Delegate and Verify the Update Keys of Revocable Identity-Based Encryption

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Abstract

Revocable identity-based encryption (RIBE) is an extension of identity-based encryption (IBE) and it supports efficient revocation of private keys. In the past, many efficient RIBE schemes have been proposed, but research on efficiently delegating the generation of update keys to a cloud server is somewhat insufficient. In this paper, we newly introduce the concept of delegated RIBE (DRIBE) that can delegate the generation of update keys to the semi-trusted cloud server and define the security models of DRIBE. Next, we propose a DRIBE scheme by generically combining a hierarchical IBE (HIBE) scheme, an identity-based broadcast encryption (IBBE) scheme, and a collision-resistant hash function. In addition, we propose a DRIBE-INC scheme that generates an occasional base update key and a periodic incremental update key to reduce the size of update keys in our DRIBE scheme.

Keywords: Identity-based encryption, Key revocation, Subset cover, Update key delegation, Public verifiability.

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1 Introduction

Revocable identity-based encryption (RIBE) is an extension of identity-based encryption (IBE) in which an identity string plays the role of a public key and additionally it supports the key revocation functionality [3,6]. In a public key encryption (PKE) scheme, a credential of a user can be revoked by using a certificate revocation mechanism since there is a certificate that binds the public key of a user with the identity of the user. However, it is difficult to provide the key revocation for an IBE scheme because the IBE scheme does not have a certificate. In the IBE scheme, there are two methods of revoking the credential of a user: a direct revocation method in which a sender specifies a receiver set in a ciphertext, and an indirect revocation method in which a trusted center periodically issues new (updated) keys for non-revoked users. In this paper, we consider IBE schemes that support the indirect revocation method because the sender does not need to care about revoked users when generating ciphertexts.

The first revocation method for IBE was presented by Boneh and Franklin [6], but their method has the disadvantage of requiring a secure channel between a user and the trusted center. An RIBE scheme that efficiently processes the key revocation of a user's private key by using a binary tree was first proposed by Boldyreva et al. [3]. The main idea of their RIBE scheme is that a private key is associated with the path nodes of the binary tree and an update key is associated with the cover nodes of the binary tree that excludes leaf nodes that are related to revoked private keys. In this case, a common node exists between the path nodes and the cover nodes unless the private key is revoked in the update key. If the master key of the RIBE scheme is separated for each tree node by using a secret sharing scheme, then a decryption key can be derived by recovering the shared secret for the corresponding common node and this decryption key can be used to decrypt a ciphertext. After the first construction of an efficient RIBE scheme have been proposed [20,23,26,30,33]. The key revocation method of RIBE also can be applied to an HIBE scheme that supports private key delegation, so various revocable HIBE (RHIBE) schemes have been proposed [19, 21, 28, 29, 31].

As described above, most of the RIBE schemes require a trusted center to generate a user's private key and periodically issue an update key for non-revoked users. In order to reduce the load on the trusted center, we may consider to delegate the generation of update keys to a cloud server. However, the previous RIBE schemes using a binary tree require the same master key for the generation of private keys and update keys because the private key generation and the update key generation algorithms use the same state information of the binary tree. For this reason, if the generation of update keys is simply delegated to the cloud server, then it is possible for the cloud server to easily derive the user's private key from the state information. In order to support secure delegation of update keys, an RIBE scheme that does not use a binary tree has been proposed [22], but this scheme has the disadvantage such that the update key size is linearly dependent on the number of non-revoked users in the system. In this paper, we ask whether it is possible to design an RIBE scheme that can delegate the generation of update keys to a *semi-trusted* cloud server while supporting efficient key revocation by using a binary tree.

1.1 Out Contributions

Definition of DRIBE. We first define delegated RIBE (DRIBE) that can delegate the generation of an update key in RIBE to a semi-trusted cloud server. In DRIBE, a trusted center only generates private keys by using a master secret key and manages a revocation list *RL*. For the generation of update keys, a semi-trusted cloud server periodically generates an update key for the revocation list by using a master update key received from the trusted center, and then it broadcasts the update key to non-revoked users. At this time, anyone can publicly verify that the update key generated by the cloud server is valid on the revocation list *RL*. Similar

to the security of RIBE, the DRIBE scheme also provides indistinguishability under chosen-plaintext attack (IND-CPA) security in which an external attacker cannot distinguish between challenge messages. We also define indistinguishability under update-key attack (IND-UKA) security in which the semi-trusted cloud server cannot obtain any useful information to distinguish between challenge messages if a private key for a challenge identity is not given.

Delegated RIBE. Next, we construct a DRIBE scheme that supports the delegation of update keys by generically combining an HIBE scheme, an IBBE scheme, and a hash function, and then we prove the security of our construction when a cloud server is semi-trusted. The reason why it is difficult to support the delegation of update keys in the previous RIBE schemes that use a binary tree is that the same state information must be shared for the generation of private keys and update keys. To support the delegation of update keys, we pay attention to the RIBE scheme of Ma and Lin (ML-RIBE) [24] that additionally provides the decryption key exposure resistance (DKER) property. The ML-RIBE scheme combines an IBE scheme and an HIBE scheme, and the generation of private keys and the generation of update keys are separated from each other because the master secret key of HIBE is used to generate private keys and the master secret key of IBE is only used to generate update keys. The DRIBE scheme proposed in this paper combines an HIBE scheme, and a hash function, so that the ciphertext size and the secret key size is proportional to the product of the number of revoked users and the security parameter.

DRIBE with Incremental Updates. The drawback of our DRIBE scheme is that the update key size is somewhat large because the depth of a binary tree is set to be proportional to the length of an identity string. To overcome this shortcoming, we propose a DRIBE-INC scheme that supports the generation of incremental update keys and prove the security when a cloud server is semi-trusted. The concept of incremental revocation was already used in the form of delta certificate revocation lists (delta-CRLs) when issuing CRLs for certificate revocation in the public-key infrastructure [11]. The DRIBE-INC scheme separates the update key into two types, a base update key and an incremental update key. For this, a time step T_s to generate the base update key is fixed and a time period T is expressed as $T = T_b + T_c$ where $T \equiv T_c \mod T_s$. At this time, if T is a multiple of T_s ($T = T_b$), a base update key that considers non-revoked users before T_b is issued. Otherwise, an incremental update key that considers non-revoked users from T_b to T is issued. When a ciphertext with an identity ID and time T is given, we can decrypt the ciphertext by combining a private key with base and incremental update keys if ID is not revoked both the base update key at time T_b and the incremental update keys at time T. In general, the size of an incremental update key is relatively small since the number of revoked users during the short period of time is rather small compared to the number of revoked users in the base update key. To design the DRIBE-INC scheme, we use the DRIBE scheme to process base update keys, and an HIBE scheme, an IBBE scheme, and hash function to process incremental update keys.

1.2 Related Work

IBE is an extension of public-key encryption (PKE) that can use the user's identity string as a public key [32]. The first IBE scheme was proposed by Boneh and Franklin [6], and they constructed their IBE scheme by using a bilinear map and proved its security in the random oracle model. Since then, various IBE schemes have been proposed in bilinear maps, quadratic residues, and lattices [4, 10, 13]. In order to use an IBE scheme in a real application environment, an RIBE scheme that provides the functionality of effectively revoking a user's private key is required. An RIBE scheme that provides efficient key revocation using a binary tree was first proposed by Boldyreva et al. [3]. Since then, various RIBE schemes have been proposed

to enhance the security or improve the performance [9, 20, 23, 30]. Recently, generic methods for designing RIBE schemes using binary trees has been proposed [18, 24]. A key principle that enables the generic RIBE design is to make the path of a binary tree associated with a ciphertext instead of associated with a private key. However, since the generic RIBE design requires a larger binary tree compared to the existing direct RIBE design method, there is a problem of inefficiency in terms of update key size. In order to reduce the computational load of a key generation center in RIBE, an RIBE scheme that delegates the generation of update keys to a cloud server was proposed, but the proposed RIBE scheme has a problem that the size of an update key increases in proportion to the number of users [22].

HIBE is an extension of IBE that expresses the identity of a user as an hierarchical identity vector string and provides the functionality of delegating the private key generation to reduce the computational burden of a key generation center [14, 16]. After the first constructions of HIBE, various HIBE schemes have been proposed in bilinear maps and lattices [2, 5, 8, 34]. The first RHIBE scheme that provides the revocation of private keys was proposed by Seo and Emura [29]. In order to design the first RHIBE scheme, they devised a method similar to the RIBE scheme to support the revocation of private keys by using a binary tree for each individual user. After that, Seo and Emura also proposed a more efficient RHIBE scheme in which the private key of an individual user do not need to remember the history of private key delegation [31]. Lee and Park proposed a new RHIBE scheme that surprisingly reduced the private key size and update key size of the existing RHIBE scheme [21]. They devised a new type of HIBE scheme to improve the performance so that the private key and update key size of their RHIBE scheme are not significantly affected by the depth of an identity string. In addition, other RHIBE schemes with improved security and new functionalities have been proposed [17, 19, 28].

2 Preliminaries

In this section, we review the definitions of HIBE, IBBE, hash function, and the complete subtree (CS) method in a binary tree, which are the building blocks of our DRIBE scheme.

2.1 Hierarchical Identity-Based Encryption

Hierarchical IBE (HIBE) is an extension of IBE, which expresses the user identity as a hierarchical identity vector and supports the delegation of the generation of private keys [14, 16]. In HIBE, a trusted center generates the private key of a user by using a master key, and an upper-level user who owns a private key can issue the private key of a lower-level user. A sender creates a ciphertext by specifying the hierarchical identity of a receiver. If the hierarchical identity of the receiver's private key belongs to the prefix set of the hierarchical identity in the ciphertext, the receiver can decrypt the ciphertext. A more detailed syntax of HIBE is given as follows.

Definition 2.1 (Hierarchical Identity-Based Encryption, HIBE). An HIBE scheme consists of five algorithms **Setup**, **GenKey**, **DelegateKey**, **Encrypt**, and **Decrypt**, which are defined as follows:

- **Setup** $(1^{\lambda}, L_{max})$. The setup algorithm takes as input a security parameter 1^{λ} and maximum hierarchical depth L_{max} . It outputs a master key *MK* and public parameters *PP*.
- **GenKey**($ID|_k, MK, PP$). The key generation algorithm takes as input a hierarchical identity $ID|_k = (I_1, ..., I_k) \in \mathcal{I}^k$, the master key MK, and the public parameters PP. It outputs a private key $SK_{ID|_k}$ for $ID|_k$.

- **DelegateKey** $(ID|_k, SK_{ID|_{k-1}}, PP)$. The delegation algorithm takes as input a hierarchical identity $ID|_k$, a private key $SK_{ID|_{k-1}}$ for $ID|_{k-1}$, and the public parameters *PP*. It outputs a delegated private key $SK_{ID|_k}$ for $ID|_k$.
- **Encrypt**($ID|_{\ell}, M, PP$). The encryption algorithm takes as input a hierarchical identity $ID|_{\ell} = (I_1, \dots, I_{\ell}) \in \mathcal{I}^{\ell}$, a message M, and public parameters PP. It outputs a ciphertext $CT_{ID|_{\ell}}$.
- **Decrypt**($CT_{ID|_{\ell}}, SK_{ID'|_{k}}, PP$). The decryption algorithm takes as input a ciphertext $CT_{ID|_{\ell}}$, a private key $SK_{ID'}$, and public parameters *PP*. It outputs a message *M* or \perp .

The correctness of HIBE is defined as follows: For all MK, PP generated by $\mathbf{Setup}(1^{\lambda})$, all $ID|_{\ell}$, $ID'|_{k}$, any $SK_{ID'|_{k}}$ generated by $\mathbf{GenKey}(ID'|_{k}, MK, PP)$, it is required that

• If $ID'|_k \in \operatorname{Prefix}(ID|_\ell)$, then $\operatorname{Decrypt}(\operatorname{Encrypt}(ID|_\ell, M, PP), SK_{ID'|_\ell}, PP) = M$.

The security model of HIBE is similar to that of IBE except that it additionally considers the delegation of private keys [14]. In the security model, public parameters are given to an attacker, and the attacker can query a private key for an hierarchical identity. In the challenge phase, the attacker submits challenge ID^* , M_0^* , and M_1^* and receives a challenge ciphertext. At this time, there is a constraint that the hierarchical identities of private keys requested by the attacker do not belong to the prefix set of the challenge ID^* . After that, the attacker can query additional private keys and finally submits a guess for the challenge ciphertext. The attacker's advantage is the value subtracting 1/2 from the probability of guessing the message. An HIBE scheme is secure if the advantage of all efficient attackers is negligible.

2.2 Identity-Based Broadcast Encryption

Identity-based broadcast encryption (IBBE) is an extension of public-key broadcast encryption (PKBE) except that individual users are specified as identity strings rather than indexes and it supports exponential numbers of system users [12]. In IBBE, a trusted center generates a private key for a user's identity. A sender creates a ciphertext by specifying a set of receiver's identities. A receiver can decrypt the ciphertext if his/her identity of the private key belongs to the receiver's set in the ciphertext. A more detailed syntax of IBBE is given as follows.

Definition 2.2 (Identity-Based Broadcast Encryption, IBBE). An IBBE scheme consists of four algorithms **Setup**, **GenKey**, **Encrypt**, and **Decrypt**, which are defined as follows:

- **Setup** $(1^{\lambda}, n)$: The setup algorithm takes as input a security parameter 1^{λ} and the maximum size *n* of a broadcast set. It outputs a master key *MK* and public parameters *PP*.
- **GenKey**(*ID*,*MK*,*PP*): The private key generation algorithm takes as input an identity $ID \in \mathcal{I}$, the master key *MK*, and public parameters *PP*. It outputs a private key *SK*_{*ID*}.
- **Encrypt**(*S*,*M*,*PP*): The encryption algorithm takes as input a set $S \subseteq \mathcal{I}$ of receivers, a message $M \in \mathcal{M}$, and public parameters *PP*. It outputs a ciphertext *CT*_S.
- **Decrypt**(CT_S , SK_{ID} , PP): The decryption algorithm takes as input a ciphertext CT_S , a private key SK_{ID} , and public parameters PP. It outputs a message M or \perp .

The correctness of IBBE is defined as follows: For all *MK* and *PP* generated by **Setup** $(1^{\lambda}, n)$, *SK*_{*ID*} generated by **GenKey**(ID, MK, PP) for any *ID*, and any *S* and *M*, it is required that

• If $ID \in S$, then **Decrypt**(**Encrypt**(S, M, PP), SK_{ID}, PP) = M.

The security model of IBBE is similar to that of PKBE except that it additionally supports the private key query of an attacker for an identity string [12]. In the security model, an attacker is given public parameters, and the attacker can query a private key for an arbitrary identity string. In the challenge phase, the attacker submits a challenge set S^* , challenge messages M_0^* , M_1^* , and receives a challenge ciphertext. At this time, there is a constraint that the private keys requested by the attacker are not belong to S^* . After that, the attacker can query additional private keys with the same constraints and finally outputs a guess for the challenge ciphertext. At this time, the advantage of the attacker is defined as the value subtracting 1/2 from the probability of guessing the message. An IBBE scheme is secure if the advantage of all efficient attackers is negligible.

2.3 Collision Resistant Hash Function

A hash function family (HF) \mathcal{H} is a set of hash functions $H : \mathcal{X} \to \mathcal{Y}$ where \mathcal{X} is an input domain and \mathcal{Y} is an output range. We say that the hash function family \mathcal{H} is collision resistant if for all efficient adversaries \mathcal{A} , the advantage of \mathcal{A} defined as $\mathbf{Adv}_{HF,\mathcal{A}}^{CR}(\lambda) = \Pr[H(x) = H(x'); H \leftarrow \mathcal{H}, (x, x') \leftarrow \mathcal{A}(H)]$ is negligible in the security parameter λ .

2.4 Binary Tree

A perfect binary tree \mathcal{BT} is a tree data structure in which all internal nodes have two child nodes and all leaf nodes have the same depth. Let $N = 2^n$ be the number of leaf nodes in \mathcal{BT} . The number of all nodes in \mathcal{BT} is 2N - 1 and we denote v_i as a node in \mathcal{BT} for any $1 \le i \le 2N - 1$. The depth d_i of a node v_i is the length of the path from a root node to the node. The root node of a tree has depth zero. The depth of \mathcal{BT} is the length of the path from the root node to a leaf node. A level of \mathcal{BT} is a set of all nodes at given depth.

Each node $v_i \in \mathcal{BT}$ has an identifier $L_i \in \{0,1\}^*$ which is a fixed and unique string. An identifier of each node is assigned as follows: Each edge in the tree is assigned with 0 or 1 depending on whether it is connected to the left or right child node. The identifier L_i of a node v_i is obtained by reading all labels of edges in a path from the root node to the node v_i . The root node has an empty identifier ε . For a node v_i , we define Label (v_i) be the identifier of v_i and Depth (v_i) be the depth d_i of v_i .

A subtree \mathcal{T}_i in \mathcal{BT} is defined as a tree that is rooted at a node $v_i \in \mathcal{BT}$. A subset S_i is defined as a set of all leaf nodes in \mathcal{T}_i . For any two nodes $v_i, v_j \in \mathcal{BT}$ where v_j is a descendant of $v_i, \mathcal{T}_{i,j}$ is defined as a subtree $\mathcal{T}_i - \mathcal{T}_j$, that is, all nodes that are descendants of v_i but not v_j . A subset $S_{i,j}$ is defined as a set of leaf nodes in $\mathcal{T}_{i,j}$, that is, $S_{i,j} = S_i \setminus S_j$.

For a perfect binary tree \mathcal{BT} and a subset RV of leaf nodes, $ST(\mathcal{BT}, RV)$ is defined as the Steiner Tree induced by the set RV and the root node, that is, the minimal subtree of \mathcal{BT} that connects all the leaf nodes in RV and the root node.

2.5 Complete Subtree Method

The complete subtree method (CS) is one of the subset cover methods which are used to design symmetrickey broadcast encryption schemes using binary trees [25]. In the CS method, the assignment algorithm outputs the path nodes of a leaf node when the leaf node is given as input, and the cover algorithm outputs a set of cover nodes that covers all non-revoked leaf nodes when a set of revoked leaf nodes are given as input. The final matching algorithm outputs one node that is common to each other in the path nodes and the cover nodes. A more detailed syntax of the CS method is given as follows:

- **CS.Setup**(*N*): Let $N = 2^n$ for simplicity. It first sets a perfect binary tree \mathcal{BT} of depth *n*. Each user is assigned to a different leaf node in \mathcal{BT} . The collection S is defined as $\{S_i\}$ where S_i is a set of all leaves in a subtree \mathcal{T}_i with a subroot $v_i \in \mathcal{BT}$. It outputs the binary tree \mathcal{BT} .
- **CS.Assign**(\mathcal{BT}, v_{ID}): Let v_{ID} be a leaf node of \mathcal{BT} that is assigned to the user *ID*. Let $(v_{k_0}, v_{k_1}, \dots, v_{k_n})$ be the path from the root node $v_{k_0} = v_0$ to the leaf node $v_{k_n} = v_{ID}$. For all $j \in \{k_0, \dots, k_n\}$, it adds S_j into *PV*. It outputs the private set $PV = \{S_j\}$.
- **CS.Cover**(\mathcal{BT}, RV): It first computes the Steiner tree ST(RV). Let $\mathcal{T}_{k_1}, \ldots, \mathcal{T}_{k_m}$ be all the subtrees of \mathcal{BT} that hang off ST(RV), that is all subtrees whose roots v_{k_1}, \ldots, v_{k_m} are not in ST(RV) but adjacent to nodes of outdegree 1 in ST(RV). For all $i \in \{k_1, \ldots, k_m\}$, it adds S_i into CV. It outputs a covering set $CV = \{S_i\}$.
- **CS.Match**(CV, PV): It finds a subset S_k with $S_k \in CV$ and $S_k \in PV$. If there is such a subset, it outputs (S_k, S_k) . Otherwise, it outputs \perp .

The correctness of the CS method is that if a leaf node is not revoked in the cover nodes, the matching algorithm outputs one common node. In the CS method, the size of the cover nodes is approximately $r \log(N/r)$ when the number of revoked users is r and the total number of binary tree leaf nodes is N.

3 Revocable IBE with Delegated Update Keys

In this section, we define the syntax and security model of DRIBE and show that a DRIBE scheme can be generically constructed by combining existing HIBE and IBBE schemes and a hash function.

3.1 Definition

DRIBE is an extension of RIBE that supports user revocation and it can additionally delegate the generation of update keys to a cloud server. In addition, anyone can publicly verify the update key of DRIBE.

In a DRIBE scheme, a trusted center generates two master keys MSK, MUK, and public parameters PP, and sends the master update key MUK to a cloud server to delegate the generation of update keys. The trusted center generates the private key of each user by using the master secret key MSK and maintains a revocation list RL that records the information of revoked users. The cloud server periodically broadcasts an update key for non-revoked users by using the master update key MUK and the revocation list RL. If a user wants to deliver a message securely to another user, the sender creates a ciphertext by specifying a receiver identity ID and time T. If the private key of the receiver is not revoked in the update key at the corresponding time, the receiver can decrypt the ciphertext by combining his private key and the update key. In addition, any user can publicly verify the validity of the update key generated by the cloud server.

Definition 3.1 (Delegated Revocable IBE). A delegated revocable IBE (DRIBE) scheme that is associated with identity space \mathcal{I} , time space \mathcal{T} , and message space \mathcal{M} , consists of eight algorithms **Setup**, **GenKey**, **Revoke**, **UpdateKey**, **VerifyUK**, **DeriveKey**, **Encrypt**, and **Decrypt**, which are defined as follows:

- **Setup** (1^{λ}) : The setup algorithm takes as input a security parameter 1^{λ} . It outputs a master secret key *MSK*, a master update key *MUK*, and public parameters *PP*.
- **GenKey**(*ID*,*MSK*,*PP*): The private key generation algorithm takes as input an identity *ID*, the master secret key *MSK*, and public parameters *PP*. It outputs a private key *SK*_{*ID*}.

- **Revoke**(ID, T, RL): The revocation algorithm takes as input an identity ID, revocation time T, a current revocation list RL. It outputs an updated revocation list RL.
- **UpdateKey**(T, RL, MUK, PP): The update key generation algorithm takes as input update time $T \in \mathcal{T}$, a revocation list RL, the master update key MUK, and the public parameters PP. It outputs an update key UK_T .
- **VerifyUK**(UK, T, RL, PP): The update key verification generation algorithm takes as input an update key UK, update time $T \in T$, a revocation list RL, and the public parameters PP. It outputs 1 or 0 depending on the validity of the update key.
- **DeriveKey**(SK_{ID} , UK_T , PP): The decryption key derivation algorithm takes as input a private key SK_{ID} , an update key UK_T , and the public parameters PP. It outputs a decryption key $DK_{ID,T}$ or \bot .
- **Encrypt**(*ID*, *T*, *M*, *PP*): The encryption algorithm takes as input an identity *ID*, time *T*, a message $M \in \mathcal{M}$, and the public parameters *PP*. It outputs a ciphertext $CT_{ID,T}$.
- **Decrypt**($CT_{ID,T}$, $DK_{ID',T'}$, PP): The decryption algorithm takes as input a ciphertext $CT_{ID,T}$, a decryption key $DK_{ID',T'}$, and the public parameters PP. It outputs a message M or \perp .

The correctness of DRIBE is defined as follows: For all *MSK*, *MUK*, and *PP* generated by **Setup**(1^{λ}), *SK*_{*ID*} generated by **GenKey**(*ID*,*MSK*,*PP*) for any *ID*, *UK*_{*T*} generated by **UpdateKey**(*T*,*RL*,*MUK*,*PP*) for any *T* and *RL*, *CT*_{*ID*,*T*} generated by **Encrypt**(*ID*,*T*,*M*,*PP*) for any *ID*, *T*, and *M*, it is required that

- If $(ID, T'') \notin RL$ for all $T'' \leq T$, then **DeriveKey** $(SK_{ID}, UK_T, PP) = DK_{ID,T}$.
- If $(ID = ID') \land (T = T')$, then **Decrypt** $(CT_{ID,T}, DK_{ID',T'}, PP) = M$.
- VerifyUK $(UK_T, T, RL, PP) = 1$.

The IND-CPA security model of DRIBE is a modification of the IND-CPA security model of RIBE [3, 30] to consider that all update keys are generated by a *semi-trusted* cloud server. A semi-trusted cloud server follows the protocol but is curious and attempts to obtain extra information from the protocol. In this security model, an attacker can request private key, revocation, update key, and decryption key queries. The private key, revocation, and decryption key queries are handled by a challenger, but the update key queries are handled by a semi-trusted cloud server. Note that there is no direct communication between the cloud server and the attacker. The important restriction of this model is that if the attacker requested a private key of the challenge identity ID^* , the private key corresponding to ID^* should be revoked at the update key of the challenge time T^* . The goal of the attacker is to distinguish challenge messages when the challenge ciphertext corresponding to ID^* and T^* is given. A more detailed definition of this IND-CPA security model is described as follows.

Definition 3.2 (IND-CPA Security). The indistinguishability under chosen-plaintext attack (IND-CPA) security of DRIBE is defined as the following experiment between a challenger C, a semi-trusted cloud server S_C , and an adversary A:

1. Setup: C generates a master secret key *MSK*, a master update key *MUK*, and public parameters *PP* by running Setup (1^{λ}) . It initialize a revocation list $RL = \emptyset$. It keeps *MSK* to itself, and gives *MUK*, *PP* to A_C and *PP* to A.

- 2. Phase 1: A adaptively request a polynomial number of queries. C handles these queries as follows:
 - Private key: If this is a private key query for an identity *ID*, then it creates a private key SK_{ID} by running **GenKey**(*ID*,*MSK*,*PP*) and gives SK_{ID} to A.
 - Revocation: If this is a revocation query for an identity *ID* and time *T*, then it updates *RL* by running **Revoke**(*ID*, *T*, *RL*).
 - Update key: If this is an update key query on time *T*, then it obtains an update key UK_T from the cloud server S_C by providing time *T* and the revocation list *RL*. Next, it gives UK_T to A if **VerifyUK** $(UK_T, T, RL, PP) = 1$.
 - Decryption key: If this is a decryption key query for an identity *ID* and time *T*, then it creates a decryption key $DK_{ID,T}$ by running **DeriveKey** (SK_{ID}, UK_T, PP) and gives $DK_{ID,T}$ to A.

Note that we assume that revocation, update key, and decryption key queries are requested in nondecreasing order of time.

- 3. Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* with equal length. Next, \mathcal{C} flips a random coin $\mu \in \{0, 1\}$ and gives the challenge ciphertext CT^* to \mathcal{A} by running Encrypt (ID^*, T^*, M_u^*, PP) .
- 4. Phase 2: A may continue to request additional queries subject to the same restrictions as before.
- 5. Guess: Finally, A outputs a guess $\mu' \in \{0, 1\}$, and wins the game if $\mu = \mu'$.

The queries of the adversary in the above experiment should satisfy the following conditions:

- 1. If a private key query for ID^* was requested, then a revocation query for ID^* and T such that $T \le T^*$ should be requested.
- 2. A revocation query on T cannot be queried if an update key query on T was already requested.
- 3. A decryption key query on T cannot be requested before an update key query on T was requested.
- 4. A decryption key query for ID^* and T^* was not requested.

The advantage of \mathcal{A} is defined as $\mathbf{Adv}_{DRIBE,\mathcal{A}}^{IND-CPA}(\lambda) = |\Pr[\mu = \mu'] - \frac{1}{2}|$ where the probability is taken over all the randomness of the experiment. A DRIBE scheme is IND-CPA secure when a cloud server is semi-trusted if for all probabilistic polynomial-time (PPT) adversary \mathcal{A} and all PPT cloud server \mathcal{A}_C , the advantage of \mathcal{A} in the above experiment is negligible in the security parameter λ .

Remark 1. If a cloud server is trusted in the above IND-CPA security model of DRIBE, then it is the same as the IND-CPA security model of RIBE since all update keys are generated by a trusted center.

The IND-UKA is a security model that considers the case where a semi-trusted cloud server who can access to the master update key MUK becomes an attacker. In this security model, an attacker corresponding to the cloud server can request private key, revocation, and decryption key queries. Since the attacker can issue an arbitrary update key by using MUK, there is a restriction that the attacker cannot query a private key corresponding to the challenge identity ID^* in order to prevent a simple attack. The goal of the attacker is to distinguish challenge messages when the challenge ciphertext of ID^* and T^* is given. A more detailed definition of the IND-UKA security is described as follows.

Definition 3.3 (IND-UKA Security). The indistinguishability under update-key attack (IND-UKA) security of DRIBE is defined in terms of the following experiment between a challenger C and an adversary A:

- 1. Setup: C generates a master secret key *MSK*, a master update key *MUK*, and public parameters *PP* by running Setup (1^{λ}) . It initialize a revocation list $RL = \emptyset$. It keeps *MSK* to itself and gives *MUK*, *PP* to \mathcal{A} .
- 2. **Phase 1**: A adaptively request a polynomial number of queries. C handles these queries as follows:
 - Private key: If this is a private key query for an identity *ID*, then it creates a private key SK_{ID} by running **GenKey**(*ID*,*MSK*,*PP*) and gives SK_{ID} to A
 - Revocation: If this is a revocation query for an identity ID and time T, then it updates RL by running **Revoke**(ID, T, RL).
 - Decryption key: If this is a decryption key query for an identity *ID* and time *T*, then it takes an input UK_T from \mathcal{A} and creates a decryption key $DK_{ID,T}$ by running **DeriveKey**(SK_{ID}, UK_T, PP) and gives $DK_{ID,T}$ to \mathcal{A} .

Note that we assume that revocation and decryption key queries are requested in non-decreasing order of time.

- 3. Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* with equal length. Next, \mathcal{C} flips a random coin $\mu \in \{0, 1\}$ and gives the challenge ciphertext CT^* to \mathcal{A} by running Encrypt (ID^*, T^*, M_u^*, PP) .
- 4. Phase 2: A may continue to request additional queries subject to the same restrictions as before.
- 5. **Guess**: Finally, \mathcal{A} outputs a guess $\mu' \in \{0, 1\}$, and wins the game if $\mu = \mu'$.

The queries of the adversary in the above experiment should satisfy the following conditions:

- 1. A private key query for ID^* was not requested.
- 2. A decryption key query for ID^* and T^* was not requested.

The advantage of \mathcal{A} is defined as $\mathbf{Adv}_{DRIBE,\mathcal{A}}^{IND-UKA}(\lambda) = \left| \Pr[\mu = \mu'] - \frac{1}{2} \right|$ where the probability is taken over all the randomness of the experiment. A DRIBE scheme is IND-UKA secure if for all PPT adversary \mathcal{A} , the advantage of \mathcal{A} in the above experiment is negligible in the security parameter λ .

3.2 Design Principle

Most of previous RIBE schemes using a binary tree can efficiently process user revocation because the path of the binary tree is associated with a private key and the cover of the binary tree is associated with an update key [3, 20, 23, 30]. However, since these RIBE schemes use a secret sharing scheme to share a master secret key for each node of the binary tree, the private key generation algorithm and the update key generation algorithm require the same state information. For this reason, these RIBE schemes have a problem in that it is difficult to separate the private key generation process and the update key generation process independently, and thus it is difficult to delegate the update key generation to an external semi-trusted cloud server. In addition, in the previous RIBE schemes, it is impossible for a user to publicly verify that the update key has been properly generated without the status information used to generate the update key.

In order to design a DRIBE scheme that can delegate the update key generation, we pay attention to the RIBE scheme proposed by Ma and Lin [24]. In terms of using a binary tree, the ML-RIBE scheme is also similar to the previous RIBE schemes using a binary tree. However, in the previous RIBE schemes, the path of the binary tree is related to a private key, but the ML-RIBE scheme has a big difference in that the path of the binary tree is related to a ciphertext. In order to clearly separate the underlying cryptographic primitives used for private key generation and update key generation, we use the ML-RIBE scheme that provides the decryption key exposure resistance (DKER) property by combining a two-level HIBE scheme and an IBBE scheme. In this case, the private key generation is processed by the master key of the HIBE scheme, and the update key generation is processed by generating key elements for each cover nodes of the binary tree by using the master key of the IBBE scheme. To provide the public verification of update keys, we perform verification using the IBBE encryption process using the fact that the update key elements of the ML-RIBE scheme are all composed of the private keys of the IBBE scheme.

3.3 Construction

A generic DRIBE scheme that uses HIBE, IBBE, and CRHF schemes is described as follows:

DRIBE.Setup (1^{λ}) : Let $\mathcal{I} = \{0, 1\}^n$ be the identity space.

- 1. It first obtains MK_{HIBE} , PP_{HIBE} by running **HIBE.Setup** $(1^{\lambda}, 2)$ and obtains MK_{IBBE} , PP_{IBBE} by running **IBBE.Setup** $(1^{\lambda}, n)$. It also selects a collision resistant hash function $H \in \mathcal{H}$.
- 2. It defines a binary tree \mathcal{BT} by running **CS.Setup** (2^n) where an identity *ID* is uniquely assigned to a leaf node *v* such that Label(v) = ID.
- 3. It outputs a master secret key $MSK = MK_{HIBE}$, a master update key $MUK = MK_{IBBE}$, and public parameters $PP = (PP_{HIBE}, PP_{IBBE}, H, \mathcal{BT})$.
- **DRIBE.GenKey**(*ID*,*MSK*,*PP*): It obtains SK_{HIBE} by running **HIBE.GenKey**(*ID*,*MK*_{HIBE},*PP*_{HIBE}). It outputs a private key $SK_{ID} = SK_{HIBE}$.
- **DRIBE.Revoke**(ID, T, RL): If (ID, *) already exists in RL, it outputs RL. Otherwise, it adds (ID, T) to RL and outputs the updated RL.
- **DRIBE.UpdateKey**(*T*,*RL*,*MUK*,*PP*): To generate an update key for *T*, it proceeds as follows:
 - 1. It initializes $RV = \emptyset$. For each $(ID_j, T_j) \in RL$, it adds a leaf node $v_j \in \mathcal{BT}$ which is associated with ID_j into RV if $T_j \leq T$. It obtains CV_T by running **CS.Cover** (\mathcal{BT}, RV) .
 - 2. For each $S_i \in CV_T$, it obtains SK_{IBBE,S_i} by running **IBBE.GenKey** $(H(\text{Label}(S_i)||T), MK_{IBBE}, PP_{IBBE})$.
 - 3. It outputs an update key $UK_T = (CV_T, \{SK_{IBBE, S_i}\}_{S_i \in CV_T}).$
- **DRIBE.VerifyUK**(UK, T, RL, PP): Let $UK_T = (CV_T, \{SK_{IBBE,S_i}\})$. To verify an update key for T and RL, it proceeds as follows:
 - 1. It initializes $RV = \emptyset$. For each $(ID_j, T_j) \in RL$, it adds a leaf node $v_j \in \mathcal{BT}$ which is associated with ID_j into RV if $T_j \leq T$. It obtains CV' by running **CS.Cover** (\mathcal{BT}, RV) and checks that $CV' = CV_T$.
 - 2. It sets $S = \emptyset$. For each $S_i \in CV_T$, it adds a string $H(\text{Label}(S_i) || T)$ to S. It chooses a random $M \in \mathcal{M}$ and obtains CT_{IBBE} by running **IBBE.Encrypt** (S, M, PP_{IBBE}) .

- 3. For each $S_i \in CV_T$, it performs the followings:
 - (a) It retrieves SK_{IBBE,S_i} from UK_T and obtains M' by running **IBBE.Decrypt**(CT_{IBBE}, SK_{IBBE,S_i} , PP_{IBBE}).
 - (b) If $M' \neq M$, then it outputs 0 since UK is invalid.
- 4. Finally, it outputs 1 since UK is valid.

DRIBE.DeriveKey(SK_{ID} , UK_T , PP): Let $SK_{ID} = SK_{HIBE}$. To derive a decryption key for ID and T, it proceeds as follows:

- 1. It obtains PV_{ID} by running **CS.Assign**(\mathcal{BT}, v_{ID}) where v_{ID} is a leaf node such that $ID = \text{Label}(v_{ID})$. If $PV_{ID} \cap CV_T = \emptyset$, then it outputs \perp since ID was revoked in UK_T .
- 2. It obtains DK_{HIBE} by running **HIBE.DelegateKey**(SK_{HIBE} , T, PP_{HIBE}).
- 3. Finally, it outputs a decryption key $DK_{ID,T} = (DK_{HIBE}, UK_T)$.

DRIBE.Encrypt(*ID*, *T*, *M*, *PP*): To generate a ciphertext for *ID* and *T*, it proceeds as follows:

- 1. It selects random $M_1 \in \mathcal{M}$ and sets $M_2 = M \oplus M_1$. It obtains CT_{HIBE} by running **HIBE.Encrypt** $((ID, T), M_1, PP_{HIBE})$.
- 2. Let v_{ID} be a leaf node associated with ID such that $ID = \text{Label}(v_{ID})$. It obtains PV_{ID} by running **CS.Assign**(\mathcal{BT}, v_{ID}).
- 3. It sets $S = \emptyset$. For each $S_i \in PV_{ID}$, it adds a string $H(\text{Label}(S_i)||T)$ to S. It obtains CT_{IBBE} by running **IBBE.Encrypt** (S, M_2, PP_{IBBE}) .
- 4. Finally, it outputs a ciphertext $CT_{ID,T} = (CT_{HIBE}, CT_{IBBE})$ by implicitly including ID and T.

DRIBE.Decrypt($CT_{ID,T}$, $DK_{ID',T'}$, PP): Let $CT_{ID,T} = (CT_{HIBE}, CT_{IBBE})$ and $DK_{ID',T'} = (DK_{HIBE}, UK_T = (CV_T, \{SK_{IBBE}, S_i\}))$. It proceeds as follows:

- 1. It first obtains M_1 by running **HIBE.Decrypt**(CT_{HIBE} , DK_{HIBE} , PP_{HIBE}).
- 2. It obtains PV_{ID} by running **CS.Assign**(\mathcal{BT} , v_{ID}) where v_{ID} is a leaf node such that Label(v_{ID}) = ID.
- 3. It finds (S_i, S_i) by running **CS.Match** (CV_T, PV_{ID}) . If it fails to find, it returns \perp .
- 4. It retrieves SK_{IBBE,S_i} from UK_T and obtains M_2 by running **IBBE.Decrypt** $(CT_{IBBE}, SK_{IBBE,S_i}, PP_{IBBE})$.
- 5. Finally, it outputs a message $M = M_1 \oplus M_2$.

3.4 Correctness

In this section we show the correctness of the DRIBE scheme. The ciphertext of our DRIBE scheme consists of two elements: an HIBE ciphertext and an IBBE ciphertext. First, if the identity *ID* and time *T* of the HIBE ciphertext and the identity *ID* and time *T* of the HIBE private key are the same, we can decrypt M_1 by the correctness of the HIBE scheme. From the correctness of the CS method, a common node *v* in a binary tree exists if the path of the binary tree associated with *ID* is not revoked in the cover of the binary tree. The IBBE ciphertext sets all nodes in the path as a set of recipients, and the update key consists of the IBBE private keys associated with the cover nodes of the binary tree. Because of this, the common node *v* becomes an element of the path node set, and M_2 is decrypted by the correctness of the IBBE scheme. Therefore, we can derive the correct message with the operation $M = M_1 \oplus M_2$. The update key of our DRIBE scheme is composed of IBBE private keys for cover nodes related to leaf nodes excluding all revoked identities obtained from the revocation list *RL*. Therefore, if an IBBE ciphertext for these cover nodes as recipients are generated and this IBBE ciphertext is decrypted for each IBBE private key to verify that the correct message is decrypted, then the update key is verified correctly by the correctness of the IBBE scheme.

3.5 Security Analysis

In this section, we show that our DRIBE scheme provides the IND-CPA security when a cloud server is semi-trusted and the IND-UKA security by relying on the security of underlying cryptographic primitives.

Theorem 3.1. *The above DRIBE scheme is IND-CPA secure if the underlying HIBE and IBBE schemes are IND-CPA secure.*

Proof. Let ID^* be the challenge identity and T^* be the challenge time. We divide the behavior of an adversary as two types: Type-A and Type-B, which are defined as follows:

- **Type-A.** An adversary is type-A if it requests a private key on an identity *ID* such that $ID \neq ID^*$ for all private key queries.
- **Type-B.** An adversary is type-B if it requests a private key on an identity *ID* such that $ID = ID^*$ for some private key query. In this case, the identity ID^* should be revoked on time *T* such that $T \le T^*$ by the restriction of the security model.

Let E_i be the event that A behaves like type-i adversary. From Lemmas 3.2 and 3.3, we obtain the following result

$$\begin{aligned} \mathbf{Adv}_{DRIBE,\mathcal{A}}^{IND-CPA}(\lambda) &\leq \Pr[E_A] \cdot \mathbf{Adv}_{DRIBE,\mathcal{A}}^{IND-CPA}(\lambda) + \Pr[E_B] \cdot \mathbf{Adv}_{DRIBE,\mathcal{A}}^{IND-CPA}(\lambda) \\ &\leq \mathbf{Adv}_{HIBE,\mathcal{B}}^{IND-CPA}(\lambda) + \mathbf{Adv}_{IND-CPA}^{IND-CPA}(\lambda). \end{aligned}$$

This completes our proof.

Lemma 3.2. For the type-A adversary, the DRIBE scheme is IND-CPA secure if the HIBE scheme is IND-CPA secure.

Proof. Suppose there exists a type-A adversary A that attacks the DRIBE scheme with a non-negligible advantage. An algorithm B that attacks the HIBE scheme is initially given public parameters PP_{HIBE} by a challenger C. Then B that interacts with A is described as follows:

Setup: \mathcal{B} generates MK_{IBBE} , PP_{IBBE} by running the setup algorithm of IBBE. It initializes $RL = \emptyset$ and gives $PP = (PP_{HIBE}, PP_{IBBE}, H, \mathcal{BT})$ to \mathcal{A} .

Phase 1: A adaptively requests a polynomial number of queries. B handles these queries as follows:

- For a private key query on *ID*, \mathcal{B} proceeds as follows: It receives SK_{HIBE} from \mathcal{C} by querying a private key for *ID*. It gives $SK_{ID} = SK_{HIBE}$ to \mathcal{A} .
- For a revocation query on *ID* and *T*, \mathcal{B} updates *RL* by running the revocation algorithm of DRIBE.
- For an update key query on T, \mathcal{B} generates UK_T by using RL and MK_{IBBE} and gives UK_T to \mathcal{A} .

• For a decryption key query on *ID* and *T*, *B* proceeds as follows: It receives DK_{HIBE} from *C* by querying a private key for *ID* and *T*. It generates UK_T by using MK_{IBBE} . It gives $DK_{ID,T} = (DK_{HIBE}, UK_T)$ to *A*.

Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* . \mathcal{B} proceeds as follows:

- 1. It first select a random $M_2 \in \mathcal{M}$ and sets $M_{1,0} = M_0^* \oplus M_2, M_{1,1} = M_1^* \oplus M_2$.
- 2. Next, it receives CT^*_{HIBE} from C by submitting ID^* , T^* , and two challenge messages $M_{1,0}, M_{1,1}$.
- It obtains PV* by running CS.Assign(BT, v*) where a leaf node v* is associated with ID*. It sets S = Ø. For each S_i ∈ PV*, it adds H(Label(S_i)||T*) to S. It generates CT^{*}_{IBBE} by running DRIBE.Encrypt(S, M₂, PP_{IBBE}).
- 4. It gives a challenge ciphertext $CT^* = (CT^*_{HIBE}, CT^*_{IBBE})$ to \mathcal{A} .

Phase 2: Same as Phase 1.

Guess: Finally, \mathcal{A} outputs a guess $\mu' \in \{0, 1\}$. \mathcal{B} also outputs μ' .

In order to analyze the correctness of the simulation described above, we show that it is possible to process the private key and decryption key query of the DRIBE scheme by using the private key query of the HIBE scheme. The type-A attacker requests the DRIBE private key query with the restriction that $ID \neq ID^*$, so the DRIBE private key query can be handled by using the HIBE private key query. In the constraints of the DRIBE security model, the attacker can query the DRIBE decryption key with the restriction that $ID \neq ID^*$ or $ID = ID^* \land T \neq T^*$, so the DRIBE decryption key query also can be handled by using the HIBE private key query. The challenge message selected by the attacker in the challenge phase is linked to the HIBE challenge ciphertext. Thus the probability of distinguishing the HIBE challenge ciphertext.

Lemma 3.3. For the type-B adversary, the DRIBE scheme is IND-CPA secure if the IBBE scheme is IND-CPA secure.

Proof. Suppose there exists a type-B adversary A that attacks the DRIBE scheme with a non-negligible advantage. An algorithm B that attacks the IBBE scheme is initially given public parameters PP_{IBBE} by a challenger C. Then B that interacts with A is described as follows:

Setup: \mathcal{B} generates MK_{HIBE} , PP_{HIBE} by running the setup algorithm of HIBE. It initializes $RL = \emptyset$ and gives $PP = (PP_{HIBE}, PP_{IBBE}, H, \mathcal{BT})$ to \mathcal{A} .

Phase 1: A adaptively requests a polynomial number of private key, revocation, update key, and decryption key queries.

- For a private key query on *ID*, \mathcal{B} generates *SK*_{*ID*} by using *MK*_{*HIBE*} and gives *SK*_{*ID*} to \mathcal{A} .
- For a revocation query on *ID* and *T*, \mathcal{B} updates *RL* by running the revocation algorithm of DRIBE.
- For an update key query on T, \mathcal{B} proceeds as follows:
 - 1. It initializes $RV = \emptyset$. For each $(ID_j, T_j) \in RL$, it adds a leaf node $v_j \in \mathcal{BT}$ into RV if $T_j \leq T$. It obtains CV_T by running **CS.Cover** (\mathcal{BT}, RV) .

- 2. For each $S_i \in CV_T$, it receives SK_{IBBE,S_i} from C by querying a private key for $H(\text{Label}(S_i)||T)$.
- 3. It creates $UK_T = (CV_T, \{SK_{IBBE,S_i}\}_{S_i \in CV_T})$ and gives UK_T to \mathcal{A} .
- For a decryption key query on *ID* and *T*, \mathcal{B} proceeds as follows: It generates DK_{HIBE} for *ID* and *T* by using MK_{HIBE} . It receives UK_T by querying an update key to its own oracle. It gives $DK_{ID,T} = (DK_{HIBE}, UK_T)$ to \mathcal{A} .

Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* . \mathcal{B} proceeds as follows:

- 1. It first selects a random $M_1 \in \mathcal{M}$ and sets $M_{2,0} = M_0^* \oplus M_1, M_{2,1} = M_1^* \oplus M_1$. It generates CT^*_{HIBE} by running **HIBE.Encrypt**($(ID^*, T^*), M_1, PP_{HIBE}$).
- 2. It obtains PV^* by running **CS.Assign**(\mathcal{BT}, v^*) where a leaf node v^* is associated with ID^* . It sets $S = \emptyset$. For each $S_i \in PV^*$, it adds $H(\text{Label}(S_i) || T^*)$ to S.
- 3. It receives CT^*_{IBBE} from C by submitting a challenge set S and challenge messages $M_{2,0}, M_{2,1}$.
- 4. It gives a challenge ciphertext $CT^* = (CT^*_{HIBE}, CT^*_{IBBE})$ to \mathcal{A} .

Phase 2: Same as Phase 1.

Guess: Finally, \mathcal{A} outputs a guess $\mu' \in \{0, 1\}$. \mathcal{B} also outputs μ' .

In order to analyze whether the simulation described above is correct, we show that it is possible to process the update key and decryption key queries of the DRIBE scheme by using the private key queries of the IBBE scheme. From the restriction of a type-B attacker, we have that a private key for ID^* is revoked in an update key at time T^* if the attacker requested a private key for ID^* . When generating the update key of the DRIBE scheme, the string $H(S_i||T)$ is used as the identity of the IBBE scheme. Thus, the update key at time $T \neq T^*$ can be created by generating IBBE private keys using the fact that $H(S_i||T) \neq H(S_i||T^*)$ since $T \neq T^*$. The update key at time $T = T^*$ also can be created by generating IBBE private keys using the fact that $H(S_i||T^*) \neq H(S_i^*||T^*)$ because the path nodes of ID^* are all removed from the cover nodes at time T^* . The decryption key query can also be easily handled by using the update key query in the simulation. Finally, in the challenge phase, the attacker's challenge message is linked to the IBBE challenge message, so the DRIBE challenge ciphertext is linked to the IBBE challenge ciphertext.

Theorem 3.4. The above DRIBE scheme is IND-UKA secure if the underlying HIBE scheme is IND-CPA secure.

Proof. Suppose there exists an adversary \mathcal{A} that attacks the DRIBE scheme with a non-negligible advantage. An algorithm \mathcal{B} that attacks the HIBE scheme is initially given public parameters PP_{HIBE} by a challenger \mathcal{C} . Then \mathcal{B} that interacts with \mathcal{A} is described as follows:

Setup: \mathcal{B} generates MK_{IBBE} , PP_{IBBE} by running the setup algorithm of IBBE. It initializes $RL = \emptyset$ and gives $MUK = MK_{IBBE}$, $PP = (PP_{HIBE}, PP_{IBBE}, H, \mathcal{BT})$ to \mathcal{A} .

Phase 1: A adaptively requests a polynomial number of private key, revocation, and decryption key queries.

- For a private key query on *ID*, \mathcal{B} proceeds as follows: It receives SK_{HIBE} from \mathcal{C} by querying a private key for *ID*. It gives $SK_{ID} = SK_{HIBE}$ to \mathcal{A} .
- For a revocation query on *ID* and *T*, \mathcal{B} updates *RL* by running the revocation algorithm of DRIBE.

• For a decryption key query on *ID* and *T*, \mathcal{B} proceeds as follows: It receives DK_{HIBE} from \mathcal{C} by querying a private key for *ID* and *T*. Next, it generates UK_T by using MK_{IBBE} . It gives $DK_{ID,T} = (DK_{HIBE}, UK_T)$ to \mathcal{A} .

Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* . \mathcal{B} proceeds as follows:

- 1. It first select a random $M_2 \in \mathcal{M}$ and sets $M_{1,0} = M_0^* \oplus M_2, M_{1,1} = M_1^* \oplus M_2$.
- 2. Next, it receives CT^*_{HIBE} from C by submitting ID^* , T^* , and two challenge messages $M_{1,0}, M_{1,1}$.
- It obtains PV* by running CS.Assign(BT, v*) where a leaf node v* is associated with ID*. It sets S = Ø. For each S_i ∈ PV*, it adds H(Label(S_i)||T*) to S. It generates CT^{*}_{IBBE} by running DRIBE.Encrypt(S, M₂, PP_{IBBE}).
- 4. It gives a challenge ciphertext $CT^* = (CT^*_{HIBE}, CT^*_{IBBE})$ to \mathcal{A} .

Phase 2: Same as Phase 1.

Guess: Finally, \mathcal{A} outputs a guess $\mu' \in \{0, 1\}$. \mathcal{B} also outputs μ' .

The restrictions of the attacker in the IND-UKA security model are the same as those of the type-A attacker in the Lemma 3.2. Thus the correctness of this simulation is the same as that of the simulation in Lemma 3.2. \Box

3.6 Discussions

Efficiency Analysis. The public parameters of the DRIBE scheme consist of HIBE and IBE public parameters. In addition, the public parameters require binary tree information to be used in the DRIBE scheme, and the binary tree has a depth of 2λ where λ is the security parameter. The DRIBE private key is compact since it composed of one HIBE private key. The DRIBE update key is related to the number of cover nodes in the binary tree. If the number of revoked users is r, then the size of the cover nodes is $r \log(2^{2\lambda}/r)$. Thus the update key consists of approximately $2r\lambda$ IBBE private keys. The DRIBE ciphertext is compact because it consists of one HIBE ciphertext and one IBBE ciphertext. The DRIBE encryption algorithm performs one HIBE decryption. Since the DRIBE update key verification algorithm needs to check all IBBE private keys in the update key, it requires one IBBE encryption and $2r\lambda$ IBBE decryption operations.

Server-Aided Decryption. In order to improve the decryption performance of an RIBE scheme, a serveraided RIBE scheme, in which a cloud server processes part of the decryption operation, was proposed [27]. Our DRIBE scheme naturally supports the server-aided decryption functionality. That is, a decrypter first sends the IBBE ciphertext of a DRIBE ciphertext and the DRIBE update key of a DRIBE decryption key to a cloud server. Then, the cloud server obtains a partial message M_2 by decrypting the IBBE ciphertext using an IBBE private key which is associated to the matching node of a binary tree, and returns it to the decrypter. Note that the cloud server cannot obtain any information about the original message since M_2 was selected as a random value. After that, the decrypter decrypts the HIBE ciphertext to obtain M_1 , and combines M_1 with M_2 to derive the original message. The decryption process of the decrypter is efficient since the decrypter needs only one HIBE decryption operation.

Reducing the Update Key Size. In our DRIBE scheme, the path of a binary tree is associated with a receiver's identity. Thus the depth of the binary tree should be set to be proportional to the length of an

identity, and the depth should be the output length of a hash function if an arbitrary long string is used for the identity. That is, when the security parameter of the system is λ , the depth of the binary tree should be 2λ . Since the binary tree is also involved in the generation of an update key, the size of the update key is $r\log(2^{2\lambda}/r)$ where *r* is the number of revoked users. The problem of our DRIBE scheme is that the depth of the binary tree should be 2λ , whereas the depth of the previous RIBE schemes is just $\log N$ where *N* is the number of system users. Specifically, if we set $\lambda = 80$ and $N = 2^{30}$, then the update key size of the previous RIBE schemes is approximately r * 30, but the update key size of our DRIBE scheme is r * 160. Thus the update key of the DRIBE scheme is 5 times larger than that of the previous RIBE schemes. To reduce the update key size, we propose a DRIBE-INC scheme in the next section that generates an incremental update key for revoked users in a short period of time.

4 Delegated RIBE with Incremental Update Keys

In this section, we define the syntax and security model of DRIBE-INC that supports the generation of incremental update keys. We next propose a DRIBE-INC scheme by generically combining DRIBE, HIBE, IBBE schemes and a hash function, and prove the security of our construction.

4.1 Definition

A DRIBE-INC scheme is similar to a DRIBE scheme that delegate the generation of update keys to an external cloud server except that it additionally supports the generation of incremental update keys. To support incremental update, the DRIBE-INC scheme separates an update key into a base update key and an incremental update key. If we let T_s be an interval period for generating the base update key, a time period T is expressed as $T = T_b + T_c$ where $T_c = T \mod T_s$. The cloud server generates a base update key that includes all users who were not revoked before the time T_b if $T = T_b$, and generates an incremental update key that includes all users that were not revoked between time T_b and time T if $T \neq T_b$. Similar to the DRIBE scheme, a sender creates a ciphertext for an identity *ID* and time T and delivers the ciphertext to a receiver. The receiver can decrypt the ciphertext if *ID* is not revoked in both the base update key of T_b and the incremental update key of T. The detailed syntax of DRIBE-INC is defined as follows.

Definition 4.1 (Incremental Delegated RIBE). An incremental DRIBE (DRIBE-INC) scheme that is associated with identity space \mathcal{I} , time space \mathcal{T} , and message space \mathcal{M} , consists of eight algorithms **Setup**, **GenKey**, **UpdateKey**, **IncUpdateKey**, **DeriveKey**, **Encrypt**, **Decrypt**, and **Revoke**, which are defined as follows:

- Setup(1^{λ}): The setup algorithm takes as input a security parameter 1^{λ} . It outputs a master key *MSK*, a master update key *MUK*, and public parameters *PP*.
- **GenKey**(ID, MSK, PP): The private key generation algorithm takes as input an identity ID, the master key MK and public parameters PP. It outputs a private key SK_{ID} .
- **Revoke**(ID, T, RL): The revocation algorithm takes as input an identity ID and revocation time T, a revocation list RL. It outputs an updated revocation list RL.
- **UpdateKey**(T_b , RL, MUK, PP): The base update key generation algorithm takes as input base update time $T_b \in \mathcal{T}$, a revocation list RL, the master update key MUK, and the public parameters PP. It outputs a base update key BUK_{T_b} for a base time T_b .

- **IncUpdateKey**(T, RL, MUK, PP): The incremental update key generation algorithm takes as input update time $T \in \mathcal{T}$, a revocation list RL, the master update key MUK, and the public parameters PP. It outputs an incremental update key IUK_T .
- **VerifyBUK**(BUK, T_b , RL, PP): The base update key verification algorithm takes as input a base update key BUK, base time $T_b \in \mathcal{T}$, a revocation list RL, and the public parameters PP. It outputs 1 or 0 depending on the validity of the base update key.
- **VerifyIUK**(*IUK*, *T*, *RL*, *PP*): The incremental update key verification algorithm takes as input an incremental update key *IUK*, update time $T \in \mathcal{T}$, a revocation list *RL*, and the public parameters *PP*. It outputs 1 or 0 depending on the validity of the incremental update key.
- **DeriveKey**(SK_{ID} , BUK_{T_b} , IUK_T , PP): The decryption key derivation algorithm takes as input a private key SK_{ID} , a base update key BUK_{T_b} , an incremental update key IUK_T , and the public parameters PP. It outputs a decryption key $DK_{ID,T}$ or \bot .
- **Encrypt**(*ID*, *T*, *M*, *PP*): The encryption algorithm takes as input an identity *ID*, time *T*, a message $M \in \mathcal{M}$, and the public parameters *PP*. It outputs a ciphertext $CT_{ID,T}$.
- **Decrypt**($CT_{ID,T}$, $DK_{ID',T'}$, PP): The decryption algorithm takes as input a ciphertext $CT_{ID,T}$, a decryption key $DK_{ID',T'}$, and the public parameters PP. It outputs a message M or \perp .

The correctness of DRIBE-INC is defined as follows: For all MSK, MUK, and PP generated by **Setup** (1^{λ}) , SK_{ID} generated by **GenKey**(ID, MSK, PP) for any ID, BUK_{T_b} and IUK_T generated by **UpdateKey** (T_b, RL, MUK, PP) and **IncUpdateKey**(T, RL, MUK, PP) respectively for any $T = T_b + T_c$ and RL, $CT_{ID,T}$ generated by **Encrypt**(ID, T, M, PP) for any ID, T, and M, it is required that

- If $(ID, T') \notin RL$ for all $T' \leq T$, then **DeriveKey** $(SK_{ID}, BUK_{T_b}, IUK_T, PP) = DK_{ID,T}$.
- If $(ID = ID') \land (T = T')$, then **Decrypt** $(CT_{ID,T}, DK_{ID',T'}, PP) = M$.
- VerifyBUK $(BUK_{T_b}, T_b, RL, PP) = 1$.
- **VerifyIUK** $(IUK_T, T, RL, PP) = 1$.

The security models of DRIBE-INC are similar to those of DRIBE, which are the IND-CPA security model that defines the message hiding against external attackers and the IND-UKA security model that defines the message hiding against external cloud severs. The only change in the security models is that an update key is divided into a base update key and an incremental update key. For definitions of security models, please refer to the security definitions of DRIBE in Section 3.1.

4.2 Construction

To design a DRIBE-INC scheme, we express time T as $T = T_b + T_c$ where $T_c \equiv T \mod T_s$. If $T \equiv 0 \mod T_s$, we use the DRIBE scheme to generate a base update key for non-revoked users before time T_b . If $T \neq 0 \mod T_s$, we use the HIBE and IBBE schemes to generate an incremental update key for non-revoked users between time T_b and time T. The method of creating the incremental update key is similar to that in the DRIBE scheme.

A generic DRIBE-INC scheme that uses DRIBE, HIBE, IBBE, and CRHF schemes is described as follows:

DRIBE-INC.Setup (1^{λ}) : Let $\mathcal{I} = \{0, 1\}^n$ be the identity space.

- 1. It first obtains MSK_{DRIBE} , MUK_{DRIBE} , RL_{DRIBE} , PP_{DRIBE} by running **DRIBE.Setup** (1^{λ}) . It obtains MK_{HIBE} , PP_{HIBE} by running **HIBE.Setup** $(1^{\lambda}, 2)$ and obtains MK_{IBBE} , PP_{IBBE} by running **IBBE.Setup** $(1^{\lambda}, n)$. It also selects a collision resistant hash function $H \in \mathcal{H}$.
- 2. It sets a binary tree \mathcal{BT} with depth *n* where an identity $ID \in \mathcal{I}$ is uniquely assigned to a leaf node such that Label(v) = ID.
- 3. It outputs a master secret key $MSK = (MSK_{DRIBE}, MK_{HIBE})$, a master update key $MUK = (MUK_{DRIBE}, MK_{IBBE})$, and public parameters $PP = (PP_{DRIBE}, PP_{HIBE}, PP_{IBBE}, H, \mathcal{BT})$.

DRIBE-INC.GenKey(*ID*,*MSK*,*PP*): To generate a private key of *ID*, it proceeds as follows:

- 1. It obtains *SK*_{DRIBE} by running **DRIBE.GenKey**(*ID*,*MSK*_{DRIBE},*PP*_{DRIBE}). It obtains *SK*_{HIBE} by running **HIBE.GenKey**(*ID*,*MK*_{HIBE},*PP*_{HIBE}).
- 2. It outputs a private key $SK_{ID} = (SK_{DRIBE}, SK_{HIBE})$.
- **DRIBE-INC.Revoke**(ID, T, RL): If (ID, *) already exists in RL, it outputs RL. Otherwise, it adds (ID, T) to RL and outputs the updated RL.
- **DRIBE-INC.UpdateKey**(T_b , RL, MUK, PP): Let T_b be base time such that $T_b \equiv 0 \mod T_s$. If $T_b \not\equiv 0 \mod T_s$, then it returns \perp since a base update key will not be generated.
 - 1. It initializes $BRL = \emptyset$. For each $(ID_j, T_j) \in RL$, it adds (ID_j, T_j) to BRL if $T_j \leq T_b$. It obtains UK_{DRIBE} by running **DRIBE.UpdateKey** $(T_b, BRL, MUK_{DRIBE}, PP_{DRIBE})$.
 - 2. Finally, it outputs a base update key $BUK_{T_b} = UK_{DRIBE}$.

DRIBE-INC.IncUpdateKey(T, RL, MUK, PP): Let $T = T_b + T_c$ where $T_b \equiv 0 \mod T_s$ and $0 \le T_c < T_s$.

- 1. It initializes $IRV = \emptyset$. For each $(ID_i, T_i) \in RL$, it adds v_i which is associated with ID_i into IRV if $T_b < T_i \leq T$. It obtains ICV_T by running **CS.Cover** (\mathcal{BT}, IRV) .
- 2. For each $S_i \in ICV_T$, it obtains SK_{IBBE,S_i} by running **IBBE.GenKey** $(H(\text{Label}(S_i)||T), MK_{IBBE}, PP_{IBBE})$.
- 3. Finally, it outputs an incremental update key $IUK_T = (ICV_T, \{SK_{IBBE,S_i}\}_{S_i \in ICV_T})$.
- **DRIBE-INC.VerifyBUK**(BUK, T_b , RL, PP): To verify the validity of BUK, it returns **DRIBE.VerifyUK** (BUK, T_b , RL, PP_{DRIBE}).

DRIBE-INC.VerifyUK(*IUK*, *T*, *RL*, *PP*): Let $IUK = (ICV_T, \{SK_{IBBE,S_i}\})$. It proceeds as follows:

- 1. It initializes $RV = \emptyset$. For each $(ID_j, T_j) \in RL$, it adds a leaf node $v_j \in \mathcal{BT}$ which is associated with ID_j into RV if $T_j \leq T$. It obtains CV' by running **CS.Cover**(\mathcal{BT}, RV) and checks that $CV' = CV_T$.
- 2. It sets $S = \emptyset$. For each $S_i \in CV_T$, it adds a string $H(\text{Label}(S_i) || T)$ to S. It chooses a random $M \in \mathcal{M}$ and obtains CT_{IBBE} by running **IBBE.Encrypt** (S, M, PP_{IBBE}) .
- 3. For each $S_i \in CV_T$, it performs the followings:
 - (a) It retrieves SK_{IBBE,S_i} from UK_T and obtains M' by running **IBBE.Decrypt** $(CT_{IBBE}, SK_{IBBE,S_i}, PP_{IBBE})$.

- (b) If $M' \neq M$, then it outputs 0 since UK is invalid.
- 4. Finally, it outputs 1 since UK is valid.

DRIBE-INC.DeriveKey(SK_{ID} , BUK_{T_b} , IUK_T , PP): Let $SK_{ID} = SK_{DRIBE}$, $BUK_{T_b} = UK_{DRIBE}$, and $IUK_T = (ICV_T, \{SK_{IBBE,S_i}\})$. If $T \neq T_b + T_c$ for some T_c such that $0 \leq T_c < T_s$, then it returns \perp since BUK_{T_b} and IUK_T are not a valid update key pair.

- 1. It obtains DK_{DRIBE} by running **DRIBE.DeriveKey**(SK_{DRIBE} , UK_{DRIBE} , PP_{DRIBE}). If $DK_{DRIBE} = \bot$, it returns \bot since *ID* was revoked.
- 2. It obtains PV_{ID} by running **CS.Assign**(\mathcal{BT} , v_{ID}) where v_{ID} is a leaf node such that $ID = \text{Label}(v_{ID})$. If $PV_{ID} \cap ICV_T = \emptyset$, then it outputs \perp since ID was revoked in IUK_T .
- 3. It obtains *DK_{HIBE}* by running **HIBE.DelegateKey**(*SK_{HIBE}*, *T*, *PP_{HIBE}*).
- 4. Finally, it outputs a decryption key $DK_{ID,T} = (DK_{DRIBE}, DK_{HIBE}, IUK_T)$.

DRIBE-INC.Encrypt(*ID*, *T*, *M*, *PP*): Let $T = T_b + T_c$ where $T_b \equiv 0 \mod T_s$ and $0 \le T_c < T_s$.

- 1. It selects random $M_1, M_2 \in \mathcal{M}$ and sets $M_3 = M \oplus M_1 \oplus M_2$. It obtains CT_{DRIBE} by running **DRIBE.Encrypt**(ID, T_b, M_1, PP_{DRIBE}). It also obtains CT_{HIBE} by running **HIBE.Encrypt**(ID, T, M_2, PP_{HIBE}).
- 2. Let v_{ID} be a leaf node associated with ID such that $ID = \text{Label}(v_{ID})$. It obtains PV_{ID} by running **CS.Assign**(\mathcal{BT}, v_{ID}).
- 3. It sets $S = \emptyset$. For each $S_i \in PV_{ID}$, it adds a string $H(\text{Label}(S_i) || T)$ to S. Next, it obtains CT_{IBBE} by running **IBBE.Encrypt** (S, M_3, PP_{IBBE}) .
- 4. Finally, it outputs a ciphertext $CT_{ID,T} = (CT_{DRIBE}, CT_{HIBE}, CT_{IBBE})$.

DRIBE-INC.Decrypt($CT_{ID,T}, DK_{ID',T'}, PP$): Let $CT_{ID,T} = (CT_{DRIBE}, CT_{HIBE}, CT_{IBBE})$ and $DK_{ID',T'} = (DK_{DRIBE}, DK_{HIBE}, IUK_T)$ where $IUK_T = (ICV_T, \{SK_{IBBE,S_i}\})$. If $(ID \neq ID') \lor (T \neq T')$, then it returns \bot . Otherwise, it proceeds as follows:

- 1. It obtains M_1 by running **DRIBE.Decrypt**(CT_{DRIBE} , DK_{DRIBE} , PP_{DRIBE}). It obtains M_2 by running **HIBE.Decrypt**(CT_{HIBE} , DK_{HIBE} , PP_{HIBE}).
- 2. It obtains PV_{ID} by running **CS.Assign**(\mathcal{BT} , v_{ID}) where v_{ID} be a leaf node such that Label(v_{ID}) = ID.
- 3. It finds (S_i, S_i) by running **CS.Match** (CV_T, PV_{ID}) . If it fails to find, it returns \perp .
- 4. It retrieves SK_{IBBE,S_i} from IUK_T and obtains M_3 by running **IBBE.Decrypt**(CT_{IBBE}, SK_{IBBE,S_i} , PP_{IBBE}).
- 5. Finally, it outputs a message $M = M_1 \oplus M_2 \oplus M_3$.

4.3 Correctness

In this section we show the correctness of the DRIBE-INC scheme. The ciphertext of our DRIBE-INC scheme consists of three elements: a DRIBE ciphertext, an HIBE ciphertext, and an IBBE ciphertext. First, if the identity ID of the DRIBE ciphertext is not revoked in a base update key, we can decrypt M_1 by the correctness of the DRIBE scheme. Then, if *ID* and *T* of the HIBE ciphertext and *ID* and *T* of an HIBE decryption key are the same, we can decrypt M_2 by the correctness of the HIBE scheme. Now, when the

leaf node of a binary tree associated with *ID* is not revoked in an incremental update key, a common node v exists by the correctness of the CS scheme. At this time, the IBBE ciphertext sets path nodes as a set of recipients, and an update key consists of IBBE private keys associated with cover nodes. Because of this, the common node becomes an element in path nodes, so we can decrypt M_3 by the correctness of the IBBE scheme. Therefore, we can derive the original message by computing $M = M_1 \oplus M_2 \oplus M_3$.

4.4 Security Analysis

In this section, we show that our DRIBE-INC scheme provides the IND-CPA security and the IND-UKA security by relying on the security of underlying cryptographic primitives.

Theorem 4.1. The above DRIBE-INC scheme is IND-CPA secure if the underlying DRIBE scheme is IND-CPA secure, HIBE and IBBE schemes are IND-CPA secure.

Proof. Let ID^* be the challenge identity and T^* be the challenge time such that $T^* = T_b^* + T_c^*$. We divide the behavior of an adversary as three types: Type-A, Type-B, and Type-C. These types are defined as follows:

- **Type-A.** An adversary is type-A if it queries a private key corresponding to $ID \neq ID^*$ for all private keys.
- **Type-B.** An adversary is type-B if it queries a private key corresponding to $ID = ID^*$ and the private key of ID^* is revoked at some time T such that $T \le T_h^*$.
- **Type-C.** An adversary is type-C if it queries a private key corresponding to $ID = ID^*$ and the private key of ID^* is revoked at some time T such that $T_h^* < T \le T^*$.

Let E_i be the event that A behaves like type-i adversary. From Lemmas 4.2, 4.3, and 4.4, we obtain the following result

This completes our proof.

Lemma 4.2. For the type-A adversary, the DRIBE-INC scheme is IND-CPA secure if the HIBE scheme is IND-CPA secure.

Proof. Suppose there exists a type-A adversary A that attacks the DRIBE-INC scheme with a non-negligible advantage. An algorithm B that attacks the HIBE scheme is initially given public parameters PP_{HIBE} by a challenger C. Then B that interacts with A is described as follows:

Setup: \mathcal{B} obtains $MSK_{DRIBE}, MUK_{DRIBE}, PP_{DRIBE}$ by running the **DRIBE.Setup** algorithm. It obtains MK_{IBBE}, PP_{IBBE} by running the **IBBE.Setup** algorithm. It initializes $RL = \emptyset$ and gives $PP = (PP_{DRIBE}, PP_{HIBE}, PP_{IBBE}, H, \mathcal{BT})$ to \mathcal{A} .

Phase 1: A adaptively requests a polynomial number of private key, revocation, base update key, incremental update key, and decryption key queries.

• For a private key query on *ID*, \mathcal{B} proceeds as follows: It generates SK_{DRIBE} by using MSK_{DRIBE} . Next, it receives SK_{HIBE} from \mathcal{C} by querying a private key for *ID*. It gives $SK_{ID} = (SK_{DRIBE}, SK_{HIBE})$ to \mathcal{A} .

- For a revocation query on *ID* and *T*, \mathcal{B} proceeds as follows: It adds (*ID*,*T*) to *RL* if *ID* was not revoked before.
- For a base update key query on T_b , \mathcal{B} proceeds as follows: It generates BUK_{T_b} by using MUK_{DRIBE} . It gives BUK_{T_b} to \mathcal{A} .
- For an incremental update key query on $T = T_b + T_c$, \mathcal{B} proceeds as follows: It generates IUK_T by using MK_{IBBE} . It gives IUK_T to \mathcal{A} .
- For a decryption key query on *ID* and $T = T_b + T_c$, \mathcal{B} proceeds as follows: It generates DK_{DRIBE} for T_b by using MSK_{DRIBE} and MUK_{DRIBE} . It receives DK_{HIBE} from \mathcal{C} by querying a private key for *ID* and T. Next, it generates IUK_T by using MK_{IBBE} . It gives $DK_{ID,T} = (DK_{DRIBE}, DK_{HIBE}, IUK_T)$ to \mathcal{A} .

Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* where $T^* = T_b^* + T_c^*$. \mathcal{B} proceeds as follows:

- 1. It selects random M_1, M_3 and sets $M_{2,0} = M_0^* \oplus M_1 \oplus M_3, M_{2,1} = M_1^* \oplus M_1 \oplus M_3$.
- 2. Next, it generates CT_{DRIBE}^* by running **DRIBE.Encrypt** $(ID^*, T_b^*, M_1, PP_{DRIBE})$. It receives CT_{HIBE}^* from C by submitting challenge ID^* , T^* , and challenge messages $M_{2,0}^*, M_{2,1}^*$.
- 3. It obtains PV^* by running **CS.Assign** (v^*) where v^* is associated with ID^* . It sets $S = \emptyset$. For each $S_i \in PV_{ID}$, it adds a string $H(\text{Label}(S_i)||T)$ to S. It creates CT^*_{IBBE} by running **IBBE.Encrypt** (S, M_3, PP_{IBBE}) .
- 4. It gives a challenge ciphertext $CT^* = (CT^*_{DRIBE}, CT^*_{HIBE}, CT^*_{IBBE})$ to \mathcal{A} .

Phase 2: Same as Phase 1.

Guess: Finally, \mathcal{A} outputs a guess $\mu' \in \{0,1\}$. \mathcal{B} also outputs μ' .

To complete the proof, we analyze the correctness of the simulation. For this, we show that it is possible to process the private key and decryption key query for the DRIBE-INC scheme by using the private key query for the HIBE scheme. Similar to analysis of Lemma 3.2, all private key and decryption key queries can be handled using the HIBE private key query by the restrictions of the type-A adversary and the restrictions of the decryption key queries in the DRIBE-INC security model. The challenge ciphertext is set so that the distinction of the DRIBE-INC challenge message is related with that of the HIBE challenge message.

Lemma 4.3. For the type-B adversary, the DRIBE-INC scheme is IND-CPA secure if the DRIBE scheme is IND-CPA secure.

Proof. Suppose there exists a type-B adversary A that attacks the DRIBE-INC scheme with a non-negligible advantage. An algorithm B that attacks the DRIBE scheme is initially given public parameters PP_{DRIBE} by a challenger C. Then B that interacts with A is described as follows:

Setup: \mathcal{B} generates MK_{HIBE} , PP_{HIBE} by running the **HIBE.Setup** algorithm and generates MK_{IBBE} , PP_{IBBE} by running the **IBBE.Setup** algorithm. It initializes $RL = \emptyset$ and gives $PP = (PP_{DRIBE}, PP_{HIBE}, PP_{IBBE}, H, \mathcal{BT})$ to \mathcal{A} .

Phase 1: A adaptively requests a polynomial number of private key, revocation, base update key, incremental update key, and decryption key queries.

• For a private key query on *ID*, \mathcal{B} proceeds as follows: It receives SK_{DRIBE} from \mathcal{C} by querying a private key with *ID*. It generates SK_{HIBE} by using MK_{HIBE} . It gives $SK_{ID} = (SK_{DRIBE}, SK_{HIBE})$ to \mathcal{A} .

- For a revocation query on *ID* and *T*, *B* proceeds as follows: It queries the revocation of *ID* and *T* to *C*. Next, it adds (*ID*, *T*) to *RL* if *ID* was not revoked before.
- For a base update key query on T_b , \mathcal{B} proceeds as follows: It receives UK_{DRIBE} from \mathcal{C} by querying an update key with T_b . It gives $BUK_{T_b} = UK_{DRIBE}$ to \mathcal{A} .
- For an incremental update key query on T, \mathcal{B} proceeds as follows: It generates IUK_T by using MK_{IBBE} . It gives IUK_T to \mathcal{A} .
- For a decryption key query on *ID* and *T*, \mathcal{B} proceeds as follows: It first receives DK_{DRIBE} from \mathcal{C} by querying a decryption key for *ID* and T_b . It derives DK_{HIBE} of SK_{HIBE} by using MK_{HIBE} . Next, it generates IUK_T by using MK_{IBBE} . It gives $DK_{ID,T} = (DK_{DRIBE}, DK_{HIBE}, IUK_T)$ to \mathcal{A} .

Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* where $T^* = T_b^* + T_c^*$. \mathcal{B} proceeds as follows:

- 1. It select random M_2, M_3 and sets $M_{1,0} = M_0^* \oplus M_2 \oplus M_3, M_{1,1} = M_1^* \oplus M_2 \oplus M_3$.
- 2. Next, it receives CT^*_{DRIBE} from C by submitting ID^* , T^*_b , and two challenge messages $M_{1,0}, M_{1,1}$. It obtains CT^*_{HIBE} by running **HIBE.Encrypt** $(ID^*, T^*, M_2, PP_{HIBE})$.
- 3. It obtains PV^* by running **CS.Assign** (v^*) where v^* is associated with ID^* . It sets $S = \emptyset$. For each $S_i \in PV^*$, it adds a string $H(\text{Label}(S_i) || T^*)$ to S. It creates CT^*_{IBBE} by running **IBBE.Encrypt** (S, M_3, PP_{IBBE}) .
- 4. It gives a challenge ciphertext $CT^* = (CT^*_{DRIBE}, CT^*_{HIBE}, CT^*_{IBBE})$ to \mathcal{A} .

Phase 2: Same as Phase 1.

Guess: Finally, \mathcal{A} outputs a guess $\mu' \in \{0, 1\}$. \mathcal{B} also outputs μ' .

To analyze the correctness of the simulation, we show that it is possible to process all DRIBE-INC queries of the adversary by using DRIBE queries. The private key and base update key queries are handled correctly using the private key and the update key of DRIBE, respectively. In the case of a type-B adversary, the decryption key query can be processed under the constraint that if the private key for ID^* is queried, then the corresponding ID^* is revoked before the time T_b^* . For reference, if you query the decryption key for ID^* and $T \ge T_b^*$, then the simulator simply outputs \bot as a decryption key since the decryption key for ID^* and $T \ge T_b^*$ does not exist when ID^* has already been revoked. The challenge ciphertext is set so that the DRIBE-INC challenge message is related to the DRIBE challenge message.

Lemma 4.4. For the type-C adversary, the DRIBE-INC scheme is IND-CPA secure if the IBBE scheme is IND-CPA secure.

Proof. Suppose there exists a type-C adversary A that attacks the DRIBE-INC scheme with a non-negligible advantage. An algorithm B that attacks the IBBE scheme is initially given public parameters PP_{IBBE} by a challenger C. Then B that interacts with A is described as follows:

Setup: \mathcal{B} obtains MSK_{DRIBE} , MUK_{DRIBE} , PP_{DRIBE} by running the **DRIBE.Setup** algorithm. It also obtains MK_{HIBE} , PP_{HIBE} by running **HIBE.Setup** algorithm. It initializes $RL = \emptyset$ and gives $PP = (PP_{DRIBE}, PP_{HIBE}, PP_{HIBE}, PP_{HIBE}, PP_{HIBE}, H, \mathcal{BT})$ to \mathcal{A} .

Phase 1: A adaptively requests a polynomial number of private key, revocation, base update key, incremental update key, and decryption key queries.

- For a private key query on *ID*, \mathcal{B} proceeds as follows: It generates SK_{DRIBE} by using MSK_{DRIBE} . Next, it generates SK_{HIBE} by using MK_{HIBE} . It gives $SK_{ID} = (SK_{DRIBE}, SK_{HIBE})$ to \mathcal{A} .
- For a revocation query on *ID* and *T*, \mathcal{B} proceeds as follows: It adds (*ID*,*T*) to *RL* if *ID* was not revoked before.
- For a base update key query on T_b , \mathcal{B} proceeds as follows: It generates UK_{DRIBE} for T_b by using MUK_{DRIBE} . It gives $BUK_{T_b} = UK_{DRIBE}$ to \mathcal{A} .
- For an incremental update key query on $T = T_b + T_c$, \mathcal{B} proceeds as follows:
 - 1. It initializes $IRV = \emptyset$. For each $(ID_i, T_i) \in RL$, it adds v_i of ID_i into IRV if $T_b < T_i \leq T$. It obtains ICV_T by running **CS.Cover**(\mathcal{BT}, IRV).
 - 2. For each $S_i \in ICV_T$, it receives SK_{IBBE,S_i} from C by querying a private key for $H(\text{Label}(S_i)||T)$.
 - 3. It creates $IUK_T = (ICV_T, \{SK_{IBBE,S_i}\}_{S_i \in ICV_T})$ and gives IUK_T to \mathcal{A} .
- For a decryption key query on *ID* and $T = T_b + T_c$, \mathcal{B} proceeds as follows: It generates DK_{DRIBE} by using MSK_{DRIBE} and MUK_{DRIBE} . Next, it retrieves IUK_T by querying an incremental update key to its own oracle. It generates a delegated key DK_{HIBE} of SK_{HIBE} by using MK_{HIBE} . It gives $DK_{ID,T} = (DK_{DRIBE}, DK_{HIBE}, IUK_T)$ to \mathcal{A} .

Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* where $T^* = T_b^* + T_c^*$. \mathcal{B} proceeds as follows:

- 1. It selects random M_1, M_2 and sets $M_{3,0} = M_0^* \oplus M_1 \oplus M_2, M_{3,1} = M_1^* \oplus M_1 \oplus M_2$.
- 2. Next, it generates CT^*_{DRIBE} by running **DRIBE.Encrypt** $(ID^*, T^*_b, M_1, PP_{DRIBE})$. It generates CT^*_{HIBE} by running **HIBE.Encrypt** $((ID^*, T^*), M_2, PP_{HIBE})$.
- 3. It obtains PV^* by running **CS.Assign**(\mathcal{BT}, v^*) where a leaf node v^* is associated with ID^* . It sets $S = \emptyset$. For each $S_i \in PV^*$, it adds $H(\text{Label}(S_i) || T^*)$ to S. It receives CT^*_{IBBE} from \mathcal{C} by submitting a challenge set S and challenge messages $M_{3,0}, M_{3,1}$.
- 4. It gives a challenge ciphertext $CT^* = (CT^*_{DRIBE}, CT^*_{HIBE}, CT^*_{IBBE})$ to \mathcal{A} .

Phase 2: Same as Phase 1.

Guess: Finally, \mathcal{A} outputs a guess $\mu' \in \{0, 1\}$. \mathcal{B} also outputs μ' .

To analyze the correctness of the simulation, we show that it is possible to process all DRIBE-INC queries of the adversary by using IBBE queries. From the restriction of a type-C adversary, we have that the challenge identity ID^* is revoked from an incremental update key at time T^* if the private key for ID^* is queried. The incremental update key at time T^* is composed of the IBBE private key corresponding to the cover nodes of a binary tree, and the ciphertext for ID^* and T^* is an IBBE ciphertext that uses the path nodes for ID^* as the receiver set. In this case, since the path nodes for ID^* are removed from the incremental update key at time T^* , the IBBE private key belonging to the recipient set is not created. Thus the incremental update key can be generated by using the IBBE private key queries. The IBBE decryption key query can also be generated since the incremental update key is correctly processed.

Theorem 4.5. The above DRIBE-INC scheme is IND-UKA secure if the HIBE scheme is IND-CPA secure.

Proof. Suppose there exists an adversary \mathcal{A} that attacks the DRIBE-INC scheme with a non-negligible advantage. An algorithm \mathcal{B} that attacks the HIBE scheme is initially given public parameters PP_{HIBE} by a challenger \mathcal{C} . Then \mathcal{B} that interacts with \mathcal{A} is described as follows:

Setup: \mathcal{B} generates $MSK_{DRIBE}, MUK_{DRIBE}, PP_{DRIBE}$ by running **DRIBE.Setup** algorithm. It also generates MK_{IBBE}, PP_{IBBE} by running the **IBBE.Setup** algorithm. It initializes $RL = \emptyset$ and gives $MUK = (MUK_{DRIBE}, MK_{IBBE}), PP = (PP_{DRIBE}, PP_{HIBE}, PP_{IBBE}, H, \mathcal{BT})$ to \mathcal{A} .

Phase 1: A adaptively requests a polynomial number of private key, revocation, and decryption key queries.

- For a private key query on *ID*, \mathcal{B} proceeds as follows: It generates SK_{DRIBE} by using MSK_{DRIBE} . It receives SK_{HIBE} from \mathcal{C} by querying a private key for *ID*. It gives $SK_{ID} = (SK_{DRIBE}, SK_{HIBE})$ to \mathcal{A} .
- For a revocation query on *ID* and *T*, \mathcal{B} updates *RL* by running **DRIBE.Revoke**(*ID*, *T*, *RL*).
- For a decryption key query on *ID* and *T*, \mathcal{B} proceeds as follows: It receives DK_{HIBE} from \mathcal{C} by querying a private key for *ID* and *T*. It generates IUK_T by using MK_{IBBE} . It gives $DK_{ID,T} = (DK_{DRIBE}, DK_{HIBE}, IUK_T)$ to \mathcal{A} .

Challenge: \mathcal{A} submits a challenge identity ID^* , challenge time T^* , and two challenge messages M_0^*, M_1^* where $T^* = T_b^* + T_c^*$. \mathcal{B} proceeds as follows:

- 1. It first select random $M_1, M_3 \in \mathcal{M}$ and sets $M_{2,0} = M_0^* \oplus M_1 \oplus M_3, M_{2,1} = M_1^* \oplus M_1 \oplus M_3$.
- 2. Next, it generates CT^*_{DRIBE} by running **DRIBE.Encrypt** $(ID^*, T^*_b, M_1, PP_{DRIBE})$. It receives CT^*_{HIBE} from C by submitting challenge ID^* , T^* , and challenge $M_{2,0}, M_{2,1}$.
- 3. It obtains PV^* by running **CS.Assign**(\mathcal{BT}, v^*) where a leaf node v^* is associated with ID^* . It sets $S = \emptyset$. For each $S_i \in PV^*$, it adds $H(\text{Label}(S_i) || T^*)$ to S. It generates CT^*_{IBBE} by running **DRIBE.Encrypt**(S, M_3, PP_{IBBE}).

4. It gives a challenge ciphertext $CT^* = (CT^*_{DRIBE}, CT^*_{HIBE}, CT^*_{IBBE})$ to \mathcal{A} .

Phase 2: Same as Phase 1.

Guess: Finally, \mathcal{A} outputs a guess $\mu' \in \{0, 1\}$. \mathcal{B} also outputs μ' .

4.5 Discussions

Efficiency Analysis. The private key of our DRIBE-INC scheme is compact because it is composed of a DRIBE private key which is an HIBE private key and an additional HIBE private key. The ciphertext is also compact because it consists of a DRIBE ciphertext, an HIBE ciphertext, and an IBBE ciphertext. The base update key consists of a DRIBE update key and an incremental update key consists of many IBBE private keys. For concrete analysis of the update key size, the number of revoked users *r* in the base update key and the number of revoked users *s* in the incremental update key must be determined. We set the maximum number of users in the system to 2^{30} , the security parameter to 80 bits, and the hash length to 160 bits. For comparison, consider a scenario in which an RIBE scheme issues a daily update key. In this case, we compare the update key size of the RIBE scheme and the DRIBE-INC scheme. The update key of the RIBE scheme which is generated every day consists of $r \log 2^{30} = 30r$ binary tree nodes. The base update key of the DRIBE-INC scheme which is generated once a month consists of $r \log 2^{160} = 160r$ binary tree nodes. The

Scheme	PP Size	SK Size	UK Size	CT Size	DKER, GC, UKD
BF [6]	<i>O</i> (1)	<i>O</i> (1)	O(N-r)	<i>O</i> (1)	Yes, Yes, No
BGK [3]	O(1)	$O(\log N)$	$O(r\log \frac{N}{r})$	O(1)	No, No, No
LV [23]	$O(\lambda)$	$O(\log N)$	$O(r\log \frac{N}{r})$	O(1)	No, No, No
SE [30]	$O(\lambda)$	$O(\log N)$	$O(r\log \frac{N}{r})$	O(1)	Yes, No, No
LLP [20]	O(1)	$O(\log^2 N)$	O(r)	O(1)	Yes, No, No
WES [33]	O(1)	$O(\log N)$	$O(r\log \frac{N}{r})$	O(1)	Yes, No, No
ML1 [24]	O(1)	O(1)	O(rn)	O(n)	Yes, Yes, No
ML2 [24]	O(n)	O(1)	$O(rn^2)$	O(1)	Yes, Yes, No
Lee [18]	O(1)	O(1)	O(r)	$O(n^2)$	Yes, Yes, No
DRIBE	O(n)	<i>O</i> (1)	O(rn)	<i>O</i> (1)	Yes, Yes, Yes
DRIBE-INC	O(n)	O(1)	$O(\frac{rn}{m}+sn)$	O(1)	Yes, Yes, Yes

Table 1: Comparison of RIBE schemes in bilinear groups

Let N be the number of maximum users, r be the number of revoked users, n be the depth of a binary tree in generic constructions, m be the interval of base update keys, and s be the number of revoked users in incremental update keys. We count the number of group elements to measure the size. We use symbols DKER for decryption key exposure resistance, GC for generic construction, and UKD for update key delegation.

incremental update key of the DRIBE-INC scheme is $s \log 2^{160} = 160s = 160(r/10) = 16r$ binary tree nodes if we simply set s = r/10. Therefore, the amortized size of the update key of the DRIBE-INC scheme is 160r/30 + 16r = 21.3r binary tree nodes, and it is similar to that of the RIBE scheme.

5 Instantiations

In this section, we instantiate our DRIBE schemes by using bilinear groups or lattices.

5.1 DRIBE from Bilinear Maps

We instantiate our DRIBE scheme using pairing-based encryption schemes. First, we consider realizing a DRIBE scheme that provides the full-model security. For this, we select the HIBE scheme of Waters [34] that provides full-model security under the standard assumption. We select the IBBE scheme of Gentry and Waters [15] which has a constant-size ciphertext and a short private key because it provides the full-model security in the random oracle model. For a cryptographic hash function, we select the SHA256 scheme and truncate the hash output if necessary. Next, we consider realizing a DRIBE scheme that provides the selective security. We select the efficient HIBE scheme of Boneh and Boyen [4] which provides the selective security under the standard assumption. Alternatively, if we want to reduce the ciphertext size, we can select the HIBE scheme of Boneh et al. [5] with constant size ciphertext. We also select the SHA256 scheme of Delerablee [12] which has a constant size ciphertext and a short private key. We also select the SHA256 scheme as a hash function.

5.2 DRIBE from Lattices

We instantiate our DRIBE scheme using lattice-based encryption schemes. For a lattice HIBE scheme, we select the efficient HIBE scheme of Agrawal et al. [1] that provides the selective security under the LWE assumption. For a lattice IBBE scheme, we try to use the IBBE scheme of Brakerski and Vaikuntanathan [7] which is derived from their ciphertext-policy attribute-based encryption scheme. One drawback of this IBBE scheme is that it lacks the formal security analysis. Another alternative for the IBBE scheme is to use the fixed-dimension HIBE scheme of Agrawal et al. [2] with short ciphertexts to replace the IBBE scheme. In this case, the IBBE encryption is replaced by the HIBE encryption on the path string of a leaf node, and the IBBE key generation is replaced by the HIBE key generation for cover nodes in a binary tree. The IBBE decryption is possible by using the private key delegation of the HIBE scheme. Finally, we select the SHA256 scheme and truncate the hash output if necessary.

6 Conclusion

In this paper, we introduced the concept of DRIBE that delegates the generation of update keys to a semitrusted cloud server, and proposed an efficient DRIBE scheme by generically combining an HIBE scheme, an IBBE scheme, and a hash function. Our proposed DRIBE scheme satisfies not only the IND-CPA but also the IND-UKA security. In addition, we proposed an DRIBE-INC scheme that supports incremental update keys to reduce the update key size of our DRIBE scheme. Our DRIBE-INC scheme has the effect of reducing the overall update key size by issuing a large-sized base update key occasionally and a small-sized incremental update key periodically.

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