Analyzing the Provable Security Bounds of GIFT-COFB and Photon-Beetle

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December 31, 2021

Abstract. We study the provable security claims of two NIST Lightweight Cryptography (LwC) finalists, GIFT-COFB and Photon-Beetle, and present several attacks whose complexities contradict their claimed bounds in their final round specification documents. For GIFT-COFB, we show an attack using q_e encryption queries and no decryption query to break privacy (IND-CPA). The success probability is $O(q_e/2^{n/2})$ for n-bit block while the claimed bound contains $O(q_e^2/2^n)$. This positively solves an open question posed in [Khairallah, ePrint 2021/648]. For Photon-Beetle, we show attacks using q_e encryption queries (using a small number of input blocks) followed by a single decryption query and no primitive query to break authenticity (INT-CTXT). The success probability is $O(q_e^2/2^b)$ for b-bit block permutation, and it is significantly larger than what the claimed bound tells. We also analyze other (improved/modified) bounds of Photon-Beetle shown in the subsequent papers [Chakraborty et al., ToSC 2020(2) and Chakraborty et al., ePrint 2019/1475].

We emphasize that our results do not contradict the claimed "bit security" in the LwC specification documents for any of the schemes that we studied. That is, we do not negate the claims that GIFT-COFB is $(n/2-\log n)$-bit secure for $n = 128$, and Photon-Beetle is $(b/2 - \log b/2)$-bit secure for $b = 256$ and $r = 128$, where r is a rate.

1 Introduction

NIST Lightweight cryptography[3] aims at standardizing authenticated encryption (AE) schemes for resource-constrained devices. In March 2021, NIST has announced ten finalists among the 32 second-round candidates. The finalists include GIFT-COFB [3] and Photon-Beetle [5]. GIFT-COFB is a block cipher-based AE that combines a variant of COFB mode [9] and the lightweight 128-bit block cipher GIFT [4]. Photon-Beetle is a permutation-based AE that combines Beetle mode [7] and the lightweight cryptographic permutation Photon [14], which is an

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[*] Alphabetical order
[3] https://csrc.nist.gov/projects/lightweight-cryptography

ISO standard [1]. This paper studies the provable security bounds of GIFT-COFB and Photon-Beetle, and shows some attacks whose success probabilities are inconsistent with the presented security bounds in the final round specification documents of NIST LwC.

GIFT-COFB. For the original COFB and GIFT-COFB, the security bounds with respect to the combined AE notion of IND-CPA and INT-CTXT were presented in [3, 9]. Assuming a nonce-respecting attacker and that the underlying block cipher is a random permutation, GIFT-COFB's AE bound is roughly $\sigma^2/2^n + nq_d/2^{n/2}$ for $\sigma = \sigma_e + \sigma_d + q_e + q_d$, where σ_e (resp. σ_d) denotes the total queried blocks in encryption (resp. decryption) queries, and q_e (resp. q_d) denotes the number of encryption (resp. decryption) queries. This bound suggests that, if (1) σ_e reaches $2^{n/2}$, or (2) σ_d reaches $2^{n/2}$, or (3) q_d reaches $2^{n/2}/n$, the bound reaches 1 and hence no security guarantee is possible. The tightness of these conditions has been studied by Khairallah [16, 17, 18] and Inoue and Minematsu (IM21) [15]. Khairallah [16, 17, 18] showed attacks with $q_d = 2^{n/2}$ with about $\sigma_e = 2^{n/2}$ or $\sigma_e = 2^{n/4}$, called Weak Key attack and Mask collision attack [16, 17]. Khairallah finally showed one with $q_e = 1$, $\sigma_e = O(1)$ (a few blocks) and $q_d = 2^{n/2}$, called Mask Presuming attack [18]. The last one implies that the tightness condition (3) has only the small gap of $\log n$ factor. Inoue and Minematsu [15] studied the tightness of (1) and showed an attack with $\sigma_e = 2^{n/2}$ and $q_d = 1$. As in the previous attacks, this attack breaks the authenticity, and matches the aforementioned bound. For (2) it remains unsolved, and [15] mentioned that it might be an artifact in the proofs.

We take a closer look at the condition (1). IM21's attack with q_e encryption queries and 1 decryption query has success probability roughly $q_e^2/2^n$. However, we found an improved attack that needs q_e encryption queries to break privacy (hence the combined AE notion) success probability roughly $q_e/2^{n/2}$. The existence of such an attack has been posed as an open problem by Khairallah [18]. We solved this positively. This implies a contradiction with the bound in the NIST LwC document although the bit level security maintains. We give a brief analysis on the root of this contradiction in Sect. 3.2.

Photon-Beetle. For Photon-Beetle, the security proofs for the original version and the NIST LwC version have been shown in [5,7,8]. For b-bit block permutation with $b = 256$ and rate (which is the length of one message block processed in one permutation call) $r = 128$, the security bounds roughly tell $b/2 - \log b/2 = 121$-bit security for both IND-CPA and INT-CTXT. Dobraunig and Mennink commented on a constant factor related to a key recovery attack [13], and Mège analysed the security of the hash function [19].

We focus the authenticity bound shown in the final round NIST LwC submission document [5], which is roughly $q_p(q + q')/2^b + rq_p/2^{b/2} + q_p^r/2^{(b/2)\cdot(r-1)} + r\sigma'/2^{256-r}$, where q_p, q, q' and σ' denote the number of primitive queries, the number of encryption queries, the number of decryption queries, and the total number of blocks in decryption queries. The rate can be either $r = 128$ or 32, where $r = 128$ is the primary setting. The tag length is 128 bits for both cases.

When $r = 128$, we observed that if $q_p = 0$, *i.e.* we do not query the primitive (permutation), the above authenticity bound reduces to the bound that has no contribution from encryption queries. We invalidate this by presenting a simple forgery using $2^{b/2}$ encryption queries and single decryption query. The success probability is close to 1, while the claimed bound indicates a negligibly small probability with that complexity. This attack shows an inconsistency with the claimed bound and implies the lack of the birthday term with respect to the block size, $O(q_e^2/2^b)$, in the claimed bound. Moreover, when $r = 32$, the INT-CTXT bound reduces to the bound that is smaller than $q'/2^{128}$, which is impossible to achieve for any AE of 128-bit tags. Thus, a simple tag guessing attack (*i.e.*, decryption queries with identical nonce, AD, ciphertext, and distinct tags) invalidates the claimed bound. This implies even the break of bit level security suggested by the bound. However, the bit security shown in [5, Table 4.1] claims 128-bit authenticity. We clarify that we do not break the figure. Moreover, we study other (improved or modified) security bounds for Photon-Beetle shown in the subsequent papers [11, 12]. In [12], an improved bound AE bound is presented. The bound claims that the IND-CPA security is maintained beyond $2^{b/2}$ encryption queries, but this is not possible to achieve. The same paper presents a simplified AE bound, and we point out that this cannot be true. We then clarify that the ePrint version [11] of [12] addresses the issue, while we still see an issue in simplification.

Our attacks do not depend on the primitives, and do not break the primitives. The attack against GIFT-COFB does not work against the COFB versions in [9,10] because of the shorter nonce length than the NIST LwC version. Our attacks show some inconsistencies in the claimed security bounds of GIFT-COFB and Photon-Beetle. At the same time, we would like to emphasize that these results do not negate the claimed bit security levels of GIFT-COFB and Photon-Beetle.

2 Notations

For the specifications of GIFT-COFB and Photon-Beetle, refer to the specification documents [3,5]. We use the same notations as [3,5] to describe our attacks. We assume the basic knowledge on the authenticated encryption and its syntax and the relevant security notions (see *e.g.* [6]).

3 Analysis of **GIFT-COFB**

We show our attack against GIFT-COFB that contradicts the claimed security bound. As mentioned earlier, this does not invalidate the claimed bit security levels, namely 64-bit IND-CPA security and 58-bit INT-CTXT security in the specification document.

3.1 Our Attack

For an AE scheme Π, let $\mathbf{Adv}_{\Pi}^{\mathrm{AE}}(\mathcal{A})$ denote the "AE advantage" against Π by an attacker $\mathcal{A}$, which is the indistinguishability between the tuple of real encryption
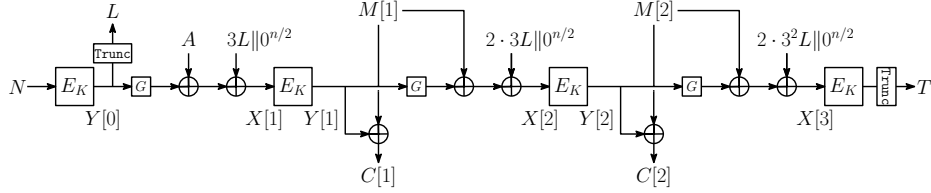
Fig. 1: The first encryption query of the attack against GIFT-COFB.

and decryption routines of Π (also called the real world) and the tuple of the random-bit oracle that always returns a random string and the rejection oracle that always returns the rejection symbol (also called the ideal world). See *e.g.* [20]. The security bound shown in the latest NIST LwC specification document is as follows (with minor changes in notations):

Theorem 1 (Chapter 4 in [3]).

$$\mathbf{Adv}^{\mathrm{AE}}_{\mathsf{GIFT\text{-}COFB}}(\mathcal{A}) \leq \mathbf{Adv}^{\mathrm{prp}}_{\mathsf{GIFT}}(q',t') + \frac{\binom{q'}{2}}{2^n} + \frac{1}{2^{n/2}} + \frac{q_d(n+4)}{2^{n/2+1}}$$
$$+ \frac{3\sigma_e^2 + q_d + 2(q_e + \sigma_e + \sigma_d)\cdot\sigma_d}{2^n},$$

where $q' = q_e + q_d + \sigma_e + \sigma_d$, which corresponds to the total number of block cipher calls through the game, and $t' = t + O(q')$. Note that the advantage has been taken by the maximum advantage over all the adversaries making q_e encryption queries, q_d decryption queries and running in time t, such σ_e, σ_d are the total number of blocks queried in the encryption and decryption queries, respectively.

When we only use encryption queries, the above bound effectively reduces to about $\sigma_e^2/2^n$ and hence about $q_e^2/2^n$ if each message is short. We present an attack using q_e encryption queries (where each message is short) with success probability about $q_e/2^{n/2}$. This contradicts the bound of Theorem 1, since $q_e^2/2^n \leq q_e/2^{n/2}$ necessarily holds when $1 \leq q_e \leq 2^{n/2}$. The attack proceeds as follows.

1. The attacker makes a query (N, A, M) to the encryption oracle such that $|A| = n$, $|M| = 2n$ and $M = M[1] \,\|\, M[2]$ (for arbitrarily chosen N, single-block A and two-block M), and it obtains corresponding (C, T), where $C = C[1] \,\|\, C[2]$, as shown in Fig. 1.
2. The attacker computes $Y[1]$, $Y[2]$, and $\mathtt{lsb}_{n/2}(X[2]) = \mathtt{lsb}_{n/2}(G(Y[1]) \oplus M[1])$. Note that $\mathtt{msb}_{n/2}(X[2])$ is unknown; nevertheless, the attacker can mount a privacy attack by using *the guessed $X[2]$* as the nonce of the next encryption query.
3. For $0 \leq i \leq 2^{n/2}-1$, the attacker queries (N_i, A_i, M_i), where $|A_i| = |M_i| = n$, to the encryption oracle such that

$$N_i = (i)_{n/2} \,\|\, \mathtt{lsb}_{n/2}(X[2]), \quad L_i := \mathsf{Trunc}_{n/2}(Y[2]),$$
$$A_i = N_i \oplus G(Y[2]) \oplus 3L_i \,\|\, 0^{n/2},$$
$$M_i = N_i \oplus G(Y[2]) \oplus 3^2 L_i \,\|\, 0^{n/2},$$

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where $(i)_{n/2}$ denotes $n/2$-bit string of a binary representation of i. The attacker obtains corresponding (C_i, T_i). In the real world, there always exists i such that $M_i \oplus C_i = Y[2]$ and $T_i = \mathsf{Trunc}_\tau(Y[2])$, where i fulfilling $N_i = X[2]$. In the ideal world, $\Pr[M_i \oplus C_i = Y[2], T_i = \mathsf{Trunc}_\tau(Y[2])] = 1/2^{n+\tau}$ holds for all i, and thus the attacker can find i such that $M_i \oplus C_i = Y[2]$ and $T_i = \mathsf{Trunc}_\tau(Y[2])$ holds with a negligibly small probability, $1/2^{n/2+\tau}$.

In the real world, the above attack fails when $N = X[2]$ accidentally holds because it prevents the attacker from using $X[2]$ for the next nonce. To prevent such a case, the attacker can query a longer plaintext in Step 1, and it can find $X[\cdot]$ s.t. $\mathtt{lsb}_{n/2}(X[\cdot]) \neq \mathtt{lsb}_{n/2}(N)$ with a sufficiently high probability.

We remark that this attack does not work against versions of COFB in TCHES 2017 [9] and Journal of Cryptology [10] because the nonce length of these versions is $n/2$ bits.

3.2 Brief analysis on the security proof

As we mentioned in the previous section, the security bound shown in [3, Chapter 4] does not include the term $O(q_e/2^{n/2})$ nor $O(\sigma_e/2^{n/2})$. However, in [3, Sect. 4.2], the authors provide INT-CTXT bound, which includes the term $3\sigma_e/2^{64}$ assuming $n = 128$. This term is somehow missing in the final bound of the AE advantage that combines privacy and authenticity. Still, in any case, since our attack uses only encryption queries, the terms $O(q_e/2^{n/2})$ or $O(\sigma_e/2^{n/2})$ should appear in the IND-CPA security bound, originally presented in [3, Sect. 4.1]. Let us look into [2] which shows the full proof of GIFT-COFB. The authors define the following two events as the bad events.

B1: $X_{i_1}[j_1] = X_{i_2}[j_2]$ for some $(i_1, j_1) \neq (i_2, j_2)$ where $j_1, j_2 > 0$.
B2: $Y_{i_1}[j_1] = Y_{i_2}[j_2]$ for some $(i_1, j_1) \neq (i_2, j_2)$ where $j_1, j_2 > 0$.

Here, $X_i[j]$ and $Y_i[j]$ denote input and output of the j-th underlying block cipher call in the i-th encryption query. Also, $X_i[0] := N_i$, where N_i is the nonce value in the i-th encryption query. As our attack shows, the attacker can produce a collision between $X_i[0]$ and $X_1[2]$ with probability $q_e/2^{n/2}$. One can speculate that this inconsistency could be fixed by setting $j_1, j_2 \geq 0$ in the above events (then it covers the presented attack), rather than $j_1, j_2 > 0$.

4 Analysis of Photon-Beetle

We here show our attacks against Photon-Beetle that violate its claimed security bound in NIST LwC documentation [5]. We emphasize that our attacks do not violate the claimed "bit security" levels of Photon-Beetle, which are 121-bit IND-CPA and INT-CTXT security when $r = 128$, and 128-bit IND-CPA and INT-CTXT security when $r = 32$.

4.1 Claimed security bound and our attack

In [5], Photon-Beetle is claimed to be provably secure, with the security bound of

$$
O\left(\frac{\sigma^2}{2^{256}} + \frac{q_p}{2^{256-r}} + \frac{q \cdot q_p}{2^{256}} + \frac{rq_p}{2^{128}} + \frac{\sigma_e^r}{2^{128(r-1)}} \right)
$$

for privacy (IND-CPA), where σ is the total number of blocks in encryption queries, q_p is the number of offline queries, r is the rate ($r = 32$ or 128), q is the number of encryption queries, and σ_e is the total number of blocks in encryption queries [5, Sect. 4.1][4]. For authenticity (INT-CTXT), the claimed bound is

$$
O\left(\frac{q_p(q + q')}{2^{256}} + \frac{rq_p}{2^{128}} + \frac{q_p^r}{2^{128(r-1)}} + \frac{r\sigma'}{2^{256-r}} \right) , \tag{1}
$$

where q_p is the number of offline queries, q is the number of encryption queries, q' is the number of decryption queries, r is the rate ($r = 32$ or 128), and σ' is the total number of blocks in decryption queries [5, Sect. 4.2].

We present two attacks that invalidate the bound in (1). The observation is that, when $q_p = 0$, *i.e.*, when the attacker does not make offline queries, then the bound (1) is simplified into

$$
O\left(\frac{r\sigma'}{2^{256-r}} \right) . \tag{2}
$$

We observe that the bound (2) claims that the authenticity security is maintained even if the attacker makes unlimited number of encryption queries, and that the success probability is smaller than $\sigma'/2^{128}$ when $r = 32$. In what follows, we present attacks based on these observations.

Birthday forgery against Photon-Beetle. The attack is as follows.

1. Let $q = 2^{b/2}$, and fix q distinct nonces $N_1, \ldots, N_q$, q distinct AD $A_1, \ldots, A_q$ with $|A_i| = b$, and q distinct messages $M_1, \ldots, M_q$ with $|M_i| = b + r$. The attacker chooses $M_1, \ldots, M_q$ of the form $M_i = M' \| M_i'$, where $|M'| = b$, $|M_i'| = r$, and $M_1', \ldots, M_q'$ take q distinct values. That is, the first b bits of $M_1, \ldots, M_q$ take the same value M', and the corresponding portions of ciphertexts are used to detect a full-state collision.
2. Make q encryption queries $(N_1, A_1, M_1), \ldots, (N_q, A_q, M_q)$ and obtain (C_1, T_1), $\ldots, (C_q, T_q)$, where $|C_i| = b + r$.
3. Find (i, j) such that $C_i' = C_j'$, where C_i' is the first b bits of C_i, and the same for C_j'.
4. Output (N_i, A_i, C_j, T_j) (or (N_j, A_j, C_i, T_i)) as the forgery.

See Fig. 2 for the process of (N_i, A_i, M_i) and (N_j, A_j, M_j) when $r = 128$. With a high probability, we have a full-state collision, *i.e.*, we have (i, j) such that $S_i = S_j$ in the figure. The collision can be detected from C_i' and C_j', which are
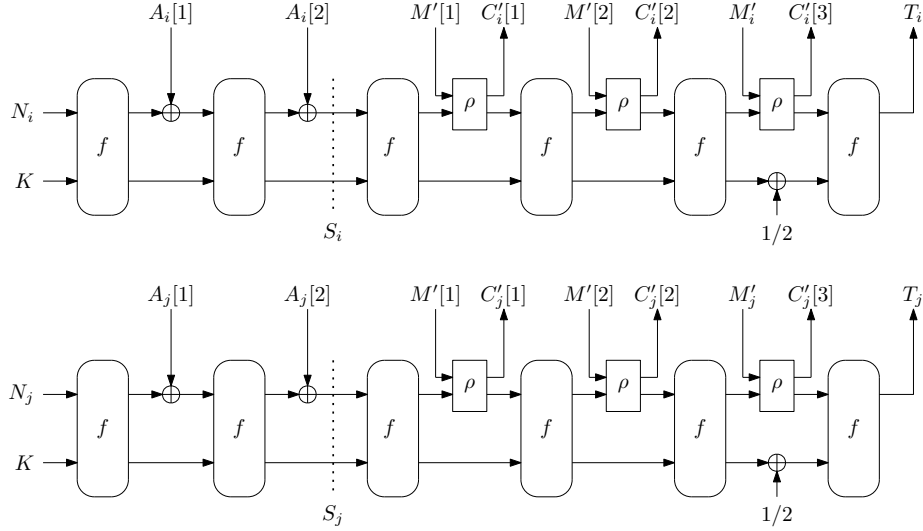
Fig. 2: Two encryption queries (N_i, A_i, M_i) and (N_j, A_j, M_j) when $r = 128$. Here, $A_i = A_i[1] \,\|\, A_i[2]$ and $M_i = M'[1] \,\|\, M'[2] \,\|\, M'_i$.

the first b bits of C_i and C_j. If this happens, we see that the forgery in Step 4 succeeds.

The bound (2) claims that the success probability of the attack is negligibly small and at most $O(7r/2^{256-r})$ when $r = 128$ (or at most $O(6r/2^{256-r})$ depending on the interpretation of σ'), while the attack succeeds with an overwhelming probability. Therefore, the bound (1) is invalidated.

Tag guessing attack against Photon-Beetle with $r = 32$**.** When $r = 32$, the above setting of $q_p = 0$ makes the INT-CTXT bound (1) reduces to $32\sigma'/2^{256-32} = \sigma'/2^{219}$ which is smaller than $\sigma'/2^{128}$. When σ' is close to q', this implies a bound that is not possible to achieve with 128-bit tags. A simple tag guessing attack invalidates this bound, that is, q' decryption queries using identical (nonce, AD, ciphertext) tuple with distinct tags will succeed with probability about $q'/2^{128}$.

Discussion and Implication. In [5, Sect. 4.2], the designers outline the proof of the bound (1). To quote:

> Also, if an adversary can obtain a state collision among the input/output of a permutation query with the state of an encryption query or decryption query, it can use the fact to mount an forgery attack.

The argument here ignores a full-state collision among encryption queries, resulted in the first attack. Here is another quote from the same document:

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[4] We do not know the difference between σ and σ_e.

The trivial solution for forging is to guess the key or the tag which can be bounded by $\frac{q+q'}{2^{128}}$.

We do not find an issue here, while for $r = 32$, the bound (1) makes a stronger security claim than this argument.

We note that the above two attacks need 2^{128} complexity, and thus do not violate the claimed 121-bit security (when $r = 128$) or 128-bit security (when $r = 32$). However, our attacks show that the theoretical reasoning for the bit security in the NIST LwC document [5] is inaccurately mentioned.

4.2 Analysis of the bound in [12]

There are various provable security claims related to Beetle $[5, 7, 8, 11, 12]$. We do not consider the bound in $[7, 8]$ for the difference in the specification.

For Photon-Beetle, we write the combined AE advantage as $\mathbf{Adv}^{\mathsf{aead}}_{\mathsf{Photon\text{-}Beetle}}(\mathcal{A})$, which is the same as the case of COFB except that the attacker has additional oracles to compute the forward and inverse directions of the permutation. In [12], improved provable security bounds of Photon-Beetle are presented. Corollary 1 in [12] claims that, in the combined AE notion, the success probability of the attacker for the case $r = 128$ is

$$
\mathbf{Adv}^{\mathsf{aead}}_{\mathsf{Photon\text{-}Beetle}}(\mathcal{A}) \leq \frac{4\tau\sigma_d}{2^c} + \frac{4r\sigma_d}{2^c} + \frac{4b\sigma_d}{2^c} + \frac{q_p}{2^\kappa} + \frac{2q_d}{2^\tau} + \frac{2\sigma_d(\sigma + q_p)}{2^b}
$$
$$
+ \frac{6\sigma_e q_p}{2^b} + \frac{8rq_p}{2^c} + \frac{4\tau q_p}{2^{b-\tau}} + \frac{\sigma_e + q_p}{2^b} + \frac{4rq_p\sigma_d}{2^{2c}}, \qquad (3)
$$

where τ is the tag length, c is the capacity, r is the rate, $b = r + c$, κ is the key length, q_e is the number of encryption queries, q_d is the number of decryption queries, σ_e is the total number of blocks in encryption queries, σ_d is the total number of blocks in decryption queries, q_p is the number of offline queries, and $\sigma = \sigma_e + \sigma_d$.

When $q_p = 0$ and $q_d = \sigma_d = 0$, the bound (3) is

$$
\mathbf{Adv}^{\mathsf{aead}}_{\mathsf{Photon\text{-}Beetle}}(\mathcal{A}) \leq \frac{\sigma_e}{2^b},
$$

i.e., it claims IND-CPA security up to $\sigma_e = 2^b$, which is flawed as we show below.

We note that the birthday forgery attack in Sect. 4.1 implies a distinguishing attack with a comparable complexity as follows:

1. Let $q_e = 2^{b/2}$, and fix q_e distinct nonces $N_1, \ldots, N_{q_e}$, q_e distinct AD $A_1, \ldots, A_{q_e}$ with $|A_i| = b$. We also fix a message M with $|M| = b$.
2. Make q_e encryption queries $(N_1, A_1, M), \ldots, (N_{q_e}, A_{q_e}, M)$ and obtain (C_1, T_1), $\ldots, (C_{q_e}, T_{q_e})$, where $|C_i| = b$.
3. If there exists (i, j) such that $(C_i, T_i) = (C_j, T_j)$, then output 1 (real world). Otherwise, output 0 (ideal world).

Since the b-bit state collision can be expected in the real world, the attacker finds (i, j) in Step 3 with a high probability. The attack makes $q_e = 2^{b/2}$ encryption queries, no primitive query ($q_p = 0$), and no decryption query ($q_d = \sigma_d = 0$), violating the bound (3).

In [12, Sect. 7.2], the following AE bound is claimed for $r = 128$:

$$\mathbf{Adv}_{\text{Photon-Beetle}}^{\text{aead}}(\mathcal{A}) \leq \frac{q_p}{2^\kappa} + \frac{13 r q_p}{2^c} \tag{4}$$

When $q_p = 0$, the bound claims perfect security both in IND-CPA and INT-CTXT. Even the ideal AE scheme cannot have a perfect security bound in authenticity, and our birthday forgery in Sect. 4.1 invalidates the INT-CTXT claim, and the above distinguishing attack invalidates the IND-CPA claim.

The bound (4) is obtained from the bound (3) by using the relation

$$\sigma \leq q_p \,, \tag{5}$$

which is not the case in our attacks. We do not see how the relation (5) can be ensured, as our attacks demonstrate that there are attackers with $q_p = 0$.

We clarify that the ePrint version [11] of [12] addresses the issue in the bound (3) with the following revised bound for $r = 128$:

$$\mathbf{Adv}_{\text{Photon-Beetle}}^{\text{aead}}(\mathcal{A}) \leq \frac{8 r \sigma_d}{2^c} + \frac{8 b^3 q_p^2 \sigma_d}{2^{b+c}} + \frac{q_p}{2^\kappa} + \frac{2 q_d}{2^r} + \frac{2\sigma(2\sigma + q_p)}{2^b}$$
$$+ \frac{q_p^2}{2^b} + \frac{6 \sigma_e q_p}{2^b} + \frac{12 r q_p}{2^c} + \frac{\sigma_e + q_p}{2^b} + \frac{4 r q_p \sigma_d}{2^{2c}} \,, \tag{6}$$

i.e., the revised bound contains a term $\sigma^2/2^b$. A full-state collision in encryption queries is covered in the analysis of [12], and the above attack no longer applies. The source of the gap seems to be an error in the final step of the proof in [12] to take the summation of various terms, where a term $2\sigma_e^2/2^b$ has been somewhat missing.

In the ePrint version [11, Sect. 7.3.1], a simplified bound is presented. For $r = 128$, the bound is

$$\mathbf{Adv}_{\text{Photon-Beetle}}^{\text{aead}}(\mathcal{A}) \leq \frac{q_p}{2^\kappa} + \frac{2\sigma}{2^r} + \frac{10 b^2 q_p^2}{2^b} + \frac{24 r q_p}{2^c} + \frac{12 \sigma q_p}{2^b} \,,$$

which is obtained from the bound (6) by using the relation (5). We do not have an attack for this, but we do not know its correctness, as there are attackers outside of the relation (5).

5 Conclusions

We have investigated the provable security bounds in the specification documents of two NIST LwC finalists, GIFT-COFB and Photon-Beetle, and reported some attacks whose success probabilities are higher that what their bounds tell. We have also analyzed other bounds of Photon-Beetle shown in the subsequent papers and shown some attacks. We remark that our attacks do not invalidate the claimed bit security levels of them.

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