# Fault-Injection Attacks against NIST's Post-Quantum Cryptography Round 3 KEM Candidates

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Abstract. We investigate *all* NIST PQC Round 3 KEM candidates from the viewpoint of fault-injection attacks: Classic McEliece, Kyber, NTRU, Saber, BIKE, FrodoKEM, HQC, NTRU Prime, and SIKE. All KEM schemes use variants of the Fujisaki-Okamoto transformation, so the equality test with re-encryption in decapsulation is critical.

We survey effective key-recovery attacks when we can skip the equality test. We found the existing keyrecovery attacks against Kyber, NTRU, Saber, FrodoKEM, HQC, one of two KEM schemes in NTRU Prime, and SIKE. We propose a new key-recovery attack against the other KEM scheme in NTRU Prime. We also report an attack against BIKE that leads to leakage of information of secret keys.

The open-source pqm4 library contains all KEM schemes except Classic McEliece and HQC. We show that giving a single instruction-skipping fault in the decapsulation processes leads to skipping the equality test *virtually* for Kyber, NTRU, Saber, BIKE, and SIKE. We also report the experimental attacks against them. We also report the implementation of NTRU Prime allows chosen-ciphertext attacks freely and the timing side-channel of FrodoKEM reported in Guo, Johansson, and Nilsson (CRYPTO 2020) remains, while there are no such bugs in their NIST PQC Round 3 submissions.

**keywords:** post-quantum cryptography, NIST PQC standardization, KEM, the Fujisaki-Okamoto transformation, fault-injection attacks.

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# 1 Introduction

# 1.1 Background

**Key encapsulation mechanism:** Public-key encryption (PKE in short) allows us to send a message secretly without a pre-shared secret key [DH76, RSA78, Sin99], which is a fundamental task of cryptography. PKE consists of three algorithms; a key-generation algorithm that generates a public key and a secret key, an encryption

algorithm that takes a message and a public key as input and outputs a ciphertext, and a decryption algorithm that takes a secret key and a ciphertext as input and outputs a message.

Key encapsulation mechanism (KEM in short) is also fundamental cryptographic primitive [Sho00, CS03, ISO06], which can be considered as a variant of public-key encryption (PKE). KEM's encryption algorithm, which we call the encapsulation algorithm, takes a public key as input and outputs a ciphertext and *a key* (or an ephemeral key). KEM's decryption algorithm, which we call the decapsulation algorithm, takes a secret key and a ciphertext as input and outputs a key instead of a message. KEM's sender and receiver share a key instead of a message in the case of PKE. KEM is a versatile primitive and has a lot of applications, e.g., key exchange, hybrid encryption, secure authentication, and authenticated key exchange.

The most standard security notion of KEM is indistinguishability against chosen-ciphertext attacks (IND-CCA-security) [RS92, CS03]. Since it is hard to construct efficient IND-CCA-secure KEMs directly, cryptographers often use the transformations from weakly-secure PKE/KEM into IND-CCA-secure KEM. The Fujisaki-Okamoto (FO) transformation [FO99, FO13, Den03] is one of the transformations often used in the design of IND-CCA-secure PKE/KEM in the random oracle model (ROM). Roughly speaking, the FO transformation transforms an underlying PKE scheme into KEM as follows: Let G and H be two random oracles. A key-generation algorithm of KEM is that of PKE. An encapsulation algorithm on input a public key *pk* chooses a message *m* randomly, encrypts it into ct = Enc(pk, m; G(m)), where Enc is an encryption algorithm of PKE and the randomness of encryption is computed as G(m), and outputs a ciphertext *ct* and a key K = H(m). A decapsulation algorithm on input *sk* and *ct* decrypts *ct* into m' = Dec(sk, ct), where Dec is a decryption algorithm of PKE, re-encrypts m' into ct' = Enc(pk, m'; G(m')), and outputs a key K = H(m') if ct = ct' and a rejection symbol otherwise.

*Post-quantum cryptography:* Scalable quantum computers will threaten classical public-key cryptography since Shor's algorithm on a quantum machine solves factorization and discrete logarithms efficiently [Sho94]. The recent progress in developing quantum machines motivates us to replace classical public-key cryptography with post-quantum cryptography (PQC). Hence, in the past decade, the security proofs of the FO transformation and its variants have been extended to those in the quantum random oracle model (QROM) [BDF<sup>+</sup>11] to show the security against *quantum* polynomial-time adversary. See e.g., [TU16, HHK17, SXY18, JZC<sup>+</sup>18, BHH<sup>+</sup>19, JZM19, KSS<sup>+</sup>20].

Moreover, in 2016, NIST PQC standardization called for proposals on PKE/KEM and signatures as the basic primitives <sup>4</sup>. In 2020, NIST selected four finalists and five alternate candidates for KEM in Round 3 [AAA<sup>+</sup>20]. All use the FO-like transformations to construct IND-CCA-secure KEMs in the (Q)ROM.

**Fault-injection attacks:** In the real world, the decapsulation algorithm is implemented physically. Hence, investigations into side-channel attacks (SCA) [Koc96, KJJ99] and fault-injection attacks (FIA) [BS97, BDL01] against proposed KEMs are strongly promoted by NIST. The attacks' targets are recovery of an ephemeral key of a given ciphertext or a secret key of a given public key. We call the former and the latter ephemeral-key-recovery attack and key-recovery attack, respectively.

We focus on FIA against KEM and review the scenario of it. Suppose that an adversary can inject faults into a decapsulation machine that contains a secret key. In this situation, it is natural to think the adversary has the machine itself (e.g., decapsulation machines in card, sensor, robot, and TV box) and uses it freely because the adversary can physically access the machine. Hence, the adversary can decrypt any ciphertexts and recover the corresponding ephemeral key of the target ciphertext. Thus, if we consider FIA, ephemeral-key-recovery attacks are not so important.

On the other hand, recovery of secret key via FIA is non-trivial and interesting, because the key-recovery attack logically breaks a tamper-resilient memory by extracting the secret from it. In addition, once one obtains a secret key from a decapsulation machine, one can copy the machine. Thus, we examine how FIA leads to a key-recovery attack.

There are a lot of techniques to make decapsulation faulty; shooting a LASER to set/reset a bit of SRAM [SA03], injecting a clock or power glitch [SMR09, ?, ESH<sup>+</sup>11, BBPP09], using electromagnetic (EM) pulses [HHS<sup>+</sup>11]. (Un)fortunately, an injection of fault often fails to obtain an expected result, say, a skip of an instruction of the assembly code. Thus, the less number of faults in a single run of decapsulation an attack requires, the better. Especially, we are interested in *single-fault* key-recovery attacks.

<sup>&</sup>lt;sup>4</sup> https://csrc.nist.gov/Projects/post-quantum-cryptography/post-quantum-cryptography-standardization/ Call-for-Proposals

Skipping-the-equality-test attack: In the FO-like transformations, the decapsulation algorithm given a ciphertext ct first decrypts the ciphertext into m', re-encrypts it into ct', and returns K = H(m', aux) if ct = ct' and pseudorandom value K = H(s, aux) or the rejection symbol  $\perp$  otherwise, where H is a hash function modeled by a random oracle, aux depends on pk and ct, and s is a secret value.

By injecting a fault carefully, we could force the decapsulation machine to *skip* the equality test ct = ct' and return K = H(m', aux) always, where m' = Dec(sk, ct). This enables us to implement a plaintext-checking oracle on input guess  $m_{guess}$  and ciphertext ct by checking if  $K = H(m_{guess}, aux)$  or not and a key-mismatch oracle on input guess  $K_{guess}$  and ciphertext ct by checking if  $K = K_{guess}$  or not. Such oracles would enable an adversary to mount a key-recovery attack against KEM.

*Fault-injection attack against pre-quantum KEMs:* Factoring/RSA-based PKE/KEM is vulnerable against FIA. For example, safe-error attacks [YJ00, YKLM02] are effective to guess a bit of secret key. They are also applicable to Discrete-logaritm (DL)-based PKE/KEM. DL-based PKE/KEM has several attack surfaces vulnerable to FIA. See, for example, invalid point/curve attacks [BMM00, BG15, ABM<sup>+</sup>03, TT19].

We note that the existing key-recovery FIAs do not target the equality test of the FO transformation. It is not known whether this plaintext-checking/key-mismatch oracle (or even decryption oracle) enables us to recover the secret key of the underlying PKE, say, the textbook RSA. (See e.g., [BV98] and [AM09].) Thus, the key-recovery FIA against pre-quantum KEMs that skips the equality test are not so explored.

*Fault-injection attack against post-quantum KEMs:* This situation is changed in post-quantum KEMs. Unfortunately, underlying PKEs in the post-quantum PKE/KEMs are often vulnerable to key-recovery chosen-ciphertext attacks. For example, Hall, Goldberg, and Schneier [HGS99] pointed out message-recovery and key-recovery chosen-ciphertext attacks against the McEliece PKE [McE78, Nie86] and the Ajtai-Dwork PKE [AD97], respectively. Fluhrer pointed out that a simple key-exchange scheme based on ring learning with errors (RLWE) is vulnerable to the key-mismatch attack if a user fixes its secret [Flu16]. Galbraith, Petit, Shani, and Ti [GPST16] gave a key-recovery key-mismatch attack against SIDH [JD11, DJP14] with fixed secret. Therefore, the equality test is an important target of FIA.

Although Pessl and Prokop [PP21] pointed out that the equality test is 'an obvious faulting target,' we do not know how easily we can mount a skipping-the-equality-test attack by injecting a single fault against the implementations in the wild and how effective the skipping-the-equality-test attack is against the NIST PQC Round 3 KEM candidates.

### 1.2 Our Contribution

We systematically study how effective fault-injection attacks that lead to the skip of the equality test of FO-like transformations are against *all* KEMs in the NIST PQC Round 3 finalists and the alternates: Classic McEliece [ABC<sup>+</sup>20], Kyber [SAB<sup>+</sup>20], NTRU (ntruhps and ntruhrss) [CDH<sup>+</sup>20], Saber [DKR<sup>+</sup>20], BIKE [ABB<sup>+</sup>20], FrodoKEM [NAB<sup>+</sup>20], HQC [AAB<sup>+</sup>20], NTRU Prime (sntrupr and ntrulpr) [BBC<sup>+</sup>20], and SIKE [JAC<sup>+</sup>20]. We summarize our findings in Table 1.

**Theoretical analysis:** We study whether the underlying PKEs of KEMs are resilient to key-recovery plaintextchecking attacks (KR-PCA) or not, since skipping the equality test enables an adversary to obtain K = H(Dec(sk, ct), aux)instead of pseudorandom string or  $\bot$  and to implement a plaintext-checking oracle easily.

We found that almost all PKEs except the underlying PKE of Classic McEliece leaks information of the decryption key in the presence of plaintext-checking oracle *in vitro*. Our findings are summarized as follows (see also Table 2):

- **Kyber, NTRU, Saber, FrodoKEM, HQC, sntrupr of NTRU Prime, and SIKE:** We survey the literature and found that there are KR-PCAs against the underlying PKEs of Kyber, ntruhps and ntruhrss of NTRU, Saber, FrodoKEM, HQC, sntrupr of NTRU Prime, and SIKE.
- **ntrulpr of NTRU Prime:** We propose a KR-PCA against the underlying PKE of NTRU LPRime (ntrulpr of NTRU Prime) by mimicking the KR-PCAs against the underlying PKEs of Saber and Kyber [HV20]. See section 4.
- **BIKE:** The underlying PKE of BIKE in round 3 also leaks the secret key's information from the plaintextchecking oracle as QC-MDPC [MTSB13] is vulnerable to the KR-PCA proposed by Guo, Johansson, and Stankvoski [GJS16]. However, the change of a decoder algorithm in round 3 makes key-recovery attacks difficult. See subsection C.5.

Table 1: Summary of our findings on NIST PQC Round 3 KEM Candidates (finalists and alternates) and their implementations in pqm4: PCA implies plaintext-checking attack.

Name	Effect of PCA	Attack Surface in pqm4	Effect of FIA in pqm4
Classic McEliece [ABC <sup>+</sup> 20]	Unknown	N/A	N/A
Kyber [SAB <sup>+</sup> 20]	Key recovery	Skip	Key recovery
NTRU – ntruhps [CDH <sup>+</sup> 20]	Key recovery	Skip	Key recovery
NTRU – ntruhrss [CDH <sup>+</sup> 20]	Key recovery	Skip	Key recovery
Saber [DKR <sup>+</sup> 20]	Key recovery	Skip	Key recovery
BIKE [ABB <sup>+</sup> 20]	Key leakage (New)	Skip	Key leakage
FrodoKEM [NAB <sup>+</sup> 20]	Key recovery	Timing bug	Key recovery
HQC [AAB <sup>+</sup> 20]	Key recovery	N/A	N/A
NTRU Prime – sntrupr [BBC <sup>+</sup> 20	] Key recovery	CCA bug	Key recovery
NTRU Prime – ntrulpr [BBC <sup>+</sup> 20	] Key recovery (New	) CCA bug	Key recovery
SIKE [JAC <sup>+</sup> 20]	Key recovery	Skip	Key recovery

Table 2: Theoretical plaintext-checking attacks and key-mismatch attacks against the underlying PKEs of NIST PQC Round 3 KEM Candidates.

Name	Results
Classic McEliece [ABC <sup>+</sup> 20]	Unknown
Kyber [SAB <sup>+</sup> 20]	Key recovery [QCD19, RRCB20, HV20, QCZ <sup>+</sup> 21]
NTRU – ntruhps [CDH <sup>+</sup> 20]	Key recovery [DDS <sup>+</sup> 19]
NTRU – ntruhrss [CDH <sup>+</sup> 20]	Key recovery [ZCQD21]
Saber [DKR <sup>+</sup> 20]	Key recovery [HV20, QCZ <sup>+</sup> 21]
BIKE [ABB <sup>+</sup> 20]	Key leakage (New, adapted KR-PCA against QC-MDPC [GJS16])
FrodoKEM [NAB <sup>+</sup> 20]	Key recovery [BDH <sup>+</sup> 19, RRCB20, VV20, QCZ <sup>+</sup> 21]
HQC [AAB <sup>+</sup> 20]	Key recovery [HV20]
NTRU Prime – sntrupr [BBC <sup>+</sup> 20]	Key recovery [REB <sup>+</sup> 21]
NTRU Prime – ntrulpr [BBC <sup>+</sup> 20]	Key recovery (New, adapted KR-PCA against Kyber, Saber, and FrodoKEM)
SIKE [JAC <sup>+</sup> 20]	Key recovery [GPST16]

**Classic McEliece:** There are no known KR-PCAs against the underlying PKE of Classic McEliece if the decoder in a decryption algorithm rejects invalid plaintexts <sup>5</sup> (We note that the specifications seem to allow the use of any decoder that decodes binary Goppa codes.)

*Trade-off:* Skipping the equality test enables the adversary to obtain K = KDF(m, aux) with m = Dec(sk, ct) rather than the plaintext-checking oracle. Thus, the adversary can check if  $m = m_{guess}$  by checking  $K = KDF(m_{guess}, aux)$  from *a single faulty experiment*. If the number of candidates of *m* is small, then we can determine the value of *m* by an exhaustive search. By using this property, there are trade-offs between the computational cost and the number of faulty experiments in the cases of Kyber, Saber, FrodoKEM, and ntrulpr of NTRU Prime. See the details in section 4 for the case of ntrulpr of NTRU Prime.

**Investigation of KEMs in pqm4:** We investigate implementation of KEMs in pqm4 [KRSS], which include Kyber, NTRU (ntruhps and ntruhrss), Saber, BIKE, FrodoKEM, NTRUPrime (sntrupr and ntruhpr), and SIKE <sup>6</sup>

- **NTRU Prime:** In the pqm4 implementation of NTRU Prime (sntrupr and ntrulpr), a decapsulation program contains a fatal bug that forces the result of the equality test to be true. <sup>7</sup> Thus, we can mount a chosen-ciphertext attack against them freely. See subsection 5.1.
- **FrodoKEM:** In 2020, Guo et al. [GJN20] pointed out that the implementation of FrodoKEM (and HQC) contains a leaky equality test that leaks information of the secret key from the timing side channel and succeeded

<sup>&</sup>lt;sup>5</sup> The plaintext space is a set of *n*-dimensional vectors whose Hamming weight is *t*.

<sup>&</sup>lt;sup>6</sup> We use 2021 Jun. 5 version. https://github.com/mupq/pqm4/commit/8d3384d879b10619c8c36947e4be6ab13ec6d268.

<sup>&</sup>lt;sup>7</sup> We report it in https://github.com/mupq/pqm4/issues/195

in mounting a key-recovery attack using the timing information. Although FrodoKEM in Round 3 repaired this leaky equality test, the bug still remains in the pqm4 implementation.<sup>8</sup> See subsection 5.2.

- **Kyber, NTRU, and Saber:** They shared a same structure to compute a key. Roughly speaking, decapsulation programs use a flag for the equality test and overwrite the decrypted result *m*' by a secret seed *s* if the flag is set. This overwriting is done by a single function call of 'cmov' (conditional-move). (Un)fortunately, we can skip this function call by a single fault and mount FIA. See subsection 5.3
- **BIKE:** The decapsulation program of BIKE in pqm4 computes mask, which is -1 or 0 depending on the reencryption check, and overwrites the decryption result m' by a secret seed s or keep it as " $m' \leftarrow (m' \land \neg \text{mask}) \lor (s \land \text{mask})$ ". <sup>9</sup> (Un)fortunately, we identify a single operation such that if we skip the operation, then mask is set to 0 always. Thus, we can skip the overwrite procedure virtually by a single fault. See subsection 5.4.
- **SIKE:** The implementation of SIKE in pqm4 simply uses an 'if' statement to overwrite the decrypted result *m*' by a secret seed s. In the assembly code, this if-then-overwrite is implemented as 'compare' and 'conditional jump'. (Un)fortunately, we can skip this 'conditional jump' by a single fault. See subsection 5.5.

**Experimental results:** On the basis of our findings, we conduct the experimental skip attacks on Kyber, NTRU, Saber, BIKE, and SIKE. The target is STM32F415 whose core is ARM Cortex-M4, which is a de-facto standard platform as NIST suggested. We run 100 fault injections to each scheme and succeeded in injecting faults correctly with 15–50%. See section 6.

## 1.3 Related Works

For PQC candidates and their implementation, we recommend the reader to read an exhaustive survey written by Howe, Prest, and Apon [HPA21]. Ravi and Roy gave a lecture on SCAs and FIAs against lattice-based PQC candidates [RR21]. Costello wrote a survey of isogeny-based cryptography [Cos21]. For SCA, FIA, and key-recovery plaintext-checking/key-mismatch attacks against NIST PQC KEM Candidates, see our survey in Appendix C.

### 1.4 Organization

Section 2 reviews basic notions and notations. Section 3 reviews the variants of the FO transformation. Section 4 gives a key-recovery attack against ntrulpr of NTRU Prime using plaintext-checking oracle and discusses a tradeoff between efficiency and the number of queries if we consider the fault-injection attack. Section 5 describes the equality test of KEMs and how we can mount skipping attack. Section 6 reports our experimental results. Appendix A contains missing definitions, say, security notions of PKE and KEM. Appendix B also reviews the variants of the FO transformation. Appendix C reviews the KEM schemes and KR-PCAs against all of them and includes our report of key-leakage PCAs against BIKE.

# 2 Preliminaries

#### 2.1 Notation

A security parameter is denoted by  $\lambda$ . We use the standard *O*-notations. DPT, PPT, and QPT stand for deterministic polynomial-time, probabilistic polynomial-time, and quantum polynomial-time, respectively. A function  $f(\lambda)$  is said to be *negligible* if  $f(\lambda) = \lambda^{-\omega(1)}$ . We denote a set of negligible functions by negl( $\lambda$ ). For a statement *P* (e.g.,  $r \in [0, 1]$ ), we define boole(*P*) = 1 if *P* is satisfied and 0 otherwise.

For a distribution  $\chi$ , we often write " $x \leftarrow \chi$ ," which indicates that we take a sample x in accordance with  $\chi$ . For a finite set S, U(S) denotes the uniform distribution over S. We often write " $x \leftarrow S$ " instead of " $x \leftarrow U(S)$ ." If inp is a string, then "out  $\leftarrow A(inp)$ " denotes the output of algorithm A when run on input inp. If A is deterministic, then out is a fixed value and we write "out := A(inp)." We use the notation "out := A(inp; r)" to make the randomness r explicit.

For an odd positive integer q, we define  $r' := r \mod^{\pm} q$  to be the unique element  $r' \in [-(q-1)/2, (q-1)/2]$ with  $r' \equiv r \pmod{q}$ .

<sup>&</sup>lt;sup>8</sup> pqm4 noticed this issue. See https://github.com/mupq/pqm4/issues/161.

<sup>&</sup>lt;sup>9</sup> If mask = 0, then we have  $m' \leftarrow m'$ . Otherwise, we have  $m' \leftarrow s$ .

## 2.2 Public-Key Encryption (PKE)

The model for PKE schemes is summarized as follows:

**Definition 2.1.** A PKE scheme PKE consists of the following triple of polynomial-time algorithms (Gen, Enc, Dec):

- Gen $(1^{\lambda}; r_g) \rightarrow (pk, sk)$ : a key-generation algorithm that takes as input  $1^{\lambda}$ , where  $\lambda$  is the security parameter, and randomness  $r_g \in \mathscr{R}_{Gen}$  and outputs a pair of keys (pk, sk). pk and sk are called the encryption key and decryption key, respectively.
- $Enc(pk, m; r_e) \rightarrow ct$ : an encryption algorithm that takes as input encryption key pk, message  $m \in \mathcal{M}$ , and randomness  $r_e \in \mathcal{R}_{Enc}$  and outputs ciphertext  $ct \in \mathcal{C}$ .
- $Dec(sk, ct) \rightarrow m/\perp$ : a decryption algorithm that takes as input decryption key sk and ciphertext ct and outputs message  $m \in \mathcal{M}$  or a rejection symbol  $\perp \notin \mathcal{M}$ .

**Definition 2.2.** We say a PKE scheme PKE is deterministic if Enc is deterministic, that is, it takes pk and m and does not take a randomness  $r_e$ . DPKE stands for deterministic public-key encryption.

*Plaintext-checking oracle:* Since we review and propose key-recovery attacks using plaintext-checking oracle (PCO), we formally review the definition of the plaintext-checking oracle [OP01, ABP15].

**Definition 2.3 (Plaintext-Checking Oracle).** A plaintext-checking oracle PCO takes as input a plaintext m and a ciphertext ct and outputs 1 if and only if m is equal to the decrypted result Dec(sk, ct). That is, PCO(m, ct) := boole(m = Dec(sk, ct)).

#### 2.3 Key Encapsulation Mechanism (KEM)

The model for KEM schemes is summarized as follows:

**Definition 2.4.** *A KEM scheme* KEM *consists of the following triple of polynomial-time algorithms* (Gen, Encaps, Decaps):

- Gen $(1^{\lambda}; r_g) \rightarrow (pk, sk)$ : a key-generation algorithm that takes as input  $1^{\lambda}$ , where  $\lambda$  is the security parameter, and randomness  $r_g \in \mathscr{R}_{Gen}$  and outputs a pair of keys (pk, sk). pk and sk are called the encapsulation key and decapsulation key, respectively.
- Encaps $(pk; r_e) \rightarrow (ct, K)$ : an encapsulation algorithm that takes as input encapsulation key pk and randomness  $r_e \in \mathscr{R}_{Encaps}$  and outputs ciphertext  $ct \in \mathscr{C}$  and key  $K \in \mathscr{K}$ .
- Decaps $(sk, ct) \rightarrow K/\perp$ : a decapsulation algorithm that takes as input decapsulation key sk and ciphertext ct and outputs key K or a rejection symbol  $\perp \notin \mathscr{K}$ .

*Key-mismatch oracle:* We review the key-mismatch oracle, which is an analogue of the plaintext-checking oracle for PKE.

**Definition 2.5 (Key-Mismatch Oracle).** A key-mismatch oracle KMO takes as input a key K and a ciphertext ct and outputs 1 if and only if K is equal to the decapsulated result Decaps(sk, ct). That is, KMO(K, ct) := boole(K = Decaps(sk, ct)).

# 3 Variants of the Fujisaki-Okamoto Transformation

We review the variants of the FO transformation that are used by NIST PQC Round 3 candidate KEMs:  $FO^{\ell}$  in this section and  $FO^{\ell'}$ ,  $FO^{\ell''}$ ,  $HFO^{\ell}$ ,  $HFO^{\ell}$ , SXY, and  $HU^{\ell'}$  in section B.

Let PKE = (Gen, Enc, Dec) be a PKE, whose ciphertext space is  $\mathscr{C}_{PKE}$ . If PKE is probabilistic, then  $\mathscr{R}_{Enc}$  denotes the randomness space of Enc. Let  $\{0, 1\}^{k(\lambda)}$  be the key space of KEM.

$Gen(1^{\lambda})$	Encaps( <i>pk</i> )	$Decaps(\overline{sk}, ct)$ , where $\overline{sk} = (sk, pk, s)$
$(pk, sk) \leftarrow \operatorname{Gen}(1^{\lambda})$	$m \leftarrow \{0,1\}^{\ell(\lambda)}$	$m' := \operatorname{Dec}(sk, ct)$
$s \leftarrow \{0, 1\}^{\ell(\lambda)}$	r := G(m) //  for BIKE	r' := G(m') // for BIKE
$\overline{sk} := (sk, pk, s)$	r := G(m, pk) //  for SIKE	r' := G(m', pk) //  for SIKE
<b>return</b> $(pk, \overline{sk})$	$ct := \operatorname{Enc}(pk, m; r)$	$ct' := \operatorname{Enc}(pk, m'; r')$
	K := H(m, ct)	if $ct = ct'$ , then return $K := H(m', ct)$
	return $(K, ct)$	else return $K := H(s, ct)$

Fig. 1: KEM :=  $FO^{\perp}[PKE, G, H]$  for BIKE and SIKE.

## 3.1 FO with implicit rejection

 $FO^{\perp}$  transforms a weakly-secure probabilistic PKE into IND-CCA-secure KEM, where the identifier " $\perp$ " implies *implicit rejection* [HHK17]. This variant is used by BIKE and SIKE.

Let  $\{0, 1\}^{\ell(\lambda)}$  be the plaintext space of PKE. Let  $G : \{0, 1\}^* \to \mathscr{R}_{Enc}$  and  $H : \{0, 1\}^{\ell(\lambda)} \times \mathscr{C}_{PKE} \to \{0, 1\}^{k(\lambda)}$  be hash functions modeled by the random oracles. The FO<sup> $\ell$ </sup> is summarized as Figure 1. Assuming the IND-CPA security of PKE, the obtained KEM scheme is IND-CCA-secure in the QROM (see e.g., [KSS<sup>+</sup>20]).

*Remark 3.1.* BIKE and SIKE do *not* test whole re-encryption check. Roughly speaking, their encryption algorithm Enc is separable into two algorithms  $Enc_1$  and  $Enc_2$ .  $Enc_1$  takes pk and randomness r and outputs  $c_1$  and  $k \in \{0, 1\}^{\ell(\lambda)}$ .  $Enc_2$  takes m and k and outputs  $c_2 := k \oplus m$ .

Using this property, BIKE omits the re-encryption check. Concretely speaking, k in BIKE's Enc<sub>1</sub> is computed as k := H(r), where H is a hash function modeled by the random oracle. BIKE's Dec internally obtains r' and checks the validity of  $c_1$ . It then retrieves  $m' := c_2 \oplus H(r')$  and checks the validity of the ciphertext by checking r' = G(m') or not.

SIKE's Decaps performs the test  $c'_1 = c_1$  but omits the test  $c'_2 = c_2$ . Since Dec retrieves  $m' := c_2 \oplus k$  deterministically, we do not need to check the equality of  $c_2$  and  $c'_2$ .

# 4 Key-Recovery Plaintext-Checking Attack against ntrulpr of NTRU Prime

We propose a new key-recovery attack using plaintext-checking oracle against ntrulpr of NTRU Prime [BBC<sup>+</sup>20]. NTRU LPRime (ntrulpr) is a variant of the LPR PKE [LPR10], which is also based on the Lindner–Peikert PKE [LP11], and has a similar structure to Kyber and Saber. We mimic the KR-PCA against Kyber and Saber proposed by Băetu et al. [BDH<sup>+</sup>19] and Huguenin-Dumittan and Vaudenay [HV20].

*ntrulpr of NTRU Prime:* NTRU LPRime has parameter sets  $p, q, w, \delta, \tau_0, \tau_1, \tau_2$ , and  $\tau_3$ . We note that q = 6q' + 1 for some q' and  $q \ge 16w + 2\delta + 3$ . For concrete values, see Table 3.

parameter sets	p	q	w	δ	$ au_0$	$ au_1$	$ au_2$	$ au_3$
ntrulpr653	653	4621	252	289	2175	113	2031	290
ntrulpr761	761	4591	250	292	2156	114	2007	287
ntrulpr857	857	5167	281	329	2433	101	2265	324
ntrulpr953	953	6343	345	404	2997	82	2798	400
ntrulpr1013	1013	7177	392	450	3367	73	3143	449
ntrulpr1277	1277	7879	429	502	3724	66	3469	496

Table 3: Parameter sets of ntrulpr of NTRU Prime

Let  $\mathscr{R} := \mathbb{Z}[x]/(x^p - x - 1)$  and  $\mathscr{R}_q := \mathbb{Z}_q[x]/(x^p - x - 1)$ . Let  $\mathscr{S} := \{a = \sum_{i=0}^{p-1} a_i x^i \in \mathscr{R} \mid a_i \in \{-1, 0, +1\}, HW(a) = w\}$ , a set of "short" polynomials.

Tał	ole 4: The PC	O's behaviors
$sk_i$	$PCO(\vec{1}_{256}, ct_0)$	$PCO(\vec{1}_{256}, ct_1)$
1	1	1
0	1	0
-1	0	0

For  $a \in [-(q-1)/2, (q-1)/2]$ , define Round $(a) = 3 \cdot [a/3]$ .<sup>10</sup> For a polynomial  $A = \sum_i a_i x^i \in \mathcal{R}_q$ , we define trunc $(A, l) = (a_0, \dots, a_{l-1}) \in \mathbb{Z}_q^l$ . For  $C \in [0, q)$ , define Top $(C) = \lfloor (\tau_1(C + \tau_0) + 2^{14})/2^{15} \rfloor$ . For  $T \in [0, 16)$ , define Right $(T) = \tau_3 T - \tau_2 \in \mathbb{Z}_q$ . For  $a \in \mathbb{Z}$ , define Sign(a) = 1 if a < 0, 0 otherwise.

The underlying CPA-secure PKE scheme<sup>11</sup> works as follows:

- Gen(*pp*): Generate  $A \leftarrow \mathcal{R}_q$  and  $sk \leftarrow \mathcal{S}$ . Compute  $B := \text{Round}(A \cdot sk)$ . Output pk := (A, B) and sk.
- $\text{Enc}(pk, \mu \in \{0, 1\}^{256})$ : Choose  $t \leftarrow S$  and output

 $(U, V) := (\text{Round}(t \cdot A), \text{Top}(\text{trunc}(t \cdot B, 256) + \mu(q-1)/2)).$ 

- Dec(sk, (U, V)): Compute  $r := \text{Right}(V) - \text{trunc}(sk \cdot U, 256) + (4w + 1) \cdot \vec{1}_{256} \in \mathbb{Z}^{256}$  and outputs  $m := \text{Sign}(r \mod^{\pm} q)$ .

## 4.1 Key-Recovery Attack

We mainly follow the KR-PCAs against Kyber and Saber in Baetu et al. [BDH<sup>+</sup>19] and Huguenin-Dumittan and Vaudenay [HV20], but we need some tweaks. Roughly speaking, to determine the *i*-th coefficient of *sk*, their attack queries  $(a, b \cdot x^i)$  with constant *a* and *b* and a candidate plaintext, because in the case of Kyber and Saber, the dimension of *V* is the same as that of the base ring. However, ntrulpr truncates *tB* to reduce redundancy, so we need to modify the query ciphertext. Note that we can *shift* the effect of *sk<sub>i</sub>* into *constant coefficient* by multiplying  $x^{p-i}$ . That is, for i = 1, ..., p-1 and  $sk = sk_0 + sk_1x + ... sk_{p-1}x^{p-1} \in \mathcal{R}$ , we have

$$x^{p-i} \cdot sk = sk_i + (sk_i + sk_{i+1})x + (sk_{i+1} + sk_{i+2})x^2 + \dots + (sk_{p-2} + sk_{p-1})x^{p-i-1} + (sk_{p-1} + sk_0)x^{p-i} + sk_1x^{p-i+1} + sk_2x^{p-i+2} + \dots + sk_{i-1}x^{p-1}.$$

Using this relation, we show the following two lemmas:

**Lemma 4.1 (For general**  $i \in [1, p)$ ). Let  $c = \tau_2 - (4w + 1)$ ,  $b = \lfloor (c - 1)/6 \rfloor \cdot 3$  and  $t_\beta = \lfloor (\beta b + c - 1)/\tau_3 \rfloor$  for  $\beta \in \{0, 1\}$ . Let us consider our test ciphertext  $ct_\beta = (b \cdot x^{p-i}, (t_\beta, 0, ..., 0))$  for  $\beta \in \{0, 1\}$  and candidate plaintext  $\vec{1}_{256}$ . Then, we have the relations between the *i*-th coordinate of decryption key and the behavior of PCO as in Table 4.

*Proof.* The decryption algorithm computes  $r = \text{Right}((t_{\beta}, 0, ..., 0)) - \text{trunc}(sk \cdot b \cdot x^{p-i}, 256) + (4w + 1) \cdot \vec{1}_{256}$ . Expanding this, we have

$$\begin{cases} r_0 = \tau_3 t_\beta - b \cdot sk_i - c, \\ r_j = -b \cdot (sk_{i+j-1 \mod p} + sk_{i+j \mod p}) - c & (j = 1, 2, \dots, \min\{256, p - i\}) \\ r_j = -b \cdot sk_{j-(p-i) \mod p} - c & (j = p - i + 1, \dots, \min\{256, p - 1\}). \end{cases}$$

Recall that  $sk_i \in \{-1, 0, +1\}$  for all *i* since *sk* is in  $\mathscr{S}$ . Thus, we have  $r_j \in \{-2b - c, -b - c, -c, b - c, 2b - c\}$  for j = 1, ..., 256. Since we set  $b = \lfloor (c-1)/6 \rfloor \cdot 3 \leq (c-1)/2$ , we have -2b - c > -2c and 2b - c < 0. Fortunately, we have  $-2c = -2\tau_2 - 8w - 2 \geq -(q-1)/2$  for all parameter sets. Thus,  $r_j$ 's are decoded into 1 for j = 1, ..., 256.

Let us consider  $r_0$ . We have

$$r_0 = \tau_3 t_\beta - b \cdot sk_i - c > 0 \iff (\tau_3 t_\beta - c)/b > sk_i$$

By our setting, if  $t_{\beta} = t_0$  (and  $t_1$ ), then  $(\tau_3 t_{\beta} - c)/b$  is slightly smaller than 0 (and 1) for all parameter sets, respectively. In addition, we have  $\tau_3 t_1 + b - c \le (q - 1)/2$  for all parameter sets. Therefore,  $r_0$  for  $t_0$  is decoded into 0 if and only if  $sk_i < 0$  and  $r_0$  for  $t_1$  is decoded into 0 if and only if  $sk_i < 1$ . This completes the proof.

<sup>&</sup>lt;sup>10</sup> When q = 6q' + 1, Round([-(q-1)/2, (q-1)/2])  $\in [-(q-1)/2, (q-1)/2]$ .

<sup>&</sup>lt;sup>11</sup> 'NTRU LPRime Core' in the specification.

By a similar argument, we have the following lemma on  $sk_0$ .

**Lemma 4.2** (*i* = 0). Let  $c = \tau_2 - (4w + 1)$ ,  $b = \lceil (c - 1)/6 \rceil \cdot 3$  and  $t_\beta = \lfloor (\beta b + c - 1)/\tau_3 \rfloor$  for  $\beta \in \{0, 1\}$ . Let us consider our test ciphertext  $ct_\beta = (b, (t_\beta, 0, ..., 0))$  and candidate plaintext  $\vec{1}_{256}$ . Then, we have the relations between the constant term of decryption key and the behavior of PCO as in Table 4.

Using the above lemmas, we can determine  $sk_i$  for i = 0, ..., p - 1 by testing 2p queries with the PCO.

#### 4.2 Trade-Off

We observe that an adversary can obtain K' = H(m', ct) by skipping the equality test instead of the equality of K' and  $K_{guess}$  or the equality of m' and  $m_{guess}$ . Therefore, the adversary can check if  $m' = m_{guess}$  or not by computing  $K_{guess} = H(m_{guess}, ct)$  by itself. This enables the adversary to determine  $\ell$  coefficients of the secret key at once by sacrificing the computational efficiency.

For simplicity, we let  $\ell = 2^k < 256$ .

Determine  $sk_{y\ell}, \dots, sk_{y\ell+\ell-1}$  for  $y = 0, \dots, 256/\ell - 1$ : Let us determine  $\ell$  coefficients  $sk_{y\ell}, \dots, sk_{y\ell+\ell-1}$  of sk at once, where  $y = 0, \dots, 256/\ell - 1$ . Suppose that we query two ciphertexts

$$ct_{\beta} = (U, V_{\beta}) = \left(b, \underbrace{(0, \dots, 0)}_{\ell}, \underbrace{t_{\beta}, \dots, t_{\beta}}_{\ell}, \underbrace{256 - (y+1)\ell}_{0, \dots, 0}\right)\right)$$

for  $\beta \in \{0, 1\}$ . The decryption algorithm computes  $r = \text{Right}(V_{\beta}) - \text{trunc}(sk \cdot b, 256) + (4w + 1) \cdot \vec{1}_{256}$ . Expanding this, we have

$$r_{j} = \begin{cases} \tau_{3}t_{\beta} - b \cdot sk_{j} - c & (j = y\ell, \dots, y\ell + \ell - 1) \\ -b \cdot sk_{j} - c & (j = 0, \dots, y\ell - 1, (y + 1)\ell, \dots, 256). \end{cases}$$

By using the argument in the proof of Lemma 4.1,  $r_j$ 's are decoded into 1 for j = 0, ..., yl - 1, (y + 1)l, ..., 256. We also have, for j = yl, ..., yl + l - 1,  $r_j$  for  $t_1$  is decoded into 0 if and only if  $sk_i < 0$  and  $r_j$  for  $t_2$  is decoded into 0 if and only if  $sk_i < 1$ .

Seeing  $K = H(m', ct_{\beta})$  where  $m' = \text{Dec}(sk, ct_{\beta})$ , we compute  $K_{\text{guess}} = H(m_{\text{guess}}, ct_{\beta})$  for  $m_{\text{guess}} = \vec{1}_{y\ell} ||m''|| \vec{1}_{256-(y+1)\ell}$  for all  $m'' \in \{0, 1\}^{\ell}$  and determine  $sk_j$  for  $j = y\ell, ..., y\ell + \ell - 1$ .

Determine  $sk_{y\ell}, ..., sk_{y\ell+\ell-1}$  for  $y = 256/\ell, ..., \lfloor p/\ell \rfloor$ : Suppose that we have determined  $y\ell$  coefficients  $sk_0, ..., sk_{y\ell-1}$  for some  $y \in \{256/\ell, ..., \lfloor p/\ell \rfloor\}$ . Let us determine  $\ell$  coefficients  $sk_{y\ell}, ..., sk_{y\ell+\ell-1}$  at once: Let  $t_{\beta} = \lfloor (\beta b + c - 1)/\tau_3 \rfloor$  for  $\beta \in \{-1, 0, 1, 2\}$ . Suppose that we query four ciphertexts

$$ct_{\beta} = (U, V_{\beta}) = \left(b \cdot x^{p-y\ell-1}, (0, \overline{t_{\beta}, \dots, t_{\beta}}, \overline{0, \dots, 0})\right)$$

for  $\beta \in \{-1, 0, 1, 2\}$ . The decryption algorithm computes  $r = \text{Right}(V_{\beta}) - \text{trunc}(sk \cdot bx^{p-y\ell-1}, 256) + (4w+1) \cdot \vec{1}_{256}$ . Expanding this, we have

$$r_{j} = \begin{cases} -b \cdot sk_{y\ell-1} - c & (j = 0) \\ \tau_{3}t_{\beta} - b \cdot (sk_{y\ell+j-2 \mod p} + sk_{y\ell+j-1 \mod p}) - c & (j = 1, 2, \dots, \ell) \\ -b \cdot (sk_{y\ell+j-2 \mod p} + sk_{y\ell+j-1 \mod p}) - c & (j = \ell + 1, \dots, \min\{256, p - y\ell\}) \\ -b \cdot sk_{j-(p-i) \mod p} - c & (j = \min\{256, p - y\ell + 1\}, \dots, 256). \end{cases}$$

By using the argument in the proof of Lemma 4.1,  $r_j$ 's are decoded into 1 for j = 0 and  $j = \ell + 1, ..., 256$ .

Let us consider  $r_j$  for  $j = 1, ..., \ell$ . We have

$$r_j = \tau_3 t_\beta - b \cdot (sk_j + sk_{j+1}) - c > 0 \iff (\tau_3 t_\beta - c)/b > sk_j + sk_{j+1}$$

By our setting,  $(\tau_3 t_\beta - c)/b$  is slightly smaller than  $\beta$  for all parameter sets, respectively. In addition, we have  $-(q-1)/2 \le \tau_3 t_\beta - 2b - c$  and  $\tau_3 t_\beta + 2b - c \le (q-1)/2$  for all parameter sets. Therefore,  $r_j$  for  $t_\beta$  is decoded into 0 if and only if  $sk_i < \beta$ .

Seeing  $K' = H(m', ct_{\beta})$  where  $m' = \text{Dec}(sk, ct_{\beta})$ , we compute  $K_{\text{guess}} = H(m_{\text{guess}}, ct_{\beta})$  for  $m_{\text{guess}} = 1 ||m''|| \vec{1}_{256-\ell-1}$  for all  $m'' \in \{0, 1\}^{\ell}$  and determine  $sk_{y\ell+j-2} + sk_{y\ell+j-1} \in \{-2, -1, 0, 1, 2\}$  for  $j = 1, ..., \ell$ . Since we know  $sk_{y\ell-1}$ , we can determine  $sk_{y\ell}, ..., sk_{y\ell+\ell-1}$  sequentially.

# 5 Skipping the Equality Test by Skipping a Single Instruction

In this section, we describe the fault-injection attack on the equality checking of each KEM implementation. First, we examine the implementation of pqm4 [KRSS] for each scheme and discuss the possibility of skipping the equivalence test. To identify the instructions to be skipped, we cross-compiled the C code in pqm4 with GCC 8.3.1 running on Debian bullseye. The compilation options were basically according to pqm4, with "-O3" as an optimization option.

We do not mention the attacks on Classic McEliece and HQC in this section because pqm4 does not include their ARM Cortex M4-optimized code. Hereafter, we describe the possibility of skip attacks on NTRU Prime, FrodoKEM, Kyber, Saber, NTRU, BIKE, and SIKE.

If the reader is unfamiliar to Arm Cortex M4, please see the manual  $^{12}$ .

## 5.1 NTRU Prime - CCA Bug

The functions in the C code related to the FO-like transformation are crypto\_kem\_dec, Decap, and Ciphertexts\_diff\_mask.<sup>13</sup> Figure 2 shows the source code of NTRU Prime's comparison in pqm4. Note that we omit the crypto\_kem\_dec function as it just calls Decap.

Let us consider how Ciphertexts\_diff\_mask computes the return value. It initializes the uint16 variable differentbits as 0. After some computations, it outputs ((-1)-((differentbits-1)»31)) in line 17. The value is initialized as 0 and *unchanged* before the return value is computed; these computations only involve differentbits2. Thus, we eventually obtain 0 as the result of (-1)-((0-1)»31) and ciphertexts\_diff\_mask always outputs 0.

Decap first decrypts r := Dec(sk, c) in line 13 and encodes it into r\_enc and re-encrypts it into cnew in line 14. In line 15, mask is always 0, since Ciphertexts\_diff\_mask always returns 0 as we explained. Thus, r\_enc, which is the result of faulty decryption, is unchanged, and Decap always sets k as the result of H(1,r\_enc,c). This means that there is no re-encryption check and the implementation opens the attack surface of chosen-ciphertext attacks.

# 5.2 FrodoKEM – Timing Attack

The decapsulation of FrodoKEM is performed in the crypto\_kem\_dec function.<sup>14</sup> Figure 3 shows the source code of the equality test in the function. From the source code, this function uses the memcmp function *with* && to compare the ciphertext and the re-encryption result. This indicates that the current implementation is still vulnerable to the timing attack by Guo et al. [GJN20].

### 5.3 Kyber, Saber, and NTRU - cmov

In this subsection, we describe the skip attacks on Kyber, Saber, and NTRU among the finalists. The basic idea of the skip attacks on these implementations is identical, and thus we describe the case of Saber as an example to explain the skip attack procedure. Figure 4 shows the crypto\_kem\_dec function that performs the decapsulation of FO transformation<sup>15</sup>.

The crypto\_kem\_dec function performs re-encryption using the indcpa\_kem\_enc\_cmp function at line 13 and stores the comparison results of the ciphertext and the re-encryption result into a variable fail. If these ciphertexts are not the same, fail becomes 1 and, if they are the same, fail becomes 0. At line 15, the cmov substitutes a random value for kr when fail is 1. Note here that the hash value calculated from the decrypted result is stored in the variable kr before cmov is called, and this means that we can perform a key-recovery attack by skipping the call of cmov even when fail is 1.

Figure 5 shows the assembly code corresponding to the call of cmov. This program first calls the sha3\_256 function at line 1, prepares the arguments of cmov at line 4–7, calls cmov at line 8, and finally prepares the arguments and call the sha3\_256 function at line 10–14. From this code, we notice that Saber can be attacked by skipping b1 cmov at line 8 using fault injection. In addition to Saber, NTRU and Kyber also use cmov in the same manner, and therefore, this attack can be applied to all of them.

<sup>&</sup>lt;sup>12</sup> https://developer.arm.com/documentation/100166/0001. See https://developer.arm.com/documentation/100166/0001/ Programmers-Model/Instruction-set-summary/Table-of-processor-instructions?lang=en for instruction set.

<sup>&</sup>lt;sup>13</sup> The source code of these functions is https://github.com/mupq/pqm4/blob/master/crypto\_kem/sntrup761/m4f/kem.c.

<sup>&</sup>lt;sup>14</sup> https://github.com/mupq/pqm4/blob/master/crypto\_kem/frodokem640shake/m4/kem.c

<sup>&</sup>lt;sup>15</sup> https://github.com/mupq/pqm4/blob/master/crypto\_kem/saber/m4f/kem.c

```
1 static int Ciphertexts_diff_mask(const unsigned char *c,
2
                                                     const unsigned char *c2)
3
   {
     uint16 differentbits = 0;
4
     int len = Ciphertexts_bytes+Confirm_bytes;
5
6
7
     int *cc = (int *)(void *)c;
     int *cc2 = (int *)(void *)c2;
8
     int differentbits2 = 0;
9
10
     for (len-=4 ;len>=0; len-=4) {
       differentbits2 = __USADA8((*cc++),(*cc2++),differentbits2);
11
12
13
     c = (unsigned char *)(void *) cc;
14
     c2 = (unsigned char *)(void *) cc2;
     for (len &= 3; len > 0; len--)
15
       differentbits2 =__USADA8((*c++),(*c2++),differentbits2);
16
17
     return ((-1)-((differentbits-1)>>31));
18 }
```

```
static void Decap(unsigned char *k, const unsigned char *c,
1
2
                                                      const unsigned char *sk)
3
   {
     const unsigned char *pk = sk + SecretKeys_bytes;
4
     const unsigned char *rho = pk + PublicKeys_bytes;
5
     const unsigned char *cache = rho + Inputs_bytes;
6
7
     Inputs r;
8
     unsigned char r_enc[Inputs_bytes];
9
     unsigned char cnew[Ciphertexts_bytes+Confirm_bytes];
10
     int mask;
11
     int i;
12
13
     ZDecrypt(r,c,sk);
     Hide(cnew,r_enc,r,pk,cache);
14
15
     mask = Ciphertexts_diff_mask(c,cnew);
     for (i = 0;i < Inputs_bytes;++i) r_enc[i] ^= mask&(r_enc[i]^rho[i]);</pre>
16
17
     HashSession(k,1+mask,r_enc,c);
18
   }
```

Fig. 2: NTRU Prime's comparison in pqm4.

```
// Is (Bp == BBp & C == CC) = true
if (memcmp(Bp, BBp, 2 * PARAMS_N * PARAMS_NBAR) == 0 &&
    memcmp(C, CC, 2 * PARAMS_NBAR * PARAMS_NBAR) == 0) {
    // Load k' to do ss = F(ct || k')
    memcpy(Fin_k, kprime, CRYPTO_BYTES);
} else {
    // Load s to do ss = F(ct || s)
    memcpy(Fin_k, sk_s, CRYPTO_BYTES);
}
shake(ss, CRYPTO_BYTES, Fin, CRYPTO_CIPHERTEXTBYTES + CRYPTO_BYTES);
```

Fig. 3: FrodoKEM's comparison in pqm4

```
1
       int crypto_kem_dec(uint8_t *k, const uint8_t *c, const uint8_t *sk)
2
   {
3
       uint8_t fail;
4
       uint8_t buf[64];
5
       uint8_t kr[64]; // Will contain key, coins
       const uint8_t *pk = sk + SABER_INDCPA_SECRETKEYBYTES;
6
7
       const uint8_t *hpk = sk + SABER_SECRETKEYBYTES - 64;
                                        // Save hash by storing h(pk) in sk
8
9
10
       indcpa_kem_dec(sk, c, buf);
       memcpy(buf + 32, hpk, 32);
11
12
       sha3_512(kr, buf, 64);
13
       fail = indcpa_kem_enc_cmp(buf, kr + 32, pk, c);
14
       sha3_256(kr + 32, c, SABER_BYTES_CCA_DEC);
15
       cmov(kr, sk + SABER_SECRETKEYBYTES - SABER_KEYBYTES,
16
                                                       SABER_KEYBYTES, fail);
17
       sha3_256(k, kr, 64);
18
       return (0);
19
   }
20
```



```
bl sha3_256
1
2
    .LVL26:
    .loc 1 79 3 is_stmt 1 view .LVU62
3
        uxtb r3, r7
add r1, r4, #1536
4
5
6
         add r0, sp, #64
7
         movs
                 r2, #32
8
         bl cmov
9
    .LVL27:
         .loc 1 82 3 view .LVU63
10
                 r2, #64
11
         movs
         mov r0, r6
12
13
         add r1, sp, r2
         bl sha3_256
14
```

Fig. 5: Assembly code of Saber's comparison in pqm4

#### 5.4 BIKE – For loop

We describe the skip attack on BIKE in this subsection. Figure 6 shows the C code of BIKE's comparison in the decapsulation<sup>16</sup>. We also show secure\_cmp function and secure\_132\_mask function in Figure 7. Line 4–5 in Figure 6 compares the hash value of the original message and that of the decrypted message from the ciphertext. Then, if they are equal, the for block at line 9–12 stores the decrypted message into m\_prime.raw[i]. Therefore, the goal of the fault-injection attack is to store the decrypted message even when these hash values differ. For this purpose, we need to force the variable mask to be 0.

Figure 8 shows the assembly code corresponding to the line 5–7 in the C code to explain the position of a fault injection. Line 1–30 and line 31–44 in the assembly code correspond to line 5 and line 7 in the C code, respectively. The operation we need to skip for a key-recovery attack is "ldr r2, [sp, #20]" at line 33 in this assembly code for the following reason.

Before line 33 in the assembly code, the r2 register is used in "cmp r2, #0" at line 26. This corresponds to "return (0 == res);" at line 11 in secure\_cmp function (Figure 7). Therefore, at this time, the r2 register contains the value of the res variable. The value of the r2 register does not become 0 from the attack assumption because the value of the res variable is not 0 when the two arguments of secure\_cmp are not equal. Thus, the r2 register must be a non-zero value if line 33 in the assembly code is skipped. After line 33, the value of the r2 register is used at line 41. This line corresponds to line 8 in the secure\_l32\_mask function (Figure 7). The secure\_l32\_mask function compares the two arguments v1 and v2 and returns 0 when v1 < v2 holds. mask becomes 0 when v2 is not 0 because v1 is 0 as shown in Figure 6. Meanwhile, we note that the variable v2 does not become 0 when we skip line 33 in the assembly code because the r2 register corresponds to the v2 variable. From the above, we can fix mask to 0 by the fault injection, and thus the key-recovery attack is possible.

```
// Check if H(m') is equal to (e0', e1')
1
2
     // (in constant-time)
3
     GUARD(function_h(&e_tmp, &m_prime));
     success_cond = secure_cmp(PE0_RAW(&e_prime), PE0_RAW(&e_tmp), R_BYTES);
4
5
     success_cond &= secure_cmp(PE1_RAW(&e_prime), PE1_RAW(&e_tmp), R_BYTES);
6
7
     // Compute either K(m', C) or K(sigma, C) based on the success condition
8
     mask = secure_132_mask(0, success_cond);
9
     for(size_t i = 0; i < M_BYTES; i++) {</pre>
10
       m_prime.raw[i] &= u8_barrier(~mask);
11
       m_prime.raw[i] |= (u8_barrier(mask) & l_sk.sigma.raw[i]);
12
     }
```

Fig. 6: BIKE's comparison in pqm4.

# 5.5 SIKE – Simple If

This subsection describe the skip attack on SIKE. Figure 9 and Figure 10 shows the C code and its assembly of the comparison process in the FO transformation<sup>17</sup>.

The target of fault injection in C code is the if statement at line 3–4. The assembly code in Figure 10 corresponds to the if statement. The process of condition in the if statement at line 3 in the C code corresponds to line 1-4 in the assembly code. In the assembly code, "b1 memcmp" compares the variables  $c0_$  and ct. If they differ, "cbnz r0, .L500" performs a jump to line 28. Note that, even if we jump to line 28, the procedure comes back to line 5 because of "b .L495" at line 40. In other words, line 28–40 in the assembly code correspond to the process in the if block at line 4 in the C code. Thus, we can perform the skip attack on SIKE by injecting a fault into "cbnz r0, .L500" at line 3.

<sup>&</sup>lt;sup>16</sup> https://github.com/mupq/pqm4/blob/master/crypto\_kem/bikel1/m4f/kem.c

<sup>&</sup>lt;sup>17</sup> https://github.com/mupq/pqm4/blob/master/crypto\_kem/sikep434/m4/sike.inc

```
1
   _INLINE_ uint32_t secure_cmp(IN const uint8_t *a,
                                 IN const uint8_t *b,
2
                                 IN const uint32_t size)
3
4
   {
5
     volatile uint8_t res = 0;
6
     for(uint32_t i = 0; i < size; ++i) {</pre>
7
       res |= (a[i] ^ b[i]);
8
9
     }
10
     return (0 == res);
11
12
   }
1 // Return 0 if v1 < v2, (-1) otherwise
2
   _INLINE_ uint32_t secure_l32_mask(IN const uint32_t v1,
3
                                                IN const uint32_t v2)
4
   {
5
     // If v1 >= v2 then the subtraction result is 0^{32}||(v1-v2).
     // else it is 1^{32}|(v^2-v^1+1). Subsequently, negating the upper
6
7
     // 32 bits gives 0 if v1 < v2 and otherwise (-1).
8
     return ~((uint32_t)(((uint64_t)v1 - (uint64_t)v2) >> 32));
9
   }
```

Fig. 7: secure\_cmp and secure\_132\_mask function of BIKE in pqm4.

1 .L26: 2 .loc 1 69 5 is\_stmt 1 view .LVU627 r2, [r5, #1]! 3 ldrb .LVL169: 4 .loc 1 69 9 view .LVU629 5 r4, [r1, #1]! 6 ldrb 7 r3, [sp, #18] ldrb 8 eors r2, r2, r4 9 orrs r3, r3, r2 10 .loc 1 68 3 view .LVU630 11 cmp r0, r5 .loc 1 69 9 view .LVU631 12 13 strb r3, [sp, #18] .LVL170: 14 .loc 1 68 3 view .LVU632 15 .L26 16 bne .LBE629: 17 18 .loc 1 72 3 is\_stmt 1 view .LVU633 19 .LVL171: 20.loc 1 72 13 is\_stmt 0 view .LVU634 r2, [sp, #18] 21 ldrb .LBE628: 22 23 .LBE627: .loc 2 278 16 view .LVU635 24 r3, [sp, #20] 25 ldr cmp 26 r2, #0 27 ite ne r3, #0 28 movne 29 andeq r3, r3, #1 30 str r3, [sp, #20] 31 .loc 2 282 3 is\_stmt 1 view .LVU636 .loc 2 282 10 is\_stmt 0 view .LVU637 32 33 ldr r2, [sp, #20] .LVL172: 34 .LBB630: 35 .LBI630: 36 37 .loc 1 113 19 is\_stmt 1 view .LVU638 38 .LBB631: 39 .loc 1 140 3 view .LVU639 40 .loc 1 140 37 is\_stmt 0 view .LVU640 41 rsbs r2, r2, #0 42 sbc r3, r3, r3 .loc 1 140 10 view .LVU641 43 r5, r3 44 mvns

#### Fig. 8: Assembly code of BIKE's comparison in pqm4

```
1 // Generate shared secret ss <- H(m||ct) or output ss <- H(s||ct)
2 EphemeralKeyGeneration_A(ephemeralsk_, c0_);
3 if (memcmp(c0_, ct, CRYPT0_PUBLICKEYBYTES) != 0) {
4 memcpy(temp, sk, MSG_BYTES);
5 }
6 memcpy(&temp[MSG_BYTES], ct, CRYPT0_CIPHERTEXTBYTES);
7 shake256(ss, CRYPT0_BYTES, temp, CRYPT0_CIPHERTEXTBYTES+MSG_BYTES);
```

Fig. 9: SIKE's comparison in pqm4

```
1
        bl memcmp
        .loc 5 88 8 view .LVU4945
2
3
                r0, .L500
        cbnz
   .LVL1930:
 4
   .L495:
 5
        .loc 5 91 5 is_stmt 1 view .LVU4946
 6
 7
        mov r1, r4
 8
        add r0, sp, #508
 9
        mov r2, #346
10
        bl memcpy
11
    .LVL1931:
        .loc 5 92 5 view .LVU4947
12
13
        mov r0, r8
14
        add r2, sp, #492
15
        mov r3, #362
        movs
                r1, #16
16
17
        bl shake256
18
    .LVL1932:
19
        .loc 5 94 5 view .LVU4948
        .loc 5 95 1 is_stmt 0 view .LVU4949
20
               r0, #0
21
        movs
22
        add sp, sp, #856
23
   .LCFI116:
24
        .cfi_remember_state
25
        .cfi_def_cfa_offset 24
26
        pop {r4, r5, r6, r7, r8, pc}
27
   .LVL1933:
28
   .L500:
29
   .LCFI117:
30
        .cfi_restore_state
31
        .loc 5 89 9 is_stmt 1 view .LVU4950
32
        ldr r0, [r5]
33
        ldr r1, [r5, #4]
34
        ldr r2, [r5, #8]
35
        ldr r3, [r5, #12]
        add r5, sp, #492
36
37
    .LVL1934:
38
        .loc 5 89 9 is_stmt 0 view .LVU4951
39
        stmia
              r5!, {r0, r1, r2, r3}
40
        b
            .L495
```

Fig. 10: Assembly code of SIKE's comparison in pqm4



Fig. 11: Experimental setup overview.

|--|

Name	# failures	# Successes	Expected # required queries	Expected time [s]
Kyber – Kyber512	60	52	5908	626
NTRU – ntruhps2048509	74	46	2235	384
Saber – LightSaber	33	33	15515	1,567
BIKE – Bikel1	49	34	-	-
SIKE – sikep434	30	15	1787	19, 478

# 6 Experimental Attacks

In this section, we conduct the experimental skip attacks on the pqm4 implementation of the above mentioned KEM schemes. The target schemes in this section are Kyber, NTRU, Saber, BIKE, and SIKE, which were shown to be attackable by a single fault injection in the previous section. In this experiment, we used the parameters of the security level 1 for all schemes.

### 6.1 Setup

Figure 11 shows the experimental environment. The target chip under attack is an STM32F415 microcontroller with an ARM Cortex M4 core, which is a de-facto standard platform to evaluate software implementation of schemes running in NIST's PQC process. The target device is mounted on a ChipWhisperer cw308 UFO baseboard, which enables us to perform fault-injection attacks using a glitchy clock. The ChipWhisperer cw1200 capture box is used to generate the base clock, and the clock frequency was set to 24 MHz. The glitch parameters for instruction skipping were searched by sweeping the parameters to find the one that successfully skips the instruction. We use the implementation in pqm4 for each KEM scheme, and "O3" was specified as an optimization option during compilation.

## 6.2 Results

Table 5 reports the experimental results of the proposed skip attacks. In Table 5, we show the number of times when a fault occurred on the device and the number of successful instruction skips when we performed 100 fault injections for each scheme. Also, the table shows the number of required queries to recover the secret key

from each scheme using fault injection.<sup>1819</sup> These required query numbers are calculated by multiplying the minimum required number of queries for a key-recovery attack and the inverse of the success rate of a skip attack. We only omitted the number of required queries for the case of BIKE in this table because it is difficult to fully recover the secret key. We also show the expected time to recover the secret key for each scheme. From the table, we confirm that the probability of a successful attack was about 15-50%, and there is a difference in the probability of successful attacks among Saber, Kyber, and NTRU, although the fault-injection capability is almost the same. This would be because of the difference in instructions before and after the call of the cmov function that affects the state of pipeline registers in the microcontroller.

In addition, in this experiment, the injected faults did not always cause a single instruction skip as expected and sometimes crashed the device, which led to a non-negligible cost for an oracle access. A similar phenomenon was also observed in [PP21] in fault-injection attacks on lattice KEMs using ChipWhisperer, and more sophisticated equipment for fault injection should achieve higher attack stability.

## 7 Countermeasure

*Default fail:* The one of major countermeasures is the 'default fail' technique, which initiates a variable with the fail result and if a condition is satisfied then the variable is overwritten by the sensitive data [EHiH<sup>+</sup>14].

Recall Saber's decapsulation in Figure 4: We want to compute  $K = H(\bar{K}', H(ct))$  or H(s, H(ct)) depending on the re-encryption test result, where  $\bar{K}'$  is computed from the decrypted result m' and pk and s is a secret seed (see Figure 14 in Appendix B.1). If we skip the function call of cmov, then  $\bar{K}'$  in kr is unchanged and we obtain  $K = H(\bar{K}', H(ct))$  as the faulty decapsulation result. According to the 'default fail' technique, we put a secret seed s as the *default* value of kr and apply cmov to overwrite s by  $\bar{K}'$  depending on the value flag. (In addition, we will need to clear the original  $\bar{K}'$ .) If it was, then skipping cmov results in K = H(s, H(ct)) irrelevant to the decrypted result m'.

Moreover, a concrete assembly-level implementation of conditional branch resistant to single instruction skipping by default fail was presented in [EHiH<sup>+</sup>14]. Their countermeasure enables that sensitive instruction(s) should be performed only if a condition is surely tested and satisfied. In other words, if the condition test is skipped by a single-fault attack, the implementation with their countermeasure always outputs the rejection.

*Instruction duplication:* The other major countermeasures is the 'assembly-level instruction duplication' technique: If every instructions are duplicated carefully, then a single-fault instruction skipping attack is ineffective. See, e.g., [BBK<sup>+</sup>10] for the effectiveness and cost.

*Random delay:* Random delays are yet another major countermeasure of fault-injection analysis. If a random delay is inserted, then it is hard to determine the timing for injecting a fault. See, e.g., [CK09] for such technique.

# 8 Conclusion

From the viewpoint of fault-injection attacks, we have investigate *all* NIST PQC Round 3 KEM candidates, which use variants of the FO transformation. We survey effective key-recovery attacks if we can skip the equality test.

We found the existing key-recovery attacks against Kyber, NTRU, Saber, FrodoKEM, HQC, and SIKE (Table 2). We have proposed a new key-recovery attack against ntrulpr of NTRU Prime. We also pointed out trade-offs between the number of queries and computational costs when the target is Kyber, Saber, or ntrulpr. We also reported attacks against sntrupr of NTRU Prime and BIKE that lead to leakage of information of secret keys.

The open-source pqm4 library contains Kyber, NTRU, Saber, BIKE, FrodoKEM, NTRU Prime, and SIKE. We show that giving a single instruction-skipping fault in the decapsulation processes leads to skipping the equality test *virtually* for Kyber, NTRU, Saber, BIKE, and SIKE. We also report the implementation of NTRU Prime allows chosen-ciphertext attacks freely and the timing side-channel of FrodoKEM reported in Guo et al. [GJN20] remains.

Finally, we have reported the experimental attacks against Kyber, NTRU, Saber, BIKE, and SIKE on pqm4. We also discuss possible countermeasures.

<sup>&</sup>lt;sup>18</sup> In practice, we may need more queries than the values shown in the table, because the value of the secret key may occasionally carry an error due to an inserted fault. For simplicity, we ignore such situations here.

<sup>&</sup>lt;sup>19</sup> On Saber and Kyber, we have trade-offs between the number of expected queries and efficiency. In this table, we use  $\ell = 1$ .

Table 6: Summary of our findings on NIST PQC Round 3 KEM Candidates (finalists and alternates) and their implementations in pqm4: PCA implies plaintext-checking attack.

Name	Effect of PCA	Attack Surface in pqm4	Effect of FIA in pqm4
Classic McEliece [ABC <sup>+</sup> 20]	Unknown	N/A	N/A
Kyber [SAB <sup>+</sup> 20]	Key recovery	Skip	Key recovery
NTRU – ntruhps [CDH <sup>+</sup> 20]	Key recovery	Skip	Key recovery
NTRU – ntruhrss [CDH <sup>+</sup> 20]	Key recovery	Skip	Key recovery
Saber [DKR <sup>+</sup> 20]	Key recovery	Skip	Key recovery
BIKE [ABB <sup>+</sup> 20]	Key leakage (New)	Skip	Key leakage
FrodoKEM [NAB <sup>+</sup> 20]	Key recovery	CCA bug (Timing)	Key recovery
HQC [AAB <sup>+</sup> 20]	Key recovery	N/A	N/A
NTRU Prime – sntrupr [BBC <sup>+</sup> 20]	Key recovery	CCA bug	Key recovery
NTRU Prime – ntrulpr [BBC <sup>+</sup> 20]	Key recovery (New)	CCA bug	Key recovery
SIKE [JAC <sup>+</sup> 20]	Key recovery	Skip	Key recovery

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$Expt^{^{\mathrm{ow-cpa}}}_{PKE,\mathscr{D}_{\mathscr{M}},\mathscr{A}}\!$	$Expt^{\mathrm{ind-cpa}}_{PKE,\mathscr{A}}(\lambda)$
$(pk, sk) \leftarrow \text{Gen}(1^{\lambda})$	$b \leftarrow \{0, 1\}$
$m^* \leftarrow \mathscr{D}_{\mathscr{M}}$	$(pk, sk) \leftarrow \text{Gen}(1^{\lambda})$
$ct^* \leftarrow Enc(pk, m^*)$	$(m_0, m_1, st) \leftarrow \mathscr{A}_1(pk)$
$m' \leftarrow \mathscr{A}(pk, ct^*)$	$ct^* \leftarrow \operatorname{Enc}(pk, m_b)$
<b>return</b> boole( $m' \stackrel{?}{=} \text{Dec}(sk, ct^*)$ )	$b' \leftarrow \mathscr{A}_2(ct^*, st)$
	<b>return</b> boole( $b' \stackrel{?}{=} b$ )

Fig. 12: Games for PKE schemes

# **Supplementary Materials**

## **A** Missing Definitions

*Notation:* For a statement P (e.g.,  $r \in [0, 1]$ ), we define boole(P) = 1 if P is satisfied and 0 otherwise.

For a positive integer q, we define  $r' := r \mod^+ q$  to be the unique element  $r' \in [0, q)$  with  $r' \equiv r \pmod{q}$ . For an even positive integer q, we define  $r' := r \mod^{\pm} q \pmod{r'} := r \mod^{\pm} q$ , resp.) to be the unique element  $r' \in (-q/2, q/2] \pmod{r'} \in [-q/2, q/2]$ , resp.) with  $r' \equiv r \pmod{q}$ . For an element  $x \in \mathbb{R}$ , we define  $[x] = [x-1/2] \in \mathbb{Z}$ , which is the nearest integer.

*Security Notions of PKE:* We define onewayness under chosen-plaintext attacks (OW-CPAsecurity) and indistinguishability under chosen-plaintext attacks (IND-CPAsecurity) for a PKE.

**Definition A.1 (Security notions for PKE).** Let  $\mathcal{D}_{\mathcal{M}}$  be a distribution over the message space  $\mathcal{M}$ . For any adversary  $\mathcal{A}$ , we define its OW-CPA and IND-CPA advantages against a PKE scheme PKE = (Gen, Enc, Dec) as follows:

$$\begin{aligned} \mathsf{Adv}_{\mathsf{PKE},\mathscr{D}_{\mathcal{M}},\mathscr{A}}^{\mathrm{ow-cpa}}(\lambda) &:= \Pr[\mathsf{Expt}_{\mathsf{PKE},\mathscr{D}_{\mathcal{M}},\mathscr{A}}^{\mathrm{ow-cpa}}(\lambda) = 1],\\ \mathsf{Adv}_{\mathsf{PKE},\mathscr{A}}^{\mathrm{ind-cpa}}(\lambda) &:= \big| \Pr[\mathsf{Expt}_{\mathsf{PKE},\mathscr{A}}^{\mathrm{ind-cpa}}(\lambda) = 1] - 1/2 \big|, \end{aligned}$$

where  $\operatorname{Expt}_{\mathsf{PKE}, \mathscr{D}_{\mathcal{M}}, \mathscr{A}}^{\operatorname{ow-cpa}}(\lambda)$  and  $\operatorname{Expt}_{\mathsf{PKE}, \mathscr{A}}^{\operatorname{ind-cpa}}(\lambda)$  are experiments described in Figure 12. We say that PKE is OW-CPAsecure and IND-CPA-secure if  $\operatorname{Adv}_{\mathsf{PKE}, \mathscr{D}_{\mathcal{M}}, \mathscr{A}}^{\operatorname{ow-cpa}}(\lambda)$  and  $\operatorname{Adv}_{\mathsf{PKE}, \mathscr{A}}^{\operatorname{ind-cpa}}(\lambda)$  is negligible for any PPT adversary  $\mathscr{A}$ , respectively. We omit  $\mathscr{D}_{\mathcal{M}}$  from OW-CPA security if  $\mathscr{D}_{\mathcal{M}}$  is the uniform distribution over  $\mathscr{M}$ .

*Security Notions of KEM:* We define indistinguishability under chosen-ciphertext attacks (IND-CCA security) for KEM.

**Definition A.2.** For any adversary  $\mathcal{A}$ , we define its IND-CCA advantage against a KEM scheme KEM = (Gen, Encaps, Decaps) as follows:

$$\operatorname{Adv}_{\operatorname{KEM},\mathscr{A}}^{\operatorname{ind-cca}}(\lambda) := \left| \operatorname{Pr}[\operatorname{Expt}_{\operatorname{KEM},\mathscr{A}}^{\operatorname{ind-cca}}(\lambda) = 1] - 1/2 \right|,$$

where  $\text{Expt}_{\text{KEM},\mathscr{A}}^{\text{ind-cca}}(\lambda)$  is an experiment described in Figure 13. We say that KEM is IND-CCA-secure if  $\text{Adv}_{\text{KEM},\mathscr{A}}^{\text{ind-cca}}(\lambda)$  is negligible for any PPT adversary  $\mathscr{A}$ .

# **B** The variants of FO

# B.1 Other FO with implicit rejection

 $FO^{\ell'}$  and  $FO^{\ell''}$  are slightly modified versions of  $FO^{\ell}$ , which are used by Kyber [SAB<sup>+</sup>20, Section 1] and Saber [DKR<sup>+</sup>20, Section 8], and FrodoKEM [NAB<sup>+</sup>20, Section 2], respectively. The differences from  $FO^{\ell}$  are how to generate *K* in Encaps and Decaps.

$Expt^{\mathrm{ind-cca}}_{KEM,\mathscr{A}}(\lambda)$	$\operatorname{Dec}_{ct^*}(ct)$
$b \leftarrow \{0, 1\}$	if $ct = ct^*$ , return $\perp$
$(pk, sk) \leftarrow \text{Gen}(1^{\lambda})$	K := Decaps(sk, ct)
$(ct^*, K_0^*) \leftarrow Encaps(pk)$	return K
$K_1^* \leftarrow \mathscr{K}$	
$b' \leftarrow \mathcal{A}^{\text{Dec}_{ct^*}(\cdot)}(pk, ct^*, K_b^*)$	
<b>return</b> boole( $b' \stackrel{?}{=} b$ )	

Fig. 13: Games for KEM schemes

Let  $\{0, 1\}^{\ell(\lambda)}$  be the plaintext space of PKE. Let  $G : \{0, 1\}^* \to \{0, 1\}^{\ell(\lambda)} \times \mathscr{R}_{Enc}, H' : \{0, 1\}^* \to \{0, 1\}^{\ell(\lambda)}$ , and  $H : \{0, 1\}^{\ell(\lambda)} \times \{0, 1\}^{\ell(\lambda)} \to \{0, 1\}^{k(\lambda)}$  be hash functions modeled by the random oracles. FO<sup>*L*</sup> and FO<sup>*L*</sup> are summarized as Figure 14 and Figure 15, respectively.

One might consider assuming the IND-CPA security of PKE, the obtained KEM schemes are IND-CCA-secure in the QROM. Unfortunately, Grubbs, Maram, and Paterson [GMP21] pointed out that we cannot directly apply the existing security proof in the QROM to those variants, because computing *K* requires nested applications of random oracles G and H to *m*. Grubbs et al. overcome this barrier for the case of FO<sup> $\mathcal{L}''$ </sup> in [GMP21, Section 5.2]. However, they failed to apply their technique to the case of FO<sup> $\mathcal{L}'$ </sup> which computes  $K = H(\bar{K}, H'(ct))$  instead of  $K = H(\bar{K}, ct)$ . They left the IND-CCA security of FO<sup> $\mathcal{L}'$ </sup> in the QROM as an open problem [GMP21, Section 5.3].

$Gen(1^{\lambda})$	Encaps( <i>pk</i> )	Decaps( $\overline{sk}$ , $ct$ ), where $\overline{sk} = (sk, pk, h, s)$
$(pk, sk) \leftarrow \operatorname{Gen}(1^{\lambda})$	$m \leftarrow \{0, 1\}^{\ell(\lambda)}$	$m' := \operatorname{Dec}(sk, ct)$
$h \leftarrow H'(pk)$	m := H'(m)	$(\bar{K}',r'):=G(m',h)$
$s \leftarrow \{0,1\}^{\ell(\lambda)}$	$(\bar{K},r):={\rm G}(m,{\rm H}'(pk))$	$ct' := \operatorname{Enc}(pk, m'; r')$
$\overline{sk} := (sk, pk, h, s)$	$ct := \operatorname{Enc}(pk, m; r)$	if $ct = ct'$ , then return $K := H(\overline{K}', H'(ct))$
<b>return</b> $(pk, \overline{sk})$	$K := H(\bar{K}, H'(ct))$	else return $K := H(s, H'(ct))$
<u>,</u> ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	return $(K, ct)$	

Fig. 14: KEM  $:= FO^{\perp}(PKE, G, H', H]$  in Kyber and Saber.

$Gen(1^{\lambda})$	Encaps( <i>pk</i> )	Decaps( $\overline{sk}$ , $ct$ ), where $\overline{sk} = (sk, pk, h, s)$
$(pk, sk) \leftarrow \operatorname{Gen}(1^{\lambda})$	$m \leftarrow \{0,1\}^{\ell(\lambda)}$	$m' := \operatorname{Dec}(sk, ct)$
$h \leftarrow H'(pk)$	$(\bar{K},r) := \mathcal{G}(m,\mathcal{H}'(pk))$	$(\bar{K}',r'):=G(m',h)$
$s \leftarrow \{0,1\}^{\ell(\lambda)}$	$ct := \operatorname{Enc}(pk, m; r)$	$ct' := \operatorname{Enc}(pk, m'; r')$
$\overline{sk} := (sk, pk, h, s)$	$K := H(\bar{K}, ct)$	if $ct = ct'$ , then return $K := H(\bar{K}', ct)$
<b>return</b> $(pk, \overline{sk})$	return $(K, ct)$	else return $K := H(s, ct)$

Fig. 15: KEM :=  $FO^{\ell''}[PKE, G, H', H]$  in FrodoKEM.

# B.2 FO with additional hash

 $\text{HFO}^{\perp}$  and  $\text{HFO}^{\perp}$  (as known as  $\text{QFO}^{\perp}$  and  $\text{QFO}^{\perp}$ ) [TU16, HHK17, JZC<sup>+</sup>18, JZM19] transform a weakly-secure probabilistic PKE into IND-CCA-secure KEM like FO and add hash value of the message. Those variants are used by HQC and ntrulpr of NTRU Prime, respectively.

Let  $\{0, 1\}^{\ell(\lambda)}$  be the plaintext space of PKE. Let  $G : \{0, 1\}^* \to \mathscr{R}_{Enc}$ ,  $F : \{0, 1\}^{\ell(\lambda)} \times \{0, 1\}^* \to \{0, 1\}^{\ell'(\lambda)}$ ,  $H : \{0, 1\}^{\ell(\lambda)} \times (\mathscr{C}_{PKE} \times \{0, 1\}^{\ell'(\lambda)}) \to \{0, 1\}^{k(\lambda)}$ , and  $H_0 : \{0, 1\}^{\ell(\lambda)} \times (\mathscr{C}_{PKE} \times \{0, 1\}^{\ell'(\lambda)}) \to \{0, 1\}^{k(\lambda)}$  be hash functions modeled by the random oracles. The HFO<sup> $\perp$ </sup> and HFO<sup> $\perp'$ </sup> is summarized as Figure 16. Assuming the IND-CPA security of PKE, the obtained KEM scheme is IND-CCA-secure in the QROM. See e.g., [KSS<sup>+</sup>20]. For the case of explicit rejection HFO<sup> $\perp$ </sup>, we need to invoke [BHH<sup>+</sup>19, Theorem 4].

$Gen(1^{\lambda})$	Encaps( <i>pk</i> )	$Decaps(\overline{sk}, ct)$ , where $\overline{sk} = (sk, pk[, s])$
$(pk, sk) \leftarrow \text{Gen}(1^{\lambda})$	$m \leftarrow \{0,1\}^{\ell(\lambda)}$	$\overline{m' := \operatorname{Dec}(sk, ct)}$
$\overline{sk} := (sk, pk) // \text{ for HQC}$	$r := \mathbf{G}(m)$	$r' := \mathcal{G}(m')$
$s \leftarrow \{0, 1\}^{\ell(\lambda)} // \text{ for ntrulpr}$	$ct_0 := \operatorname{Enc}(pk,m;r)$	$ct'_0 := \operatorname{Enc}(pk, m'; r')$
$\overline{sk} := (sk, pk, s) // \text{ for ntrulpr}$	$ct_1 := F(m) // \text{ for HQC}$	$ct'_1 := F(m') // \text{ for HQC}$
return $(pk, \overline{sk})$	$ct_1 := F(m, pk) // \text{ for ntrulpr}$	$ct'_1 := F(m', pk) // $ for ntrulpr
4,	$ct := (ct_0, ct_1)$	$ct' := (ct'_0, ct'_1)$
	K := H(m, ct)	if $ct = ct'$ , then return $K := H(m', ct)$
	return $(K, ct)$	else return $K := \perp //$ for HQC
		<b>else return</b> $K := H_0(s, ct) // $ for ntrulpr

Fig. 16: KEM :=  $HFO^{\perp}$  [PKE, G, F, H, H<sub>0</sub>] for ntrulpr of NTRU Prime and  $HFO^{\perp}$  [PKE, G, F, H] for HQC.

### B.3 SXY

SXY transforms a weakly-secure *deterministic* PKE into IND-CCA-secure KEM. This variant is employed by NTRU (ntruhps and ntruhrss).

Let  $\mathcal{M}$  be the plaintext space of PKE. Let  $H : \mathcal{M} \to \{0, 1\}^{k(\lambda)}$  and  $H_0 : \{0, 1\}^{\ell(\lambda)} \times \mathscr{C}_{PKE} \to \{0, 1\}^{k(\lambda)}$  be hash functions modeled by the random oracles. The SXY is summarized as Figure 17. Assuming 'disjoint-simulatability'<sup>20</sup> of PKE, the obtained KEM scheme is IND-CCA-secure in the QROM [SXY18].

$Gen(1^{\lambda})$	Encaps( <i>pk</i> )	Decaps( $\overline{sk}$ , $ct$ ), where $\overline{sk} = (sk, pk, s)$
$(pk, sk) \leftarrow \text{Gen}(1^{\lambda})$	$m \leftarrow \mathcal{M}$	$m' := \operatorname{Dec}(sk, ct)$
$s \leftarrow \{0, 1\}^l$	ct := Enc(pk, m)	if $m' = \bot$ , then return $K := H_0(s, ct)$
$\overline{sk} := (sk, pk, s)$	K := H(m)	$ct' := \operatorname{Enc}(pk, m')$
<b>return</b> $(pk, \overline{sk})$	return $(K, ct)$	if $ct = ct'$ , then return $K := H(m')$
		else return $K := H_0(s, ct)$

Fig. 17: KEM := SXY[PKE, H, H<sub>0</sub>] in NTRU (ntruhps and ntruhrss).

*Remark B.1.* NTRU also omits an explicit re-encryption check invoking Enc. In NTRU, a ciphertext is c = hr + m, where h is a public key and  $(r, s) \in \mathcal{R} \times \mathcal{M}$  is a plaintext. The decryption algorithm first computes  $r' \in \mathcal{R}$ , computes m' = c - hr', and checks if (r', m') is in  $\mathcal{R} \times \mathcal{M}$  or not. This check is equivalent to checking c = hr' + m', because h is *invertible*. See [Sch18, Section 5.1] for the details. Bernstein and Persichetti dubbed this property *rigidity* [BP18].

<sup>&</sup>lt;sup>20</sup> Roughly speaking, disjoint-simulatability means that a random ciphertext is indistinguishable from a random string in  $\mathscr{C}_{\mathsf{PKE}}$ , that is,  $\mathsf{Enc}(pk, U(\mathscr{M})) \sim_c U(\mathscr{C}_{\mathsf{PKE}})$ , and  $\#(\mathsf{Enc}(pk, \mathscr{M}) \cap \mathscr{C}_{\mathsf{PKE}}) \ll \#\mathscr{C}_{\mathsf{PKE}}$ .

#### **B.4** HU with implicit rejection

The final one is a transformation that transforms a weakly-secure *deterministic* PKE into IND-CCA-secure KEM, employed by Classic McEliece and sntrupr of NTRU Prime. We interpret the transformation as a variant of HU [JZM19] (Or, we can interpret it as a variant of Dent4<sup> $\ell$ </sup> [Den03] or SXY-KC [SXY18]).

Let  $\mathcal{M}$  be the plaintext space of PKE. Let  $F: \mathcal{M} \to \{0, 1\}^{\ell'(\lambda)}$ . Let  $H: \mathcal{M} \times (\mathscr{C}_{PKE} \times \{0, 1\}^{\ell'(\lambda)}) \to \{0, 1\}^{k(\lambda)}$ and  $H_0: \{0, 1\}^{\ell(\lambda)} \times (\mathscr{C}_{PKE} \times \{0, 1\}^{\ell'(\lambda)}) \to \{0, 1\}^{k(\lambda)}$  be hash functions modeled by the random oracles.  $HU^{\mathcal{L}'}$  is summarized as Figure 18. Assuming 'disjoint-simulatability' of PKE, the obtained KEM scheme is IND-CCAsecure in the QROM [SXY18, JZM19, ABC<sup>+</sup>20].

$Gen(1^{\lambda})$	Encaps( <i>pk</i> )	Decaps( $\overline{sk}$ , $ct$ ), where $\overline{sk} = (sk, pk, s)$ and $ct = (ct_0, ct_1)$
$(pk, sk) \leftarrow \operatorname{Gen}(1^{\lambda})$	$m \leftarrow \mathcal{M}$	$m' := \operatorname{Dec}(sk, ct_0)$
$s \leftarrow \{0,1\}^\ell$	$ct_0 := \operatorname{Enc}(pk, m)$	if $m' = \bot$ , then return $K := H_0(s, ct)$
$\overline{sk} := (sk, pk, s)$	$ct_1 := F(m) // CM$	$ct'_0 := \operatorname{Enc}(pk, m')$
<b>return</b> ( $sk$ , $\overline{sk}$ )	$ct_1 := F(m, pk) // $ sntrupr	$ct'_1 := F(m') // \operatorname{CM}$
	$ct := (ct_0, ct_1)$	$ct'_1 := F(m', pk) // \text{ sntrupr}$
	K := H(m, ct)	$ct := (ct'_0, ct'_1)$
	<b>return</b> $(K, ct)$	if $ct = ct'$ , then return $K := H(m', ct)$
		else return $K := H_0(s, ct)$

Fig. 18: KEM :=  $HU^{\perp\prime}$ [PKE, F, H, H<sub>0</sub>] in Classic McEliece and sntrupr of NTRU Prime.

*Remark B.2.* One might wonder Decaps in Classic McEliece has no explicit re-encryption check ([ABC<sup>+</sup>20, Sec.2.3.3]). In their specification, Dec in Classic McEliece internally checks  $ct'_0 = \text{Enc}(pk, m')$  or not ([ABC<sup>+</sup>20, Sec.2.2.4]).

# C Survey of Key-Recovery Plaintext-Checking Attacks

## C.1 Classic McEliece

On the McEliece and Niederreiter PKE, we recommend to read an excellent servery by Engelbert, Overbeck, and Schmidt [EOS07]. To the best of the authors' knowledge, there are no key-recovery plaintext-checking attack against the McEliece and Niederreiter PKE [McE78, Nie86].

*Review of Classic McEliece:* Classic McEliece [ABC<sup>+</sup>20] is based on the Niederreiter PKE, in which a public key is a scrambled parity-check matrix, a plaintext is an error vector, and a ciphertext is a syndrome.

Table 7: Parameter sets of Classic McEliece in Round 3. Note that  $q = 2^m$  and k = n - mt. (We omit the semi-systematic forms.)

parameter sets	m	n	t	k
kem/mceliece348864	12	3488	64	2720
kem/mceliece460896	13	4608	96	3360
kem/mceliece6688128	13	6688	128	5024
kem/mceliece6960119	13	6960	119	5413
kem/mceliece8192128	13	8192	128	6528

Define  $S = \{e \in \mathbb{F}_2^n \mid HW(e) = t\}$ , which is a plaintext space. The underlying PKE of Classic McEliece is summarized as follows, where we only consider the systematic form and omit the details for the semi-systematic form:

- Gen(*pp*): Choose a monic irreducible polynomial g in  $\mathbb{F}_q[x]$  of degree t and distinct  $\alpha_1, \ldots, \alpha_n \leftarrow \mathbb{F}_q$ . Compute a parity-check matrix  $\hat{H} \in \mathbb{F}_2^{n \times k}$  of the Goppa code generated by g and  $\alpha_1, \ldots, \alpha_n$ . Reduce  $\hat{H}$  to systematic form  $[I_{n-k} \mid T]$ . (If this fails, return  $\perp$ ). Output  $pk := T \in \mathbb{F}_2^{(n-k) \times k}$  and  $sk := (T, \Gamma)$ , where  $\Gamma := (g, \alpha_1, \ldots, \alpha_n)$ . We note that using  $\Gamma$ , one can correct an error of the codeword up to t, because the minimum distance of the Goppa code is at least 2t + 1 by design.
- $\operatorname{Enc}(pk, e)$ : Define  $H := [I_{n-k} \mid T] \in \mathbb{F}_2^{(n-k) \times n}$ . Compute  $c := He \in \mathbb{F}_2^{n-k}$ . Output c.
- Dec(*sk*, *c*): Extend *c* to  $v := (c, 0, ..., 0) \in \mathbb{F}_2^n$ . Find the unique codeword  $\tilde{c}$  in the Goppa code defined by  $\Gamma'$  that satisfies HW( $\tilde{c} v$ )  $\leq t$ . Set  $e := v + \tilde{c}$ . If HW(e) = t and c = He, then return e. Otherwise, return  $\perp$ .

Notice that there are no specification on the decoding algorithm and we can choose it from existing decoding algorithms: The submitted implementation uses the Berlekamp-Massey decoding algorithm [Mas69], which corrects the error up to *t*. We can use the Patterson decoding algorithm [Pat75] which sometimes corrects a (t + 1)-error. However, the decryption algorithm checks the Hamming weight of *e* and such (t + 1)-error will be rejected.

#### Review of key-recovery attacks against the McEliece/Niederreiter PKE:

*Review of KR-PCA:* There are few key-recovery attacks against the McEliece/Niederreiter PKE exploiting a plaintext-checking oracle. Hall, Goldberg, and Schneier [HGS99] gave a message-recovery reaction attack against the McEliece PKE. The attack queries a ciphertext plus an *i*-th unit vector and determines the *i*-th bit of error by seeing the decryption error occurs or not (this corresponding to t + 1 error or t - 1 error). They also pointed out if the unpermuted code is public and the decryption oracle internally decodes t + 1 errors sometimes, then it could be used to determine the secret permutation matrix by calculating decryption failure rate on each bits. Engelbert, Overbeck, and Schmidt [EOS07] surveyed the security of the McEliece and Niederreiter PKEs. They pointed out that, when the support of the Goppa code is known, if one can obtain the permutation matrix, then one can recover the whole secret key. Thus, we have a key-recovery plaintext-checking attack against the McEliece and Niederreiter PKEs with certain conditions by combining them.

However, there are no known key-recovery plaintext-checking attacks against the McEliece/Niederreiter PKEs with the weight check. We leave investigating such key-recovery plaintext-checking attack as a long-standing open problem.

*Review of key-recovery SCA/FIA:* Strenzke [Str10] gave a timing attack against the McEliece PKE using Patterson's decoding algorithm which retrieves the secret permutation. Heyse, Moradi, and Paar [HMP10] gave key-recovery SCAs against the McEliece PKE using Patterson's decoding algorithm based on power consumption. Strenzke [Str13] improve his previous attack and gave practical key-recovery timing attack which exploits the secret permutation of the McEliece PKE using Patterson's decoding algorithm. Petrvalsky, Richmond, Drutarovsky, Cayrel, and Fischer [PRD<sup>+</sup>16] gave a DPA-based SCA against the McEliece PKE with the Patterson decoder which retrieves a secret permutation. Bucerzan, Cayrel, Dragoi, and Richmond [BCDR17] improved timing attack against the McEliece PKE with the Patterson decoder. Danner and Kreuzer [DK20] gave a key-recovery FIA against the Niederreiter PKE with a binary irreducible Goppa code.

Lahr, Niederhagen, Petri, Samardjiska [LNPS20] adapted a message-recovery SCA against the McEliece PKE with the Patterson decoder by Heyse et al. [HMP10] to Classic McEliece with a constant-time Berlekamp-Massey decoder. Cayrel, Colombier, Drăgoi, Menu, and Bossuet [CCD<sup>+</sup>21] recently gave a practical message-recovery FIA against Classic McEliece, in which the attacker can inject faults to replace instruction of the computation and obtain a *faulty syndrome*. Those might lead to key-recovery SCA/FIA in the future.

## C.2 Kyber

*Review of Kyber in Round 3:* Kyber [SAB<sup>+</sup>20] is a KEM scheme based on the Module LWE problem. We briefly review the underlying PKE scheme of Kyber.

Define  $\mathscr{R} = \mathbb{Z}[x]/(x^n + 1)$  and  $\mathscr{R}_q = \mathbb{Z}_q[x]/(x^n + 1)$ . For a positive integer  $\eta$ , we define a central-binomial distribution  $\Psi_\eta$  as  $(a_1, b_1, \dots, a_\eta, b_\eta) \leftarrow \{0, 1\}^{2\eta}$  and return  $\sum_{i=1}^{\eta} (a_i - b_i)$ . For a polynomial  $P \in \mathscr{R}, P \leftarrow \Psi_\eta$  implies each coefficient of the polynomial is chosen from  $\Psi_\eta$  independently.

Table 8: Parameter sets of Kyber in Round 3.

parameter sets	n	k	q	$\eta_1$	$\eta_2$	$d_U$	$d_V$
Kyber512	256	2	3329	3	2	10	4
Kyber768	256	3	3329	2	2	10	4
Kyber1024	256	4	3329	2	2	11	5

For  $x \in \mathbb{Z}$ , we define two functions:  $\operatorname{comp}_{q}(x, d) := \left[ (2^{d}/q) \cdot x \right] \operatorname{mod}^{\pm} 2^{d}$  and  $\operatorname{decomp}_{q}(x, d) := \left[ (q/2^{d}) \cdot x \right]$ . For  $x = (x_1, ..., x_k) \in \mathbb{Z}^k$  with some k, we define  $\operatorname{comp}_q(x, d) := (\operatorname{comp}_q(x_1, d), ..., \operatorname{comp}_q(x_k, d))$  and  $\operatorname{decomp}_q(x,d) := (\operatorname{decomp}_q(x_1,d), \dots, \operatorname{decomp}_q(x_k,d))$ 

We have  $\left| \left( x - \operatorname{decomp}_q(\operatorname{comp}_q(x, d), d) \right) \operatorname{mod}^{\pm} q \right| \leq \left\lceil q/2^{d+1} \right|$ . We also note that  $\operatorname{comp}_q(x, 1) = 1$  if  $|x \mod^{\pm} q| \leq \left\lceil q/2^{d+1} \right\rceil$ .  $|q| \leq \lceil q/4 \rceil$  and 0 otherwise.

The underlying PKE scheme of Kyber is summarized as follows:

- $\begin{array}{l} \ \operatorname{Gen}(pp): A \leftarrow \mathscr{R}_q^{k \times k} \ \text{and} \ (sk,d) \leftarrow (\Psi_{\eta_1}^k)^2. \ \operatorname{Compute} B := A \cdot sk + d. \ \operatorname{Output} \ pk := (A,B) \ \text{and} \ sk. \\ \ \operatorname{Enc}(pk,\mu): \ \operatorname{Sample} t \leftarrow \Psi_{\eta_1}^k, \ e \leftarrow \Psi_{\eta_2}^k, \ \text{and} \ f \leftarrow \Psi_{\eta_2}. \ \operatorname{Compute} (U,V) := (tA + e, tB + f + \left\lceil q/2 \right\rceil \cdot \mu) \in \mathscr{R}_q^k \times \mathscr{R}_q. \\ \operatorname{Output} (U',V') := (\operatorname{comp}_q(U,d_U), \operatorname{comp}_q(V,d_V)). \end{array}$
- $\operatorname{Dec}(sk, (U', V'))$ : Compute  $(U, V) := (\operatorname{decomp}_a(U', d_U), \operatorname{decomp}_a(V', d_V))$ . Output  $\mu' := \operatorname{comp}_a(V U \cdot sk, 1)$ .

# Review of key-recovery attacks against Kyber:

Review of KR-PCA: There are key-recovery attacks against Kyber exploiting a plaintext-checking oracle or keymismatch oracle: Qin, Cheng, and Ding [QCD19], Ravi, Roy, Chattopadhyay, and Bhasin [RRCB20], Huguenin-Dumittan and Vaudenay [HV20], Ravi, Bhasin, Roy, and Chattopadhyay [RBRC20], and Qin, Cheng, Zhang, Pan, Hu, and Ding  $[QCZ^+21]$ .

We will follow the KR-PCA against Kyber512 in Huguenin-Dumittan and Vaudenay [HV20]. Kyber has three parameter sets Kyber512, Kyber756, and Kyber1024. In Round 3, the submitter changed some parameters for Kyber512 from those of Round 2.<sup>21</sup> Since Huguenin-Dumittan and Vaudenay [HV20] (and Qin et al. [QCD19]) targets the Round 2 version of Kyber512, we need to adjust parameters in the attack.

Review of key-recovery SCA/FIA: Ravi et al. [RRCB20] implemented a plaintext-checking oracle by using SCA against the PRF of Kyber and proposed a key-recovery SCA against Kyber. Sim et al. [SKL<sup>+</sup>20] gave a singletrace message-recovery SCA against an encryption program of the underlying PKE of Kyber, which is an extension of a single-trace message-recovery SCA against NewHope proposed by Amiet, Curiger, Leuenberger, and Zbinden [ACLZ20]. Their technique could be used to implement a plaintext-checking oracle, since the FO transformation checks the re-encryption test. (See, e.g., Ravi and Roy [RR21].) Xu, Pemberton, Roy, and Oswald [XPRO20] gave a key-recovery SCA exploiting inverse NTT and improved the key-recovery SCA using the message encoding/decoding of Kyber. Ravi, Bhasin, Roy, and Chattopadhyay [RBRC20] gave message recovery SCAs exploiting the message decoding or the PRF and turned them into key-recovery SCAs against Kyber.

Bhasin, D'Anvers, Heinz, Pöppelmann, and Van Beirendonck ... [BDH<sup>+</sup>21].

Pessl and Prokop [PP21] gave key-recovery FIA which skips an instruction of message decoding.

**Key-recovery attack against Kyber512 in Round 3:** Let  $\mu = 0 \in \mathcal{R}$  and let  $\rho = \lceil q/4 \rceil = 832$ . Suppose that we query (U', V') to the plaintext-checking oracle with candidate plaintext  $\mu = 0$ . For ease of notation, we define  $\delta = (\delta_0, \dots, \delta_{n-1}) := V - U \cdot sk - \text{encode}(pt)$ , where  $U = \text{decomp}_q(U', d_U)$  and  $V = \text{decomp}_q(V', d_V)$ . The plaintext-checking oracle returns T if and only if  $|\delta_i \mod^{\pm} q| \leq \rho$  for all  $i \in [n]$ . (If so, (U', V') is decrypted into 0.)

<sup>&</sup>lt;sup>21</sup> See "Increase noise parameter for Kyber512" and "Reduce ciphertext compression of Kyber512" in Changes to the core Kyber design. Kyber512 has parameters  $(n, q, \eta_1, \eta_2, d_U, d_V) = (256, 3329, 2, 2, 10, 3)$  in Round 2 and = (256, 3329, 3, 2, 10, 4) in Round 3

Table 9: The behavior of  $m'_i$  of m' = Dec(sk, (U', V')) on a ciphertext (U', V') with  $U = (-276, 0^{k-1})$  and V = $208t \cdot x^i$ .

(a) Kyber512							(1.) I	7.1	7/0 -	1 T	7.1			
$\overline{k_i}^{t}$	-3 –	2 -	-1	0	1	2	3	$\frac{(b) \mathbf{r}}{ \mathbf{r} }$	3 -2	/08 a	0	1	2	4
-3 1	. 1	1	L	0	0	0	0	$sk_i$	5 1	1	Ū	1	-	
-2  1	. 1	C	)	0	0	0	0	-2   1	1	0	0	0	0	
-1 1	0	C	)	0	0	0	0	-1  1	0	0	0	0	0	
0 0	0	C	)	0	0	0	0	0 0	0	0	0	0	0	
+1 0	0	C	)	0	0	0	1	+1 0	0	0	0	0	0	
+2 0	0	0	)	0	0	1	1	+2 0	0	0	0	0	1	
+3 0	0	C	)	0	1	1	1							

**Lemma C.1.** Let U = (-276, 0) and  $U' = \operatorname{comp}_q(U, d_U)$ . Let  $t \in \{-5, -4, -3, \dots, 4, 5\}$ . Let  $V = 208t \cdot x^i = 1000$  $(0, ..., 208 \cdot t, ..., 0)$  be a polynomial with 208t in the *i*-th coefficient and 0 elsewhere and V' = comp<sub>a</sub>(V, d<sub>V</sub>). Let m' = Dec(sk, (U', V')). We have  $m'_i = 0$  for all j but i and

$$m'_i = 0 \iff |276 \cdot sk_i + 208 \cdot t| \le \rho$$

The proof is very similar to that of Huguenin-Dumittan and Vaudenay [HV20, Lemma 1] and we omit it.

See the pattern in Table 9a for  $sk_i = s$  and  $t \in \{-5, -4, \dots, 4, 5\}$ . According to the table, we examine  $t \in \{-5, -4, \dots, 4, 5\}$ .  $\{-3, -2, -1, 1, 2, 3\}$  to determine  $sk_i \in \{-3, -2, \dots, 2, 3\}$ .

Trade-off: In the case of the skipping-equality-test attack, we can reduce the number of queries as in the case of ntrulpr. For example, we can determine  $sk_0, \ldots, sk_{\ell-1}$  by six faulty decapsulation results as follows:

1. For  $t \in \{-3, -2, -1, 1, 2, 3\}$ , we prepare ciphertext  $(U', V'_t)$  with U = (-276, 0) and  $V_t = \sum_{i=0}^{t-1} 208tx^i$  and obtain faulty decapsulation results  $K'_t = H(m'_t, (U', V'_t))$  where  $m'_t = \text{Dec}(sk, (U', V'_t))$ . 2. We then compute  $K_{\text{guess},t} = H(m_{\text{guess}}, (U', V'_t))$  for all  $m_{\text{guess}} = m'' \| 0^{256-\ell}$  with  $m'' \in \{0, 1\}^{\ell}$  and t.

- 3. We determine the *i*-th coefficient of  $m'_t$  by comparing  $K_{guess,t}$  with  $K_t$ .
- 4. We determine  $sk_i$  by using the table and the *i*-th coefficients of all  $m'_t$

Key-recovery attack against Kyeber 768 and Kyber 1024: We examine  $U = (-276, 0^{k-1})$  with  $V = 208 t \cdot x^{i}$  and obtain the same table as Kyber512, while  $sk_i \in [-2, +2]$  because  $\eta_1 = 2$  in Kyber768 and Kyber1024. See Table 9b for the behavior of  $m'_i$  of m' = Dec(sk, (U', V')) with  $U = (-276, 0^{k-1})$  and  $V = 208 \cdot t \cdot x^i$  for  $t \in \{-3, -2, \dots, 2, 3\}$ . According to the table, we can determine  $dk_i$  by querying (U', V') for  $t \in \{-3, -2, +2, +3\}$ .

Again, in the case of the skipping-equality-test attack, we can reduce the number of queries as in the case of ntrulpr. We can determine  $\ell$  coefficients of *sk* by four faulty decapsulation results as in the case of Kyber512.

#### C.3 NTRU

Review of NTRU: NTRU [CDH<sup>+</sup>20] is based on NTRU [HPS98] and NTRU-HRSS [HRSS17]. We here briefly review NTRU [HPS98].

Define  $\mathscr{R} = \mathbb{Z}[x]/(x^n-1)$  and  $\mathscr{R}_a = \mathbb{Z}_a[x]/(x^n-1)$  for  $a = q = 2^{\epsilon_q}$  and 3. Let  $\mathscr{T} = \{\sum_{i=0}^{n-1} t_i x^i \mid t_i \in \{-1, 0, +1\}\}$ . Let  $\mathscr{L}_{f}, \mathscr{L}_{g}, \mathscr{L}_{r}, \mathscr{L}_{m} \subseteq \mathscr{T}$  be carefully-chosen subsets of  $\mathscr{T}$ .

The underlying PKE scheme of NTRU is summarized as follows:

- Gen(pp):  $(f, g) \leftarrow \mathscr{L}_f \times \mathscr{L}_g$ . Compute  $f_q := f^{-1} \in \mathscr{R}_q$  and  $h := 3gf_q \in \mathscr{R}_q$ . Output pk := h and sk := (f, h). Enc(pk, (r, m)): Output  $c := hr + m \in \mathscr{R}_q$ .
- $\operatorname{Dec}(sk, c)$ : Compute  $a := cf \operatorname{mod}_{\downarrow}^{\pm} q$ .  $m := a \cdot f^{-1} \operatorname{mod}^{\pm} 3$ .  $r := (c m) \cdot h^{-1} \operatorname{mod}_{\downarrow}^{\pm} q$ . If  $(r, m) \in \mathscr{L}_r \times \mathscr{L}_m$ then return (r, m); else, return  $\perp$ .

#### Review of key-recovery attacks against NTRU:

*Review of KR-PCA and more:* Hoffstein and Silverman [HS00], Jaulmes and Joux [JJ00], Han, Hong, Han, and Kwon [HHHK03], and Mol and Yung [MY08] gave key-recovery reaction attacks against *unpadded* NTRU. We note that the key-recovery attack of Hoffstein and Silverman [HS00] and one of key-recovery attacks in Jaulmes and Joux [JJ00] can be used in the key-recovery plaintext-checking attacks. Howgrave-Graham, Nguyen, Pointcheval, Proos, Silverman, Singer, and Whyte [HNP<sup>+</sup>03] and Gama and Nguyen [GN07] gave key-recovery chosen-ciphertext attacks against *padded* NTRUs.

Ding, Deaton, Schmidt, Vishakha, and Zhang [DDS<sup>+</sup>19] gave a KR-PCA against NTRU. Since the target of their attack [DDS<sup>+</sup>19] is old-school unpddded NTRU, we need to adjust their attack in order to make ntruhps of NTRU in Round 3 as a target but the adjustmen is subtle and we omit the detail. Zhang, Cheng, Qin, and Ding [ZCQD21] recently gave a KR-PCA against ntruhrss of NTRU.

*Review of key-recovery SCA/FIA against NTRU:* There are a lot of key-recovery SCA/FIA against NTRU. Silverman and Whyte [SW07] proposed a key-recovery timing attack against padded NTRUEncrypt. Atici, Batina, Gierlichs, and Verbauwhede [ABGV08] gave key-recovery differential power analysis attack against NTRU on FPGA. Lee, Song, Choi, and Han [LSCH10] also gave key-recovery attack using the correlation power analysis against software implementaiton of NTRU. Kamal and Youssef gave key-recovery reaction attack using fault [KY11] and scan-based key-recovery SCA [KY12]. Zheng, Wang, and Wei [ZWW13] gave another keyrecovery attack using power analysis against NTRU. Paterson and Villanueva-Polanco gave a cold-boot attack against NTRU [PV17]. Gunter discussed timing attacks against reference implementations of NTRU [Gun19]. Askeland and Rønjom [AR21] proposed a key-recovery side-channel attack exploiting EM leakage of unpack of the secret key. All of them do not exploit the plaintext-checking/key-mismatch oracle.

**KR-PCA against NTRU:** We review how their KR-PCA [DDS<sup>+</sup>19] works against *old-school* NTRU here. We omit the details of their KR-PCAs [DDS<sup>+</sup>19, QCZ<sup>+</sup>21] against NTRU-HPS and NTRU-HRSS.

Notice that there are equivalent keys  $(\hat{f}, \hat{g}) = (\pm fx^i, \pm gx^{-i})$  such that  $h = 3\hat{g}\hat{f}^{-1} \mod q$ . It is enough to get one of such  $\hat{g}$  to recover whole secret key  $\hat{f}$  and  $\hat{g}$ , since we can obtain  $\hat{f} = 3\hat{g} \cdot h^{-1} \mod q$ .

Determine the longest chain: We call g's sequential coefficients as chain if they are 1's ore -1's: A chain in g is  $(s,l) \in [n]^2$  such that  $g_{s \mod n} = g_{s+1 \mod p} = \cdots = g_{s+l-1 \mod p} = v \in \{-1,+1\}$ . The length of chain (s,l) is l. Their key-recovery attack first find the length of the longest chain of g and assume that  $g_0 = g_1 = \cdots = g_{l-1} = 1$ .

The attack first determine the length of the longest chain as follows: Let us consider  $r = \sum_{i=0}^{j-1} t_j \cdot x^i$ , where  $t_j$  is carefully chosen. We query a ciphertext hr + 0 and a corresponding plaintext. In the decryption, we will have  $a \equiv cf \equiv pgr \pmod{q}$  and  $a_i \equiv pt_j(g_i \mod n + g_{i-1} \mod n + \dots + g_{i-(j-1)} \mod n) \pmod{q}$ . For  $j = 1, \dots, k-1$ , we will get 'mismatch' because  $t_j$  is chosen as  $\max\{|a_i|\} > q/2$  and, for j = k, we get 'match' because  $\max\{|a_i|\} < q/2$ . The mismatch occurs a result of *wrap failure* in attacks against NTRU [HNP<sup>+</sup>03]. (We note that we can obtain the same result by setting  $c = h \cdot 0 + m$  with  $m = \sum_{i=0}^{j-1} t_j \cdot x^i$ . In the case, we obtain  $a = mf \pmod{q}$ .)

*Determine the rest:* Once we assume  $\hat{g} = (1, 1, ..., 1, ?, ..., ?)$ , we can determine rest coefficients by querying two ciphertexts for each coefficients. For simplicity, we assume that the longest chain is unique.

In order to determine *j*-th coefficient for  $j \ge k$ , we query two ciphertexts  $hr^+$  and  $hr^-$ , where  $r^{\pm} = \sum_{i=0}^{k-1} tx^i \pm t \cdot x^j$ , with corresponding plaintexts.

*Number of queries:* In order to determine the length k of the longest chain, we need k faulty decapsulation results. In order to determine the rest coefficients, we need 2 faulty-decapsulation results on each coefficients. Thus, we need at most 3n to recover a whole key. (2n + 10 may be enough for 99% secret keys.)

#### C.4 Saber

*Review of Saber:* Saber [DKR<sup>+</sup>20] is a KEM scheme based on the Module LWR problem. Saber has three parameter sets LightSaber (lv.1), Saber (lv.3), and FireSaber (lv.5). See Table 10.

Define  $\mathscr{R} = \mathbb{Z}[x]/(x^n+1)$  and  $\mathscr{R}_a = \mathbb{Z}_a[x]/(x^n+1)$  for a = q, p, T, 2. Let  $\epsilon_q = \lg(q), \epsilon_p = \lg(p), \operatorname{and} \epsilon_T = \lg(T)$ . For an even positive integer  $\mu$ , we define a central-binomial distribution  $\beta_\eta$  as  $(a_1, b_1, \dots, a_{\mu/2}, b_{\mu_2}) \leftarrow \{0, 1\}^{\mu}$  and return  $\sum_{i=1}^{\mu/2} (a_i - b_i) \in [-\mu/2, \mu/2]$ . For a polynomial  $P \in \mathscr{R}, P \leftarrow \beta_\mu$  implies each coefficient of the polynomial is chosen from  $\beta_\mu$  independently. For a positive integer x, we define shiftright(x, d) as  $\lfloor x/2^d \rfloor$ , the result of d bit

Table 10: Parameter sets of Saber in Round 3.

parameter sets	n n	k	q	p	Т	μ
LightSaber	256	2	8192	1024	8	10
Saber	256	3	8192	1024	16	8
FireSaber	256	4	8192	1024	64	6

shift of x to right. We define  $h_1 := \sum_{i=0}^{n-1} 2^{\epsilon_q - \epsilon_p - 1} x^i \in \mathscr{R}_q, h_2 := \sum_{i=0}^{n-1} (2^{\epsilon_p - 2} - 2^{\epsilon_p - \epsilon_T - 1} + 2^{\epsilon_q - \epsilon_p - 1}) x^i \in \mathscr{R}_q$ , and  $h:=(h_1,\ldots,h_1)\in \mathscr{R}_q^k.$  The underlying PKE scheme of Saber is summarized as follows:

- Gen(*pp*):  $A \leftarrow \mathscr{R}_q^{k \times k}$  and  $sk \leftarrow \beta_{\mu}^k$ . Compute  $B := \text{shiftright}(A \cdot sk + h, \epsilon_q \epsilon_p)$  Output pk := (A, B) and sk.
- $\operatorname{Enc}(pk,\mu)$ : Sample  $t \leftarrow \beta_{\mu}^{k}$ . Output  $(U,V) := (\operatorname{shiftright}(tA+h,\epsilon_{q}-\epsilon_{p}),\operatorname{shiftright}(t\cdot B+h_{1}-2^{\epsilon_{p}-1}\mu \mod p,\epsilon_{p}-1))$  $(\epsilon_T)) \in \mathscr{R}_p^k \times \mathscr{R}_T.$
- $\operatorname{Dec}(sk, (U, V))$ : Return  $\mu' := \operatorname{shiftright}(U \cdot sk 2^{\epsilon_p \epsilon_T} \cdot V + h_2 \mod p, \epsilon_p 1) \in \mathcal{R}_2$ .

#### Review of key-recovery attacks against Saber:

Review of KR-PCA: For LightSaber, we follow the key-recovery attack exploiting a plaintext-checking oracle proposed by Huguenin-Dumittan and Vaudenay [HV20]. For Saber and FireSaber, we follow the key-recovery attack exploiting a plaintext-checking oracle proposed by Osumi, Uemura, Kudo, and Takagi [OUKT21]. Ravi et al. gave a key-recovery side-channel attack against Saber [RRCB20] while they omit the details because Saber is very similar to Kyber. Ngo, Dubrova, Guo, and Johansson [NDG]21] proposed a key-recovery side-channel attacks against *first-order masked Saber* [BDK<sup>+</sup>21] and gave a KR-PCA as the building block.

Although their attacks target the Round 2 version, we can mount them against the Round 3 versions since Saber has no changes in Round 3.

Review of key-recovery SCA/FIA: Ravi et al. [RRCB20] gave a key-recovery SCA against Saber. Sim et al. [SKL<sup>+</sup>20] gave a single-trace message-recovery SCA against an encryption program of the underlying PKE of Saber, which could be used to implement a PCO of Saber. Ngo, Dubrova, Guo, and Johansson [NDG]21] gave key-recovery higher-order SCAs against masked Saber. Ngo, Dubrova, and Johansson [NDJ21] also gave key-recovery higherorder SCAs against masked and shuffled Saber.

KR-PCA against LightSaber: We follow Huguenin-Dumittan and Vaudenay [HV20, Section 6]. We first determine  $sk_i = -5, -4, -3, -2, +2, +3, +4, +5$  or some of -1, 0, +1 by querying  $(U, 2x^i)$  with U = (u, 0) and  $u = \{-60/5, -60/4, -60/3, -60/2, +60/2, +60/3, +60/4, +60/5\}$  with guessing plaintext 0. We define  $V^+ = \sum_{i \in [0,n]: sk_i = 4 \text{ or } 5} 5x^i$  and  $V^- = \sum_{i \in [0,n]: sk_i = -4 \text{ or } -5} 5x^i$  and determine whether  $sk_i = -1, 0, +1$  by checking  $((60, 0), 2x^i + V^+)$  and  $((-60, 0), 2x^i + V^-)$  with guessing plaintext 0. Thus, we can determine a coefficient of *sk* by ten non-adaptive queries to plaintext-checking oracle for LightSaber.

KR-PCA against Saber and FireSaber: Since the principle of the attack is very similar to the KR-PCA against Kyber, we omit the detail of them. Adapting and summarizing the result of Osumi, Uemura, Kudo, and Takagi [OUKT21], we obtain the table of the behavior of decrypted messages in special ciphertexts in Table 11.<sup>22</sup> We can determine a coefficient of sk by eight and six non-adaptive queries to plaintext-checking oracle for Saber and FireSaber, respectively.

Trade-Off: In the case of the skipping-equality-test attack, we can reduce the number of queries as in the case of ntrulpr and Kyber. For example, we can determine first  $\ell$  coefficient by querying (U, V) with  $V = \sum_{i=0}^{\ell} 2x^i$ instead of  $V = 2x^{i}$ . We can determine  $\ell$  coefficients of sk by ten, eight, and six faulty decapsulation results for LightSaber, Saber, and FireSaber, respectively.

<sup>&</sup>lt;sup>22</sup> They used  $U = (u \cdot x^{n-i}, 0^{k-1})$  and V = t to determine  $sk_i$ . We adapt it in the form of  $U = (u, 0^{k-1})$  and  $V = t \cdot x^i$ .

		(a)	Sabe	er wi	th u	= 54	and	57		
u = 54 $u = 57$										
$k_i$	0	1	0	1	2	3	4	5	6	7
-4	0	1	0	1	1	1	1	1	1	1
-3	0	0	0	1	1	1	1	1	1	1
-2	0	0	0	0	1	1	1	1	1	1
-1	0	0	0	0	0	1	1	1	1	1
0	0	0	0	0	0	0	1	1	1	1
⊥ 1	0	Õ		0 0	Ô	0	0	1	1	1
+ 1	0	0		0	0	0	0	0	1	1
+2	0	0	0	0	0	0	0	0	1	1
+3	0	0	0	0	0	0	0	0	0	1
+4	0	0	0	0	0	0	0	0	0	0

Table 11: Saber and FireSaber: The behavior of  $m'_i$  of m' = Dec(sk, (U, V)) on a ciphertext (U, V) with  $U = (u, 0^{k-1})$  and  $V = t \cdot x^i$ .

## C.5 BIKE

*Review of BIKE:* BIKE in round 3 [ABB<sup>+</sup>20] is a KEM scheme based on QC-MDPC [MTSB13], which is a variant of the McEliece PKE upon a code with quasi-cyclic (QC) moderate density parity-check (MDPC) matrix. BIKE can be considered as the Niederreiter PKE scheme upon a code with the QC-MDPC matrix. Let  $\mathscr{R} := \mathbb{F}[x]/(x^r - 1)$ . Let  $\mathscr{H}_w := \{(h_0, h_1) \in \mathscr{R}^2 \mid HW(h_0) = HW(e_1) = w/2\}$ . Let  $\mathscr{E}_t := \{(e_0, e_1) \in \mathscr{R}^2 \mid HW(e_0, e_1) = t\}$ .

Table 12: Parameter sets of BIKE in Round 3.

parameter sets	r w t
BIKE-1	12,323 142 134
BIKE-3	24,659 206 199
BIKE-5	40,973 274 264

We first review a simplified version of QC-MDPC.

- Gen(pp):  $sk := (h_0, h_1) \leftarrow \mathscr{H}_w$ , which defines a parity-check matrix  $H = [H_0 \mid H_1] \in \mathbb{F}_2^{r \times 2r}$  with companion matrices  $H_0$  and  $H_1$  of  $h_0$  and  $h_1$ , respectively, and its systematic form is  $[I_r \mid \tilde{H}]$  with an identity matrix  $I_r$  of dimension r and  $\tilde{H} = H_0^{-1} \cdot H_1$ . Output  $pk = h := h_0^{-1} \cdot h_1 \in \mathscr{R}$  and sk.
- Enc(*pk*, *m*; (*e*<sub>0</sub>, *e*<sub>1</sub>) ∈  $\mathcal{E}_t$ ): Construct a generator matrix  $G = [H^\top | I_r] \in \mathbb{F}_2^{r \times 2r}$  from a companion matrix *H* of *h*. Output *c* := *mG* + (*e*<sub>0</sub>, *e*<sub>1</sub>) ∈  $\mathbb{F}^{2r}$ .
- Dec(sk, c): Output  $(e_0, e_1) \leftarrow decode(c, (h_0, h_1))$ , where decode is a decoding algorithm of the QC-MDPC code. Compute  $mG := c (e_0, e_1)$ . Extract *m* from *mG* by taking the last *r* position of *mG*.

The underlying CPA-secure PKE scheme of BIKE is summarized as follows:

- Gen(pp):  $sk := (h_0, h_1) \leftarrow \mathscr{H}_{w}$ . Output  $pk = h := h_1 \cdot h_0^{-1} \in \mathscr{R}$  and sk.
- $\operatorname{Enc}(pk, (e_0, e_1) \in \mathscr{C}_t)$ : Output  $c := e_0 + e_1h \in \mathscr{R}$ .
- Dec(*sk*, *c*): Output ( $e_0, e_1$ ) ← decode( $ch_0, (h_0, h_1)$ ).

Notice that  $ch_0 = e_0h_0 + e_1h_1$ , which is the syndrome of  $(e_0, e_1)$  with the parity-check matrix spanned by  $h_0$  and  $h_1$ .

### Review of key-recovery attacks against QC-MDPC/BIKE:

*Review of KR-PCA:* Guo, Johansson, and Stankovski [GJS16] gave a key-recovery reaction attack against QC-MDPC, which is a variant of the McEliece encryption scheme. They observed that 1) the decryption-failure rates (DFR) for carefully crafted ciphertexts are strongly related to the distances between 1's in the decryption key and 2) one can reconstruct the decryption key from the knowledge of the distances between 1's. Paiva and Terada [PT18] also gave a faster key-reconstruction algorithm for 2) while it requires the computation of DFRs approximately twice. (There is a trade off.)

*Review of key-recovery SCA/FIA:* Chen, Eisenbarth, von Maurich, and Steinwantdt [CEvMS15] gave DPA-based key-recovery attack against QC-MDPC implemented in a FPGA board. Rossi, Hamburg, Hutter, and Marson [RHHM17] gave DPA-based key-recovery attack against QcBits [Cho16], which is an instantiation of QC-MDPC.

**Applicability to BIKE:** Huguenin-Dumittan and Vaudenay [HV20] suggested that the GJS attack against QC-MDPC may be applicable to BIKE. However, we do not know whether the GJS attack is applicable to *Round-3* BIKE or not, because Round-3 BIKE is different from QC-MDPC in two points: The one is that BIKE is based on the Niederreiter PKE, while QC-MDPC is based on the McEliece PKE. The other is that BIKE in Round 3 uses the Black-Gray-Flip (BGF) decoder instead of the Black-Gray (BG) decoder. The former difference is not essential, but the latter difference of the decoder would affect the power of the GJS attack.

We here report how the GJS attack is effective for round-3 BIKE.

**The GJS attack against QC-MDPC:** Suppose that  $\tau$  is even and chosen carefully slightly larger than *t* to increase the decryption failure. Let

$$\mathscr{P}_{\tau,d} := \{(e,0) \in \mathscr{R}^2 \mid \mathsf{HW}(e) = \tau \land \exists \text{ distinct } s_1, \dots, s_\tau \text{ s.t. } e_{s_i} = 1 \text{ with } s_{2i} = (s_{2i-1} + d) \text{ mod } r \text{ for } i = 1, \dots, \tau/2 \}.$$

The adversary sends a ciphertext crafted by a random sample from  $\mathcal{P}_{\tau,d}$  to the decryption oracle and it sees the reaction (yes or no). It can estimate DFR for each d = 1, ..., U for the upper bound U < r/2. Moreover, they infer  $\mu(h_0)$ , which is defined as follows: Let  $s_1, ..., s_\tau$  be the indices such that  $h_0[s_i] = 1$ . Let  $d_r(s_i, s_j)$  be the distance between  $s_i$  and  $s_j$ , that is,  $d_r(s_i, s_j) = \min\{|s_i - s_i|, r - |s_j - s_i|\}$ . Define distance profile as

$$\mu(h_0) := \{ (d, \mu_d) \mid d \in [0, r), \mu_d = \#\{(s_i, s_j) : 0 \le s_i < s_j < r, d_r(s_i, s_j) = d \} \}$$

Guo et al. gave a key-recovery algorithm from distance profile  $\mu(h_0)$  [GJS16, Alg.2]. Paiva and Terada [PT18] also gave a faster key-recovery algorithm from distance profiles  $\mu(h_0)$  and  $\mu(h_1)$ .

#### Applying the GJS attack to BIKE:

*Experimental Result:* We examine the behavior of DFRs with respect to BGF decoder. We use BIKE-1, where r = 12323, w = 142, and t = 134. We pick a key and estimate DFR for random M = 2000 plaintexts chosen from  $\mathcal{P}_{\tau,d}$  for U = 1, 2, ..., 6162 with  $\tau = 161$  rather than t = 134. Figure 19 shows the behavior of DFR for d = 1, ..., 6162, which varies in the range 0.0–0.5. In figure, we depict the multiplicity 0–4 by blue circle, orange tri-down, green tri-up, red tri-left, and purple tri-right, respectively. For d = 1, ..., 1500, we can see that the multiplicities are well separated and determine them by estimating DFR for  $\mathcal{P}_{\tau,d}$ . However, they are mixed in the right-hand side of figure and we cannot determine the multiplicity for large distances. Hence, it seems hard to apply the key-recovery algorithm in the GJS attack (and that in Paiva and Terada [PT18]).

We leave further investigation of key-recovery attack using DFR's behavior as an open problem.

#### C.6 FrodoKEM

Review of FrodoKEM: FrodoKEM [NAB<sup>+</sup>20] is an LWE-based KEM scheme in the alternates,

Let  $q = 2^D$  for some  $D \le 16$ . For a positive integer B < D,  $\bar{m}$ , and  $\bar{n}$ , they use encode :  $\{0, 1\}^{B\bar{m}\bar{n}} \to \mathbb{Z}_q^{\bar{m}\times\bar{n}}$ and decode :  $\{0, 1\}^{B\bar{m}\bar{n}} \to \{0, 1\}^{B\bar{m}\bar{n}}$ . (Roughly speaking, they compute ec :  $k \in [0, 2^B) \mapsto k \cdot q/2^B \in \mathbb{Z}_q$  and dc :  $K \in \mathbb{Z}_q \mapsto [K2^B/q] \mod 2^B$  and arrange the result.) Let  $\ell = B\bar{m}\bar{n}$  be a message length. They use a distribution  $\chi_s$  that is a centered symmetric distribution whose support is  $\{-s, -(s-1), \dots, s-1, s\}$ . (See [NAB<sup>+</sup>20, Sect.2.2.4 and Table 3] for the concrete distribution.)

The underlying PKE scheme of FrodoKEM [NAB<sup>+</sup>20] is summarized as follows:



Fig. 19: BIKE: DFR for 2000 plaintexts chosen from  $\mathcal{P}_{\tau,d}$  with  $\tau = 161$  and  $d = 1, 2, \dots, 6162$ .

parameter sets	n	q	σ	S	В	ħ	ñ
Frodo-640	640	$2^{15}$	2.8	12	2	8	8
Frodo-976	976	$2^{16}$	2.3	10	3	8	8
Frodo-1344	1344	$2^{16}$	1.4	6	4	8	8

Table 13: Parameter sets of Frodok EM in Round 3
--

- Gen(*pp*): Choose  $A \leftarrow \mathbb{Z}_q^{n \times n}$ ,  $S \leftarrow \chi^{n \times n}$  and  $E \leftarrow \chi^{n \times n}$ . Compute B := AS + E. Output pk := (A, B) and sk := S.
- $\operatorname{Enc}(pk,\mu)$ : Choose  $S', E' \leftarrow \chi^{\bar{m} \times n}$  and  $E'' \leftarrow \chi^{\bar{m} \times \bar{n}}$ . Output  $c = (U,V) := (S'A + E', S'B + E'' + \operatorname{encode}(\mu))$ .
- Dec(sk = S, (U, V)): Compute  $M := V U \cdot S$  and output  $\mu' := decode(M)$ .

## Review of key-recovery attacks against FrodoKEM:

*Review of KR-PCA:* There are several KR-PCAs against FrodoKEM by Băetu et al. [BDH<sup>+</sup>19], Ravi et al. [RRCB20], Vacek and Vàclavek [VV20], and Qin et al. [QCZ<sup>+</sup>21]. Guo et al.'s attack can be considered as KR-PCA [GJN20].

*Review of key-recovery SCA/FIA:* Ravi et al. [RRCB20] gave a message-recovery SCA exploiting the message decoding against FrodoKEM. They use it to implement a plaintext-checking oracle and proposed a key-recovery SCA against FrodoKEM using the above KR-CPA. Guo et al. [GJN20] gave a key-recovery timing attack against FrodoKEM. (See subsection 5.2.) Sim et al. [SKL<sup>+</sup>20] gave a single-trace message-recovery SCA against an encryption program of the underlying PKE of FrodoKEM. Their technique could be used to implement a plaintextchecking oracle, since the FO use the encryption algorithm for the re-encryption test. (See, e.g., Ravi and Roy [RR21].)

**KR-PCA against FrodoKEM:** We only give a rough idea: We have  $V - US = \text{encode}(\mu) + \Delta$ , where  $\Delta = E'' + S'E - E'S \in \mathbb{Z}^{\bar{m}\times\bar{n}}$ . The decoding is correct if and only if  $-q/2^{B+1} \leq \Delta_{i,j} < q/2^{B+1}$  for all i, j [NAB<sup>+</sup>20, Lamma 2.18]. Thus, we can craft U and V to check S's value directly. For the detail of KR-PCA, see [BDH<sup>+</sup>19, RRCB20, VV20, QCZ<sup>+</sup>21].

# C.7 HQC

**Review of HQC:** HQC [AAB<sup>+</sup>20] is another code-based KEM scheme in the alternates.

Table 14: Parameter sets of HQC in Round 3.

parameter sets		r	$n_1$	$k_1$	$d_1$	$n_2$	$k_2$	$d_2$	w	w <sub>e</sub>	w <sub>r</sub>
hqc-128	17,66	9	46	16	31	384	8	192	66	75	75
hqc-192	35, 85	1	56	24	32	640	8	320	100	114	114
hqc-256	57,63	7	90	32	59	640	8	320	131	149	149

Let  $\mathscr{R} := \mathbb{F}_2[x]/(x^r - 1)$ . Let  $\mathscr{C}$  be a decodable  $[n_1n_2, k]$  code generated by  $G \in \mathbb{F}_2^{k \times n_1n_2}$ , where  $n_1n_2 \leq r$ . Let decode be a decoder algorithm which corrects an error up to  $\delta$ . Let  $\mathcal{S}_w := \{x \in \mathcal{R} \mid HW(x) = w\}$ . For a polynomial  $A = \sum_{i} a_{i} x^{i} \in \mathcal{R}$ , we define trunc $(A, l) = (a_{0}, \dots, a_{l-1}) \in \mathbb{F}_{2}^{l}$ .

The underlying PKE scheme of HQC is summarized as follows:

- Gen(pp):  $h_0 \leftarrow \mathscr{R}$ .  $(x, y) \leftarrow \mathscr{S}^2_w$ . Compute  $h_1 := x + h_0 y$ . Output sk := (x, y) and  $pk := (h_0, h_1)$ . Enc $(pk, m \in \mathbb{F}_2^k; (e, f, t) \in \mathscr{S}_{w_e} \times \mathscr{S}_{w_r} \times \mathscr{S}_{w_r})$ : Output

 $c = (u, v) := (h_0 t + f, \operatorname{trunc}(h_1 t + e, n_1 n_2) \oplus mG) \in \mathscr{R} \times \mathbb{F}_2^{n_1 n_2}.$ 

- Dec(*sk*, (*u*, *v*)): Compute  $a := v \oplus \text{trunc}(uy, n_1n_2) \in \mathbb{F}_2^{n_1n_2}$  and output decode(*a*).

Code in Round 3: In Round 3, the submitter changed the code & from the BCH-Repetition code to the RS-RM code: For  $m \in \mathbb{F}_2^k \simeq \mathbb{F}_{2^8}^{k_1}$ , *m* is encoded into  $m_1 \in \mathbb{F}_{2^8}^{n_1}$  with the Reed-Solomon codes with  $[n_1, k_1, d_1]_{2^8}$ , then each  $m_{1,i} \in \mathbb{F}_{2^8} \simeq \mathbb{F}_2^8$  is encoded into  $\tilde{m}_{1,i} \in \mathbb{F}_2^{n_2}$  with the duplicated Reed-Muller code with  $[n_2, k_2, d_2]_2$ .

## Review of key-recovery attacks against HQC:

Review of KR-PCA: Wafo-Tapa, Bettaieb, Bidoux, Gaborit, and Marcatel [WTBB<sup>+</sup>20] gave KR-PCA using the information whether a decrypted message is 0 or not. Huguenin-Dumittan and Vaudenay [HV20] gave a KR-PCA against HQC, which is inspired by a KR-PCA against Lepton [YZ17] by Băetu et al. [BDH<sup>+</sup>19]. Unfortunately, their targets are HQC with the BCH-Repetition code.

Review of key-recovery SCA/FIA: Paiva and Terada [PT19] gave a key-recovery timing attacks against HQC, which exploits the relation between the timing information of the internal non-constant-time decoder and the spectrum of the secret key (as the attack against QC-MDPC). Wafo-Tapa, Bettaieb, Bidoux, Gaborit, and Marcatel [WTBB<sup>+</sup>20] gave key-recovery timing attack against HQC as above. Guo et al. [GJN20] pointed out a potential timing-leakage of the equality test of HQC. Again, unfortunately, their targets are HQC with the BCH-Repetition code.

**KR-PCA against HQC in Round 3:** We give a rough idea for HQC with the RS-RM code  $\mathscr{C}$ : Let  $\tilde{y}$  = trunc( $y, n_1 n_2$ ), the first  $n_1 n_2$  coefficients of y. Let us consider (1, v) as a ciphertext and  $m_{guess} = 0^{256}$  and query them to the plaintext-checking oracle. The decryption algorithm will compute  $a := v \oplus \text{trunc}(1 \cdot y, n_1 n_2) = v \oplus \tilde{y}$ and decode it into decode(a). Hence, the plaintext-checking oracle on input (1, v) and  $0^{256}$  tells us if decode( $v \oplus \tilde{y}$ ) is decoded into  $0^{256}$  or not.

Băetu et al. [BDH<sup>+</sup>19, Section 3.5] gave an efficient algorithm to learn  $\delta \in \{0, 1\}^n$  from the oracle BOO(x) which returns boole(HW( $x \oplus \delta$ )  $\leq \rho$ ), whose number of queries is at most  $n + \lg(n)$ . We note that we can use the learning algorithm of Băetu et al. [BDH<sup>+</sup>19, Section 3.5] for  $\{0, 1\}^n$ , while we consider the Reed-Solomon code over  $\mathbb{F}_{2^8}$ .

We will mount a two-phase attack as the attacks in [BDH<sup>+</sup>19, HV20]. Let us consider a string of  $n_1$  packets of  $n_2$  bits. Let  $t_1 := (d_1 - 1)/2$  be the maximum Hamming weight of an error that the Reed-Solomon decoder can correct.

1. At first, we learn which packets of  $\tilde{y}$  contain an error using the learning algorithm of Băetu et al.with  $n_1 + \lg(n_1)$  queries.

Each packet represents 0 and 1 by  $0^{n_2}$  and  $1^{n_2}$ , which can be considered as the codeword of the duplicated Reed-Muller code corresponding to 0 and 1 in  $\mathbb{F}_2^8$ , respectively. Notice that  $\tilde{y}$ 's Hamming weight is at most

*w*, since *y* is in  $S_w$ , and  $d_2$  are larger than the double of *w*. Thus, each packet of  $\tilde{y}$  is decoded into 0 originally and the packet xored by  $1^{n_2}$  is decoded into 1. The Reed-Solomon decoder will fail to decode the received word into 0 if the received word contains at least  $(t_1 + 1)$  1's. Thus, we can use the learning algorithm for  $\{0, 1\}^{n_1}$ .

- 2. Next, for each packet, we modify  $\tilde{y}$  to have exactly  $t_1 1$  incorrect other packets and apply the learning algorithm on the packet with the threshold of the duplicate Reed-Muller codes. This requires  $n_2 + \lg(n_2)$  queries on each packet. After that we know  $\tilde{y}$ .
- 3. Finally, we compute the last rest  $n n_1 n_2$  bits of y by checking if  $h_1 h_0 y \in S_w$  or not. This is done by brute force on  $2^{n-n_1n_2}$  candidates.

## C.8 NTRU Prime

**NTRU LPRime (ntrulpr) of NTRU Prime:** Since we already gave the key-recovery attack using the plaintextchecking oracle in section 4, we omit the details.

## Streamlined NTRU Prime (sntrupr) of NTRU Prime

Streamlined NTRU Prime (sntrupr) of NTRU Prime: Streamlined NTRU Prime (sntrupr) has parameter sets p, q, and w. p and q are prime numbers and w is a positive integer. We note that  $2p \ge 3w$  and  $q \ge 16w + 1$ . They choose q = 6q' + 1 for some q'. For concrete values, see Table 15.

Table 15: Parameter sets of sn	ntrupr of NTRU Prime
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parameter sets	p	q	w
sntrupr653	653	4621	288
sntrupr761	761	4591	286
sntrupr857	857	5167	322
sntrupr953	953	6343	396
sntrupr1013	1013	7177	448
sntrupr1277	1277	7879	492

Let  $\mathscr{R} := \mathbb{Z}[x]/(x^p - x - 1)$  and  $\mathscr{R}_a := (\mathbb{Z}/a)[x]/(x^p - x - 1)$  for a = 3, q. Let  $\mathscr{T} := \{a = \sum_{i=0}^{p-1} a_i x^i \in \mathscr{R} \mid a_i \in \{-1, 0, +1\}\}$ , a set of "small" polynomials. Let  $\mathscr{S} := \{a = \sum_{i=0}^{p-1} a_i x^i \in \mathscr{R} \mid a_i \in \{-1, 0, +1\}, HW(a) = w\}$ , a set of "short" polynomials. For  $a \in [-(q-1)/2, (q-1)/2]$ , define Round $(a) = 3 \cdot [a/3]$ .<sup>23</sup>

The underlying CPA-secure PKE scheme<sup>24</sup> works as follows:

- Gen(*pp*): Choose  $g \leftarrow \mathcal{T}$  that satisfies  $g \in \mathscr{R}_3^{\times}$  at random. Compute  $1/g \in \mathscr{R}_3$ . Choose  $f \leftarrow \mathcal{S}$ . Compute  $h := g/(3f) \in \mathscr{R}_q$ . Output pk := h and sk := (f, 1/g).
- $\text{Enc}(pk, r \in S)$ : Compute  $hr \in \mathcal{R}_q$  and output  $c := \text{Round}(hr \mod^{\pm} q)$ .
- Dec(sk = (f, v), c): Compute  $e := (3fc \mod^{\pm} q) \mod^{\pm} 3$ . Compute  $r' := ev \mod^{\pm} 3$ . Output r' if HW(r') = w. Otherwise, output  $r'_{\text{invalid}} := (1, 1, ..., 1, 0, ..., 0)$  with  $\text{HW}(r'_{\text{invalid}}) = w$ .

Due to rounding, we have a 'short' error *m* such that c = hr + m.

#### Review of key-recovery attacks against Streamlined NTRU Prime:

<sup>&</sup>lt;sup>23</sup> When q = 6q' + 1, Round([-(q-1)/2, (q-1)/2])  $\in [-(q-1)/2, (q-1)/2]$ .

<sup>&</sup>lt;sup>24</sup> 'Streamlined NTRU Prime Core' in the specification.

*Review of KR-PCA:* One might consider that designing a key-recovery plaintext-checking attack for sntrupr (Streamlined NTRU Prime)is easy by following the key-recovery plaintext-checking attacks for NTRU-HPS [DDS<sup>+</sup>19] and that for NTRU-HRSS [ZCQD21]. However, there are several obstacles and we fail to design the KR-PCA.

The first obstacle is that it is hard to fix m = 0, since *m* is determined by *hr* and Round(*hr*).

Even if we could fix m = 0, there are more obstacles. Notice that Dec checks the Hamming weight of r'. In the KR-PCAs against NTRU, they use small-weight plaintext (r, 0) to check the information of the secret key. The Hamming-weight check judges such plaintexts invalid.

Very recently, Ravi, Ezerman, Bhasin, Chattopadhyay, and Roy [REB<sup>+</sup>21] proposed a key-recovery plaintextchecking attack against the underlying PKE of sntrupr by extending the key-recovery attack by Jaulmes and Joux [JJ00], which they call a key-recovery attack using the decryption failure oracle. They mount their attack against sntrupr761.

*Review of key-recovery SCA/FIA:* Huang, Chen, and Yang [HCY19] gave key-recovery SCAs against Streamlined NTRU Prime. Ravi, Ezerman, Bhasin, Chattopadhyay, and Roy [REB<sup>+</sup>21] gave two key-recovery SCAs. The first one exploits side-channel information whether  $r' = ev \mod^{\pm} 3$  is 0 or not in decryption [REB<sup>+</sup>21, Section 3]. The second one exploits side-channel information whether r' output by Dec is valid or invalid one  $r'_{invalid}$  [REB<sup>+</sup>21, Section 4].

# C.9 SIKE

*Brief Review of SIKE:* SIKE [JAC<sup>+</sup>20] is KEM scheme based on SIDH [JD11, DJP14]. For a survey of isogeny-based cryptography, we recommend reading [Cos21].

Let  $p = 2^{e_2}3^{e_3} - 1$ . Let *E* be a supersingular elliptic curve over  $\mathbb{F}_{p^2}$ . Let  $P_2, Q_2 \in E[2^{e_2}]$  and  $P_3, Q_3 \in E[3^{e_3}]$  linearly independent points of order  $2^{e_2}$  and  $3^{e_3}$  respectively. Let  $\{0, 1\}^n$  be a message space and let  $\mathbb{F} : \mathbb{F}_{p^2} \to \{0, 1\}^n$  be a random oracle.

Roughly speaking, the underlying PKE scheme  $[JAC^+20, Algorithm 1]$  is summarized as follows (for the details, see the specification):

- $\operatorname{isogen}_{\ell}(sk_{\ell})$  with  $(m, \ell) = (2, 3)$  or (3, 2): On input  $sk_{\ell} \in [0, \ell^{e_{\ell}})$ , compute  $S := P_{\ell} + [sk_{\ell}]Q_{\ell}$ , compute isogeny  $\phi_{\ell} : E \to E/\langle S \rangle$ , and compute  $E'_{m} := E/\langle S \rangle = \phi_{\ell}(E)$ . Compute  $P'_{m} := \phi_{\ell}(P_{m})$  and  $Q'_{m} := \phi_{\ell}(Q_{m})$ . Output  $(E'_{m}, P'_{m}, Q'_{m})$ .<sup>25</sup>
- $\operatorname{isoex}_{\ell}(pk_m, sk_{\ell})$  with  $(m, \ell) = (2, 3)$  or (3, 2): On input  $pk_m = (E'_{\ell}, P'_{\ell}, Q'_{\ell})$  and  $sk_{\ell} \in [0, \ell^{e_{\ell}})$ , compute  $S := P'_{\ell} + [sk_{\ell}]Q'_{\ell}$  and compute  $E''_{\ell} := E'_{\ell}/\langle S \rangle = E'_{\ell}/\langle \phi_m(P_{\ell} + [sk_{\ell}]Q_{\ell}) \rangle$ . Compute  $j_{\ell}$  as the *j*-invariant of  $E''_{\ell}$ .
- Gen(*pp*): Choose  $sk_3 \leftarrow [0, 3^{e_3})$  and  $pk_3 := isogen_3(sk_3)$ . Output  $pk_3$  and  $sk_3$ .
- $\operatorname{Enc}(pk_3, \mu)$ : Choose  $sk_2 \leftarrow [0, 2^{e_2})$  and  $c_2 := \operatorname{isogen}_2(sk_2)$ . Compute  $j := \operatorname{isoex}_2(pk_3, sk_2)$ . Compute  $c' := F(j) \oplus \mu$ . Output  $(c_2, c')$ .
- $\text{Dec}(sk_3, (c_2, c'))$ : Compute  $j' := \text{isoex}_3(c_2, sk_3)$  and output  $\mu' := c' \oplus F(j')$ .

## Review of key-recovery attacks against SIDH/SIKE:

*Review of KR-PCA:* Galbraith, Petit, Shani, and Ti [GPST16] gave a key-recovery key-mismatch against SIDH with a fixed key. This can be easily converted into a key-recovery plaintext-checking attack against the underlying PKE of SIKE. See e.g., a writeup by goulov and mandlebro on the problem sidhe in PlaidCTF 2020 [gm20].

*Review of key-recovery SCA/FIA:* Ti [Ti17] gave a key-recovery FIA against SIDH with a fixed secret and signature schemes based on SIDH, which queries a random point *X*, obtains  $\phi(X)$  for a secret isogeny  $\phi$ , and recovers  $\phi$ . Thus, it cannot be used in the context of a key-recovery attack against PKE. Koziel, Azarderakhsh, and Jao [KAJ17] gave key-recovery SCAs against SIDH with a fixed key and a PKE version of SIDH, which is equivalent to the underlying PKE of SIKE. Gélin and Wesolowski [GW17] gave a key-recovery FIA against SIDH with fixed key and the PKE version of SIDH, which uses *loop-abort* fault-injection to stop iterating computation of elliptic curves. Koppermann, Pop, Heyszl, and Sigl [KPHS18] gave a key-recovery SCA against SIKE and discussed countermeasures. Zhang et al. [ZYD<sup>+</sup>20] also gave a key-recovery SCA against SIKE. Tasso, De Feo, El

<sup>&</sup>lt;sup>25</sup> Correctly speaking, this algorithm outputs  $(P'_m, Q'_m, R'_m := P'_m - Q'_m)$  and omits  $E'_m$ . We can reconstruct  $E'_m$  from  $P'_m, Q'_m$ , and  $R'_m$ .

$$pp = (E, P_2, Q_2, P_3, Q_3) \xrightarrow{r} (E_2', P_2', Q_2'):$$

$$isoex_2(pk_3, sk_2) \xrightarrow{r} (E_2'') = E_2'/\langle P_2' + [sk_2]Q_2' \rangle \xrightarrow{r} (sogen_3(sk_3)) \xrightarrow{r} (sogen_3(sk_3)) \xrightarrow{r} (sogen_2(sk_2)) \xrightarrow{r} (sogen_2(s$$

Fig. 20: Diagram of the underlying KE scheme of SIKE.

Mrabet, and Pontié [TDFEMP21] implemented Ti's attack [Ti17] against the SIKE round 3 implementation and discussed countermeasures. Genêt, and Linard de Guertechin, and Kaluðerović [GLdGK21] gave a single-trace SCA against SIKE. We note that all of them do not exploits the equality test of SIKE.

**KR-PCA against the underlying PKE scheme of SIKE:** We follow the GPST attack proposed by Galbraith, Petit, Shani, and Ti [GPST16] and adapt it to the PKE scheme. They explicitly write down a key-recovery attack using the key-mismatch oracle against SIDH, where its secret key is  $sk_2$ . They confirmed their attack is easily applicable to the case of  $sk_3$  in [GPST16, Remark 2]. For the case of  $sk_3$ , see e.g., a writeup by goulov and mandlebro on the problem sidhe in PlaidCTF 2020 [gm20]. We here review how the attack works, because there are some differences. For example, we need the plaintext-checking oracle instead of the key-mismatch oracle; we do not need the scale-up factor  $\theta$  in the attacks, since the uncompressed SIKE does not involve the pairing checks.

In order to count the number of queries, we briefly review how the attack extracts  $sk_3$ . Suppose that we know the first *i* trits of  $sk_3$  and write  $sk_3$  as

$$sk_3 = k_i + s_i 3^i + s' 3^{i+1}$$
,

where  $k_i \in [0, 3^{i-1})$  is known,  $s_i \in \{0, 1, 2\}$ , and  $s' \in \mathbb{Z}$  are unknown.

Let  $pk_3 = (E'_2, P'_2, Q'_2)$ . We generate  $c_2 = (E'_3, P'_3, Q'_3)$ , where  $E'_3 := E/\langle P'_2 + [sk_2]Q'_2\rangle$ ,  $P'_3 = \phi_2(P_3)$ , and  $Q'_3 = \phi_2(Q_3)$ . We also generate  $E''_2 := E'_2/\langle P'_2 + [sk_2]Q'_2\rangle$ , and its *j*-invariant  $j_k := j(E'_2/\langle P'_2 + [sk_2]Q'_2\rangle)$ , and  $k := F(j_k)$  as the encryption. In order to recover  $s_i \in \{0, 1, 2\}$ , we compute

$$c^{(z)} = (E'_3, P^{(z)}, Q^{(z)}) = (E'_3, P'_3 - [3^{e_3 - i - 1}(k_i + z3^i)]Q'_3, [1 + 3^{e_3 - i - 1}]Q'_3)$$

for z = 0, 1, 2 and query  $(c^{(z)}, k)$  with guessing plaintext  $0^n$ .

The decryption algorithm first computes

$$\begin{split} S^{(z)} &= P^{(z)} + [sk_3]Q^{(z)} \\ &= P'_3 - [3^{e_3 - i - 1}(k_i + z3^i)]Q'_3 + [sk_3][1 + 3^{e_3 - i - 1}]Q'_3 \\ &= P'_3 + [sk_3]Q'_3 + [-3^{e_3 - i - 1}(k_i + z3^i) + 3^{e_3 - i - 1}(k_i + s_i3^i + s'3^{i + 1})]Q'_3 \\ &= P'_3 + [sk_3]Q'_3 + [(s_i - z)3^{e_3 - 1}]Q'_3, \end{split}$$

where we used the fact that  $P'_3$  and  $Q'_3$  are of order  $3^{e_3}$ . The subgroups  $\langle P'_3 + [sk_3]Q'_3\rangle$ ,  $\langle P'_3 + [sk_3]Q'_3 + [3^{e_3-1}]Q'_3\rangle$ , and  $\langle P'_3 + [sk_3]Q'_3 + [2 \cdot 3^{e_3-1}]Q'_3\rangle$  are distinct and, (heuristically speaking),  $j_k = j(E/\langle P'_3 + [sk_3]Q'_3 + [(s_i - z)3^{e_3-1}]Q'_3\rangle)$  if and only if  $s_i = z$ . If  $s_i = z$ , then the decryption algorithm obtains the plaintext  $0^n$  and the PCO returns 1. Otherwise, it will obtain the plaintext  $F(j_k) \oplus F(j(E'_3/\langle P'_3 + [sk_3]Q'_3 + [(s_i - z)3^{e_3-1}]Q'_3\rangle))$ , which is not  $0^n$  heuristically, and the PCO returns 0.

In the context of the skipping-equality-test attack, we will check  $K = H(0^k, ct)$  or not. Summarizing the above, we can determine  $s_i \in \{0, 1, 2\}$  for  $i = 0, ..., e_3 - 1$  by sending two queries with z = 0 and 1 and guessing key *K* and checking the returned value.