set of messages seen by the adversary (through the corrupted nodes) during the execution of  $\text{op}_i$ . Let  $\text{op}$  denote the sequence of  $q$  operations generated by the environment. Let  $\ell_1, \dots, \ell_q$  be the labels of the operations in  $\text{op}$ , and let  $t_1, \dots, t_q$  be the corresponding random strings obtained by replacing  $F_K(\ell_i)$  with random strings. Because **DHT** is  $(\varepsilon, \delta, \theta)$ -balanced, we know that with probability at least  $1 - \delta$ , the overlay  $(\omega, \mathbf{C})$  will be  $(\varepsilon, \theta)$ -balanced. So for the remainder of the proof, we assume the overlay is  $(\varepsilon, \theta)$ -balanced.

First, we treat the case where  $t_i$  (or equivalently  $\ell_i$ ) has never been seen before. Let  $\mathcal{E}_i$  be the event that  $\psi(t_i) \in \text{Vis}(\text{fe}(t_i), I)$ . For all possible views  $\mathbf{v}$ , we have

$$\begin{aligned}
& \Pr [\text{view}_2^i(I) = \mathbf{v}] \\
&= \Pr [\text{view}_2^i(I) = \mathbf{v} \wedge \mathcal{E}_i] + \Pr [\text{view}_2^i(I) = \mathbf{v} \wedge \overline{\mathcal{E}_i}] \\
&= \Pr [\text{view}_2^i(I) = \mathbf{v} \mid \mathcal{E}_i] \cdot \Pr [\mathcal{E}_i] + \Pr [\text{view}_2^i(I) = \mathbf{v} \mid \overline{\mathcal{E}_i}] \cdot (1 - \Pr [\mathcal{E}_i]) \\
&= \Pr [\text{view}_2^i(I) = \mathbf{v} \mid \mathcal{E}_i] \cdot \Pr [\mathcal{E}_i]
\end{aligned}$$

where the third equality follows from the fact that, conditioned on  $\overline{\mathcal{E}_i}$ , the nodes in  $I$  do not see any messages at all.

Turning to  $\mathbf{view}_3$ , let  $\mathcal{Q}_i$  be the event that  $b_i = 1 \wedge b'_i = 1$ . Then for all possible views  $\mathbf{v}$ , we have

$$\begin{aligned}
& \Pr [\mathbf{view}_3^i(I) = \mathbf{v}] \\
&= \Pr [\mathbf{view}_3^i(I) = \mathbf{v} \wedge \mathcal{Q}_i] + \Pr [\mathbf{view}_3^i(I) = \mathbf{v} \wedge \overline{\mathcal{Q}_i}] \\
&= \Pr [\mathbf{view}_3^i(I) = \mathbf{v} \mid \mathcal{Q}_i] \cdot \Pr [\mathcal{Q}_i] + \Pr [\mathbf{view}_2^i(I) = \mathbf{v} \mid \overline{\mathcal{Q}_i}] \cdot (1 - \Pr [\mathcal{Q}_i]) \\
&= \Pr [\mathbf{view}_3^i(I) = \mathbf{v} \mid \mathcal{Q}_i] \cdot \Pr [\mathcal{Q}_i]
\end{aligned} \tag{5}$$

where the third equality follows from the fact that, for all  $i$ , conditioned on  $\overline{\mathcal{Q}_i}$ , either  $\mathbf{Sim}$  is never executed or  $\mathbf{Sim}$  does nothing. In either case, the nodes in  $I$  will not see any messages so for all  $\mathbf{v}$  we have  $\Pr [\mathbf{view}_3^i(I) = \mathbf{v} \mid \overline{\mathcal{Q}_i}] = 0$ .

Notice, however, that

$$\Pr [\mathcal{Q}_i] = \Pr [b_i = 1 \wedge b'_i = 1] = \varepsilon \cdot \frac{\Pr [\psi(t_i) \in \mathbf{Vis}(\mathbf{fe}_\phi(t_i), I)]}{\varepsilon} = \Pr [\mathcal{E}_i],$$

so to show that the views are equally distributed it remains to show that for all  $\mathbf{v}$ ,

$$\Pr [\mathbf{view}_2^i(I) = \mathbf{v} \mid \mathcal{E}_i] = \Pr [\mathbf{view}_3^i(I) = \mathbf{v} \mid \mathcal{Q}_i].$$

To see why this holds, notice that, conditioned on  $\mathcal{E}_i$  and  $\mathcal{Q}_i$ , the only difference between  $\mathbf{Game}_2$  and  $\mathbf{Game}_3$  is that, in the former, the labels  $t_i$  are mapped to an address  $a$  according to an allocation  $\psi$  generated using  $\mathbf{Alloc}$ , whereas in the latter, the labels  $t_i$  are programmed to an address  $a$  sampled from  $\Delta(\mathbf{Vis}(\mathbf{fe}(t_i), I))$ . We show, however, that in both cases, the labels  $t_i$  are allocated with the same probability distribution. In  $\mathbf{Game}_2$ , for all  $a \in \mathbf{A}$ , we have,

$$\begin{aligned}
\Pr [\psi(t_i) = a \mid \mathcal{E}_i] &= \frac{\Pr [\psi(t_i) = a \wedge \mathcal{E}_i]}{\Pr [\mathcal{E}_i]} \\
&= \frac{\Pr [\psi(t_i) = a \wedge \psi(t_i) \in \mathbf{Vis}(\mathbf{fe}(t_i), I)]}{\Pr [\psi(t_i) \in \mathbf{Vis}(\mathbf{fe}(t_i), I)]}
\end{aligned} \tag{6}$$

We see that for  $a \notin \mathbf{Vis}(\mathbf{fe}(t_i), I)$ , the numerator is 0, and therefore for  $a \notin \mathbf{Vis}(\mathbf{fe}(t_i), I)$ , we have that,

$$\Pr [\psi(t_i) = a \mid \mathcal{E}_i] = 0$$

However, for  $a \in \mathbf{Vis}(\mathbf{fe}(t_i), I)$ , Eqn 6 evaluates to:

$$\Pr [\psi(t_i) = a \mid \mathcal{E}_i] = \frac{\Pr [\psi(t_i) = a]}{\Pr [\psi(t_i) \in \mathbf{Vis}(\mathbf{fe}(t_i), I)]}$$

which follows from the fact that for  $a \in \mathbf{Vis}(\mathbf{fe}(t_i), I)$ , the event  $\{\psi(t_i) = a\} \subseteq \mathcal{E}_i$ .

In  $\mathbf{Game}_3$ , since the simulator only programs  $t_i$  to an address in  $\mathbf{Vis}(\mathbf{fe}(t_i), I)$  when  $b_i = 1$  and  $b'_i = 1$ , we have that for all  $a \notin \mathbf{Vis}(\mathbf{fe}(t_i), I)$ ,

$$\Pr [\psi(t_i) = a \mid \mathcal{Q}_i] = 0$$

However, for  $a \in \mathbf{Vis}(\mathbf{fe}(t_i), I)$ , we have that,

$$\Pr[\psi(t_i) = a \mid \mathcal{Q}_i] = \frac{\Pr[\psi(t_i) = a]}{\Pr[\psi(t_i) \in \text{Vis}(\text{fe}(t_i), I)]}$$

where the first equation follows from the fact that  $a$  is sampled from  $\Delta(\text{Vis}(\text{fe}(t_i), I))$ . Since, for all  $i$ , conditioned on  $\mathcal{Q}_i$  and  $\mathcal{E}_i$ , labels are allocated to addresses with the same distribution in both games and since this is the only difference between the games,

$$\Pr[\mathbf{view}_3^i(I) = \mathbf{v} \mid \mathcal{Q}_i] = \Pr[\mathbf{view}_2^i(I) = \mathbf{v} \mid \mathcal{E}_i]. \quad (7)$$

Plugging Eq. 7 into Eq. 5, we have that for all  $i$  and all  $\mathbf{v}$ ,

$$\Pr[\mathbf{view}_2^i(I) = \mathbf{v}] = \Pr[\mathbf{view}_3^i(I) = \mathbf{v}].$$

Now we consider the case where  $t_i$  has been seen in the past. In this case, Put or Get operations will produce the same messages that were generated in the past which means that  $\mathbf{view}_2^i(I)$  will be the same as before. Similarly,  $\mathbf{view}_3^i(I)$  will be the same as before because, whenever  $t_i$  has been seen in the past, Sim behaves the same as the last time it saw  $t_i$ .  $\square$

**Security of the Chord-based EDHT.** In the following Corollary we formally state the security of the standard scheme when its underlying DHT is instantiated with Chord. The proof follows directly from the fact that Chord has non-committing allocations and that it is balanced for:

$$\varepsilon = \frac{8\theta \log n}{n} \quad \text{and} \quad \theta \leq \frac{n}{8 \log n} \quad \text{and} \quad \delta = 1 - o\left(\frac{1}{n}\right)$$

**Corollary 4.3.** *If  $|\mathbf{L}| = \Theta(2^k)$ ,  $|I| = \theta \leq n/\log^2 n$ , and if EDHT is instantiated with Chord, then it is  $\mathcal{L}_\varepsilon$ -secure with probability at least  $1 - o(\frac{1}{n}) - \text{negl}(k)$  in the random oracle model, where  $\varepsilon = \frac{8\theta \log n}{n}$ .*

*Proof.* The corollary follows from Theorem 4.2, Theorem 3.6 and the fact that Chord has non-committing allocations when  $H_2$  is modeled as a random oracle. Note that during the simulation, the probability that  $\mathcal{A}$  queries  $H_2$  on at least one of the strings  $t_1, \dots, t_q$  is at most  $\text{poly}(k)/|\mathbf{L}|$ . This is because  $\mathcal{A}$  is polynomially-bounded so it can make at most  $\text{poly}(k)$  queries to  $H_2$ . And since for all  $i$ ,  $t_i = f(\ell_i)$ , where  $f$  is a random function, the probability that  $\mathcal{A}$  queries  $H_2$  on at least one of  $t_1, \dots, t_q$  is at most  $\text{poly}(k)/|\mathbf{L}|$ . And since  $|\mathbf{L}| = \Theta(2^k)$ , this probability is negligible in  $k$ .  $\square$

Notice that if the number of corruptions  $\theta$  is at most  $n/(\alpha \log n)$ , where  $\alpha > 8$ , then we get that  $\varepsilon = O(1/\alpha)$ . Recall that, on each query, the leakage function leaks the query equality with probability at most  $\varepsilon$ . So, intuitively, this means that if an  $\alpha$  fraction of  $n/\log n$  nodes are corrupted then, the adversary can expect to learn the operation equality of an  $O(1/\alpha)$  fraction of client queries. Note that this confirms the intuition that distributing an STE scheme suppresses its leakage.

**Efficiency of EDHT.** The standard scheme does not add any overhead to time, round, communication and storage complexities of the underlying DHT.

## 5 Transient DHTs

In this section, we consider DHTs in the transient setting where nodes are not known a-priori and can join and leave at any time. While perpetual DHTs are suitable for “permissioned” settings like the backend infrastructure of large companies, transient DHTs are better suited to “permissionless” settings like peer-to-peer networks and permissionless blockchains. Similar to the perpetual setting, we will use Chord as our running example.

**Syntax.** Transient DHTs are a collection of eight algorithms  $\text{DHT}^+ = (\text{Overlay}, \text{Alloc}, \text{FrontEnd}, \text{Daemon}, \text{Put}, \text{Get}, \text{Leave}, \text{Join})$ . The first six algorithms are same as in the perpetual setting. The seventh is an algorithm `Leave` executed by a node  $N \in \mathbf{C}$  when it wishes to leave the network. `Leave` takes the DHT parameters as input and outputs nothing but it halts the `Daemon` algorithm. The eighth is an algorithm `Join` that is executed by a node  $N \in \mathbf{N} \setminus \mathbf{C}$  that wishes to join the network. It takes nothing as input and outputs nothing but executes the `Daemon` algorithm. When a node executes a `Leave` or `Join`, the routing tables of all the other nodes are updated and label/value pairs are moved around in the network according to allocation  $\psi$ . In other words, when a node leaves, its pairs are reallocated in the network and when a node joins, some pairs stored on the other nodes are moved to the new node.

Note that when a node  $N \in \mathbf{C}$  leaves the network, the set of active nodes  $\mathbf{C}$  automatically shrinks to exclude  $N$ . Similarly, when a node  $N \in \mathbf{N} \setminus \mathbf{C}$  joins the network, the set of active nodes  $\mathbf{C}$  expands to include  $N$ . From now on, whenever we write  $\mathbf{C}$  we are referring to the current set of active nodes.

**Leaves and joins in Chord.** The Chord paper [28] does not precisely specify how joins and leaves should be handled. In particular, when a node  $N$  leaves, it describes which nodes should receive  $N$ 's pairs, but it does not describe exactly how the pairs should get there. Similarly, when a node  $N$  joins, it describes which pairs should move to  $N$ , but it does not describe how these pairs should move to  $N$ . Because of this, we describe a simple approach based on “re-hashing”. We note that this is not the most efficient way to handle leaves and joins but it is correct and our focus is on security rather than efficiency.

When a new node  $N \in \mathbf{N} \setminus \mathbf{C}$  joins the network, it is first assigned an address  $H_1(N) \in \mathbf{A}$ . Then, the routing tables of all the other nodes are updated. Finally, all the label/value pairs stored at  $\text{succ}_{\chi_{\mathbf{C}}}(H_1(N))$  are re-hashed and stored at their new destination (if necessary). When a node  $N \in \mathbf{C}$  leaves, the routing tables of all the other nodes are updated, and all the label/value pairs stored at  $N$  are moved to the  $\text{succ}_{\chi_{\mathbf{C}}}(H_1(N))$ .

Intuitively, when a node  $N$  joins, it splits the arc of its successor, and all the pairs that hashed to the part of the arc that is now the arc of  $N$ , are moved to  $N$ . As shown in Figure 4, when a new node  $N_9$  joins,  $\ell_1$  which was previously stored at  $N_2$  moves to  $N_9$ . Similarly, when a node  $N$  leaves, its arc becomes a part of its successor  $N'$ 's arc. Hence all the pairs that initially hashed to  $N$ 's arc, now hash to  $N'$ 's arc, and hence move to  $N'$ . For example, in Figure 4, when  $N_1$  leaves, all its pairs move to  $N_4$ .

**Stability.** To prove the security of EDHTs in the transient setting, we need the underlying DHT to satisfy a stronger notion than balance which we call *stability*. Stability requires that `Overlay` returns an overlay parameter  $\omega$  such that, with high probability,  $(\omega, \mathbf{C})$  is balanced *for all* possible subsets of active nodes  $\mathbf{C}$  simultaneously. Balance, on the other hand, only requires that for all sets of active nodes  $\mathbf{C}$ , with high probability `Overlay` will output an overlay parameter  $\omega$  such that



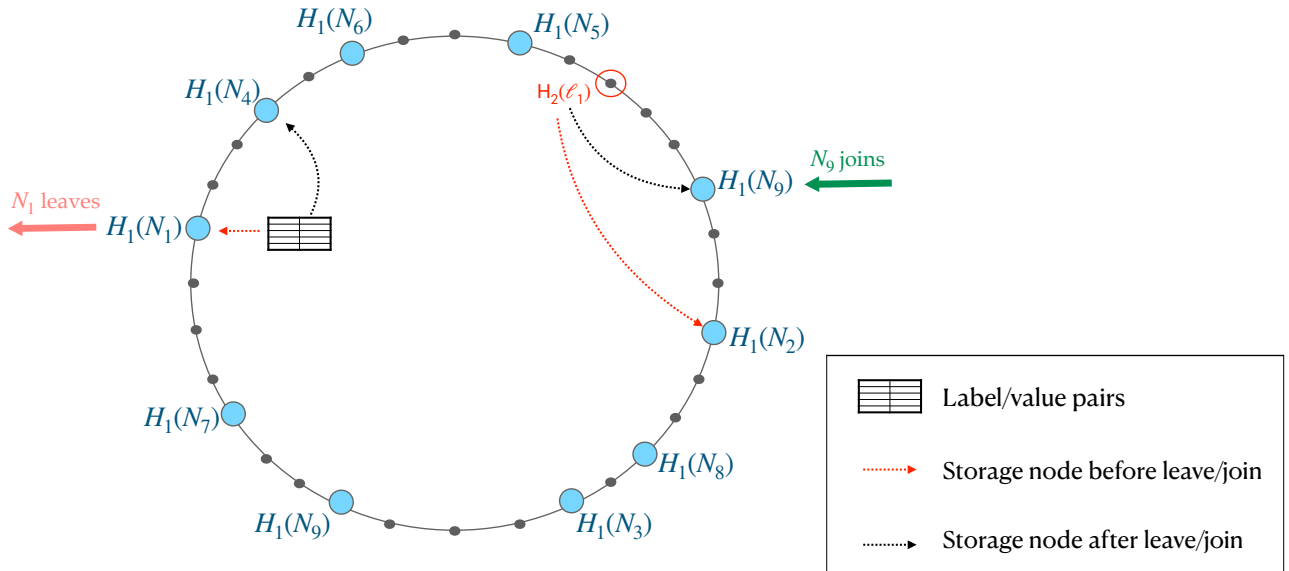


Figure 4: Leaves and joins in Chord. When a node joins, label/value pairs stored at its successor are reshaped, and as a result some of the pairs stored at the successor move to the newly joined node. For example, when  $N_9$  joins,  $\ell_1$  moves to  $N_9$  while  $\ell_2$  continues to be stored at  $N_2$ . When a node leaves, all its pairs are moved to its successor. For example, when  $N_1$  leaves, all its pairs are moved to  $N_4$ .

$(\omega, \mathbf{C})$  is balanced. In other words, stability requires a single overlay parameter  $\omega$  that is “good” for all subsets of active nodes whereas balance does not.

**Definition 5.1** (Stability). *We say that a transient distributed hash table  $\text{DHT}^+ = (\text{Overlay}, \text{Alloc}, \text{FrontEndDaemon}, \text{Put}, \text{Get}, \text{Leave}, \text{Join})$  is  $(\varepsilon, \delta, \theta)$ -stable if*

$$\Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}: |\mathbf{C}| \geq \theta} \left\{ (\omega, \mathbf{C}) \text{ is } (\varepsilon, \theta)\text{-balanced} \right\} \right] \geq 1 - \delta$$

where the probability is over the choice of  $\omega$ , and  $\varepsilon$  and  $\theta$  are functions of  $\mathbf{C}$ .

**Stability of Chord.** Recall that in the perpetual setting, we have a single configuration  $\chi_{\mathbf{C}}$  corresponding to a fixed set of active nodes  $\mathbf{C}$ . However, in the transient setting, we have multiple configurations — every time a node leaves/joins, the set  $\mathbf{C}$  changes and hence the configuration  $\chi_{\mathbf{C}}$  changes. In order to show that Chord is stable, we need to show that all the configurations  $\chi_{\mathbf{C}}$  are balanced. And in order to do so, for each configuration, we need to bound the probability of (1) the front end node being corrupted, (2) a label being stored at a corrupted node, and (3) a label being routed by a corrupted node.

Notice that given a configuration  $\chi_{\mathbf{C}}$ , the probability that a front-end node is corrupted only depends on the fraction of nodes currently corrupted and hence is always  $\theta/|\mathbf{C}|$ . Similarly, the probability that a label is routed by a corrupted node only depends on the path lengths, which are  $\log |\mathbf{C}|$  long in any configuration. Therefore, we bound the probability of (3) by  $\theta \log |\mathbf{C}|/|\mathbf{C}|$  following the same argument we used to bound the probability of a label being routed by a corrupted node in the persistent setting (Theorem 3.5).

Notice that bounding (2) simultaneously for all the configurations is non-trivial, and it is because the event of a label being stored at a corrupted node is not independent across configurations. For example, if an uncorrupted node adjacent to a corrupted node leaves, in the new configuration, the corrupted node also occupies the arc of the node that left the system, and hence it has a higher likelihood of storing a label than what it previously had in the old configuration.

As before, for a given configuration  $\chi_{\mathbf{C}}$ , in order to bound (2), we upper bound the total lengths of the  $\theta$  largest arcs in  $\chi_{\mathbf{C}}$ . However, instead of bounding it as a function of the number of currently active nodes  $|\mathbf{C}|$ , we bound it as function of the size of the namespace  $|\mathbf{N}|$ . We rely on two main observations. The first is that any configuration  $\chi_{\mathbf{C}}$  can be expressed as  $\chi_{\mathbf{N}} \setminus \chi_{\mathbf{N} \setminus \mathbf{C}}$  which, intuitively, means we can recover  $\chi_{\mathbf{C}}$  by starting with  $\chi_{\mathbf{N}}$  (which includes every node in the name space) and removing the nodes  $\mathbf{N} \setminus \mathbf{C}$ . The second observation is that if we start with a given configuration  $\chi_{\mathbf{C}}$  and remove a node  $N$ , then  $N$ 's arc becomes visible to some other (currently active) node.

But how can we use these observations to bound the total lengths of  $\theta$  largest arcs in  $\chi_{\mathbf{C}}$  using the bound in  $\chi_{\mathbf{N}}$ ? We start with  $\chi_{\mathbf{N}}$  and remove the nodes in  $\mathbf{N} \setminus \mathbf{C}$ ; but for each node  $N$  that is removed, we assume the worst-case and assign  $N$ 's arc to one of the  $\theta$  nodes with largest arcs. The resulting area will be an upper bound on the true maximum area. More formally, we have that  $\text{sumarcs}(\chi_{\mathbf{C}}, \theta) \leq \text{sumarcs}(\chi_{\mathbf{N}}, \theta + |\mathbf{N}| - |\mathbf{C}|)$ . We next show that for large enough  $\mathbf{C}$ 's, i.e., when  $|\mathbf{C}| \geq |\mathbf{N}| - d$ ,  $\text{sumarcs}(\chi_{\mathbf{N}}, \theta + |\mathbf{N}| - |\mathbf{C}|) \leq \text{sumarcs}(\chi_{\mathbf{N}}, \theta + d)$ . Finally, we bound  $\text{sumarcs}(\chi_{\mathbf{N}}, \theta + d)$  using the same result from [4] which we used earlier.

**Theorem 5.2.** *Let  $\chi_{\mathbf{N}}$  be a configuration drawn u.a.r and let  $d$  be a positive integer such that  $\theta + d \leq 4|\mathbf{N}|e^{-2}$ . Then,*

$$\Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq |\mathbf{N}| - d} \left\{ \text{sumarcs}(\chi_{\mathbf{C}}, \theta) \leq \frac{6(\theta + d)|\mathbf{A}|}{|\mathbf{N}|} \log \left( \frac{|\mathbf{N}|}{\theta + d} \right) \right\} \right] \geq 1 - o \left( \frac{1}{|\mathbf{N}|} \right)$$

*Proof.* Proof follows directly from the observation that for all the configurations  $\chi_{\mathbf{C}}$ , the probability of the event  $\{\text{sumarcs}(\chi_{\mathbf{C}}, \theta) < \alpha\}$  is at least as the probability of the event  $\{\text{sumarcs}(\chi_{\mathbf{N}}, \theta + d) < \alpha\}$ . Precisely,

$$\begin{aligned} & \Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq |\mathbf{N}| - d} \left\{ \text{sumarcs}(\chi_{\mathbf{C}}, \theta) \leq \frac{6(\theta + d)|\mathbf{A}|}{|\mathbf{N}|} \log \left( \frac{|\mathbf{N}|}{\theta + d} \right) \right\} \right] \\ & \geq \Pr \left[ \text{sumarcs}(\chi_{\mathbf{N}}, \theta + d) \leq \frac{6(\theta + d)|\mathbf{A}|}{|\mathbf{N}|} \log \left( \frac{|\mathbf{N}|}{\theta + d} \right) \right] \\ & \geq 1 - o \left( \frac{1}{|\mathbf{N}|} \right) \end{aligned}$$

where the last step follows from Theorem 3.4. □

We finally show that Chord is  $(\varepsilon, \delta, \theta)$  stable, where  $\varepsilon$  and  $\theta$  depend on the number of nodes currently active.

**Theorem 5.3.** *Transient Chord is  $(\varepsilon, \delta, \theta)$  stable for*

$$\varepsilon = \frac{6(\theta + d) \log |\mathbf{N}|}{|\mathbf{N}|} + \frac{2\theta \log |\mathbf{C}|}{|\mathbf{C}|} \quad \text{and} \quad \theta \leq 4|\mathbf{N}|e^{-2} - d \quad \text{and} \quad \delta = 1 - o \left( \frac{1}{|\mathbf{N}|} \right),$$

where  $d$  is some positive integer.

*Proof.* For a given set of active nodes  $\mathbf{C}$ , let  $\mathcal{E}_{\mathbf{C}}$  be the following event:

$$\left\{ \Pr \left[ I \cap \text{route}_{\chi_{\mathbf{C}}}(\text{fe}_{H_3}(\ell), \text{server}_{\chi_{\mathbf{C}}}(\ell)) \neq \emptyset \right] \leq \varepsilon_{\mathbf{C}} \right\}$$

Let us rewrite  $\varepsilon_{\mathbf{C}} = \varepsilon_{\mathbf{C}}^1 + \varepsilon_{\mathbf{C}}^2 + \varepsilon_{\mathbf{C}}^3$ , where:

$$\begin{aligned} \varepsilon_{\mathbf{C}}^1 &= \frac{\theta_{\mathbf{C}}}{|\mathbf{C}|} \\ \varepsilon_{\mathbf{C}}^2 &= \frac{6(\theta + d) \log |\mathbf{N}|}{|\mathbf{N}|} + \frac{2\theta \log |\mathbf{C}|}{|\mathbf{C}|} \\ \varepsilon_{\mathbf{C}}^3 &= \frac{\theta_{\mathbf{C}} \log |\mathbf{C}|}{|\mathbf{C}|} \end{aligned}$$

and let us define three new events as follows:

$$\begin{aligned} \mathcal{E}_{\mathbf{C}}^1 &= \left\{ \Pr \left[ \text{fe}_{H_3}(\ell) \in I \right] \leq \varepsilon_{\mathbf{C}}^1 \right\} \\ \mathcal{E}_{\mathbf{C}}^2 &= \left\{ \Pr \left[ \text{server}_{\chi_{\mathbf{C}}}(\ell) \in I \right] \leq \varepsilon_{\mathbf{C}}^2 \right\} \\ \mathcal{E}_{\mathbf{C}}^3 &= \left\{ \Pr \left[ \left\{ I \cap \text{route}_{\chi_{\mathbf{C}}}(\text{fe}_{H_3}(\ell), \text{server}_{\chi_{\mathbf{C}}}(\ell)) \right\} \neq \emptyset \mid \text{fe}_{H_3}(\ell) \notin I \wedge \text{server}_{\chi_{\mathbf{C}}}(\ell) \notin I \right] \leq \varepsilon_{\mathbf{C}}^3 \right\} \end{aligned}$$

Then,

$$\Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq \theta} \bigwedge_{i \in [3]} \mathcal{E}_{\mathbf{C}}^i \right] = \Pr \left[ \bigwedge_{i \in [3]} \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq \theta} \mathcal{E}_{\mathbf{C}}^i \right] = \prod_{i \in [3]} \Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq \theta} \mathcal{E}_{\mathbf{C}}^i \right] \quad (8)$$

where the last inequality follows from the fact that  $\mathcal{E}_{\mathbf{C}}^i$ 's are independent. We next evaluate the three terms inside the product one by one.

We start by evaluating  $\Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq \theta} \mathcal{E}_{\mathbf{C}}^1 \right]$ . We notice that given any configuration, probability that front end of label is a corrupted node only depends on the fraction of nodes currently corrupted, and not on how nodes are arranged in a configuration. Precisely, for all  $\mathbf{C}$ ,

$$\Pr \left[ \text{fe}_{H_3}(\ell) \in I \right] = \frac{\theta_{\mathbf{C}}}{|\mathbf{C}|}$$

Therefore, for all  $\mathbf{C}$ , the event  $\mathcal{E}_{\mathbf{C}}^1$  always occurs, and hence

$$\Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq \theta} \mathcal{E}_{\mathbf{C}}^1 \right] = \Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq \theta} 1 \right] = 1 \quad (9)$$

Similarly, we notice that the probability that a corrupted node falls on the path of a label to its server (excluding the ending points of the path) solely depends on the route lengths, which given any configuration, are always  $\log |\mathbf{C}|$  long. Therefore, the event  $\mathcal{E}_{\mathbf{C}}^3$  always occurs with probability 1, and hence,

$$\Pr \left[ \bigwedge_{\mathbf{C} \subseteq \mathbf{N}; |\mathbf{C}| \geq \theta} \mathcal{E}_{\mathbf{C}}^3 \right] = 1 \quad (10)$$

However, the probability that a label is stored on a corrupted node is not independent across configurations, and hence the event  $\mathcal{E}_{\mathbf{C}}^2$  is not independent for all  $\mathbf{C}$ . In particular,

$$\Pr\left[\bigwedge_{\mathbf{C}\subseteq\mathbf{N}:|\mathbf{C}|\geq\theta}\mathcal{E}_{\mathbf{C}}^2\right]=\Pr\left[\bigwedge_{\mathbf{C}\subseteq\mathbf{N}:|\mathbf{C}|\geq\theta}\left\{\text{sumarcs}(\chi_{\mathbf{C}},\theta)\leq\varepsilon_{\mathbf{C}}^2\right\}\right]\geq 1-\delta \quad (11)$$

where the last step follows from Theorem 5.2. From Equations 8–11, we conclude that:

$$\Pr\left[\bigwedge_{\mathbf{C}\subseteq\mathbf{N}:|\mathbf{C}|\geq\theta}\bigwedge_{i\in[3]}\mathcal{E}_{\mathbf{C}}^i\right]\geq 1-\delta$$

Notice that  $\mathcal{E}_{\mathbf{C}}^1 \wedge \mathcal{E}_{\mathbf{C}}^2 \wedge \mathcal{E}_{\mathbf{C}}^3$  imply the event  $\mathcal{E}_{\mathbf{C}}$ . And hence,

$$\Pr\left[\bigwedge_{\mathbf{C}\subseteq\mathbf{N}:|\mathbf{C}|\geq\theta}\mathcal{E}_{\mathbf{C}}\right]\geq 1-\delta$$

□

## 6 Encrypted Distributed Hash Tables in the Transient Setting

In this section we define the security of transient EDHTs and analyze the security of the standard construction in this setting.

### 6.1 Syntax and Security Definitions

**Syntax.** A transient EDHT is a collection of nine algorithms  $\text{EDHT}^+ = (\text{Gen}, \text{Overlay}, \text{Alloc}, \text{FrontEnd}, \text{Daemon}, \text{Put}, \text{Get}, \text{Leave}, \text{Join})$ . The first algorithm  $\text{Gen}$  is executed by a client and takes as input a security parameter  $1^k$  and outputs a secret key  $K$ . All the other algorithms have the same syntax as before (See Section 5), with the difference that  $\text{Get}$  and  $\text{Put}$  also take the secret key  $K$  as input.

We assume in this work that when a node leaves the network, all the pairs stored at that node are “re-put” in the network and when a node joins the network all the pairs currently in the network are “re-put”. We note that this is not the most efficient way to handle leaves and joins but in this work our focus is on security rather than efficiency and this strategy has the worst possible leakage.

**Security.** The real and ideal experiments are the same as in Section 4 with the following differences. First, the trusted party  $\mathcal{T}$  runs  $\text{Overlay}$  and  $\text{Alloc}$  with  $|\mathbf{N}|$  nodes; second, the environment selects and activates a subset a set  $\mathbf{C} \subseteq \mathbf{N}$  of nodes in the beginning; third, the environment also sends  $\text{Leave}$  and  $\text{Join}$  operations adaptively along with  $\text{Get}$  and  $\text{Put}$  operations to nodes; and fourth, the ideal functionality of Figure 2 is replaced with the ideal functionality described in Figure 5.

### 6.2 The Standard EDHT in the Transient Setting

In the transient setting, the standard scheme is composed of nine algorithms  $\text{EDHT}^+ = (\text{Gen}, \text{Overlay}, \text{Alloc}, \text{FrontEnd}, \text{Daemon}, \text{Put}, \text{Get}, \text{Leave}, \text{Join})$ . The first seven algorithms are exactly the same as the standard EDHT scheme in the perpetual setting (See Figure 3). The  $\text{Leave}$  algorithm simply calls  $\text{DHT}^+.\text{Leave}$  while the  $\text{Join}$  algorithm calls  $\text{DHT}^+.\text{Join}$ . We now turn to describing the leakage of this scheme. We start with a description of the leakage for join and leave operations and then discuss the leakage for put and get operations.

**Functionality  $\mathcal{F}_{\text{DHT}^+}^{\mathcal{L}}$**

$\mathcal{F}_{\text{DHT}^+}^{\mathcal{L}}$  stores a dictionary  $\text{DX}$  initialized to empty, a set  $\mathbf{C} \subseteq \mathbf{N}$  of active nodes, and a set  $I \subseteq \mathbf{N}$  of corrupted nodes. It proceeds as follows, running with client  $\mathcal{C}$ ,  $n$  active nodes in  $\mathbf{C}$  and a simulator  $\text{Sim}$ :

- **Put**( $\ell, v$ ): Upon receiving a label/value pair  $(\ell, v)$  from client  $\mathcal{C}$ , it sets  $\text{DX}[\ell] := v$ , and sends the leakage  $\mathcal{L}(\text{DX}, (\text{put}, \ell, v))$  to the simulator  $\text{Sim}$ .
- **Get**( $\ell$ ): Upon receiving a label  $\ell$  from client  $\mathcal{C}$ , it returns  $\text{DX}[\ell]$  to the client  $\mathcal{C}$  and the leakage  $\mathcal{L}(\text{DX}, (\text{get}, \ell, \perp))$  to the simulator  $\text{Sim}$ .
- **Leave**( $N$ ): Upon receiving  $N \in \mathbf{C}$ , it returns the leakage  $\mathcal{L}(\text{DX}, (\text{leave}, N))$  to the simulator  $\text{Sim}$  and updates its set  $\mathbf{C}$ .
- **Join**( $N$ ): Upon receiving  $N \in \mathbf{N} \setminus \mathbf{C}$ , it returns the leakage  $\mathcal{L}(\text{DX}, (\text{join}, N))$  to the simulator  $\text{Sim}$  and updates its set  $\mathbf{C}$ .

Figure 5:  $\mathcal{F}_{\text{DHT}^+}^{\mathcal{L}}$  : The  $\text{DHT}^+$  functionality parameterized with leakage function  $\mathcal{L}$ .

**Join and leave leakage.** Roughly speaking, during the execution of the scheme, the adversary sees leakage on label/value pairs that are either stored at corrupted nodes or routed through corrupted nodes. Now, when a join or leave operation occurs, label/value pairs are moved throughout the network (e.g., during a leave, the leaving node’s pairs are redistributed to other nodes). At this point, the adversary could get new leakage about pairs that it had not seen before the leave/join operation. For example, this would occur if a previously unseen label/value pair (i.e., that was stored on the leaving node) gets routed through a corrupted node during the re-distribution.

To simulate a leave/join operation correctly, the simulator will have to correctly simulate the re-distribution of pairs including of pairs it has not seen yet. But at this stage, it does not even know how many such pairs exist. This is because it does not get executed on put operations for labels not stored or routed by corrupted nodes. To overcome this, we reveal to the simulator how many of these pairs exist through the leakage function.

This, however, affects the get and put leakages for these pairs: now that the pairs have been re-distributed to (or routed through) a corrupted node the adversary will receive get and put leakages on these pairs. There is a technical challenge here, which is that we do not know how to simulate *only* the pairs that are re-distributed to (or routed through) corrupted nodes, so to address this we additionally reveal to the simulator the leakage of all the previously unseen pairs. It is not clear if this is strictly necessary and it could be that the scheme achieves a “tighter” leakage function. Note that this does not affect new pairs, i.e., pairs that are added after the leave/join operation (until another leave/join operation occurs). We denote the number of previously unseen pairs by  $\kappa$ .

**The leakage profile.** We are now ready to formally describe the leakage profile achieved by the standard scheme in the transient setting.

- $\mathcal{L}_\varepsilon\left(\text{DX}, \left\{(\text{op}, \ell, v), (\text{op}, N)\right\}\right)$ :
  1. if  $\text{op} = \text{get} \vee \text{put}$  and  $\ell$  has never been seen
    - (a) sample and store  $b_\ell \leftarrow \text{Ber}(\varepsilon_{\mathbf{C}})$
  2. if  $b_\ell = 1$

- (a) if  $\text{op} = \text{put}$  output  $(\text{put}, \text{oqeq}(\ell))$
- (b) else if  $\text{op} = \text{get}$  output  $(\text{get}, \text{oqeq}(\ell))$
- 3. else if  $b_\ell = 0$ 
  - (a) Increment  $\kappa$  if  $\text{op} = \text{put}$  and  $\ell$  has never been seen
  - (b) output  $\perp$
- 4. if  $\text{op} = \text{leave} \vee \text{join}$ 
  - (a) output  $(\text{op}, N, \kappa)$
  - (b) if  $\text{op} = \text{leave}$ ,  $\mathbf{C} = \mathbf{C} \setminus N$
  - (c) if  $\text{op} = \text{join}$ ,  $\mathbf{C} = \mathbf{C} \cup N$
  - (d) set  $b_\ell = 1$  for all the put labels that have been seen in the past
  - (e) reset  $\kappa$  to 0

We now show that  $\text{EDHT}^+$  is  $\mathcal{L}_\varepsilon$ -secure in the transient setting with probability negligibly close to  $1 - \delta$  when its underlying transient DHT is  $(\varepsilon, \delta, \theta)$  stable and is non-committing.

**Theorem 6.1.** *If  $|I| \leq \theta$  and  $\text{DHT}^+$  is  $(\varepsilon, \delta, \theta)$  stable and has non-committing allocations, then  $\text{EDHT}^+$  is  $\mathcal{L}_\varepsilon$ -secure with probability at least  $1 - \delta - \text{negl}(k)$ .*

*Proof.* Consider the simulator  $\text{Sim}$  that works as follows. Given a set of corrupted nodes  $I \subseteq \mathbf{N}$ , and a set of active nodes  $\mathbf{C} \subseteq \mathbf{N}$ , it computes  $\omega \leftarrow \text{DHT}^+.\text{Overlay}(n)$ ,  $\phi \leftarrow \text{DHT}^+.\text{FrontEnd}(n)$ , initializes  $n$  nodes  $N_1, \dots, N_n$  in  $\mathbf{C}$ , simulates the adversary  $\mathcal{A}$  with  $I$  as input, and generates a symmetric key  $K \leftarrow \text{SKE.Gen}(1^k)$ . It then sets  $I' = \mathbf{C} \cap I$ .

When a leave/join operation is executed, the simulator receives from  $\mathcal{F}_{\text{DHT}^+}$  the leakage

$$\lambda \in \left\{ \left( \text{leave}, N, \kappa \right), \left( \text{join}, N, \kappa \right) \right\}.$$

For each  $j \in [\kappa]$ , it sets  $t_j \xleftarrow{\$} \{0, 1\}^d$  and  $e_j \leftarrow \text{SKE.Enc}(K, 0)$ , samples an address  $a \leftarrow \Delta(\mathbf{A} \setminus \text{Vis}(\text{fe}(t_j), I'))$ , programs  $\psi$  to map  $t_j$  to  $a$ , computes  $N' \leftarrow \text{server}(t_j)$ , and adds  $(t_j, e_j)$  to  $\text{MM}[N']$ . It also sets  $b'_j = 1$  for all the labels it has received until now.

If the operation is a leave operation, it updates  $\mathbf{C} = \mathbf{C} \setminus \{N\}$ , updates the routing tables to exclude  $N$ , and executes  $\text{DHT.Put}(t, e)$  on all the  $(t, e)$  pairs stored in  $\text{MM}[N]$ , updating  $\text{MM}$  according to how pairs move. It finally, resets  $\text{MM}[N]$  to  $\perp$ , and recomputes  $I' = I \cap \mathbf{C}$ .

If the operation is a join operation, it updates  $\mathbf{C} = \mathbf{C} \cup \{N\}$ , updates the routing tables to include  $N$ , and executes  $\text{DHT.Put}(t, e)$  on all the  $(t, e)$  pairs stored in  $\text{MM}$  for all the nodes, updating  $\text{MM}$  according to how pairs move. Finally, it recomputes  $I' = I \cap \mathbf{C}$ .

When a put/get operation is executed, it does the exact same thing as in the case of persistent setting. There are only two differences: (1) for a put operation if  $b'_i = 0$ , the simulator generates a random  $(t, e)$  pair, and program  $\psi(t) = a$ , where  $a \leftarrow \Delta(\mathbf{A} \setminus \text{Vis}(\text{fe}(t_j), I'))$ , and (2) it updates  $\text{MM}$  in the process of executing  $\text{Get}$  and  $\text{Put}$  as well.

Once all of the environment's operations are processed, the simulator returns whatever the adversary outputs.

It remains to show that the view of the adversary  $\mathcal{A}$  during the simulation is indistinguishable from its view in a **Real** experiment. We do this using a sequence of games.

$\text{Game}_0$  : is the same as a  $\text{Real}_{\mathcal{A}, \mathcal{Z}}(k)$  experiment.

**Game<sub>1</sub>** : is the same as **Game<sub>0</sub>** except that the encryption of the value  $v$  during a **Put** is replaced by  $\text{SKE.Enc}(K_2, 0)$ .

**Game<sub>2</sub>** : is the same as **Game<sub>1</sub>** except that output of the PRF  $F$  is replaced by a truly random string of  $d$  bits.

**Game<sub>3</sub>** : is the same as **Game<sub>2</sub>** except that for each operation  $\text{op}$ , if  $\text{op} \in \{(\text{get}, \ell), (\text{put}, \ell, v)\}$ , we check if the label  $\ell$  has been seen before. If not, we sample and store a bit  $b_\ell \leftarrow \text{Ber}(\varepsilon)$ , else we set  $b_\ell$  to the bit previously sampled for  $\ell$ . If  $b_\ell = 1$  and  $\text{op} = (\text{put}, \ell, v)$ , we replace the **Put** operation with  $\text{Sim}(\text{put}, \text{oqeq}(\ell))$  and if  $\text{op} = (\text{get}, \ell)$  we replace the **Get** operation with  $\text{Sim}(\text{get}, \text{oqeq}(\ell))$ . If  $b_\ell = 0$ , we do nothing. If however  $\text{op} = (\text{leave}, N)$ , we replace the **Leave** operation with  $\text{Sim}(\text{leave}, N, \kappa)$  and set  $b_\ell = 1$  for all the put labels that have been seen in the past. Similarly if  $\text{op} = (\text{join}, N)$ , we replace the **Join** operation with  $\text{Sim}(\text{join}, N, \kappa)$  and set  $b_\ell = 1$  for all the put labels that have been seen in the past.

**Game<sub>1</sub>** is indistinguishable from **Game<sub>0</sub>**, otherwise the encryption scheme is not semantically secure. **Game<sub>2</sub>** is indistinguishable from **Game<sub>1</sub>** because the outputs of pseudorandom functions are indistinguishable from random strings.

Let  $(\omega, \mathbf{C})$  be the current overlay. Since **DHT** is  $(\varepsilon, \delta, \theta)$ -stable, with probability at least  $1 - \delta$ , for all  $\mathbf{C} \subseteq \mathbf{N}$ ,  $(\omega, \mathbf{C})$  will be  $(\varepsilon, \theta)$ -balanced. It follows then that the simulator aborts with probability at most  $\delta$  so for the rest of the proof, we argue indistinguishability assuming  $(\varepsilon, \theta)$ -balanced overlays.

As in the proof of Theorem 4.2, we will consider the views of nodes in  $I'$  for each operation and show them to be indistinguishable across **Game<sub>2</sub>** and **Game<sub>3</sub>**. We will denote this by  $\mathbf{view}_2^i(I')$  and  $\mathbf{view}_3^i(I')$  for **Game<sub>2</sub>** and **Game<sub>3</sub>** respectively. Let  $\mathbf{op}$  denote the sequence of operations generated by the environment. To prove the indistinguishability of views, we divide the operations in  $\mathbf{op}$  into buckets where the bucket boundaries are the leave/join operations.

Now consider the first bucket. Since no leaves/joins have yet been simulated,  $b'_i$  can only be 0 or 1 but not  $\perp$ . Notice that for get and put operations in the bucket, when  $b'_i = 1$ , the simulator programs  $\psi$  in the same way as the simulator of Theorem 4.2. It does some extra bookkeeping in addition but that does not affect the view of the nodes in set  $I'$  for that operation. Moreover, for put operations when  $b'_i = 0$ , it only programs  $\psi$  to addresses not visible to  $I'$  and does nothing else which generates any extra view for nodes in  $I'$ . Therefore, using the same argument as in Theorem 4.2, we conclude that for get and put operations the views are indistinguishable.

Let  $\mathbf{op}_i$  be the first leave/join operation (boundary of the first bucket) and let  $t_1, \dots, t_q$  be the distinct labels of put operations in first bucket. Now let  $A_r$  be the random variable denoting the allocation of  $t_1, \dots, t_q$  to addresses in  $\mathbf{view}_2$ . Then, using the law of total probability, we get  $\Pr[\mathbf{view}_2^i(I') = \mathbf{v}]$  is equal to

$$\sum_{(\alpha_1, \dots, \alpha_q) \in \mathbf{A}^q} \Pr[\mathbf{view}_2^i(I') = \mathbf{v} \mid A_r = (\alpha_1, \dots, \alpha_q)] \cdot \Pr[A_r = (\alpha_1, \dots, \alpha_q)] \quad (12)$$

Similarly, let  $A_s$  be the random variable denoting the allocation of  $t_1, \dots, t_q$  to addresses in  $\mathbf{view}_3$ . Then,  $\Pr[\mathbf{view}_3^i(I') = \mathbf{v}]$

$$\sum_{(\alpha_1, \dots, \alpha_q) \in \mathbf{A}^q} \Pr[\mathbf{view}_3^i(I') = \mathbf{v} \mid A_s = (\alpha_1, \dots, \alpha_q)] \cdot \Pr[A_s = (\alpha_1, \dots, \alpha_q)]$$



But conditioned on a fixed allocation  $(\alpha_1, \dots, \alpha_q) \in \mathbf{A}^q$  of labels, during leave/join operations, the views of the nodes in  $I'$  will be the same in both the games, since both of them will be re-distributing the same number of pairs using `DHT.Put`. Therefore,

$$\Pr \left[ \mathbf{view}_2^i(I') = \mathbf{v} \mid A_r = (\alpha_1, \dots, \alpha_q) \right] = \Pr \left[ \mathbf{view}_3^i(I') = \mathbf{v} \mid A_s = (\alpha_1, \dots, \alpha_q) \right] \quad (13)$$

Next we show that,

$$\Pr [A_r = (\alpha_1, \dots, \alpha_q)] = \Pr [A_s = (\alpha_1, \dots, \alpha_q)]$$

Notice that we can rewrite <sup>3</sup>

$$\Pr [A_r = (\alpha_1, \dots, \alpha_q)] = \prod_{j \in [q]} \Pr [\psi(t_j) = \alpha_j]$$

The allocation in `Game3` is determined by the programmed  $\psi$  function. To avoid any confusion with the  $\psi$  function of `Game2`, we denote by  $\psi_P$ , the programmed allocation function of `Game3`. Then, we can rewrite,

$$\Pr [A_s = (\alpha_1, \dots, \alpha_q)] = \prod_{j \in [q]} \Pr [\psi_P(t_j) = \alpha_j]$$

There are two subcases to consider. In the first case,  $\alpha_j \in \text{Vis}(\text{fe}(t_j), I')$ . Then,

$$\Pr [\psi_P(t_j) = \alpha_j] = \Pr [b_j = 1 \wedge b'_j = 1 \wedge a_j = \alpha_j]$$

where  $a_j \leftarrow \Delta(\text{Vis}(\text{fe}(t_j), I'))$ . Now,

$$\begin{aligned} \Pr [b_j = 1 \wedge b'_j = 1 \wedge a_j = \alpha_j] &= \varepsilon \cdot \frac{\Pr [\psi(t_j) \in \text{Vis}(\text{fe}(t_j), I')]}{\varepsilon} \cdot \frac{\Pr [\psi(t_j) = \alpha_j]}{\Pr [\psi(t_j) \in \text{Vis}(\text{fe}(t_j), I')]} \\ &= \Pr [\psi(t_j) = \alpha_j] \end{aligned}$$

In the second case,  $\alpha_j \in \mathbf{A} \setminus \text{Vis}(\text{fe}(t_j), I')$ . Then,

$$\Pr [\psi_P(t_j) = \alpha_j] = \Pr [\mathcal{E}_1] + \Pr [\mathcal{E}_2]$$

where

$$\Pr [\mathcal{E}_1] = \Pr [b_j = 1 \wedge b'_j = 0 \wedge a_j = \alpha_j], \text{ and}$$

$$\Pr [\mathcal{E}_2] = \Pr [b_j = 0 \wedge a_j = \alpha_j]$$

such that  $a_j \leftarrow \Delta(\mathbf{A} \setminus \text{Vis}(\text{fe}(t_j), I'))$ . Let  $B = \text{Vis}(\text{fe}(t_j), I')$ , and let  $G = \mathbf{A} \setminus \text{Vis}(\text{fe}(t_j), I')$ . Then,

$$\begin{aligned} \Pr [\mathcal{E}_1] &= \Pr [b_j = 1 \wedge b'_j = 0 \wedge a_j = \alpha_j] \\ &= \varepsilon \cdot \left( 1 - \frac{\Pr [\psi(t_j) \in B]}{\varepsilon} \right) \cdot \frac{\Pr [\psi(t_j) = \alpha_j]}{\Pr [\psi(t_j) \in G]}, \text{ and} \end{aligned}$$

$$\begin{aligned} \Pr [\mathcal{E}_2] &= \Pr [b_j = 0 \wedge a_j = \alpha_j] \\ &= (1 - \varepsilon) \cdot \frac{\Pr [\psi(t_j) = \alpha_j]}{\Pr [\psi(t_j) \in G]} \end{aligned}$$

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<sup>3</sup>there is an implicit assumption made here that for each label, its allocation to an address is independent of the previous allocations. However, the proof can be extended when no such assumption is made using the chain rule of probability.

Adding the two probabilities, we get,

$$\begin{aligned}
\Pr[\mathcal{E}_1] + \Pr[\mathcal{E}_2] &= \frac{\Pr[\psi(t_j) = \alpha_j]}{\Pr[\psi(t_j) \in G]} \cdot \left( \varepsilon \cdot \left( 1 - \frac{\Pr[\psi(t_j) \in B]}{\varepsilon} \right) + (1 - \varepsilon) \right) \\
&= \frac{\Pr[\psi(t_j) = \alpha_j]}{\Pr[\psi(t_j) \in G]} \cdot \left( 1 - \Pr[\psi(t_j) \in B] \right) \\
&= \frac{\Pr[\psi(t_j) = \alpha_j]}{\Pr[\psi(t_j) \in G]} \cdot \Pr[\psi(t_j) \in G] \\
&= \Pr[\psi(t_j) = \alpha_j]
\end{aligned}$$

Hence,

$$\Pr[A_r = (\alpha_1, \dots, \alpha_q)] = \Pr[A_s = (\alpha_1, \dots, \alpha_q)] \quad (14)$$

Therefore, by substituting Equations 13 and 14 in Equation 12, we conclude that at the first churn operation,

$$\Pr[\mathbf{view}_2^i(I') = \mathbf{v}] = \Pr[\mathbf{view}_3^i(I') = \mathbf{v}]$$

Moreover, since the allocation distribution before the churn operation is the same and both the games use the same DHT.Put to move the pairs, therefore, the new allocation distribution will also be the same. Hence using induction on each bucket, we prove that views will be indistinguishable for all the buckets. The proof follows by noticing that **Game**<sub>3</sub> is same as **Ideal**<sub>Sim,Z</sub>(*k*) experiment.  $\square$

**Security of Chord-based EDHT<sup>+</sup>.** In the following Corollary we formally state the security of the standard scheme when its underlying DHT is instantiated with transient Chord. The proof follows directly from the fact that Chord has non-committing allocations and from Theorem 3.6, which shows that Chord is stable for:

$$\varepsilon = \frac{6(\theta + d) \log |\mathbf{N}|}{|\mathbf{N}|} + \frac{2\theta \log |\mathbf{C}|}{|\mathbf{C}|} \quad \text{and} \quad \theta \leq 4|\mathbf{N}|e^{-2} - d \quad \text{and} \quad \delta = 1 - o\left(\frac{1}{|\mathbf{N}|}\right)$$

**Corollary 6.2.** *If  $|\mathbf{L}| = \Theta(2^k)$ ,  $|I| = \theta \leq 4ne^{-2} - d$ , and if EDHT<sup>+</sup> is instantiated with transient Chord, then it is  $\mathcal{L}_\varepsilon$ -secure with probability at least  $1 - o(\frac{1}{|\mathbf{N}|}) - \text{negl}(k)$  in the random oracle model, where*

$$\varepsilon = \frac{6(\theta + d) \log |\mathbf{N}|}{|\mathbf{N}|} + \frac{2\theta \log |\mathbf{C}|}{|\mathbf{C}|}.$$

**Efficiency.** The time, round and communication complexities of leave and join operations of the standard scheme in transient setting are the same as the underlying DHT.

## 7 Conclusion

In this work, we initiated the study of end-to-end encryption in the context of DHTs. We studied the security properties of the standard scheme in both the perpetual and the transient settings and analyzed its security properties when the underlying DHT is instantiated with Chord. We see our work as a first step towards designing provably-secure end-to-end encrypted distributed systems like off-chain networks, distributed storage systems, key-value stores and distributed caches. Our work motivates several open problems and directions for future work.

**Beyond Chord.** The most immediate direction is to study the security of the standard EDHT when it is instantiated with other DHTs than Chord. Instantiations based on Kademlia [21] and Koorde [15] would be particularly interesting due to the former’s popularity in practice and the latter’s theoretical efficiency. Because Koorde is similar to Chord in structure (though its routing is different and based on De Bruijn graphs) the bounds we introduce in this work to study Chord’s balance and stability might find use in analyzing Koorde. Kademlia, on the other hand, has a very different structure than Chord so it is likely that new custom techniques and bounds are needed to analyze its balance and stability.

**New EDHT constructions.** Another direction is to design new EDHT schemes with better leakage profiles. Here, a “better” profile could be the same profile  $\mathcal{L}_\varepsilon$  achieved in this work but with a smaller  $\varepsilon$  than what we show. Alternatively, it could be a completely different leakage profile. This might be done, for example, by using more sophisticated techniques from structured encryption and oblivious RAMs.

**Crypto-friendly DHTs.** A third direction is to design new encryption-friendly DHTs. By this, we mean designing new DHTs that achieve better balance and stability parameters than Chord. Of course, this may come at a cost in the DHT’s traditional performance metrics (e.g., load balancing or routing time). A particularly important design goal would be to construct a DHT that achieves stability without requiring a lower bound on the number of active nodes. More precisely, our analysis of Chord shows that it is only stable when there are approximately  $.63|\mathbf{N}| + |I|$  active nodes. Decreasing or even possibly eliminating this requirement would be an interesting result. But this brings up a particularly intriguing question which is whether this requirement is inherent to Chord or simply due to the techniques we introduce to study stability.

**Encrypted key-value stores.** Another important direction of immediate practical interest is to design a *consistent* encrypted DHT. In such a system, the encrypted label/value pairs would be replicated throughout the network for reliability. Replication, however, introduces a host of challenges including the problem of updating pairs in a consistent manner. Consistent distributed systems are already very hard to design (and prove correct) but the added challenge of achieving consistency on end-to-end encrypted data would seemingly make the problem even harder. The benefit, however, is that such a system would essentially yield a provably-secure end-to-end encrypted key-value store which, in of itself, would be impactful.<sup>4</sup>

**Encrypted off-chain networks.** As mentioned in the introduction, most off-chain networks already include end-to-end encryption. Our work provides a framework with which one can formally analyze the security of such networks. It would be particularly interesting to analyze the security of both Ethereum’s Swarm and of IPFS. Leveraging our framework (in particular Theorems 4.2 and 6.1) the main challenge left would be to analyze the balance and stability of the Kademlia DHT which, as mentioned earlier, seems non-trivial.

**Stronger adversarial models.** Our security definitions are in the standalone model and against an adversary that makes static corruptions. Extending our work to handle arbitrary compositions (e.g., using universal composability [6]) and adaptive corruptions would be very interesting.

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<sup>4</sup>The NoSQL database market is very large (e.g., projected to reach \$4 billion by 2020) and key-value stores are some of the most popular NoSQL databases.

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