Subversion-Resilient Public Key Encryption with Practical Watchdogs

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Abstract. Restoring the security of maliciously implemented cryptosystems has been widely considered challenging since the subverted implementation could arbitrarily deviate from the official specification. Achieving security against adversaries that can arbitrarily subvert implementations seems to require trusted component assumptions and/or architectural properties inherently. At ASIACRYPT 2016, Russell *et al.* proposed an attractive model where a watchdog is used to test and approve individual components of an implementation before or during deployment. Such a detection-based strategy has helped design various cryptographic schemes that are provably resilient to subversion.

We consider Russell *et al.*'s watchdog model from a practical perspective regarding watchdog efficiency. We find that the asymptotic definitional framework while permitting strong positive theoretical results, does not yet guarantee practical watchdogs because the running time of a watchdog is only bounded by an abstract polynomial. Hence, in the worst case, the watchdog's running time might exceed the adversary's running time, which seems impractical for most applications. We adopt Russell *et al.*'s watchdog model to the concrete security setting and design the first subversion-resilient public-key encryption scheme, allowing for highly efficient watchdogs with only *linear* running time.

At the core of our construction is a new variant of a combiner for key encapsulation mechanisms (KEMs) by Giacon *et al.* (PKC'18). We combine this construction with a new subversion-resilient randomness generator that can also be checked by an efficient watchdog, even in *constant* time, which could be of independent interest for designing other subversion-resilient cryptographic schemes. Our work thus shows how to apply Russell *et al.*'s watchdog model to design subversion-resilient cryptography with efficient watchdogs. We insist that this work does not intend to show that the watchdog model outperforms other defense approaches but to demonstrate that practical watchdogs are achievable.

The first author was supported by the research training group "Human Centered Systems Security" (NERD.NRW) sponsored by the state of North-Rhine Westphalia. The third author was supported by the National Natural Science Foundation of China (Grant No.62122092, No. 62032005). The fourth author was supported by the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme, grant agreement 802823.

This is the full version of a work published at PKC21. We identify a subtle flaw in the proof of the previous version and show it is impossible to achieve CPA security under subversion with the proposed approach. However, the same construction can achieve one-way security under subversion.

Keywords: Subversion-Resilience · Watchdog · Randomness Generator · Public Key Encryption.

1 Introduction

It has been of increasing concern that the robustness of security guarantees provided by cryptographic tools in practice may be weaker than thought. In particular, cryptosystems in the real world could be stealthily weakened by attackers who have the capability of tampering with the actual algorithm implementation for exfiltrating secret information while keeping it indistinguishable—in black-box testing—from a truthful one. Such a powerful adversary was originally considered in the *kleptographic* setting by Young and Yung [33, 34] over two decades ago, while the striking Snowden revelations (in 2013) of massive surveillance of encrypted communication attracted renewed attention worldwide. News reports [16] have recently confirmed that a spying agency subverted a widely-used implementation of the Dual EC pseudorandom number generator, which was then also exploited by another government. This provides a concrete real-world example showing the demand for subversion-resilient cryptosystems.

Recent research showed that such impactful subversion attacks could be mounted on a large class of cryptographic primitives, including encryption schemes [6, 5, 17, 13], digital signatures [2] and non-interactive zero-knowledge proofs [3, 22]. More generally, Berndt and Liśkiewicz [9] proved that there exist universal algorithm substitution attacks on any cryptographic algorithm with sufficiently large min-entropy. These negative results, in turn, significantly increased the awareness of the research community. Consequently, extensive efforts have been made towards effective approaches to subversion-resilient cryptography.

Since subversion attacks consider a much stronger adversary than many classical security models, it turns out that further reasonable assumptions are generally needed, since otherwise there is not much hope to achieve meaningful security guarantees [6, 5, 2, 4, 17, 29–31, 15, 1, 27, 14, 19, 21]. All the different assumptions considered in these works, be they trusted components [27, 2, 14, 19, 12] or architectural requirements [29–31, 15], have their own plausibility, and thus are generally incomparable, as they rely on different assumptions and may be useful in different application contexts. Nevertheless, it is still widely considered meaningful to weaken the specific assumptions adopted within each model for more practical and/or broadly realizable subversion-resilience. As we will explain below, this is the main motivation of our work.

Subversion-resilience in the watchdog model. In this work, we consider the watchdog model introduced by Russell *et al.* [29] at ASIACRYPT 2016. This model has been useful to design a broad class of cryptographic tools secure against subversion attacks. The watchdog model is based on an architectural assumption, namely the *split-program methodology*, where an algorithm is decomposed into several functional components. The adversary supplies implementations of all components to a so-called "watchdog", which performs a black-box test to decide whether the (possibly subverted) implementation of each component is sufficiently compliant with the specification to provide the expected security properties. A cryptographic scheme is said to be subversion-resilient, if *either* there exists a watchdog that can detect the subversion of components with *non-negligible* probability; *or* the security of the cryptographic scheme is preserved even if the subverted implementation is used. It is shown that, under the aforementioned architectural assumption, such a watchdog-based approach is able to resist even complete subversion, where all algorithms are implemented by the adversary, including the key generation algorithm. Concretely, it is possible to construct various subversion-resilient primitives, including one-way-permutations [29], pseudorandom generators [29], randomness generators [30], semantically secure encryption schemes [30], random oracles [31], and signature schemes [15].

Weaker watchdogs imply stronger security. Generally, the stronger a watchdog is, the better it can prevent subversion attacks. As an extreme example, imagine a "super" watchdog with unlimited running time, which would be able to exhaustively test whether a given cryptographic algorithm perfectly meets the specification on all possible inputs, even if the input space is exponential (such as the randomness space of a key generation algorithm, or the message and randomness space of an encryption algorithm, for instance). Such a watchdog would be able to detect and reject any subverted implementation that deviates from the specification, and thus trivially imply security in the subversion setting, since no subversion is permitted. However, such an ideal watchdog is too strong to be efficiently constructable in practice.

Russell et al. [29] considered various notions of watchdogs:

- An offline watchdog performs a one-time check of the supplied implementations prior to deployment;
- An *online watchdog* is executed in parallel to the deployment of the scheme, and able to access the full transcript of cryptographic protocols by monitoring public interactions between users;
- An *omniscient watchdog* is in addition also aware of the entire internal state (*e.g.*, secret keys) of the implementation.

Note that among all of the above, the offline watchdog is the weakest and thus the most desirable that one might want to use for achieving subversion resilience in the watchdog model. In particular, recent efforts have been made to construct subversion-resistant primitives in the offline watchdog model, including encryption schemes [30] and signature schemes [15]. We emphasize that an offline watchdog can not defend against *stateful* subversions, which are out of scope of this work (for more explanations see Section 3).

Our motivation: Subversion-resilience with efficient watchdogs. The offline watchdog is particularly attractive from a practical perspective, as only a "one-time" check is required. However, it turns out that such a one-time check can require very extensive testing in order to achieve some desirable security guarantee in practice. Concretely, the current approach [29] considers a watchdog already successful if it has a *non-negligible* probability of detecting a malicious subversion. To obtain some *concrete* acceptable detection probability, this could require the offline watchdog to do a *polynomial* amount of testing, where in the worst case the running time of the watchdog might even have to exceed the running time of the adversary, which seems not very practical. As pointed out by Russell *et al.* in [30], amplifying a non-negligible detection probability ϵ to an overwhelming detection probability $1 - \delta$ would require $\epsilon^{-1} \log(\delta^{-1})$ repetitions of testing. Also, due to the asymptotic definition, it is unclear how long the watchdog would need to be run *concretely* in practice before it could state with high confidence whether a given component is considered sufficiently secure or not.

In the theory of self-testing/correcting programs by Blum, Luby and Rubinfeld [10], limited testing by the tester/corrector is also considered a central design goal. Therefore we are interested in constructing subversion-resilient cryptosystems in the watchdog model, such that we can construct extremely efficient watchdog algorithms, that are guaranteed to run significantly faster than an adversary, ideally in *linear* or even in *constant* time. We believe that this is a necessary step towards making Russell *et al.*'s [29] watchdog model applicable in real-world applications. In particular, we are interested in techniques to construct cryptographic schemes that allow for watchdogs with a concretely-bounded running time that only need to perform a very limited number of tests in order to achieve strong security guarantees.

Remark. We stress that we do not intend to show that the watchdog model outperforms other approaches in defending against subversion attacks, but mainly aim at exploring the possibility of achieving security against subversion attacks in this model using watchdogs with minimal running time. In fact, as mentioned above, all the existing models are generally incomparable, due to the adoption of different specific approaches and assumptions.

1.1 Our Results

Motivated by the aforementioned practical concerns, in this work, we design the first random number generator and public key encryption scheme with offline watchdogs that perform only limited testing, but still achieve strong standard security guarantees. In particular, we make the following contributions.

- The main theoretical contribution of our work is a parameterized refinement of Russell *et al.*'s watchdog model. More precisely, we present a generic model to capture the goal of subversion-resilience with a universal offline watchdog and trusted amalgamation for any cryptographic primitive. The model is defined with concrete security parameters so that specific bounds on the runtime of the watchdog are explicitly given. This requires a conceptual modification of the joint security experiment involving the watchdog and the adversary.
- As the first contribution, we then construct an extremely simple randomness generator that is guaranteed to output *uniformly* random bits, even if the watchdog only tests the underlying component for a *constant* time. Note that this randomness generator could also be used to design other subversion-resilient cryptographic schemes with runtime-constrained watchdogs.
- Based on this randomness generator as well as an additional trusted XOR operation⁴, we design a subversion-resilient one-way key encapsulation mechanism

⁴ Such a trusted operation is also required in the PKE construction by Russell *et al.*. in [30]

(KEM) using watchdogs running in *linear* time. This KEM then implies a subversionresilient one-way public key encryption scheme that has a watchdog with practical running time. The size of public keys and ciphertexts of this scheme are linear in the security parameter.

Difference to conference version. This is the full version of [8], where we considered CPA security of our proposed schemes. In this work, we identify a subtle flaw in the presented proof. Technically speaking, it was claimed that the simulation of Game 2 in the reduction was perfect, while the adversary can actually distinguish the simulation with non-negligible probability. We formalize this problem and argue that it seems impossible that the approach presented in [8] can be used to achieve CPA security under subversion. On the positive side, we will see that the underlying intuition (and even the same construction, together with most of the proof) still allows for positive results if one-way security is considered instead of CPA security. Note that while the security of the randomness generator based on the von Neumann extractor also uses an indistinguishability experiment, the security proof does not suffer from a similar problem as the KEM construction. This is because there we utilize an independent *information-theoretical* argument.

Below we elaborate on the proposed techniques in more detail.

1.2 Technical Overview

At the core of our proposed PKE scheme is a subversion-resilient KEM using offline watchdogs doing constant-time testing. As mentioned above, such a construction is challenging as we now only rely on watchdogs that do less testing. Below we first present the intuition why this is a non-trivial task and then the idea behind our construction.

The difficulty of recognizing a subverted KEM with a watchdog. Let KEM = (Gen, Encaps, Decaps) be the specification of a legitimate (*i.e.*, not subverted) KEM. Let R_{gen} , R_{enc} be the randomness spaces of Gen and Encaps. Let F be the deterministic function parameterized by a KEM which takes as input randomness $(r, s) \in R_{gen} \times R_{enc}$ for Gen and Encaps, respectively, and then computes

$$(pk, sk, C, K) = F_{\mathsf{KEM}}(r, s)$$

with

$$(pk, sk) \leftarrow \mathsf{Gen}(; r) \ , \ (C, K) \leftarrow \mathsf{Encaps}(pk; s).$$

Now let $\widetilde{KEM} = (\widetilde{Gen}, \widetilde{Encaps}, \widetilde{Decaps})$ be a (possibly subverted) implementation of the algorithms of KEM. We observe that if

$$F_{\mathsf{KEM}}(r,s) = F_{\widetilde{\mathsf{KEM}}}(r,s) \tag{1}$$

on all $(r, s) \in R_{gen} \times R_{enc}$, then the security of the originally specified scheme KEM implies security of KEM, if (r, s) are indeed chosen randomly. If Equation (1) holds, then the implementations Gen and Encaps agree with the specification on all inputs,

and these are the only algorithms of KEM used in the security experiment. The same holds if Equation (1) holds for all but a *negligible* fraction of all r, s, since the probability that a security experiment chose (r, s) such that Equation (1) does *not* hold would be negligible.

Unfortunately, we are not able to test efficiently whether Equation (1) holds for all but a negligible fraction of all r, s. Let

$$\mathsf{Neq} := \left\{ (r, s) : F_{\mathsf{KEM}}(r, s) \neq F_{\widetilde{\mathsf{KEM}}}(r, s) \right\}$$
(2)

and

$$\mathsf{Eq} := \left\{ (r, s) : F_{\mathsf{KEM}}(r, s) = F_{\widetilde{\mathsf{KEM}}}(r, s) \right\}.$$
(3)

That is, Neq contains all "bad" randomness values such that Equation (1) does *not* hold with respect to (KEM, $\widetilde{\text{KEM}}$). Analogously, Eq contains all "good" randomness values for which Equation (1) does hold. Since Neq and Eq are disjoint sets, we have

$$\mathsf{Neq} \cup \mathsf{Eq} = R_{\mathsf{gen}} imes R_{\mathsf{enc}}$$
 and $\mathsf{Neq} \cap \mathsf{Eq} = \emptyset$

Note that testing whether $|Neq|/2^{\lambda}$ is negligible by repeatedly running F on different inputs takes exponential time. Even if we granted the watchdog a very large running time, by allowing it to evaluate F a polynomial $P(\lambda)$ of times, where $P(\lambda)$ is large, this watchdog could still fail to recognize that |Neq| is non-negligible with very high probability.

For instance, suppose that Neq $\subset R_{gen} \times R_{enc}$ were a random subset of size $|Neq| = |R_{gen} \times R_{enc}|/P^2(\lambda)$. Then a watchdog running in time P would detect the subversion only with probability at most $1/P(\lambda)$ which results from applying the union bound and using that sampling from Neq occurs with probability $1/P^2(\lambda)$ when sampling once. At the same time, the scheme would be insecure, since we have

$$\frac{R_{\text{gen}} \times R_{\text{enc}}|/P^2(\lambda)}{|R_{\text{gen}} \times R_{\text{enc}}|} = \frac{1}{P^2(\lambda)}$$

and thus the security experiment would choose "bad" randomness $(r, s) \in Neq$ with significant probability $\frac{1}{P^2(\lambda)}$.

Our approach to overcoming the technical difficulties. We build a subversion-resilient one-way KEM KEMSR = (GenSR, EncapsSR, DecapsSR) based on a regular KEM = (Gen, Encaps, Decaps) in the following way. For ease of exposition, we describe a less efficient scheme here. Our actual scheme can be instantiated much more efficiently, by trading the size of keys and ciphertexts for reasonably increased running time of the watchdog. For more details, see Section 5.3.

A key pair $(pk,sk)=((pk_i)_{i\in[\lambda]},(sk_i)_{i\in[\lambda]})$ of KEMSR consists of λ many public keys

$$(pk_1, sk_1), \ldots, (pk_{\lambda}, sk_{\lambda}) \stackrel{s}{\leftarrow} \mathsf{Gen}()$$

of KEM. In order to generate an encapsulated key, we run $(C_i, K_i) \leftarrow \mathsf{Encaps}(pk_i)$ for all $i \in [\lambda]$, and return

$$(C,K) := ((C_1,\ldots,C_\lambda), K_1 \oplus \cdots \oplus K_\lambda).$$

Here the \oplus is part of the trusted amalgamation function.

The security proof against subversion in the watchdog model of this construction is based on the following idea. Let $\widetilde{\text{KEM}}$ be a subverted implementation of KEM ⁵ and let Neq be as in Equation (6). We construct a reduction to the security of the underlying KEM that goes through if the simulated security experiment generates *at least one* pair (pk_i, C_i) using "good" randomness, that is, choosing $(r, s) \stackrel{\$}{\leftarrow} R_{\text{gen}} \times R_{\text{enc}}$ such that $(r, s) \in \text{Eq}$.

Note that even if the underlying KEM is heavily subverted, for instance such that half of all randomness tuples (r, s) are "bad" and we have

$$|\mathsf{Neq}| = \frac{|R_{\mathsf{gen}} \times R_{\mathsf{enc}}|}{2} \tag{4}$$

we would still have

$$\Pr\left[(r,s) \notin \mathsf{Neq}: (r,s) \stackrel{\hspace{0.1em}\mathsf{\scriptscriptstyle\$}}{\leftarrow} R_{\mathsf{gen}} \times R_{\mathsf{enc}}\right] = 1/2.$$

Therefore, the probability that the experiment generates at least one pair (pk_i, C_i) using "good" randomness is $1 - 2^{\lambda}$, which is almost certain, up to a negligibly small probability.

If the adversary produces a subverted implementation where |Neq| is larger than in Equation (4), then of course it becomes less likely that the experiment chooses "good" randomness. However, already for |Neq| as in Equation (4) we are able to detect the subversion almost certainly, and with a very efficient watchdog. Concretely, a watchdog running $F \lambda$ times and comparing the output to the specification is able to detect the subversion with overwhelming probability $1-2^{-\lambda}$. This detection probability increases with larger |Neq|.

In order to ease the notation and make our approach clear, the above sketch of our construction uses λ many executions of the KEM procedures as well as a watchdog which tests each algorithm λ many times. As we will see later, in our construction these parameters can be adjusted to allow for tradeoffs between ciphertext (and key) size and runtime of the watchdog.

On the KEM combiner. Note that a similar idea of using a KEM combiner was also used by Giacon *et al.* [23]. However, the work by Giacon *et al.* considers a different setting from our work. In their work, it is assumed that there are different KEMs with different security properties, in a situation where it is unclear which one is the most suitable candidate for establishing security (*e.g.*, since they are based on different hardness assumptions). Instead, we primarily address the problem of using a possibly subverted KEM to realize secure key encapsulation. Our main approach is to use the watchdog doing limited testing to ensure that the subverted KEM is consistent with its official specification at some points, based on which we are able to have desirable security guarantee via amplification.

One may wonder whether we could use combiners for public key encryption directly to obtain a subversion-resilient PKE scheme. The answer is negative. From a

⁵ In our model the adversary provides an implementation of each building block instead of an implementation of KEMSR.

syntax level, most of the currently known combiners would be considered as part of the trusted amalgamation in our model. However, since we consider a runtime-constrained watchdog, we can not rule out the possibility that the PKE scheme would, for instance, simply output the message instead of a ciphertext for a specified message m. Such an attack is known as an "input trigger attack" [17] and prevents us from directly using most of the existing combiners/amplifiers in our setting.

Russell *et al.* [30] argued that subverted encryption algorithms can not have direct access to the input message in order to rule out input trigger attacks. Thus, they blind the message with a random coin which is output as part of the ciphertext. We remark that this approach does not work in our setting, since this still requires polynomial time testing by the watchdog in order to obtain an overwhelming detection probability. In our construction, we bypass this type of attacks by directly performing the XOR operation on the message with the output key of our designed subversion-resilient KEM.

Limitations of our approach. Note that while our construction allows for watchdogs with limited runtime, it comes with some limitations. Following Russel *et al.* [30], we proved our results under the assumption that trusted amalgamation is feasible. This means that all components of a cryptographic scheme can be split into multiple smaller parts, which can be tested individually by the watchdog. During the security experiment the amalgamation then assembles the building blocks without adversarial interference. Further, in our model we only account for *stateless* subversions, as we only rely on offline watchdogs with bounded runtime. If *stateful* subversions are allowed, a subverted algorithm could behave honestly until the watchdogs stop testing and then arbitrarily break security. For further discussion on alternative models, we refer to the following section. Furthermore, note that our proposed PKE scheme uses the key produced by our constructed subversion-resilient KEM to (in a trusted manner) XOR the message, thus limiting the message length to be encrypted. Last but not least, our work considers the weaker notion of one-way security, in contrast to previous works who consider CPA-security.

2 Related Work

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Since the Snowden revelations in 2013, extensive efforts have explored the feasibility results in the subversion setting, relying on different assumptions regarding trusted components and architectural requirements [6, 5, 2, 4, 17, 29–31, 15, 1, 27, 14, 19, 21].

2.1 Existing Constructions in the Watchdog Model

There have been various constructions in the typical watchdog model by [29]. Based on the split-program methodology [29], several cryptographic schemes were proposed and proved to be subversion-resilient in the complete subversion setting [29–31, 15]. Particularly, in [29], Russell *et al.* constructed subversion-resilient (trapdoor) one way permutations (TDOWP) in the offline watchdog model (assuming fixed public input distributions). The main idea is to use a standard hash function (modeled as a random oracle) to disable the ability of an adversary to embed any potential backdoors in the function. Further, based on this general sanitizing strategy, they built a subversion-resilient

signature scheme with online watchdogs, and subversion-resilient pseudorandom generators (PRG) with offline watchdogs. To generically eliminate subliminal channels in randomized algorithms, Russell *et al.* [30] proposed a "double-splitting" strategy where the randomness generation is carried out by mixing the output of two independent components with an immunization function. Based on this they showed how to further immunize each algorithm of an encryption scheme, including symmetric-key encryption and public-key encryption, with offline watchdogs. In [13], Chen *et al.* also discussed how to construct subversion-resilient key encapsulation mechanisms by using this useful strategy. Russell *et al.* also considered how to correct subverted random oracles in [31] and Chow *et al.* [15] further extended their results to construct subversion-resilient signature schemes in the offline watchdog model. In [1], by relying on an additional independent (untamperable) source of public randomness, Ateniese *et al.* proposed a subversion-secure immunizer in the plain model for a broad class of deterministic primitives. Based on the von Neumann extractor presented in this work, Bemmann *et al.* [7] presented a subversion-resilient authenticated symmetric encryption scheme.

There are some other constructions which also implicitly rely on the (polynomialtesting) watchdog to achieve subversion-resilience. In [6], Bellare, Patterson and Rogaway showed that symmetric encryption producing unique ciphertexts could resist subversion attacks, assuming that all subverted ciphertext are decryptable. This decryptability condition was further relaxed by [17] for considering the possibility of inputtrigger attacks. Note that both of them require an omniscient watchdog that needs to access the decryption key for verifying the ciphertext decryptability produced by the supplied implementation of encryption algorithm. Similarly, Ateniese, Magri and Venturi [2] showed that unique signatures are subversion-resilient on the condition that all subverted signatures are valid. They also proved the unforgeability of unique signatures still hold against random message attacks when the verifiability condition is relaxed in a way similar to what considered by [17]. Note that their constructions require an online watchdog as the signature scheme is publicly verifiable.

2.2 Combiner and Amplification

As mentioned earlier, Giacon *et al.* [23] also proposed the XOR combiner for KEMs but in a different setting from ours. Roughly, a combiner is an algorithm that takes as input several instantiations of the same primitive and then combines these into a single scheme, aiming at achieving desirable security on the condition that at least one of the underlying "building blocks" is secure. There have been several works constructing combiners for different primitives such as KEMs [23], authenticated encryption with associated data (AEAD) [28] and functional encryption [26].

The watchdog model generally relies on trusted amplification to build fully functional implementation from individual "secure enough" components for strong security. In fact, amplification is strongly related to cryptographic combiners. Roughly speaking, given a cryptographic scheme with some "weak" security guarantee, the amplifier can construct a scheme with stronger security guarantees (for example simply by repeated executions). Amplification has been applied to different primitives like functional encryption [25], interactive cryptographic protocols [18] and CCA-secure public key encryption [24].

2.3 Cryptographic Reverse Firewalls

Note that the watchdog model essentially relies on testing, combined with the splitprogram methodology, to achieve feasibility results in the subversion setting. Alternatively, one may consider other models relying on different assumptions, such as trusted components. In particular, Mironov and Stephens-Davidowitz [27] introduced the notion of *cryptographic reverse firewalls*, which permits quite extensive results [2, 19, 14, 11, 12]. A reverse firewall is an independent trusted on-line party, which could be viewed as a proxy located between a (potentially) subverted machine and the outside world. It is assumed that the reverse firewall has access to a source of trusted randomness and could faithfully re-randomize all incoming/outgoing communication generated by the subverted algorithm, so that subversion-resilience is achieved even if the full implementation has been tampered with by the adversary. It is worth mentioning that the reverse firewall is not assumed to be a trusted party to achieve security in absence of subversion. In particular, it has no access to any secret information, such as secret keys. Note that similar to the online watchdog model, an (active) reverse firewall is able to defend against stateful subversion, which is inherently not captured by the offline watchdog model. Furthermore, many constructions using the reverse firewall model, such as [27, 2, 19, 14, 12], require some form of "re-randomizability" of the algorithm outputs provided to an adversary, which limits their applicability to non-rerandomizable primitives. Two notable exceptions are due to Mironov and Stephens-Davidowitz [27], who proposed a generic approach to convert any protocol into a protocol that is compatible with reverse firewalls, and Bossuat et al. [11], where the reverse firewall is in possession of a public key which allows it to sanitize protocol messages without requiring rerandomizability of the underlying primitives.

2.4 Self-Guarding Mechanisms

Another alternative model is the so-called self-guarding mechanism, which was introduced by Fischlin and Mazaheri [21]. This model assumes that there exists an honest initialization phase where the algorithm is not subverted and thus produce a "clean" output. Thus, during this phase, one could gather a collection of samples by executing the honest implementation. After the implementation was tampered with, the output would be sanitized by the honest samples to resist any possible secret exfiltration. The main advantage of this model is that it does not require an active party (such as the reverse firewall or the watchdog) but rather constructs primitives that are "inherently" immune to subversion attacks. A limitation of this approach is the bounded security which depends on the number of samples collected during the good initial phase. Also, such a strategy only considers attacks that wake up at a later point in time, *e.g.*, due to the software update, while the watchdog model considers long-term subversion attacks that might be active during the whole life cycle of the cryptosystem.

3 A Definitional Framework for Subversion-Resilient Cryptography

In this section, we present a variant of the security definitions from [29] which is similar in spirit to theirs but captures our security goals for watchdogs with bounded running time better.

3.1 Notations

Before we present our model, we first introduce the notations used in this work. We will use $x \stackrel{\$}{\leftarrow} X$ to denote sampling x uniformly at random from the set X. Further, let \mathcal{A} be a randomized algorithm. In order to explicitly reference the random coins used by \mathcal{A} , we will use $y \leftarrow \mathcal{A}(x; r)$ to denote assigning y to the output of \mathcal{A} running on input x using the random coins r. [1, n] will denote the set of natural numbers from 1 to n, *i.e.* $\{1, 2, \ldots, n-1, n\}$. To denote an implementation (provided by some adversary) of some algorithm \mathcal{B} , we will use $\widetilde{\mathcal{B}}$. Finally, we will use $\widehat{\Pi}$ to denote the specification of a scheme.

3.2 A General Security Definition for Cryptographic Schemes

We define a *cryptographic scheme* Π as a tuple of *n* algorithms

$$\Pi = (\Pi_1, \ldots, \Pi_n).$$

Note that for a specific primitive, n is a fixed number and is usually small. For example, for a public-key encryption scheme, which is typically defined as a tuple of algorithms (Gen, Encrypt, Decrypt), we have n = 3 and

$$(\Pi_1, \Pi_2, \Pi_3) = (\mathsf{Gen}, \mathsf{Encrypt}, \mathsf{Decrypt}).$$

Security of Π is defined via a *security experiment* $\mathsf{Exp}_{\mathcal{A}}^{\Pi}$ which involves Π and an adversary \mathcal{A} and outputs a bit $b \in \{0, 1\}$. In the sequel, we will focus on security experiments based both on the *indistinguishability* of two distributions as well as so called *search problems*. Then we can generically define the *advantage function* of \mathcal{A} with respect to Π and experiment Exp and a value $\delta \in \{0, 1/2\}$ indicating whether a search or indistinguishability experiment is considered as

$$\operatorname{\mathsf{Adv}}_{\mathcal{A}}^{\Pi,\delta} := \left| \Pr \left[\operatorname{\mathsf{Exp}}_{\mathcal{A}}^{\Pi} = 1 \right] - \delta \right|.$$

In the concrete security setting, we say the scheme Π is (t, ϵ) -secure, if $\operatorname{Adv}_{\mathcal{A}}^{\Pi} \leq \epsilon$ for all \mathcal{A} running in time at most t. Note that in later chapters δ will be clear from context, and we thus take the liberty to drop it to ease notation.

3.3 Subversion-resilience with an Offline Watchdog

To define security against subversion attacks (adversarial implementations), we follow Russell *et al.*'s approach [29] and consider a setting where *the adversary itself* provides the implementation used in the security experiment of the considered scheme. More precisely, we consider an adversary \mathcal{A} that consists of two parts $(\mathcal{A}_0, \mathcal{A}_1)$, where \mathcal{A}_0 produces a (possibly subverted) *implementation* and a state *st*

$$(\widetilde{\Pi}_1,\ldots,\widetilde{\Pi}_n,st) \stackrel{\$}{\leftarrow} \mathcal{A}_0().$$

Then $\mathcal{A}_1(st)$ engages in the security experiment Exp, which uses $\widetilde{\mathcal{H}} = (\widetilde{\mathcal{H}}_1, \ldots, \widetilde{\mathcal{H}}_n)$. Note that in such a strong adversarial setting it is impossible to achieve meaningful security without further assumptions. Therefore, based on the fact that in the real world implementations of algorithms can be tested before deployment in an application, Russell *et al.* [29] introduced an additional party called the *watchdog*. The watchdog aims to detect a possible subversion in the implementation supplied by the adversary. The watchdog WD is aware of an "honest" (not subverted) *specification* of the scheme, denoted by

$$\Pi = (\Pi_1, \dots, \Pi_n),$$

and has oracle access to the implementation $\widetilde{\Pi} = (\widetilde{\Pi}_1, \ldots, \widetilde{\Pi}_n)$ produced by \mathcal{A}_0 . The adversary \mathcal{A} is only considered successful if it breaks the security of the scheme and the subverted implementation *evades detection* by the watchdog. Hence, we consider the *subversion-resilience* security experiment $\overline{\mathsf{SR}}_{\mathsf{Exp},\Pi}^{\mathcal{A},\mathsf{WD}}$ from Figure 1 (a), which involves a subversion adversary $\mathcal{A} = (\mathcal{A}_0, \mathcal{A}_1)$, a watchdog WD, a protocol specification $\widehat{\Pi}$ and an underlying experiment Exp .

At the beginning of the experiment, adversary \mathcal{A}_0 produces a (subverted) implementation $\widetilde{\Pi}$ and a state st. The watchdog is provided oracle access to $\widetilde{\Pi}$. If WD outputs true, which means that the watchdog has detected a subverted implementation, the experiment outputs either 0 or a random bit, depending on the value δ referring to search or indistinguishability experiments. This implies that \mathcal{A} has zero advantage, if it outputs an implementation that WD recognizes as subverted. If WD^{$\widetilde{\Pi}$} = false, then the security experiment Exp is executed, using the *adversarially-provided* implementation $\widetilde{\Pi}$ of $\widehat{\Pi}$ and with an adversary $\mathcal{A}_1(st)$ that may depend on the state produced by \mathcal{A}_0 .

In order to avoid trivial watchdogs that always output true, such that any scheme would be provably secure, we require that the watchdog is "correct" in the sense that it *always* outputs false when provided with oracle access to the actual protocol. Formally:

Definition 1. We say that WD is a correct watchdog for protocol specification $\widehat{\Pi}$, if

$$\Pr\left[\mathsf{WD}^{\widehat{\Pi}} = \mathtt{false}\right] = 1.$$

All watchdogs in this work will trivially fulfill this property. As one would intuitively expect, our watchdogs simply compare the output of the oracle with the expected results of the specification. Thus, our watchdogs will never reject the protocol specification.

Subversion-Resilient Public Key Encryption with Practical Watchdogs 13

$\overline{SR}^{\mathcal{A},WD}_{Exp,\delta,\widehat{\varPi}}$	$\underline{SR}^{\mathcal{A},WD}_{Exp,\delta,\widehat{\Pi}}$
$(\widetilde{\Pi}, st) \leftarrow \mathcal{A}_0()$	$(\widetilde{\Pi}, st) \leftarrow \mathcal{A}_0()$
If $WD^{\overline{H}}()$ then	If $WD^{\widetilde{H}}()$ then
Draw bit b with $\Pr[b=1] = \delta$	Draw bit b with $\Pr[b=1] = \delta$
Return b	Return b
Return $Exp_{\widetilde{\Pi}}^{\mathcal{A}_1(st)}$	Return $Exp_{Am(\widetilde{\Pi})}^{\mathcal{A}_1(st)}$
(a) Without trusted amalgamation and with $\widehat{\Pi} = (\Pi_1, \dots, \Pi_n)$	(b) With trusted amalgamation and $\widehat{\Pi} = (Am, \Pi_1, \dots, \Pi_n)$

Fig. 1: Security experiments with watchdog and subverted implementation.

Note that in the above security experiment (Figure 1), WD verifies \vec{H} prior to the experiment Exp. That is, our definition only considers offline watchdogs that simply check the supplied implementations by the adversary with no access to the full transcript of the experiment Exp. As discussed in [29, 30], such a watchdog is preferable over online watchdogs in the sense that it only carries out a one-time check on the implementation and does not require constant monitoring of all communication. We also remark that in this work we will only consider a *universal* watchdog, which means it is quantified before the adversary in the security definition. Thus, for a secure scheme there exists a *single* watchdog that defends against all considered adversaries.

Stateless Subversion. We also remark here that we only consider *stateless* subversion in this work. That is, the subverted implementation does not hold any state between different executions. Note that we are mainly interested in offline watchdogs which run in bounded time for testing. A trivial attack to evade such a detection is the so-called *time bomb* attack which only becomes active when the underlying algorithm is at some specific state. Specifically, the implementations would behave honestly when they are under testing by the offline watchdog, and at a later point in time the malicious behavior would be triggered to wake up. It is clear that such a tricky attack is impossible to be detected by our considered (*i.e.* bounded running time) watchdog. In fact, to prevent such an attack in hardware tokens, some previous work requires a semi-online watchdog to perform testing regularly [20]. Therefore, we insist that stateful subversion is not captured by our considered model. Another approach to consider stateful subversion are reverse firewalls, as discussed in Section 2.3.

3.4 The Split-Program Model and Trusted Amalgamation

The above offline watchdog model is meaningful and was used to establish security for some specific cryptographic primitives [29]. However, it turns out that it is still not generic enough to achieve subversion-resilience for many other primitives. Particularly, it is known that if the user makes only black-box use of the subverted implementation of randomized algorithms, it is hopeless to eliminate a steganographic channel built on the output of algorithms [30]. Therefore a non-black-box model is required for general feasibility results.

Motivated by the above, Russell *et al.* [30] proposed the *split-program model*, where the specification of each algorithm is split into a constant number of components. Precisely, a scheme Π is still represented by a tuple of algorithms (Π_1, \ldots, Π_n) , but nmay be larger than the actual number of algorithms of a protocol. The actual algorithms are then "amalgamated" by combining these underlying building blocks in a trusted way that cannot be influenced by the adversary. Using such a somewhat relaxed model, Russell *et al.* [30] showed how to generically design stego-free specifications for randomized algorithms which play a crucial role in constructing subversion-resilient encryption schemes (in their offline watchdog model). Basically, they further split the specification of any probabilistic algorithm into two parts: the randomized component and the deterministic component, that are tested individually by the watchdog. The randomized component generates random coins which (perhaps together with other inputs drawn from public distributions) are taken as input by the deterministic component to generate the output of the composed algorithm.

Note that for a meaningful construction of a subversion-resilient cryptosystem, the amalgamation should be *as-simple-as-possible*, such that most of the complexity of the involved algorithms is contained in the algorithms $\Pi = (\Pi_1, \ldots, \Pi_n)$ that may be subject to subversion. To make this approach more precise, we explicitly define an *amalgamation function* Am and include it in the specification of the scheme. For instance, for a public-key encryption scheme we would have the specification

$$\widehat{\Pi} = (\mathsf{Am}, \Pi) = (\mathsf{Am}, (\Pi_1, \dots, \Pi_n))$$

for which

$$\mathsf{Am}(\Pi_1,\ldots,\Pi_n) = (\mathsf{Gen},\mathsf{Encrypt},\mathsf{Decrypt})$$

holds.

As depicted in Figure 1 (b), the subversion-resilience security experiment with trusted amalgamation proceeds exactly as the basic experiment described above, except that the watchdog has access to all procedures

$$(\widetilde{\Pi}_1,\ldots,\widetilde{\Pi}_n,st) \stackrel{\hspace{0.1em}\hspace{0.1em}\hspace{0.1em}\hspace{0.1em}}{\leftarrow} \mathcal{A}_0()$$

produced by A_0 *individually*. The security experiment is then executed with the amalgamated primitive

$$\operatorname{Am}(\Pi_1,\ldots,\Pi_n).$$

Following our example for public key encryption, this would correspond to

$$\operatorname{Am}(\widetilde{\Pi}_1,\ldots,\widetilde{\Pi}_n) = (\widetilde{\operatorname{Gen}}, \widetilde{\operatorname{Encrypt}}, \widetilde{\operatorname{Decrypt}}).$$

With our security model set up, we can now define the advantage of a subversion adversary in the split program model with offline watchdog as

$$\mathsf{AdvSR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{Exp},\delta,\widehat{\Pi}} := \left| \Pr \left[\mathsf{SR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{Exp},\delta,\widehat{\Pi}} \right] - \delta \right|.$$

This allows to present our formal definition of subversion-resilience.

Definition 2. A specification of a cryptographic protocol $\widehat{\Pi} = (Am, \Pi)$ is $(t_{WD}, t_A, \varepsilon)$ -subversion-resilient in the offline watchdog model with trusted amalgamation, if one can efficiently construct a correct watchdog algorithm WD running in time at most t_{WD} such that for any adversary $\mathcal{A} = (\mathcal{A}_0, \mathcal{A}_1)$ running in time at most t_A it holds that

$$\mathsf{AdvSR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{Exp},\delta,\widehat{\Pi}} \leq \varepsilon$$

using the experiment shown in Figure 1 (b).

Here it might seem counterintuitive to define security with regards to the *speci*fication, if the underlying security experiment is executed with the subverted implementation. Our definition can be interpreted in the following way. While the security experiment is executed with the subverted implementation provided by the adversary, the watchdog (which is also executed in the experiment) tests the implementation with respect to that specification, and the adversary outputs subverted algorithms that syntactically follow the specification of the trusted amalgamation. Following Russell et al. [30], we split randomized algorithms into a probabilistic part (the randomness generation) and a deterministic part, where all parts can be tested individually. The trusted amalgamation then feeds the generated randomness into the deterministic algorithms. Since we are considering universal offline watchdogs, we have to make the assumption that a subverted implementation of a deterministic primitive also is deterministic. Otherwise, a subverted implementation could probabilistically deviate from the specification with some probability, where this probability could possibly be chosen depending on the watchdog and its bounded running time, so that the watchdog might fail to detect the subversion. (Note that is very closely connected to the reason why offline watchdogs (which do not depend on the adversary) cannot consider *stateful* subversion.)

3.5 Comparisons with Previous Watchdog Models

The security model presented in this section is a refinement of the security models from [30, 29]. We follow the "concrete security" approach instead of considering asymptotic definitions and assume the specification could be divided into an arbitrary number of components. Similarly to [30], we consider a single security experiment that can be separated in a "detection phase" and a "surveillance phase". Note that in [30] two advantage functions are defined: one for the watchdog and another for the adversary. Security then holds if either the detection advantage of the watchdog is non-negligible or the adversaries' advantage is negligible. We change the model in the regard that we enforce that the adversary "loses" the security experiment in case the watchdog detects subversion, by outputting a random bit instead of executing the experiment. In this way, we simplify the security definition by using a single advantage function.

Unfortunately, it seems that in this model it seems unlikely that CPA-security can be achieved, as we will show in Section 6. We remark that our refined model is slightly different from previous models [30, 29], as we distinguish between a "detection" game that involves a watchdog, and the actual security experiment involving a subverted implementation. Our choice for this model has mostly notational advantages for our goal of achieving subversion-resilience with efficient watchdogs.

$RGIND_{RG}^{\mathcal{A}}$	$SR^{\mathcal{A},WD}_{RGIND,\widehat{RGSR}}$
$b \stackrel{\$}{\leftarrow} \{0,1\}$	$(\widetilde{RGSR}, st) \leftarrow \mathcal{A}_0()$
return $\mathcal{A}^{\mathcal{O}}() == b$	If $WD^{\widehat{RGSR}}()$ then
If $b == 1$ then	$b \stackrel{s}{\leftarrow} \{0, 1\}$
$\mathbf{return} \ \mathcal{A}^{RG}() == b$	Return RGIND ^{$A_1(st)$}
(a) Experiment for a ran-	Am(RGSR)
domness generator RG.	(b) Subversion-resilience
Oracle \mathcal{O} returns uni-	experiment for random-
formly random strings.	ness generators.

Fig. 2: Security experiments with watchdog and subverted implementation.

4 Subversion-Resilient Randomness Generators

After presenting our security model we will now show how to generate randomness in a way that allows a watchdog to guarantee in *constant* time (also independent from an adversary's runtime), that the outputs of our construction are *uniformly random* (*i.e.*, not just indistinguishable from random, but truly random). This randomness generator will then later be used to generate the random coins for our subversion-resilient KEM and PKE scheme. Additionally, this construction is of independent interest as it is a general and efficient tool to provide uniformly random coins to any cryptographic primitives in our model.

A randomness generator is a randomized algorithm which on input of a security parameter outputs some strings. We consider a randomness generator secure if its outputs are indistinguishable from uniformly random strings.

Definition 3. We say that a randomness generator RG is (t, ε) -indistinguishable if for any adversary A running in time t it holds that

$$\mathsf{Adv}_{\mathcal{A}}^{\mathsf{RG}} = |\Pr[\mathsf{RGIND}_{\mathsf{RG}}^{\mathcal{A}} - 1/2]| \le \varepsilon$$

with $\operatorname{RGIND}_{\operatorname{RG}}^{\mathcal{A}}$ displayed in Figure 2 (a).

Following Definition 2, we say that a randomness generator is *subversion-resilient under trusted amalgamation* if the randomness generator produces outputs that are indistinguishable from random, even in a security experiment which uses a trusted amalgamation of a subverted implementation.

Definition 4. We say the specification of a randomness generator $RGSR = (Am_{RG}, RGSR)$ is $(t_{WD}, t_A, \varepsilon)$ -subversion-resilient in the offline watchdog model with trusted amalgamation, if one can efficiently construct a correct watchdog WD running in time at most t_{WD} , such that for any adversary $A = (A_0, A_1)$ running in time at most t_A it holds that:

$$\mathsf{AdvSR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{RGIND},\widehat{\mathsf{RGSR}}} \leq \varepsilon$$

with the used experiments shown in Figure 2 (a) and (b).

Known impossibilities. Russell *et al.* [30] showed that it is impossible to immunize a *single* randomness generator against subversion with an immunizing function. Essentially, they adopt the approach of subverting algorithms from [6, 5] to randomness generators, showing that one can easily introduce a bias into a single source via rejection sampling. This bias can then be maintained by a subverted immunizing function. This bias may furthermore be "hidden", in the sense that detecting it requires knowledge of a secret key only known to the adversary to compute some predicate, such that a watchdog would not be able to efficiently detect it, while a subverting adversary may easily distinguish the subverted RG from random.

In order to overcome this general impossibility, Russel *et al.* [30] introduce the "*double splitting*" approach. Here, two RNGs are run independently in parallel. The outputs of these two RNGs are then fed into an immunization function, which may also be subverted. Russel *et al.* showed that if the immunization function is modeled as a random oracle, then this yields a randomness generator whose output is indistinguishable from outputs of a non-subverted randomness generator, even for the subverting adversary. They provide a standard-model construction of a randomness generator that outputs a single bit and a watchdog which tests whether one bit appears significantly more often than the other. Using the Chernoff bound, they argue that the watchdog will notice a bias after gathering enough samples. The randomness generator would then be run n times independently to obtain a n bit output.

We describe a new construction, which applies the "two independent RNG" approach of [30] in a different way. Our construction is extremely simple and efficient to test, yet provides *perfect* random bits and does not require a random oracle.

4.1 Construction

The specification $\widehat{R}GSR = (Am, RG, VN)$ of our randomness generator consists of the following building blocks:

- A probabilistic algorithm RG that outputs a bit $RG() \in \{0, 1\}$.
- A simple binary and deterministic immunization function $VN : \{0, 1\} \times \{0, 1\} \rightarrow \{0, 1\}$, which is defined as follows:

$$\mathsf{VN}(b_0, b_1) := \begin{cases} 0 \text{ if } b_0 < b_1, \\ 1 \text{ if } b_0 > b_1, \\ \bot \text{ else.} \end{cases}$$

Note that this function is the classical von Neumann extractor [32].

The von Neumann extractor takes as input two bits with some (arbitrary and unknown but fixed) bias and outputs a uniformly random bit, as long as the two input bits are distinct from each other.

Using these two building blocks, we construct an algorithm outputs a single bit using trusted amalgamation. The amalgamation is essentially a very simple while-loop, given in Figure 3. It can be easily generalized to output n bits by calling it n times.

$$\frac{\operatorname{Am}_{\mathsf{RG}}(\mathsf{RG},\mathsf{VN})}{b_0 = b_1 := \bot}$$
While $b_0 == b_1$ **do**
 $b_0 \leftarrow \mathsf{RG}()$
 $b_1 \leftarrow \mathsf{RG}()$
 $b := \mathsf{VN}(b_0, b_1)$
Return b

Fig. 3: The trusted amalgamation function Am_{RG} for a randomness generator RG and a von Neumann extractor VN.

The amalgamation function Am_{RG} is extremely simple, it runs RG twice independently and applies VN to the output. This is repeated in a while-loop, until the output of VN is not the error symbol \bot , but a bit $b \in \{0, 1\}$.

Correctness. Since we have $VN(b_0, b_1) = \bot \iff b_0 = b_1$, the correctness of this algorithm depends on the probability that the two executions of RG computing b_0 and b_1 in the while-loop yield $b_0 \neq b_1$. Let $p := \Pr[RG() = 1]$, then we have

$$\Pr[b_0 \neq b_1] = 2p(1-p).$$

Hence, it takes an expected $(p(1-p))^{-1}$ executions of RG and $(2p(1-p))^{-1}$ executions of VN to generate an output bit. For instance, if RG is truly random, then we would have 4 expected executions of RG and 2 of VN. Even if RG is a rather bad random number generator, say with p = 1/4, then one would expect about 5 + 1/3 executions of RG and 2 + 2/3 of VN.

4.2 Security

The proof that $\widehat{\mathsf{RGSR}}$ is a subversion-resilient randomness generator uses the fact that the adversary provides a *single* implementation $\widetilde{\mathsf{RG}}$ which is then queried twice by the trusted amalgamation. Therefore, the two bits b_0, b_1 are computed *independently* in every while loop and are identically distributed. The watchdog only has to test the implementation of the von Neumann extractor on all four possible inputs. It is not necessary to test the implementation of the randomness generator at all to achieve security.

Theorem 1. The specification $\hat{R}GSR$ as defined above is $(\mathcal{O}(1), t_A, 0)$ -subversion-resilient in the offline watchdog model with trusted amalgamation.

Note that the theorem asserts that we can construct a *constant-time* watchdog. It will be independent of the runtime of the adversary or any bias possibly embedded in the subverted implementation of RG.

Proof. The only component that we test is the implementation of $VN : \{0, 1\} \times \{0, 1\} \rightarrow \{0, 1\}$, which is a very simple function with only four possible inputs. Therefore it can

be checked on all possible inputs in constant time. The watchdog WD runs a given implementation \widetilde{VN} on all four possible inputs and checks the correctness of the output with the specification.

In case VN deviates from the specification on any input, the watchdog will detect this with probability 1. Thus, this would immediately lead to an advantage of 0 for the adversary.

Provided that \widetilde{VN} implements VN correctly and using the fact that the two bits $b_0, b_1 \leftarrow \widetilde{RG}()$ are computed *independently* in every while loop, we obtain that when \widetilde{RG} outputs a bit b then we have

$$\Pr[b=0] = \Pr[b_0 = 0 \land b_1 = 1] = \Pr[b_0 = 1 \land b_1 = 0]$$
$$= \Pr[b=1],$$

and thus $\Pr[b=0] = \Pr[b=1] = 1/2$, again leading to an advantage of 0 for the adversary.

4.3 Discussions

The main advantage of our proposed RG is that it achieves perfect security using a *constant*-time watchdog. Note that Russell *et al.* [30] also described several alternative approaches to purify randomness in the standard model. Below we provide more discussion about their approaches. It is worth mentioning that in [1], Ateniese *et al.* proposed a different approach to eliminating the requirement of random oracles by essentially relying on an additional independent and untamperable source of public randomness.

Simple multi-splitting. The first approach proposed in [30] is simple multi-splitting, which means that n copies of RG (each outputting a single bit) are run and all outputs are concatenated and output. The main problem with this approach is that RG has to be tested very many times, otherwise the watchdog is unable to notice a small, but non-negligible bias.

More efficient construction using randomness extractors. The second approach is to use randomness extractors, but in a totally different way. Precisely, it is observed that a watchdog making $O(n^{2c})$ queries can verify that the output of each RG has at least $c \log n$ bits of entropy (for some constant c). Thus, Russell *et al.* [30] proposed to run RG for $\log n$ times to obtain a random string of length $\log n$, which is then used as a seed for a randomness extractor. This extractor can then be used to obtain more random bits from RG, which afterward can be expanded with a pseudorandom generator (PRG). Note that in this case a watchdog would not only have to check RG for entropy but also recompute all calculations of the extractor and the PRG to check if these components follow their specifications.

A disadvantage of our construction of RG is that we do not have a strict upper bound on its running time, but only expected bounds. We consider this a minor disadvantage, though, since lack of functionality will serve as an automated way to detect subversion that introduces a too heavy bias in RG. The efficiency can be improved if one is willing to do a little bit more testing. For instance, the watchdog could also test RG and check for a too heavy bias p that would significantly harm performance. Note however that

even a particularly bad underlying randomness generator RG, which always outputs a constant 0, for instance, would only harm correctness, but not the security of RG.

5 Subversion-Resilient Key Encapsulation Mechanisms

In this chapter, we will construct a (t, ε) -one-way key encapsulation mechanism that is subversion-resilient even if *all* algorithms are subject to subversion, provided that we have a very simple trusted amalgamation function. Our construction achieves subversionresilience with a watchdog whose running time is only *linear* in the security parameter, while also allowing for tradeoffs between ciphertext size and the watchdog's runtime.

5.1 Key Encapsulation Mechanisms and Security Definitions

Key encapsulation mechanisms are techniques to securely transport symmetric cryptographic key material using public key cryptography. We will use the following standard definitions for key encapsulation mechanisms and their security.

Definition 5. A key encapsulation mechanism (or KEM) consists of three algorithms KEM = (Gen, Encaps, Decaps) with the following syntax.

- Gen(): The randomized key generation algorithm outputs a key pair (sk, pk).
- Encaps(pk): The randomized encryption algorithm takes as input a public key pk. It outputs a key $K \in KS$, where KS is called the key space defined by pk (either implicitly or explicitly), and a ciphertext C.
- Decaps(sk, C): The deterministic decapsulation algorithm takes a secret key sk and a ciphertext C. It outputs a key $K \in \mathcal{KS}$ or a distinguished error symbol \perp .

Definition 6. We say that KEM = (Gen, Encaps, Decaps) is (t_A, ε) -indistinguishable if for any adversary A running in time at most t_A it holds that

$$\mathsf{Adv}_{\mathcal{A}}^{\mathsf{KEM}} := |\Pr[\mathsf{KEMIND}_{\mathsf{KEM}}^{\mathcal{A}}] - 1/2| \le \varepsilon$$

with KEMIND as defined in Figure 4 (a).

Definition 7. We say that KEM = (Gen, Encaps, Decaps) is (t_A, ε) -one-way if for any adversary A running in time at most t_A it holds that

$$\mathsf{Adv}^{\mathsf{KEM}}_{\mathcal{A}} := |\Pr[\mathsf{KEMOW}^{\mathcal{A}}_{\mathsf{KEM}}]| \leq \varepsilon$$

with KEMOW as defined in Figure 4 (b).

We define subversion-resilient KEMs by adapting Definition 2 to KEMs.

Definition 8. We say that the specification $KEMSR = (Am_{KEM}, KEMSR)$ of a key encapsulation mechanism is $(t_{WD}, t_A, \varepsilon)$ subversion-resilient one-way/indistinguishable in the offline watchdog model with trusted amalgamation, if one can efficiently construct a correct watchdog WD running in time at most t_{WD} such that for any adversary $A = (A_0, A_1)$ running in time at most t_A it holds that:

$$\mathsf{AdvSR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{Exp},\delta,\widehat{\mathsf{KEMSR}}} \leq \varepsilon$$

with $\text{Exp} \in \{\text{KEMIND}, \text{KEMOW}\}$ and $\delta \in \{0, 1/2\}$, accordingly.

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$(sk, pk) \gets Gen()$
$K_0 \stackrel{\$}{\leftarrow} \mathcal{KS}$
$(C^*, K_1) \leftarrow Encaps(pk)$
$b \stackrel{\$}{\leftarrow} \{0,1\}$
$b_{\mathcal{A}} \leftarrow \mathcal{A}(pk, K_b, C^*)$
If $b_{\mathcal{A}} == b$ then return 1
Else return 0

 $\mathsf{KEMOW}^\mathcal{A}_{\mathsf{KEM}}$

 $\begin{array}{l} (sk, pk) \leftarrow \mathsf{Gen}() \\ (C, K) \leftarrow (\mathsf{Encaps}(pk) \\ (K^*) \leftarrow \mathcal{A}(pk, C) \\ \mathbf{If} \ K^* == K \ \mathbf{then \ return} \ 1 \\ \mathbf{Else \ return} \ 0 \end{array}$

(b) One-way experiment for key encapsulation mechanisms.

(a) Indistinguishability experiment for key encapsulation mechanisms.

 $\mathsf{SR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{Exp},\delta,\widehat{\mathsf{KEMSR}}}$ $(\widetilde{\mathsf{KEMSR}}, st) \leftarrow \mathcal{A}_0()$ If $WD^{\widetilde{KEMSR}}()$ then Draw bit b with $\Pr[b=1] = \delta$ Return b **Return** $\operatorname{Exp}_{\mathcal{A}_1(st)}^{\operatorname{Am}(\widetilde{\mathsf{KEMSR}})}$ (c) Subversion-resilience exfor key periment encapsulation mechanisms where $Exp \in {KEMIND, KEMOW}$ and $\delta \in \{0, 1/2\}$, accordingly.

Fig. 4: Security experiments for KEMs.

5.2 Our Proposed KEM

Idea overview. Before we present the technical details of our construction, let us illustrate our approach. In order to obtain random coins for our scheme, we will use the subversion-resilient randomness generator from the previous chapter. Overall, we will use n instantiations of a KEM in parallel, where n is a parameter that can be chosen appropriately depending on the application. This means, we run the key generation algorithm n times in parallel to obtain n key pairs. To encapsulate a key, we will also run the Encaps algorithm n times in parallel, each time using a public key that was previously generated. This gives us n ciphertext/key pairs. While all ciphertexts are just output as the final ciphertext, the amalgamation executes an XOR function on all keys. As we will see later in the security analysis, as long as one public key and the ciphertext under that public key were executed honestly, this will be sufficient for our reduction to be successful.

Construction. With these definitions in place, we are now ready to describe our construction. Let $\widehat{\text{RGSR}} = (\text{Am}_{\text{RG}}, \text{RGSR})$ be the specification of a subversion-resilient randomness generator. Further, let n > 0 be an arbitrary constant which allows us to adjust the construction. Since we focus on the key encapsulation mechanism in this section, we will use

$$RG() := Am_{RG}(RGSR)$$

to simplify notation. Let (Gen, Encaps, Decaps) be a key encapsulation mechanism. From these building blocks we define a specification of a subversion-resilient key encapsulation mechanism

$$KEMSR = (Am_{KEM}, KEMSR) = (Am_{KEM}, (RGSR, Gen, Encaps, Decaps))$$

where the trusted amalgamation $\mathsf{Am}_{\mathsf{KEM}}$ defines algorithms (GenSR, EncapsSR, DecapsSR) as follows.

- GenSR() : Compute $r_i \leftarrow \mathsf{RG}()$ and $(sk_i, pk_i) \leftarrow \mathsf{Gen}(;r_i)$ for all $i \in [n]$ and output

$$pk := (pk_i)_{i \in [n]}$$
 and $sk := (sk_i)_{i \in [n]}$.

See Figure 5 for an illustration.

- EncapsSR(pk): On input $pk = (pk_1, \dots, pk_n)$ compute $r_i \leftarrow RG()$ and $(C_i, K_i) \leftarrow Encaps(pk_i; r_i)$ for all $i \in [n]$ and output

$$C := (C_1, \ldots, C_n)$$
 and $K := K_1 \oplus \cdots \oplus K_n$.

See Figure 6 for an illustration.

- DecapsSR(C, sk): On input $sk = (sk_1, \ldots, sk_n)$ and $C = (C_1, \ldots, C_n)$ compute $K_i = \text{Decaps}(sk_i, C_i)$ for all $i \in [n]$. If there exists $i \in [n]$ such that $K_i = \bot$, then output \bot . Otherwise output

$$K = K_1 \oplus \cdots \oplus K_n.$$

The trusted amalgamation function Am_{KEM} essentially consists of simple loops with n independent iterations of calls to the underlying RG and KEM procedures, plus a simple \oplus function. Note that a trusted \oplus was also used in [29] in order to handle large message spaces for public key encryption.



Fig. 5: Subversion-resilient KEM: Key generation algorithm.

Security analysis.

Theorem 2. Let KEM be a (t_A, ε) one-way key encapsulation mechanism and $\widehat{\text{RGSR}}$ be the specification of a $(\mathcal{O}(1), t_B, 0)$ subversion-resilient randomness generator. Then $\widehat{\text{KEMSR}}$ as defined above with parameters $n, n_{\text{WD}} > 0 \in \mathbb{N}$ is $(t_{\text{WD}}, t'_A, \varepsilon')$ subversion-resilient one-way in the offline watchdog model with trusted amalgamation with

$$t_{\mathsf{WD}} \in \mathcal{O}(n_{\mathsf{WD}}), \qquad t'_{\mathcal{A}} \in \mathcal{O}(t_{\mathcal{A}} + t_{\mathcal{B}} + n),$$
$$\varepsilon' \le \max\left\{2^{-n_{\mathsf{WD}}}, 2\varepsilon + \left(\frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^{n_{\mathsf{WD}}} \cdot \left(1 - \frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^{n}\right\}$$

Proof. The following notation and helper functions will be useful for the proof. Let $R_{\text{gen}}, R_{\text{enc}}$ denote the randomness space of the algorithms Gen and Encaps, respectively. Let F_{KEM} be the deterministic function parameterized by a key encapsulation mechanism KEM = (Gen, Encaps, Decaps) which takes as input randomness $(r, s) \in R_{\text{gen}} \times R_{\text{enc}}$ for Gen and Encaps, respectively, and then computes

$$(pk, sk, C, K) = F_{\mathsf{KEM}}(r, s) \tag{5}$$

with

$$(pk, sk) \leftarrow \mathsf{Gen}(; r)$$
 and $(C, K) \leftarrow \mathsf{Encaps}(pk; s)$

For KEM (which is part of the specification $\widehat{\text{KEMSR}}$) and a corresponding implementation $\widehat{\text{KEM}}$ we can now define sets Neq and Eq as

$$\mathsf{Neq} := \left\{ (r, s) : F_{\mathsf{KEM}}(r, s) \neq F_{\widetilde{\mathsf{KEM}}}(r, s) \right\}$$
(6)



Fig. 6: Subversion-resilient KEM: Encapsulation algorithm.

and

$$\mathsf{Eq} := \left\{ (r, s) : F_{\mathsf{KEM}}(r, s) = F_{\widetilde{\mathsf{KEM}}}(r, s) \right\}.$$
(7)

Hence, set Neq contains all "bad" randomness values where the implementation deviates from the specification, and Eq contains all "good" randomness values where specification and implementation match. Since Neq and Eq are disjoint sets, we have

$$\mathsf{Neq} \cup \mathsf{Eq} = R_{\mathsf{gen}} imes R_{\mathsf{enc}} \quad ext{ and } \quad \mathsf{Neq} \cap \mathsf{Eq} = \emptyset$$

Watchdog construction. We construct a universal offline watchdog WD which proceeds as follows.

- 1. First WD runs the watchdog for $\widehat{\text{RGSR}}$ as a subroutine. If this algorithm outputs true, then WD outputs true. Otherwise, WD proceeds.
- 2. Then, for $i \in [1, n_{\text{WD}}]$, WD picks $(r_i, s_i) \stackrel{\$}{\leftarrow} R_{\text{gen}} \times R_{\text{enc}}$ uniformly at random and checks whether

$$F_{\mathsf{KEM}}(r_i, s_i) = F_{\widetilde{\mathsf{KEM}}}(r_i, s_i)$$

holds where F is as defined in Equation (5). If any of these checks fails, then the watchdog outputs true. Otherwise, it outputs false.

Note that the above watchdog performs only a constant number of queries to check RG plus n_{WD} many evaluations of each Gen and Encaps.

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Security analysis. Before we dive into the analysis, let us start with a general bound on the success probability of adversaries that will help us out later. We will use that the fraction of randomness inputs eq to Gen × Encaps is at least 1/2 for any adversary \mathcal{A} winning the subversion security game with probability at least $1/2^{n_{\text{WD}}}$. The reason for this is that any implementation winning the subversion experiment need to pass the watchdog's test beforehand, and in both cases uniformly random coins are provided to the subverted building blocks. Thus, we naturally obtain

$$\Pr[\mathsf{WD}^{\widetilde{\mathsf{KEMSR}}}()] \geq \Pr[\mathsf{SR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{KEMOW},\widetilde{\mathsf{KEMSR}}} = 1].$$

Now, assume that eq < 1/2. Then we can conclude that

$$\Pr[\mathsf{SR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{KEMOW},\widetilde{\mathsf{KEMSR}}} = 1] \le \Pr[\mathsf{WD}^{\widetilde{\mathsf{KEMSR}}}()] < 1/2^{n_{\mathsf{WD}}}.$$

This contradicts that \mathcal{A} wins with probability at least $1/2^{n_{\text{WD}}}$, which is why we can conclude that eq $\geq 1/2$ holds.

In order to analyze the security of our scheme with respect to this watchdog, consider the following sequence of games.

Game 0. This Game is the $SR_{KEMOW, \overline{KEMSR}}^{\mathcal{A}, WD}$ experiment.

Game 1. This game is identical to Game 0, except that all invocations of \widetilde{RG} are replaced with uniformly random bits.

Since WD runs the watchdog for $\widehat{\mathsf{RGSR}}$ as a subroutine it outputs true only if the watchdog for $\widehat{\mathsf{RGSR}}$ does. By the $(\mathcal{O}(1), t_{\mathcal{B}}, 0)$ -subversion-resilience of RG this game is therefore perfectly indistinguishable from Game 0.

Game 2. This game is identical to Game 1, except that the execution of game KEMOW^A_{KEM} is changed in the following way. After computing

$$(sk, pk) = ((pk_i)_{i \in [n]}, (sk_i)_{i \in [n]})$$

for $(sk_i, pk_i) = \widetilde{\mathsf{Gen}}(; r_i)$, and then

$$(C^*, K_1) = ((C_1^*, \dots, C_n^*), (K_{11} \oplus \dots \oplus K_{1n}))$$

with $(C_i^*, K_{1i}) = \widetilde{\mathsf{Encaps}}(pk_i; s_i)$ and uniform r_i, s_i , the experiment checks whether an index $i \in [1, n]$ exists such that

$$F_{\mathsf{KEM}}(r_i, s_i) = (pk_i, sk_i, C_i, K_i) = F_{\widetilde{\mathsf{KEM}}}(r_i, s_i).$$

Thus, the experiment ensures that at least one ciphertext was computed according to the specification, with a public key that was also computed according to the specification. If such a ciphertext was not output, then the game simply aborts.

Note that Game 2 and Game 1 only differ if an abort occurs *after* the watchdog has approved the implementation. Therefore, the probability for this event is

$$\begin{aligned} \Pr[\text{Abort}] &= \Pr\left[\begin{array}{c} \mathsf{WD}^{\widetilde{\mathsf{KEM}}} = \text{ false } \land \\ \text{Challenger aborts } \mathsf{KEMOW}_{\mathsf{KEM}}^{\mathcal{A}} \right] \\ &\stackrel{(*)}{=} \Pr\left[\mathsf{WD}^{\widehat{\mathsf{KEM}}} = \text{ false} \right] \cdot \Pr\left[\text{ Challenger aborts } \mathsf{KEMOW}_{\mathsf{KEM}}^{\mathcal{A}} \right] \\ &\leq \left(\frac{|\mathsf{Eq}|}{|R_{\mathsf{gen}} \times R_{\mathsf{enc}}|}\right)^{n_{\mathsf{WD}}} \cdot \left(\frac{|\mathsf{Neq}|}{|R_{\mathsf{gen}} \times R_{\mathsf{enc}}|}\right)^{n} \\ &\stackrel{(**)}{\leq} \left(\frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^{n_{\mathsf{WD}}} \cdot \left(1 - \frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^{n} \end{aligned}$$

with Neq and Eq as defined in Equation (6) and Equation (7), respectively. Note here that the equation marked with (*) holds because the two events are independent, since they only depend on the used randomness and the watchdog samples its randomness independently from the experiment. The following inequality holds by definition of the watchdog and the abort condition. The bound marked with (**) holds since the previous line can be written as $p^{\lambda} \cdot (1-p)^{\lambda}$ for some $p \in [0, 1]$. Calculating the derivative of this function and computing the root yields that the term is maximized for

$$p = \left(\frac{|\mathsf{Eq}|}{|R_{\mathsf{gen}} \times R_{\mathsf{enc}}|}\right) = \frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}$$

Thus, if we fix n_{WD} and n, the above term states the best bound any adversary can achieve.

Now we are ready to argue that security in Game 2 is implied by the security of the underlying KEM. To this end, consider a (t_A, ε_2) adversary A_2 which breaks the security of Game 2. From this, we construct a (t_B, ε) adversary B breaking the security of the underlying KEM.

Construction of \mathcal{B} . Adversary \mathcal{B} receives as input a challenge ch = (pk^*, C^*) and then simulates Game 2 as follows.

First, \mathcal{B} obtains an implementation KEMSR and state *st* from \mathcal{A}_0 . It runs the watchdog for KEMSR as specified above. In case that watchdog outputs false, \mathcal{B} outputs 0, just like the original security experiment. Otherwise, \mathcal{B} continues to simulate Game 2.

If this is the case, then the adversary \mathcal{B} generates n keys $(sk, pk) = ((sk_1, \ldots, sk_n), (pk_1, \ldots, pk_n))$ using the amalgamated algorithm Gen, based on the implementation provided by \mathcal{A}_0 . In order to compute the challenge ciphertexts, \mathcal{B} computes ciphertexts C_i and keys K_i for $i \in [1, n]$ by running Encaps using uniformly random coins. As in Game 2, the adversary \mathcal{B} now checks whether there exists (sk_i, pk_i, C_i, K_i) for some $i \in [1, n]$ which were computed according to the specification. In case no such pair is found, \mathcal{B} aborts.

Otherwise, let *i* denote the smallest index for which this condition is fulfilled. Then, \mathcal{B} computes the challenge ciphertext for \mathcal{A} by replacing (pk_i, C_i) by its own challenge (pk^*, C^*) . More formally, \mathcal{B} outputs (st, pk, C) with $pk = (pk_1, \ldots, pk_n)$ and C = (C_1, \ldots, C_n) to \mathcal{A}_1 , where $(pk_i, C_i) = (pk^*, C^*)$. Finally, let \mathcal{A} output a key K. \mathcal{B} then computes $K^* = K \oplus_{i=1}^n K_i$ where K_i are the keys simulated by \mathcal{B} .

Now observe that if A indeed computes the correct key, then so does B, since B simulated n - 1 keys. and can therefore compute the correct solution for its own challenge.

It remains to analyze the advantage of \mathcal{B} . If the embedded challenge could also have been output by \mathcal{A} ' implementation, then \mathcal{B} simulates Game 2 correctly. We can lower bound the probability of this event by 1/2, by utilizing our observation earlier that eq $\geq 1/2$. Thus, we have

$$\begin{aligned} \Pr[\mathsf{KEMOW}^{\mathcal{B}}_{\mathsf{KEM}}] &= \Pr[\mathsf{ch} \in \mathsf{Eq}] \cdot \Pr[\mathcal{A} \text{ wins } G_2 | ch \in \mathsf{Eq}] \\ &+ \Pr[\mathsf{ch} \notin \mathsf{Eq}] \cdot \Pr[\mathcal{A} \text{ wins } G_2 | ch \notin \mathsf{Eq}] \\ &\geq 1/2 \cdot \Pr[\mathcal{A} \text{ wins } G_2 | \mathsf{ch} \in \mathsf{Eq}] \\ &= 1/2 \cdot \Pr[\mathcal{A} \text{ wins } G_2]. \end{aligned}$$

Putting the above together we obtain $2\varepsilon \ge \varepsilon_2$.

Since Game 2 and Game 1 only differ by the abort condition, we obtain that

$$\varepsilon_2 = \varepsilon_1 - \Pr[\text{Abort}] \ge \varepsilon_1 - \left(\frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^{n_{\mathsf{WD}}} \cdot \left(1 - \frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^n$$

Finally, Game 1 and Game 0 are perfectly indistinguishable due to the $(\mathcal{O}(1), t_{\mathcal{B}}, 0)$ -subversion-resilience of $\widehat{\mathsf{RG}}$. Since Game 0 is the original subversion-resilience Game $\mathsf{SR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{KEMIND},\widetilde{\mathsf{KEMSR}}}$, we obtain that

$$\varepsilon_0 \le 2\varepsilon + \left(\frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^{n_{\mathsf{WD}}} \cdot \left(1 - \frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^n$$

which completes the proof.

5.3 Efficient Instantiation of the Subversion-Resilient KEM and the Watchdog

The variable n determines the efficiency of the constructed scheme in terms of the number of parallel instances of the underlying KEM (note that this has direct impact on the size of keys and ciphertexts), while n_{WD} determines the number of tests performed by the watchdog. Both together determine the overall security guarantee inherited from the underlying KEM.

Defining n_{WD} and n as variables yields interesting tradeoffs between the watchdog's runtime, the size of ciphertexts and keys, and the obtained security bounds.

In Table 1 we consider different choices of n and n_{WD} for $\lambda \in \{128, 256\}$, *i.e.*, "128-bit" and "256-bit" security. For different values of n, we compute the number n_{WD} of tests performed by the watchdog in order to achieve that

$$\left(\frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}}+n}\right)^{n_{\mathsf{WD}}} \cdot \left(1 - \frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}}+n}\right)^n \le 2^{-\lambda}$$

Security parameter	λn [le	$\log_2(n_{WE})$,)]
128	32	8	
128	16	11	
128	8	18	
128	4	33	
256	64	9	
256	32	12	
256	16	19	
256	8	34	

Table 1: Instantiating our construction and the watchdog with different values n and n_{WD} . Recall that n is the number of parallel KEM instances used in our construction and n_{WD} is the number of tests (on each Gen and Encaps) done by the watchdog.

holds. Note that together with the assumption that the underlying KEM is instantiated such that it provides $\varepsilon \leq 2^{-\lambda}$, we thus obtain a security bound on the subversion-resilient KEM of

$$\varepsilon_0 \le 2\varepsilon + \left(\frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^{n_{\mathsf{WD}}} \cdot \left(1 - \frac{n_{\mathsf{WD}}}{n_{\mathsf{WD}} + n}\right)^n \le 3 \cdot 2^{-\lambda}.$$

Table 1 shows how our subversion-resilient KEM can be instantiated. For instance, for $\lambda = 128$ and with n = 8, the watchdog only needs to test the Gen and Encaps algorithm only 2^{18} times, which can be practically accomplished for many underlying KEM constructions within a short time on moderate hardware. Even for $\lambda = 128$ and with n as small as n = 4 only 2^{33} tests are already sufficient, which also seems practically feasible, since it can be accomplished for most underlying KEMs within minutes or at most few hours on standard hardware such as a laptop computer.

5.4 From OW to CPA

Note that one-way security is strictly weaker than CPA security. However, as we will show in Section 6, it seems that in our model and with our construction CPA-security does not seem achievable via a combiner-like approach. That being said, there are transformations to obtain a CPA secure KEM from a one-way KEM by applying a random oracle to the computed key. As the random oracle behaves like a random function and the key fed as input can not be computed by an adversary, the resulting output is indistinguishable from random keys. In [31] Russell *et al.* showed how to sanitize subverted random oracles in an asymptotic setting. Unfortunately, their approach heavily relies on their asymptotic model and that after the watchdog's testing specification and implementation deviate only on a negligible fraction of inputs, which does not seem possible to guarantee in our model.

6 Impossibility of subversion-resilient indistinguishability

The original security proof in [8] aimed to show subversion-resilience with regard to the security notion of CPA-*indistinguishability*. Unfortunately, as we will show in the following, the authors overlooked a very subtle detail which invalidates their security proof. On a very high level, the proof strategy was the following:

- The testing of the watchdog guarantees with overwhelming probability that at least one pair (pk_i, C_i) generated in the subversion security experiment does not deviate from the specification.
- We can replace this pair by the challenge pair (pk^*, C^*) obtained in the KEM security experiment.
- In order to be successful, the subversion adversary thus needs to also solve this challenge (pk^*, C^*) due to the combiner property.

Unfortunately, the above strategy does not hold up against scrutiny, as (pk^*, C^*) might never be the output of the subverted implementation. A simple example for this would be an implementation, which would never output a public key ending in '0'. The adversary could thus identify such instances and fail *intentionally*, effectively canceling out its advantage. Based on this, we now show that every reduction, which performs such a simple embedding such that the adversary has 'direct access' to it, can not be successful.

Theorem 3. Let R be a reduction which reduces the security of a subversion-resilient KEM KEMSR to the security of an indistinguishable KEM KEM. Let $pk = (pk_0, ..., pk_n)$, $C = (C_0, ..., C_n)$ be the public key and ciphertext of KEMSR. Furthermore, let R be any reduction, that after running the watchdog for KEMSR, takes a public key / ciphertext pair (pk^*, C^*) of KEM and replaces any pk_i, C_i where $i \in [n]$ with (pk^*, C^*) before handing this new challenge to some adversary. Then, if there exists an adversary \mathcal{B} which breaks the (t, ε) -subversion-resilience of KEMSR, there exists an adversary \mathcal{A} which breaks the (t, ε) -subversion-resilience of KEMSR but cannot be used by the (single-stage) reduction R of the form above to break the indistinguishability of KEM.

In other words, for every such reduction R, there is always an attacker A that will be able to break the subversion-resilience without breaking the indistinguishability for R.

Proof. First, the adversary prepares its implementation, such that the outputs of (Gen, Encaps) deviate from the specification for a fraction neq of all (randomness) inputs of Gen \times Encaps. Similarly we use eq = 1 – neq to denote the fraction of inputs for which outputs follow to the specification. Then, the watchdog performs q test on (Gen, Encaps), as described in [8].

Now, we will construct the adversary \mathcal{A} . If the watchdog approves of the implementation (i.e., it never encounters a deviation from the specification), \mathcal{A} is given its challenge ch = (pk^*, K^*, C^*) . Due to the possibility of using our von-Neumann construction, the keys in the challenge will always be uniform bitstrings. Thus, we can ignore K^* in the following and will simply use ch = (pk^*, C^*) . We now distinguish the two following scenarios:

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 - If the challenge given to \mathcal{A} is correctly distributed with regard to the subverted implementation, the adversary flips a biased coin with bias = neq/eq. If the result is heads (which happens with probability bias), the adversary runs \mathcal{B} to break the security of the scheme with probability ε . Otherwise, if the result is tails (which happens with probability 1 bias), the adversary samples a uniformly distributed bit and returns this random bit.
- If the challenge given to \mathcal{A} is not correctly distributed, there is a public key / ciphertext pair that could not have been produced by the subverted implementation. Now, \mathcal{A} tries to to deliberately output a wrong solution, as they are aware of the fact that they are used in a reduction R. To do so, \mathcal{A} runs \mathcal{B} to obtain a bit b and then outputs 1 - b. Hence, it outputs the correct bit with probability $1 - \varepsilon$.

Now, let us analyze $Adv := \mathsf{KEMIND}_{\mathsf{KEM}}^{\mathcal{R}}$, i.e., the advantage of the reduction R in breaking the indistinguishability security of the underlying KEM. By definition, this advantage is equal to $|\Pr[\mathsf{SR} = 1] - 1/2|$. Here, SR is the subversion security game played by \mathcal{A} , where the reduction embeds a challenge somewhere in a construction such that the adversary has access to this challenge. To analyze Adv, we introduce the following events:

- **detected:** This event describes that the Watchdog outputs 'true' during its testing phase, i.e., the watchdog accepts the implementation.
- A: This event ("attack") refers to \mathcal{A} flipping its coin and then trying to break the security of the considered scheme (which happens with probability bias).
- **R:** This event ("random") is the complementary event to "attack" and refers to A simply outputting a random bit.

Now, the law of total probability gives

$$\begin{split} \mathrm{Adv} &= |\Pr[\mathrm{SR} = 1 | \mathrm{detected}] \cdot \Pr[\mathrm{detected}] \\ &+ \Pr[\mathrm{SR} = 1 | \neg \ \mathrm{detected} \land \mathrm{ch} \notin \mathrm{Eq}] \cdot \Pr[\neg \ \mathrm{detected} \land \mathrm{ch} \notin \mathrm{Eq}] \\ &+ \Pr[\mathrm{SR} = 1 | \neg \ \mathrm{detected} \land \mathrm{ch} \in \mathrm{Eq} \land A] \cdot \Pr[\neg \ \mathrm{detected} \land \mathrm{ch} \in \mathrm{Eq} \land A] \\ &+ \Pr[\mathrm{SR} = 1 | \neg \ \mathrm{detected} \land \mathrm{ch} \in \mathrm{Eq} \land R] \cdot \Pr[\neg \ \mathrm{detected} \land \mathrm{ch} \in \mathrm{Eq} \land R] \\ &- 1/2 |. \end{split}$$

Plugging in the probabilities that the subverted implementation is detected (or not) and the different scenarios for A shows that this is equal to

$$\begin{aligned} \operatorname{Adv} \stackrel{(1)}{=} |1/2 \cdot (1 - \operatorname{eq}^{q}) \\ &+ \varepsilon \cdot (\operatorname{eq}^{q} \cdot \operatorname{neq}) \\ &+ (1 - \varepsilon) \cdot (\operatorname{eq}^{q+1} \cdot \operatorname{bias}) \\ &+ 1/2 \cdot (\operatorname{eq}^{q+1} \cdot (1 - \operatorname{bias})) \\ &- 1/2| \end{aligned}$$

$$\stackrel{(2)}{=} |1/2 \cdot (1 - \operatorname{eq}^{q}) \\ &+ \varepsilon \cdot (\operatorname{eq}^{q} \cdot \operatorname{neq}) \\ &+ (1 - \varepsilon) \cdot (\operatorname{eq}^{q+1} \cdot \operatorname{neq/eq}) \\ &+ 1/2 \cdot (\operatorname{eq}^{q+1} \cdot (1 - \operatorname{neq/eq})) \\ &- 1/2| \end{aligned}$$

$$\stackrel{(3)}{=} |1/2 \cdot (1 - \operatorname{eq}^{q}) \\ &+ (\operatorname{eq}^{q} \cdot \operatorname{neq}) \\ &+ 1/2 \cdot \operatorname{eq}^{q+1} \\ &- 1/2 \cdot \operatorname{eq}^{q+1} \operatorname{neq/eq})) \\ &- 1/2| \end{aligned}$$

$$= |1/2 \cdot (1 - \operatorname{eq}^{q} + \operatorname{eq}^{q} \cdot \operatorname{neq} + \operatorname{eq}^{q+1}) - 1/2| \\ = |1/2 \cdot (1 - \operatorname{eq}^{q} + \operatorname{eq}^{q} (\operatorname{neq} + \operatorname{eq})) - 1/2| \\ = |1/2 \cdot (1 - \operatorname{eq}^{q} + \operatorname{eq}^{q}) - 1/2| = 0 \end{aligned}$$

where in equation (1) we simply replaced the probabilities of the events with the corresponding values of eq and neq and the probabilities according to \mathcal{A} 's strategy. In (2) we substituted bias with neq/eq, according to its definition. All equations after (3) are simple manipulations. Hence, we conclude that \mathcal{A} is not breaking the indistinguishability of KEM.

Discussion Note that the bias bias = neq/eq chosen by the adversary \mathcal{A} is independent of the amount of tests q performed by the watchdog. Hence, this value cancels out one additional eq term, which is *always* true, independent of the size of q. Also, the size of Neq (and therefore neq) can not be made arbitrarily small by simply more testing of the watchdog, as long as the watchdog is independent of the adversary and engages in a fixed number of tests. Consider an adversary which prepares its implementation with neq = ((q/q + 1)) were q denotes the amount of testing queries by the watchdog, The probability that the adversary avoids detection is then $(1 - (q/q + 1))^q$ and approaches 1/e for $q \to \infty$, which is non-negligible, while the probability of being handed a subverted challenge is neq, which is also non-negligible.

Note that Theorem 3 is specifically phrased in order to capture the results of [8]. It seems that even broader statements about impossibility are possible in this setting of

subversion-resilience: Instead of directly embedding a challenge, a reduction could also try to rerandomize the challenge before embedding it, in case that KEM is sufficiently rerandomizeable. However, this approach also does not seem to work, as the reduction does not have knowledge whether the rerandomized challenge can be computed by the implementation, as the reduction can not recompute the randomness used for the challenge. Otherwise, it would directly break the security of KEM.

On the other hand, a general impossibility result regarding CPA security with limited testing is also not possible: If a construction shifts all computations to the trusted amalgamation, it is trivially subversion-resilient. Thus, there is a tradeoff between the amount of trust put into the amalgamation and the needed resources to guarantee this trust for real applications. We leave this formalization as an open problem for future work.

7 Subversion-Resilient Public-Key Encryption

After successfully constructing a subversion-resilient one-way KEM, we now proceed to construct a subversion-resilient one-way public key encryption scheme. We will show that the standard way to construct public-key encryption from a KEM also preserves subversion-resilience, provided that a trusted XOR operation is given.

7.1 Definitions and Construction

We begin by recalling the standard definition for public key encryption and its standard OW-style security definition.

Definition 9. Let $PKE = (Gen_{PKE}, Encrypt, Decrypt)$ be a public key encryption scheme with the following syntax:

- $Gen_{PKE}()$: The randomized key-generation algorithm outputs a key pair (sk, pk).
- Encrypt(pk, M): The randomized encrypt algorithm takes as input the public key pk and a message M and outputs the ciphertext C.
- $\mathsf{Decrypt}(sk, C)$: The deterministic decryption algorithm takes as input the secret key sk and the ciphertext C. It outputs a message M or the error symbol \perp .

Definition 10. We say that $\mathsf{PKE} = (\mathsf{Gen}_{\mathsf{PKE}}, \mathsf{Encrypt}, \mathsf{Decrypt})$ with message space \mathcal{M} is $(t_{\mathcal{A}}, \varepsilon)$ -one-way if for any adversary \mathcal{A} running in time at most $t_{\mathcal{A}}$ it holds that

$$\mathsf{Adv}_{\mathcal{A}}^{\mathsf{PKE}} := |\Pr[\mathsf{PKEOW}_{\mathsf{PKE}}^{\mathcal{A}}]| \leq \varepsilon$$

with $\mathsf{PKEOW}_{\mathsf{PKE}}^{\mathcal{A}}$ shown in Figure 7 (a).

Definition 11. We say that a specification of a public key encryption scheme $PKESR = (Am_{PKE}, PKESR)$ is $(t_{WD}, t_A, \varepsilon)$ -subversion-resilient one-way in the offline watchdog model with trusted amalgamation if one can efficiently construct a correct watchdog WD running in time at most t_{WD} such that for any adversary $A = (A_0, A_1)$ running in time t_A it holds that

$$\mathsf{AdvSR}^{\mathcal{A},\mathsf{WD}}_{\mathsf{PKEOW},\widehat{\mathsf{PKESR}}} \leq \varepsilon$$

with the used experiments shown in Figure 7 (a) and (b).

Subversion-Resilient Public Key Encryption with Practical Watchdogs

PKEOW	SR ^{A,WD} PKEOW.PKESR		
$(sk, pk) \leftarrow Gen_{PKE}()$	$(\widetilde{PKESR}, st) \leftarrow \mathcal{A}_0()$		
$m^* \stackrel{\circ}{\leftarrow} \mathcal{M}$ $C^* \leftarrow Encrypt(nk \ m^*)$	If $WD^{\widetilde{PKESR}}()$ then		
$m \leftarrow \mathcal{A}(pk, C^*)$	Return $b = 0$		
If $m^* == m$ then Return 1	Am(PKESR)		
Else Return 0	(b) Subversion-resilience ex-		
(a) One-way experiment for	periment for public key en-		
public key encryption schemes	cryption schemes.		
with message space \mathcal{M} .			

Fig. 7: Security experiments for public key encryption schemes.

Description of the construction. Let $KEMSR = (Am_{KEM}, KEMSR)$ be the specification of a subversion-resilient key encapsulation mechanism with

 $Am_{KEM}(\widehat{KEMSR}) = (GenSR_{KEM}, EncapsSR, DecapsSR).$

We then construct the specification of a public key encryption scheme PKESR =(Am_{PKESR}, KEMSR) with

$$Am_{PKESR}(KEMSR) = (GenSR_{PKE}, EncryptSR, DecryptSR)$$

where each algorithm is defined as follows:

- $\text{GenSR}_{\text{PKE}}()$: Output $(sk, pk) = \text{GenSR}_{\text{KEM}}()$.
- EncryptSR(pk, M): Compute $(C, K) \leftarrow$ EncapsSR(pk) and output $(C, K \oplus M)$.
- DecryptSR(sk, C): Parse $C = (C_0, C_1)$. Compute $K \leftarrow DecapsSR(sk, C_0)$. Output $M = C_1 \oplus K$.

Thus, the specification of our public key encryption scheme is basically the specification of the underlying subversion-resilient key encapsulation mechanism and the amalgamation Am_{PKESR} is almost identical to Am_{KEM}. The only difference is that during encrypt, the message is additionally computed via an XOR to the key K.

Security analysis. Subversion-resilience of the new public key encryption scheme follows directly from the security of the underlying KEM and the usage of a trusted \oplus .

Theorem 4. Let $\widehat{\mathsf{KEMSR}} = (\mathsf{Am}_{\mathsf{KEM}}, \mathsf{KEMSR})$ be the specification of a $(t_{\mathsf{WD}}, t_{\mathcal{A}}, \epsilon)$ subversion-resilient one-way KEM. Then $\widehat{\mathsf{PKESR}}$ as described above is $(t_{\mathsf{WD}}, t_A, \epsilon)$ subversion-resilient one-way under a trusted \oplus operation.

Proof sketch. The watchdog for PKE simply runs the watchdog for KEMSR as a subroutine. Thus, either the watchdog detects subversion or the ciphertext-key-pair output is ε -one-way. Since the \oplus operation is trusted, the resulting ciphertexts of PKE are also ε -one-way. Therefore PKE is subversion-resilient iff KEMSR is subversion-resilient.

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Discussion. One may wonder why we do not directly build a subversion-resilient public key encryption scheme, since the experiment chooses m uniformly at random, and thus do not allow the adversary to freely choose input triggers. However, we then again run into problems similar to the ones presented in Section 6. There will always be non-negligible many input trigger in the implementation, as long as the watchdog engages in polynomial many testing queries. Thus, we utilize a trusted XOR and base the security of our scheme on a subversion-resilient KEM.

Acknowledgments. We would like to thank Moti Yung and the anonymous reviewers of PKC 2021 for their helpful comments and suggestions, and in particular Cristina Onete for shepherding this paper and providing very detailed and valuable inputs. Additionally we would like Denis Diemert for pointing out the flaw in our security proof.

References

- Ateniese, G., Francati, D., Magri, B., Venturi, D.: Public immunization against complete subversion without random oracles. In: Deng, R.H., Gauthier-Umaña, V., Ochoa, M., Yung, M. (eds.) ACNS 19. LNCS, vol. 11464, pp. 465–485. Springer, Heidelberg (Jun 2019)
- Ateniese, G., Magri, B., Venturi, D.: Subversion-resilient signature schemes. In: Ray, I., Li, N., Kruegel, C. (eds.) ACM CCS 2015. pp. 364–375. ACM Press (Oct 2015)
- Bellare, M., Fuchsbauer, G., Scafuro, A.: NIZKs with an untrusted CRS: Security in the face of parameter subversion. In: Cheon, J.H., Takagi, T. (eds.) ASIACRYPT 2016, Part II. LNCS, vol. 10032, pp. 777–804. Springer, Heidelberg (Dec 2016)
- Bellare, M., Hoang, V.T.: Resisting randomness subversion: Fast deterministic and hedged public-key encryption in the standard model. In: Oswald, E., Fischlin, M. (eds.) EURO-CRYPT 2015, Part II. LNCS, vol. 9057, pp. 627–656. Springer, Heidelberg (Apr 2015)
- Bellare, M., Jaeger, J., Kane, D.: Mass-surveillance without the state: Strongly undetectable algorithm-substitution attacks. In: Ray, I., Li, N., Kruegel, C. (eds.) ACM CCS 2015. pp. 1431–1440. ACM Press (Oct 2015)
- Bellare, M., Paterson, K.G., Rogaway, P.: Security of symmetric encryption against mass surveillance. In: Garay, J.A., Gennaro, R. (eds.) CRYPTO 2014, Part I. LNCS, vol. 8616, pp. 1–19. Springer, Heidelberg (Aug 2014)
- Bemmann, P., Berndt, S., Diemert, D., Eisenbarth, T., Jager, T.: Subversion-resilient authenticated encryption without random oracles. In: Applied Cryptography and Network Security 21st International Conference, ACNS 2023, Kyoto, Japan, June 19-22, 2023, Proceedings, Part II. pp. 460–483 (2023), https://doi.org/10.1007/978-3-031-33491-7_17
- Bemmann, P., Chen, R., Jager, T.: Subversion-resilient public key encryption with practical watchdogs. In: Garay, J. (ed.) PKC 2021, Part I. LNCS, vol. 12710, pp. 627–658. Springer, Heidelberg (May 2021)
- Berndt, S., Liskiewicz, M.: Algorithm substitution attacks from a steganographic perspective. In: Thuraisingham, B.M., Evans, D., Malkin, T., Xu, D. (eds.) ACM CCS 2017. pp. 1649– 1660. ACM Press (Oct / Nov 2017)
- Blum, M., Luby, M., Rubinfeld, R.: Self-testing/correcting with applications to numerical problems. In: 22nd ACM STOC. pp. 73–83. ACM Press (May 1990)
- Bossuat, A., Bultel, X., Fouque, P.A., Onete, C., van der Merwe, T.: Designing reverse firewalls for the real world. In: Chen, L., Li, N., Liang, K., Schneider, S.A. (eds.) ES-ORICS 2020, Part I. LNCS, vol. 12308, pp. 193–213. Springer, Heidelberg (Sep 2020)

- Chakraborty, S., Dziembowski, S., Nielsen, J.B.: Reverse firewalls for actively secure MPCs. In: Micciancio, D., Ristenpart, T. (eds.) CRYPTO 2020, Part II. LNCS, vol. 12171, pp. 732– 762. Springer, Heidelberg (Aug 2020)
- Chen, R., Huang, X., Yung, M.: Subvert KEM to break DEM: Practical algorithmsubstitution attacks on public-key encryption. In: Moriai, S., Wang, H. (eds.) ASI-ACRYPT 2020, Part II. LNCS, vol. 12492, pp. 98–128. Springer, Heidelberg (Dec 2020)
- Chen, R., Mu, Y., Yang, G., Susilo, W., Guo, F., Zhang, M.: Cryptographic reverse firewall via malleable smooth projective hash functions. In: Cheon, J.H., Takagi, T. (eds.) ASI-ACRYPT 2016, Part I. LNCS, vol. 10031, pp. 844–876. Springer, Heidelberg (Dec 2016)
- Chow, S.S.M., Russell, A., Tang, Q., Yung, M., Zhao, Y., Zhou, H.S.: Let a non-barking watchdog bite: Cliptographic signatures with an offline watchdog. In: Lin, D., Sako, K. (eds.) PKC 2019, Part I. LNCS, vol. 11442, pp. 221–251. Springer, Heidelberg (Apr 2019)
- Claburn, T.: NSA: We've learned our lesson after foreign spies used one of our crypto backdoors - but we can't say how exactly. The Register, https://www.theregister. com/2020/10/28/nsa_backdoor_wyden/ (2020)
- Degabriele, J.P., Farshim, P., Poettering, B.: A more cautious approach to security against mass surveillance. In: Leander, G. (ed.) FSE 2015. LNCS, vol. 9054, pp. 579–598. Springer, Heidelberg (Mar 2015)
- Dodis, Y., Impagliazzo, R., Jaiswal, R., Kabanets, V.: Security amplification for interactive cryptographic primitives. In: Reingold, O. (ed.) TCC 2009. LNCS, vol. 5444, pp. 128–145. Springer, Heidelberg (Mar 2009)
- Dodis, Y., Mironov, I., Stephens-Davidowitz, N.: Message transmission with reverse firewalls—secure communication on corrupted machines. In: Robshaw, M., Katz, J. (eds.) CRYPTO 2016, Part I. LNCS, vol. 9814, pp. 341–372. Springer, Heidelberg (Aug 2016)
- Dziembowski, S., Faust, S., Standaert, F.X.: Private circuits III: Hardware trojan-resilience via testing amplification. In: Weippl, E.R., Katzenbeisser, S., Kruegel, C., Myers, A.C., Halevi, S. (eds.) ACM CCS 2016. pp. 142–153. ACM Press (Oct 2016)
- Fischlin, M., Mazaheri, S.: Self-guarding cryptographic protocols against algorithm substitution attacks. In: CSF. pp. 76–90. IEEE Computer Society (2018)
- Fuchsbauer, G.: Subversion-zero-knowledge SNARKs. In: Abdalla, M., Dahab, R. (eds.) PKC 2018, Part I. LNCS, vol. 10769, pp. 315–347. Springer, Heidelberg (Mar 2018)
- Giacon, F., Heuer, F., Poettering, B.: KEM combiners. In: Abdalla, M., Dahab, R. (eds.) PKC 2018, Part I. LNCS, vol. 10769, pp. 190–218. Springer, Heidelberg (Mar 2018)
- Holenstein, T., Renner, R.: One-way secret-key agreement and applications to circuit polarization and immunization of public-key encryption. In: Shoup, V. (ed.) CRYPTO 2005. LNCS, vol. 3621, pp. 478–493. Springer, Heidelberg (Aug 2005)
- Jain, A., Korb, A., Manohar, N., Sahai, A.: Amplifying the security of functional encryption, unconditionally. In: Micciancio, D., Ristenpart, T. (eds.) CRYPTO 2020, Part I. LNCS, vol. 12170, pp. 717–746. Springer, Heidelberg (Aug 2020)
- Jain, A., Manohar, N., Sahai, A.: Combiners for functional encryption, unconditionally. In: Canteaut, A., Ishai, Y. (eds.) EUROCRYPT 2020, Part I. LNCS, vol. 12105, pp. 141–168. Springer, Heidelberg (May 2020)
- Mironov, I., Stephens-Davidowitz, N.: Cryptographic reverse firewalls. In: Oswald, E., Fischlin, M. (eds.) EUROCRYPT 2015, Part II. LNCS, vol. 9057, pp. 657–686. Springer, Heidelberg (Apr 2015)
- Poettering, B., Rösler, P.: Combiners for AEAD. IACR Trans. Symmetric Cryptol. 2020(1), 121–143 (2020)
- Russell, A., Tang, Q., Yung, M., Zhou, H.S.: Cliptography: Clipping the power of kleptographic attacks. In: Cheon, J.H., Takagi, T. (eds.) ASIACRYPT 2016, Part II. LNCS, vol. 10032, pp. 34–64. Springer, Heidelberg (Dec 2016)

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- Russell, A., Tang, Q., Yung, M., Zhou, H.S.: Generic semantic security against a kleptographic adversary. In: Thuraisingham, B.M., Evans, D., Malkin, T., Xu, D. (eds.) ACM CCS 2017. pp. 907–922. ACM Press (Oct / Nov 2017)
- Russell, A., Tang, Q., Yung, M., Zhou, H.S.: Correcting subverted random oracles. In: Shacham, H., Boldyreva, A. (eds.) CRYPTO 2018, Part II. LNCS, vol. 10992, pp. 241–271. Springer, Heidelberg (Aug 2018)
- von Neumann, J.: Various techniques used in connection with random digits. In: Householder, A., Forsythe, G., Germond, H. (eds.) Monte Carlo Method, pp. 36–38. National Bureau of Standards Applied Mathematics Series, 12, Washington, D.C.: U.S. Government Printing Office (1951)
- Young, A., Yung, M.: The dark side of "black-box" cryptography, or: Should we trust capstone? In: Koblitz, N. (ed.) CRYPTO'96. LNCS, vol. 1109, pp. 89–103. Springer, Heidelberg (Aug 1996)
- Young, A., Yung, M.: Kleptography: Using cryptography against cryptography. In: Fumy, W. (ed.) EUROCRYPT'97. LNCS, vol. 1233, pp. 62–74. Springer, Heidelberg (May 1997)