Phase-shift Fault Analysis of Grain-128

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Abstract. Phase-shift fault attack is a type of fault attack used for cryptanalysis of stream ciphers. It involves clocking a cipher's feedback shift registers out of phase, in order to generate faulted keystream. Grain-128 cipher is a 128-bit modification of the Grain cipher which is one of the finalists in the eSTREAM project. In this work, we propose a phase-shift fault attack against Grain-128 loaded with key-IV pairs that result in an all-zero LFSR after initialisation. We frame equations in terms of the input and output bits of the cipher and solve them using a SAT solver. By correctly guessing 40 internal state bits, we are able to recover the entire 128-bit key with just 2 phase-shift faults for keystreams of length 200 bits.

Keywords: Grain-128 · Stream ciphers · Fault analysis · Hardware .

1 Introduction

Stream ciphers generate pseudorandom keystreams from a secret random key. This keystream is simply xored with the plaintext to get the ciphertext. If an attacker could recover the secret key, the keystream can be generated by running the key generation algorithm which is public. By the property of xor, the attacker can get the original plaintext by xoring the ciphertext with the keystream. Therefore, it should be difficult to recover the secret key of a stream cipher. Grain [16] is a hardware oriented stream cipher which is suitable for hardware applications with restricted resources such as limited storage, gate count, or power consumption. Grain is one of the finalists in the eSTREAM project [2]. Grain-128 [15] is an extension of the Grain cipher. Grain-128 was introduced to overcome attacks that take advantage of short keys. For example, time-memory-data trade-off attack [9] of complexity $O(2^{\frac{k}{2}})$ where k is the key size of a cipher, can attack Grain-v1 [16] of key size 80 with complexity $O(2^{40})$.

There are several types of attacks against ciphers. Fault attack is one among them. In a fault attack, a fault is induced in the implementation of a cipher resulting in a faulted keystream. The original and the faulted keystreams are used for cryptanalysis of the cipher. There are two types of fault attacks namely bit-flipping fault attack and phase-shift fault attack. Bit-flipping fault attack requires inducing faults in the bits of registers. There are many works in the literature that mounted bit-flipping fault attacks against Grain-128 either by targeting its LFSR [11] or NFSR [20] or both [22,7,6,5,13]. This requires additional effort for finding the location of the fault since inducing faults at an intended location may not be practical. Phase-shift fault attack involves clocking one of the shift registers ahead of the other and observing the changes in the output keystream. Phase-shift fault attack was suggested in [17] and was applied against Trivium [10] in [19] and Grain-v1 in [18].

The number of faults required for an attack signifies the number of times the device has to be reset and the number of keystream bits required signifies the data complexity required for the attack. Therefore, the lesser the number of faults and number of keystream bits required, the better the attack. The phaseshift fault analysis of Trivium in [19] required only 2 phase-shifts and needed to produce only 120 bits per keystream instead of 2 bit-flips and 420 bits per keystream in bit-flipping fault analysis [21]. By introducing bit-flipping faults in Grain-128, minimum 4 faults and 256 bits per keystream were required to recover key [22]. In this work, phase-shift attack is mounted against Grain-128. Only two phase-shifts and 200 bits per keystream is sufficient for recovering the key in case of Grain-128 loaded with a weak key-IV pair. A key-IV pair that results in an all-zero LFSR after initialisation is termed as weak key-IV pair. About 40 internal state bits are guessed to make the computation feasible. The term 'internal state' refers to the state of LFSR and NFSR at a particular point of time.

2 Design of Grain-128

Grain-128 is made up of two 128-bit registers, a linear feedback shift register (LFSR) and a nonlinear feedback shift register (NFSR) as illustrated in Figure 1a. The NFSR is initialised with the key and the first 96 bits of LFSR are initialised with the initialisation vector (IV). The rest of the bits in LFSR are initialised with ones. The shifts of both these registers are synchronized using clocks. At each clock step the register bits are shifted by one position. One bit gets discarded at one end and one bit is added at the other end of the registeries.

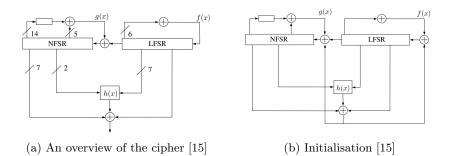


Fig. 1: Design of Grain-128

ter. The bit to be added is determined by the feedback function of the register. For one register, the feedback function is linear and for the other register, the function is nonlinear and hence they are named LFSR and NFSR respectively. Moreover before generating keystream, the cipher is clocked 256 times in the initialisation phase as shown in Figure 1b. During this phase, the output bit produced is fed back and xored with the input of both LFSR and NFSR.

3 Related Works

As mentioned in Section 1, fault attacks against Grain-128 were carried out by targeting either LFSR or NFSR or both. A fault attack by targeting LFSR was proposed in [11]. The differences between original keystream and faulted keystream were used to formulate linear equations on the LFSR state bits. After solving LFSR completely using the above equations, linear and quadratic equations in NFSR could be obtained. Such equations were solved using Gröbner basis [4]. The average number of faults to be injected in LFSR for completely recovering the internal state was calculated as 24. The highlights of this work are fault position determination and determination of internal state at a particular time and computation of previous internal states from that internal state.

Similarly a fault attack by targeting NFSR was proposed in [20], assuming that the attacker can repeat Grain-128 algorithm using different IVs with the same key. Fault traces were precomputed and was used for deriving values of NFSR bits involved in feedback and output keystreams. On an average, 3.40 bits of NFSR were obtained from one fault. When NFSR bits were completely known, LFSR bits were calculated from the output differential. For this, equations involving LFSR bits were solved using Gaussian elimination. The attack requires at most 312 faults.

Efforts were made in [7,6,5] for improving differential fault attack against the Grain family of ciphers and a refined attack of this type can be found in [22]. In this work, the attack assumes very less capabilities for the attacker and perform differential fault analysis. The injection of faults and their timing are very difficult to control. Majority of the works dealing with fault attacks assume that the attacker can inject faults in either LFSR or in the NFSR. This work uses four signature vectors to determine the fault location and can determine the location regardless of the register where the faults are injected. This means that the fault can be injected in either of these feedback registers. Moreover, the faults need not be injected immediately before the cipher starts generating keystream. The attacker can inject faults at any time after the initialisation phase. This attack requires a minimum of 4 faults. Another attack in [13] attempted to improve upon the attack in [22] considering an observation that the faults affected the 128th bit of the NFSR most of the time. Table 1 summarises bit flipping fault attacks against Grain-128.

Phase-shift analysis of Trivium cipher was carried out in [19]. The work compared phase-shifting attack and bit-flipping attack combined with phaseshift. At least two phase-shifts were required for a successful attack of Trivium.

Even with one bit-flip, one phase-shift could not successfully attack Trivium. The authors used SAT solvers and ElimLin algorithm [12] with Gröbner bases to solve equations in internal state bits.

Another interesting work along the same direction is phase-shift analysis of Grain-v1 in [18]. This work discussed four different ways in which phase-shift can be achieved and compared their results. Stopping the LFSR for one clock and producing the output was found to be the best case. The authors also experimented applying all types of phase-shifts in a single experiment. Some of the LFSR bits after initialisation (i.e., at least 28 bits) were assumed to be known in order to find out the rest of the bits.

Mounting a phase-shift fault attack on an encryption device is difficult and it is rarely implemented in published works. Synchronization attack in [14] also involves stopping a chosen register for a single step. This work discusses the technical feasibility of such an attack and claims that it requires highly sophisticated equipment. However, it is possible to mount such an attack on a test device. Also, the manufacturers of encryption devices can leave a possibility for this attack as a "trapdoor" in their implementation.

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	attack	targeted	no. of	no. of bits	no. of	solved using
		register	faults	per keystream	equations	
Ì	bit flipping fault[11]	LFSR	24	not specified	not specified	Gröbner basis
	bit flipping fault[20]	NFSR	256	256	128	Gaussian
ĺ						elimination
	bit flipping fault[22]	LFSR	4	256	3840	SAT solver
		and NFSR				

Table 1: Comparison of Related Works

4 Methodology

In this work, we choose LFSR to be phase-shifted, i.e., immediately after the initialisation phase, we clock the LFSR without clocking the NFSR and without producing keystream. Thereafter we clock both shift registers together for generating keystreams. LFSR is chosen because its feedback is not affected by the state of any of the bits of NFSR. On the other hand, NFSR feedback is dependent on the first bit of LFSR. Phase-shift attack can be carried out only if the following assumptions are true.

1. The attacker should be able to generate and observe keystreams of any length. 2. The attacker should be able to clock LFSR without clocking NFSR when needed.

3. The attacker should be able to reset the device.

We represent the internal state after initialisation phase of LFSR and NFSR as $(x_1, x_2, ..., x_{128})$ and $(y_1, y_2, ..., y_{128})$ respectively. The output keystream is

represented by $(o_1, o_2, ..., o_n)$ where n is the number of keystream bits to be produced. The feedback function of LFSR is

$$x_{i+128} = x_i + x_{i+7} + x_{i+38} + x_{i+70} + x_{i+81} + x_{i+96}$$
(1)

and that of NFSR is

$$y_{i+128} = x_i + y_i + y_{i+26} + y_{i+56} + y_{i+91} + y_{i+96} + y_{i+3}y_{i+67} + y_{i+11}y_{i+13} + y_{i+17}y_{i+18} + y_{i+27}y_{i+59} + y_{i+40}y_{i+48} + y_{i+61}y_{i+65} + y_{i+68}y_{i+84}$$

$$(2)$$

The output keystream is calculated using a Boolean function h(x, y) defined as

$$h(x,y) = y_{i+12}x_{i+8} + x_{i+13}x_{i+20} + y_{i+95}x_{i+42} + x_{i+60}x_{i+79} + y_{i+12}y_{i+95}x_{i+95}$$
(3)

The output bit is calculated as follows:

$$o_i = y_{i+2} + y_{i+15} + y_{i+36} + y_{i+45} + y_{i+64} + y_{i+73} + y_{i+89} + h(x, y) + x_{i+93}$$
(4)

In all the above equations, '+' refers to addition in GF(2), i.e., bitwise xor.

During phase-shift, if we are clocking LFSR alone for one time, i.e., one phase-shift, the corresponding keystream is represented by $(o_1^{1}, o_2^{1}, ..., o_n^{1})$ and the NFSR feedback and the output bit, change as shown by the following equations. The representation of internal state bits of the LFSR remains the same as the LFSR is linearly updated in all the three modes.

$$y_{i+128}^{1} = x_{i+1} + y_{i}^{1} + y_{i+26}^{1} + y_{i+56}^{1} + y_{i+91}^{1} + y_{i+96}^{1} + y_{i+3}^{1} y_{i+67}^{1} + y_{i+11}^{1} y_{i+13}^{1} + y_{i+17}^{1} y_{i+18}^{1} + y_{i+27}^{1} y_{i+59}^{1} + y_{i+40}^{1} y_{i+48}^{1} + y_{i+61}^{1} y_{i+65}^{1} + y_{i+68}^{1} y_{i+84}^{1}$$

$$(5)$$

$$h(x,y) = y_{i+12} \cdot x_{i+9} + x_{i+14} x_{i+21} + y_{i+95} \cdot x_{i+43} + x_{i+61} \cdot x_{i+80} + y_{i+12} \cdot y_{i+95} \cdot x_{i+96}$$

$$(6)$$

$$+y_{i+12} \cdot y_{i+95} \cdot x_{i+96} + y_{i+15} \cdot y_{i+36} \cdot y_{i+45} + y_{i+64} \cdot y_{i+73} + y_{i+89} \cdot y_{i+89} + h(x,y) \cdot y_{i+94} + y_{i+94}$$

If we are doing two phase-shifts, the corresponding keystream is represented by $(o_1^2, o_2^2, ..., o_n^2)$ and the NFSR feedback and the output bit, change as shown by the following equations:

$$y_{i+128}^{2} = x_{i+2} + y_{i}^{2} + y_{i+26}^{2} + y_{i+56}^{2} + y_{i+91}^{2} + y_{i+96}^{2} + y_{i+3}^{2} y_{i+67}^{2} + y_{i+11}^{2} y_{i+13}^{2} + y_{i+17}^{2} y_{i+18}^{2} + y_{i+27}^{2} y_{i+59}^{2} + y_{i+40}^{2} y_{i+48}^{2} + y_{i+61}^{2} y_{i+65}^{2} + y_{i+68}^{2} y_{i+84}^{2}$$

$$(8)$$

$$h(x,y)^{2} = y_{i+12}^{2} x_{i+10} + x_{i+15} x_{i+22} + y_{i+95}^{2} x_{i+44} + x_{i+62} x_{i+81} + y_{i+12}^{2} y_{i+95}^{2} x_{i+97}$$
(9)

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$$o_{i}^{2} = y_{i+2}^{2} + y_{i+15}^{2} + y_{i+36}^{2} + y_{i+45}^{2} + y_{i+64}^{2} + y_{i+73}^{2} + y_{i+89}^{2} + h(x,y)^{2} + x_{i+95}$$
(10)

The normal and phase-shifted modes of Grain-128 are coded in hardware description language, Verilog, and synthesized for Kintex-7 FPGA using Vivado 2020.2 software suite. The first 256 clocks in the initialisation phase take 513 ns to complete. After this, the output keystream bits are generated one bit per cycle.

Algorithm 1 Generate Equations

Require: LFSR and NFSR after initialisation 1: \triangleright set *n* as number of keystream bits required 2: \triangleright equations for Grain-128 3: for $i \leftarrow 1, n$ do 4: Generate normal output equation 5: Generate feedback equation of LFSR and left shift LFSR 6: Generate feedback equation of NFSR and left shift NFSR 7: end for ▷ equations for Grain-128 with one phase-shift 8: 9: Generate normal output equation 10: Generate feedback equation of LFSR and left shift LFSR 11: for $i \leftarrow 2, n$ do 12:Generate output equation Generate feedback equation of LFSR and left shift LFSR 13:14: Generate feedback equation of NFSR and left shift NFSR 15: end for 16: \triangleright equations for Grain-128 with two phase-shifts 17: Generate normal output equation 18: Generate feedback equation of LFSR and left shift LFSR 19: Generate feedback equation of LFSR and left shift LFSR 20: for $i \leftarrow 2, n$ do 21:Generate output equation 22:Generate feedback equation of LFSR and left shift LFSR Generate feedback equation of NFSR and left shift NFSR 23:24: end for

Algorithm 1 shows how the equations can be generated for normal and phaseshifted Grain-128. Equations upto five iterations of Grain-128 in each of these modes are listed in Appendix. The values of output bits denoted by $(o_1, o_2, ..., o_n)$, $(o_1^{11}, o_2^{11}, ..., o_n^{11})$ and $(o_1^{22}, o_2^{22}, ..., o_n^{22})$ are obtained by running Grain-128 algorithm and its one phase-shift and two phase-shifts modes. These values form the right-hand side of the output equations.

Since the device is reset between the normal and phase-shifted modes of operation of the cipher, $y_i = y_i^1 = y_i^2$ holds for *i* in the range from 1 to 128. These are the internal state bits after initialisation. It is after this state that the

phase-shifts are done. Since the first keystream bit is generated from the state after the initialisation phase before phase-shift, the first keystream bit will be same in all the three modes i.e., $o_1 = o_1^{-1} = o_1^{-2}$.

As only LFSR is phase-shifted, the difference in the NFSR feedback of the three modes is an outcome of the single LFSR bit that contributes to the NFSR feedback. This thought motivated us to formulate equations involving NFSR bits of the three modes. For example, the following equation is obtained by combining equations 2 and 5.

$$y_{i+128}^{\ i} = x_{i+1} + y_{i+128} + x_i \tag{11}$$

Similarly we can combine equations 5 and 8 to get,

$$y_{i+128}^{2} = x_{i+2} + y_{i+128}^{1} + x_{i+1}.$$
 (12)

The equations 11 and 12 hold for *i* in the range from 1 to 32 only, as all other terms in the pair of equations 2 and 5 and the pair 5 and 8 cancel out only in this range. Remember, $y_i = y_i^{1} = y_i^{2}$ hold for *i* in the range from 1 to 128.

Our intention is to find out the internal state of Grain-128 immediately after the initialisation using the keystreams generated by the normal and phaseshifted Grain-128. From a particular internal state, we can compute the previous internal state using the output bit generated from that state. By repeating this computation we can reverse the initialisation process to recover the initial state and find the key and IV loaded in NFSR and LFSR. Section VIII of [11] explains how this can be achieved.

An example for previous state computation is given below: We have already represented the internal state after initialisation phase of LFSR and NFSR as $(x_1, x_2, ..., x_{128})$ and $(y_1, y_2, ..., y_{128})$ respectively. Now the internal state at the last step of initialisation can be represented by $(x_0, x_1, ..., x_{127})$ and $(y_0, y_1, ..., y_{127})$ respectively. The only unknowns to find are x_0 and y_0 . During initialisation phase, the output bit is xored with the inputs, both to the LFSR and to the NFSR. Let the output bit at the last step be o_0 , then,

$$o_0 = y_2 + y_{15} + y_{36} + y_{45} + y_{64} + y_{73} + y_{89} + y_{12}x_8 + x_{13}x_{20} + y_{95}x_{42} + x_{60}x_{79} + y_{12}y_{95}x_{95} + x_{93}$$

From equation 1,

$$x_{128} = x_0 + x_7 + x_{38} + x_{70} + x_{81} + x_{96}$$

Rearranging we get,

$$x_0 = x_7 + x_{38} + x_{70} + x_{81} + x_{96} + x_{128}$$

Similarly from equation 2,

$$y_{128} = x_0 + y_0 + y_{26} + y_{56} + y_{91} + y_{96} + y_3y_{67} + y_{11}y_{13} + y_{17}y_{18} + y_{27}y_{59} + y_{40}y_{48} + y_{61}y_{65} + y_{68}y_{84}$$

we get,

$$y_0 = x_0 + y_{26} + y_{56} + y_{91} + y_{96} + y_3y_{67} + y_{11}y_{13} + y_{17}y_{18} + y_{27}y_{59} + y_{40}y_{48} + y_{16}y_{65} + y_{68}y_{84} + y_{128}$$

Thus the previous state is obtained.

Equations involving the internal state bits and the bits of the keystream generated from the internal state are generated using Algorithm 1 given above. There are 256 variables representing the internal state after initialization phase. At each clock cycle, 2 new variables and 3 new equations are added to the system. Let n be the number of keystream bits produced, then in normal mode there are 3n equations and 256 + 2n variables and in one phase-shift mode, there are 2n equations (LFSR equations remain the same as in normal mode) and n variables (one variable for NFSR feedback in each clock step). For two phase-shift mode there are 2n equations and n variables. For instance, if the cipher is executed in three modes by producing 100 bits in each keystream (i.e., n = 100), there will be 700 equations involving 656 variables in the system of equations, since the 256 initial state variables are common to all cases.

This system of equations is to be solved in order to find out the internal state bits. Solving this system of nonlinear equations involving large number of variables is a complex process. So the best method is to use SAT solvers for solving. Lingeling solver [8] is used for solving the system of nonlinear equations. Lingeling solver solves the equations in DIMACS format. Equations are converted to DIMACS [1] CNF format using SAGE mathematical software system [23]. The DIMACS CNF format is widely accepted as the standard format for Boolean formulas in conjunctive normal form. SAT solvers require their input to be in CNF (Conjunctive normal form) or XCNF (Extended conjunctive normal form) format.

5 Results

Lingeling executed without producing any result in feasible time because solving such high degree equations involving such large number of variables is beyond the limit of the available resources. So we used a weak key-IV pair as defined in [24] and conducted experiments to find out whether we are able to recover the key from the output keystream bits. A key-IV pair that results in an all-zero LFSR after initialisation is termed as weak key-IV. Since LFSR is all zeros, the problem of recovering the internal state after initialisation is reduced to recovering the 128-bit NFSR. There are 2⁹⁶ such key-IV pairs. A procedure for finding out such a key-IV pair is available in [24]. Assuming that the internal state after initialization has all zeros in the LFSR, NFSR bits are randomly selected. From this internal state, the execution of cipher is reversed (as explained in section 4) until we get the corresponding initial state. If all the bits in the last 32 bits of the LFSR are ones in the obtained initial state, then it is a valid initial state of Grain-128 and the remaining contents of NFSR and LFSR gives the weak key-IV pair. If the obtained initial state is not a valid initial state, repeat the procedure by randomly selecting NFSR bits again.

We simulated Grain-128 in normal, one phase-shift and two phase-shift modes and generated keystream bits in each mode. Without guessing any of the internal state bits, Lingeling is unable to solve the system of equations in feasible time. All experiments are performed on a DELL PowerEdge T620 Tower Server (CPU ES-2690v2@3.00 GHz x 40, 251.9 GB RAM). By guessing 40 bits, Lingeling could give the solution containing 256 internal state bits (including 88 unknown NFSR bits). Then, the key could be recovered by reversing the cipher execution from the obtained internal state as discussed in Section 4. Time taken for solving the system of equations when the number of guessed bits is varied, is illustrated in Table 2.

When three phase-shift mode is also included, the larger number of variables involved and number of equations in the system cause Lingeling to take more time to solve the system. So we restrict the number of phase-shift faults to two. The experiment is repeated by varying the number of keystream bits produced (n) from 100 bits to 200 bits. Though for 100 bits of keystream, time taken for solving the system of equation is lower than for 200 bits, 100 bits is not sufficient for recovering 88 bits of NFSR which is the highest number of unknown NFSR bits that we could recover.

available	no. of bits	unknown bits	Time taken
keystream bits	guessed	of NFSR	(seconds)
	above 80	below 48	≈ 0
	80	48	0.280
	72	56	0.601
100	64	64	1.351
	56	72	14.189
	48	80	1025.292
	40	88	didn't terminate
			in feasible time
	above 80	below 48	≈ 0
	80	48	1.904
	72	56	3.842
200	64	64	3.100
	56	72	9.630
	48	80	6663.131
	40	88	739407.952

 Table 2: Time Taken for Solving Equations

In [3], algebraic cryptanalysis of Grain-128 succeeded in recovering upto 64 unknown internal state bits. The remaining 192 internal state bits were guessed. To compare [3] with this work, we can consider the case of Grain-128 loaded with

weak key-IV pair. Even then, 64 bits are to be guessed for successfully mounting attack described in [3] whereas this work requires only 40 bits to be guessed.

As mentioned earlier, phase-shift fault attack was successful on Trivium cipher [19]. In the case of Grain-128, this attack performs worse than the attack on Trivium. This is because the build up of nonlinearity in Trivium's keystream is slow (introduced through feedback) compared to Grain-128, where both feedback and output equations are of higher order which increases nonlinearity at a much faster pace. Due to this, the solver obviously needs more time to solve the equations. This feature can be attributed to the structure of the Grain family of ciphers which is more complex than that of Trivium.

6 Conclusion

A less researched attack model, phase-shift fault analysis, is mounted against Grain-128. In case of Grain-128 loaded with a weak key-IV pair, we are able to recover the key if we guess 40 NFSR bits, calculate remaining unknown NFSR bits and determine corresponding initial state. The attack requires two phase-shift faults and a keystream of 200 bits in each execution of the cipher. This work underlines the fact that although phase-shift fault attack is practically difficult to mount, the hardware designers should be vigilant about the possibility of such an attack while implementing ciphers.

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8 Declarations

8.1 Data Availability

Data sharing not applicable to this article as no datasets were generated or analyzed during the current study.

8.2 Funding

No funds, grants, or other support was received for conducting this study.

8.3 Competing interests

The authors have no competing interests to declare that are relevant to the content of this article.

References

- 1. DIMACS. http://dimacs.rutgers.edu/, accessed: 2021-07-17
- The ECRYPT Stream Cipher Project eSTREAM. http://www.ecrypt.eu.org/, accessed: 2021-07-17
- Afzal, M., Masood, A.: Algebraic Cryptanalysis of A NLFSR Based Stream Cipher. In: 2008 3rd International Conference on Information and Communication Technologies: From Theory to Applications. pp. 1–6 (2008). https://doi.org/10.1109/ICTTA.2008.4530286
- Ajwa, I.A., Liu, Z., Wang, P.S.: Gröbner bases algorithm. Tech. rep., ICM Technical Reports Series (ICM-199502-00 (1995))
- Banik, S., Maitra, S., Sarkar, S.: A Differential Fault Attack on Grain-128a using MACs. In: Security, Privacy, and Applied Cryptography Engineering -Second International Conference, SPACE 2012, Chennai, India, November 3-4, 2012. Proceedings. pp. 111–125 (2012). https://doi.org/10.1007/978-3-642-34416-9_8, https://doi.org/10.1007/978-3-642-34416-9_8
- Banik, S., Maitra, S., Sarkar, S.: A Differential Fault Attack on the Grain Family of Stream Ciphers. In: Cryptographic Hardware and Embedded Systems -CHES 2012 - 14th International Workshop, Leuven, Belgium, September 9-12, 2012. Proceedings. pp. 122–139 (2012). https://doi.org/10.1007/978-3-642-33027-8_8, https://doi.org/10.1007/978-3-642-33027-8_8
- Banik, S., Maitra, S., Sarkar, S.: A Differential Fault Attack on the Grain Family under Reasonable Assumptions. In: Progress in Cryptology - INDOCRYPT 2012, 13th International Conference on Cryptology in India, Kolkata, India, December 9-12, 2012. Proceedings. pp. 191–208 (2012). https://doi.org/10.1007/978-3-642-34931-7_12, https://doi.org/10.1007/978-3-642-34931-7_12
- Biere, A.: Lingeling SAT Solver. http://fmv.jku.at/lingeling/, accessed: 2021-07-17
- Biryukov, A., Shamir, A.: Cryptanalytic time/memory/data tradeoffs for stream ciphers. In: Okamoto, T. (ed.) Advances in Cryptology - ASIACRYPT 2000, 6th International Conference on the Theory and Application of Cryptology and Information Security, Kyoto, Japan, December 3-7, 2000, Proceedings. Lecture Notes in Computer Science, vol. 1976, pp. 1–13. Springer (2000). https://doi.org/10.1007/3-540-44448-3_1, https://doi.org/10.1007/3-540-44448-3_1
- Cannière, C.D., Preneel, B.: Trivium. In: New Stream Cipher Designs The eS-TREAM Finalists, pp. 244–266 (2008). https://doi.org/10.1007/978-3-540-68351-3_18, https://doi.org/10.1007/978-3-540-68351-3_18
- Castagnos, G., Berzati, A., Canovas, C., Debraize, B., Goubin, L., Gouget, A., Paillier, P., Salgado, S.: Fault Analysis of Grain-128. In: IEEE International Workshop on Hardware-Oriented Security and Trust, HOST 2009, San Francisco, CA, USA, July 27, 2009. Proceedings. pp. 7–14 (2009). https://doi.org/10.1109/HST.2009.5225030, https://doi.org/10.1109/ HST.2009.5225030

- 12 Hridya P R and Jimmy Jose
- Courtois, N.T., Sepehrdad, P., Susil, P., Vaudenay, S.: Elimlin algorithm revisited. In: Fast Software Encryption 19th International Workshop, FSE 2012, Washington, DC, USA, March 19-21, 2012. Revised Selected Papers. pp. 306–325 (2012). https://doi.org/10.1007/978-3-642-34047-5_18, https://doi.org/10.1007/978-3-642-34047-5_18
- Dey, P., Chakraborty, A., Adhikari, A., Mukhopadhyay, D.: Improved Practical Differential Fault Analysis of Grain-128. In: Proceedings of the 2015 Design, Automation & Test in Europe Conference & Exhibition, DATE 2015, Grenoble, France, March 9-13, 2015. pp. 459-464 (2015), http://dl.acm.org/citation.cfm? id=2755858
- Gomulkiewicz, M., Kutylowski, M., Vierhaus, H.T., Wlaz, P.: Synchronization fault cryptanalysis for breaking A5/1. In: Nikoletseas, S.E. (ed.) Experimental and Efficient Algorithms, 4th InternationalWorkshop, WEA 2005, Santorini Island, Greece, May 10-13, 2005, Proceedings. Lecture Notes in Computer Science, vol. 3503, pp. 415–427. Springer (2005). https://doi.org/10.1007/11427186_36, https://doi.org/10.1007/11427186_36
- Hell, M., Johansson, T., Maximov, A., Meier, W.: A Stream Cipher Proposal: Grain-128. In: Proceedings 2006 IEEE International Symposium on Information Theory, ISIT 2006, The Westin Seattle, Seattle, Washington, USA, July 9-14, 2006. pp. 1614–1618 (2006). https://doi.org/10.1109/ISIT.2006.261549, https://doi. org/10.1109/ISIT.2006.261549
- 16. Hell, М., Johansson, Т., Meier, W.: Grain: Ci-А Stream Environments. IJWMC pher for Constrained 2(1),86 - 93(2007).https://doi.org/10.1504/IJWMC.2007.013798, https://doi.org/10.1504/ IJWMC.2007.013798
- Hoch, J.J., Shamir, A.: Fault Analysis of Stream Ciphers. In: Cryptographic Hardware and Embedded Systems - CHES 2004: 6th International Workshop Cambridge, MA, USA, August 11-13, 2004. Proceedings. pp. 240– 253 (2004). https://doi.org/10.1007/978-3-540-28632-5_18, https://doi.org/10. 1007/978-3-540-28632-5_18
- Hromada, V., Petho, T.: Phase-shift Fault Analysis of Grain v1. International Journal of Electronics and Telecommunications 64(2), 131–136 (2018)
- 19. Hromada, V., Varga, J.: Phase-shift Fault Analysis of Trivium. Studia Scientiarum Mathematicarum Hungarica **52**(2), 205–220 (2015)
- Karmakar, S., Chowdhury, D.R.: Fault Analysis of Grain-128 by targeting NFSR. In: Progress in Cryptology - AFRICACRYPT 2011 - 4th International Conference on Cryptology in Africa, Dakar, Senegal, July 5-7, 2011. Proceedings. pp. 298– 315 (2011). https://doi.org/10.1007/978-3-642-21969-6_19, https://doi.org/10. 1007/978-3-642-21969-6_19
- Mohamed, M.S.E., Bulygin, S., Buchmann, J.A.: Using SAT solving to improve differential fault analysis of trivium. In: Kim, T., Adeli, H., Robles, R.J., Balitanas, M.O. (eds.) Information Security and Assurance - International Conference, ISA 2011, Brno, Czech Republic, August 15-17, 2011. Proceedings. Communications in Computer and Information Science, vol. 200, pp. 62–71. Springer (2011). https://doi.org/10.1007/978-3-642-23141-4_7, https://doi.org/10.1007/ 978-3-642-23141-4_7
- Sarkar, S., Banik, S., Maitra, S.: Differential Fault Attack against Grain Family with Very Few Faults and Minimal Assumptions. IEEE Trans. Computers 64(6), 1647–1657 (2015). https://doi.org/10.1109/TC.2014.2339854, https://doi.org/ 10.1109/TC.2014.2339854

- 23. Stein, W.: Sage Mathematics Software System. http://www.sagemath.org/, accessed: 2021-07-17
- 24. Zhang, H., Wang, X.: Cryptanalysis of Stream Cipher Grain Family. IACR Cryptology ePrint Archive 2009, 109 (2009), http://eprint.iacr.org/2009/109

Appendix

The feedback equations and output equations up to five iterations in the keystream generation phase of Grain-128 in different modes are given below. The symbol '+' refers to addition in GF(2) in all the equations given below.

Equations of Grain-128

The internal state after initialisation phase of LFSR and NFSR are represented as $(x_1, x_2, ..., x_{128})$ and $(y_1, y_2, ..., y_{128})$ respectively. The output keystream is represented by $(o_1, o_2, ..., o_n)$.

```
 \begin{aligned} x_{129} &= x_1 + x_8 + x_{39} + x_{71} + x_{82} + x_{97} \\ y_{129} &= x_1 + y_1 + y_{27} + y_{57} + y_{92} + y_{97} + y_4 y_{68} + y_{12} y_{14} + y_{18} y_{19} + \\ y_{28} y_{60} + y_{41} y_{49} + y_{62} y_{66} + y_{69} y_{85} \\ o_1 &= y_3 + y_{16} + y_{37} + y_{46} + y_{65} + y_{74} + y_{90} + y_{13} x_9 + x_{14} x_{21} + y_{96} x_{43} + x_{61} x_{80} + \\ y_{13} y_{96} x_{96} + x_{94} \end{aligned}
```

```
 \begin{aligned} x_{130} &= x_2 + x_9 + x_{40} + x_{72} + x_{83} + x_{98} \\ y_{130} &= x_2 + y_2 + y_{28} + y_{58} + y_{93} + y_{98} + y_5y_{69} + y_{13}y_{15} + y_{19}y_{20} + \\ y_{29}y_{61} &+ y_{42}y_{50} + y_{63}y_{67} + y_{70}y_{86} \\ o_2 &= y_4 + y_{17} + y_{38} + y_{47} + y_{66} + y_{75} + y_{91} + y_{14}x_{10} + x_{15}x_{22} + y_{97}x_{44} + x_{62}x_{81} + \\ y_{14}y_{97}x_{97} + x_{95} \end{aligned}
```

```
 \begin{aligned} x_{131} &= x_3 + x_{10} + x_{41} + x_{73} + x_{84} + x_{99} \\ y_{131} &= x_3 + y_3 + y_{29} + y_{59} + y_{94} + y_{99} + y_6y_{70} + y_{14}y_{16} + y_{20}y_{21} + \\ y_{30}y_{62} + y_{43}y_{51} + y_{64}y_{68} + y_{71}y_{87} \\ o_3 &= y_5 + y_{18} + y_{39} + y_{48} + y_{67} + y_{76} + y_{92} + y_{15}x_{11} + x_{16}x_{23} + y_{98}x_{45} + x_{63}x_{82} + \\ y_{15}y_{98}x_{98} + x_{96} \end{aligned}
```

```
 \begin{split} x_{132} &= x_4 + x_{11} + x_{42} + x_{74} + x_{85} + x_{100} \\ y_{132} &= x_4 + y_4 + y_{30} + y_{60} + y_{95} + y_{100} + y_7 y_{71} + y_{15} y_{17} + y_{21} y_{22} + y_{31} y_{63} + y_{44} y_{52} + y_{65} y_{69} + y_{72} y_{88} \\ o_4 &= y_6 + y_{19} + y_{40} + y_{49} + y_{68} + y_{77} + y_{93} + y_{16} x_{12} + x_{17} x_{24} + y_{99} x_{46} + x_{64} x_{83} + y_{16} y_{99} x_{99} + x_{97} \end{split}
```

```
 \begin{aligned} x_{133} &= x_5 + x_{12} + x_{43} + x_{75} + x_{86} + x_{101} \\ y_{133} &= x_5 + y_5 + y_{31} + y_{61} + y_{96} + y_{101} + y_8 y_{72} + y_{16} y_{18} + y_{22} y_{23} + y_{32} y_{64} + y_{45} y_{53} + y_{66} y_{70} + y_{73} y_{89} \\ o_5 &= y_7 + y_{20} + y_{41} + y_{50} + y_{69} + y_{78} + y_{94} + y_{17} x_{13} + x_{18} x_{25} + y_{100} x_{47} + x_{65} x_{84} + y_{17} y_{100} x_{100} + x_{98} \end{aligned}
```

Equations of Grain-128 with one phase-shift

The internal state after initialisation phase of NFSR is represented as $(y_1^1, y_2^1, ..., y_{128}^1)$ and the output keystream is represented by $(o_1^1, o_2^1, ..., o_n^1)$.

 $\begin{aligned} x_{129} &= x_1 + x_8 + x_{39} + x_{71} + x_{82} + x_{97} \\ x_{130} &= x_2 + x_9 + x_{40} + x_{72} + x_{83} + x_{98} \\ y_{129}{}^1 &= x_3 + y_1{}^1 + y_{27}{}^1 + y_{57}{}^1 + y_{92}{}^1 + y_{97}{}^1 + y_4{}^1y_{68}{}^1 + y_{12}{}^1y_{14}{}^1 + y_{18}{}^1y_{19}{}^1 + y_{28}{}^1y_{60}{}^1 + y_{41}{}^1y_{49}{}^1 + y_{62}{}^1y_{66}{}^1 + y_{69}{}^1y_{85}{}^1 \\ o_1^1 &= y_3{}^1 + y_{16}{}^1 + y_{37}{}^1 + y_{46}{}^1 + y_{65}{}^1 + y_{74}{}^1 + y_{90}{}^1 + y_{13}{}^1x_9 + x_{14}x_{21} + y_{96}{}^1x_{43} + x_{61}x_{80} + y_{13}{}^1y_{96}{}^1x_{96} + x_{94} \end{aligned}$

 $\begin{array}{l} x_{131} = x_3 + x_{10} + x_{41} + x_{73} + x_{84} + x_{99} \\ y_{130}{}^1 = x_3 + y_2{}^1 + y_{28}{}^1 + y_{58}{}^1 + y_{93}{}^1 + y_{98}{}^1 + y_5{}^1 y_{69}{}^1 + y_{13}{}^1 y_{15}{}^1 + \\ y_{19}{}^1 y_{20}{}^1 + y_{29}{}^1 y_{61}{}^1 + y_{42}{}^1 y_{50}{}^1 + y_{63}{}^1 y_{67}{}^1 + y_{70}{}^1 y_{86}{}^1 \\ o_2{}^1 = y_4{}^1 + y_{17}{}^1 + y_{38}{}^1 + y_{47}{}^1 + y_{66}{}^1 + y_{75}{}^1 + y_{91}{}^1 + y_{14}{}^1 x_{11} + x_{16} x_{23} + y_{97}{}^1 x_{45} + \\ x_{63} x_{82} + y_{14}{}^1 y_{97}{}^1 x_{98} + x_{96} \end{array}$

 $\begin{aligned} x_{132} &= x_4 + x_{11} + x_{42} + x_{74} + x_{85} + x_{100} \\ y_{131}{}^1 &= x_4 + y_3{}^1 + y_{29}{}^1 + y_{59}{}^1 + y_{94}{}^1 + y_{99}{}^1 + y_6{}^1y_{70}{}^1 + y_{14}{}^1y_{16}{}^1 + \\ y_{20}{}^1y_{21}{}^1 + y_{30}{}^1y_{62}{}^1 + y_{43}{}^1y_{51}{}^1 + y_{64}{}^1y_{68}{}^1 + y_{71}{}^1y_{87}{}^1 \\ o_3{}^1 &= y_5{}^1 + y_{18}{}^1 + y_{39}{}^1 + y_{48}{}^1 + y_{67}{}^1 + y_{76}{}^1 + y_{92}{}^1 + y_{15}{}^1x_{12} + x_{17}x_{24} + y_{98}{}^1x_{46} + \\ x_{64}x_{83} + y_{15}{}^1y_{98}{}^1x_{99} + x_{97} \end{aligned}$

 $\begin{aligned} x_{133} &= x_5 + x_{12} + x_{43} + x_{75} + x_{86} + x_{101} \\ y_{132}{}^1 &= x_5 + y_4{}^1 + y_{30}{}^1 + y_{60}{}^1 + y_{95}{}^1 + y_{100}{}^1 + y_7{}^1y_{71}{}^1 + y_{15}{}^1y_{17}{}^1 + y_{21}{}^1y_{22}{}^1 + y_{31}{}^1y_{63}{}^1 + y_{44}{}^1y_{52}{}^1 + y_{65}{}^1y_{69}{}^1 + y_{72}{}^1y_{88}{}^1 \\ o_4{}^1 &= y_6{}^1 + y_{19}{}^1 + y_{40}{}^1 + y_{49}{}^1 + y_{68}{}^1 + y_{77}{}^1 + y_{93}{}^1 + y_{16}{}^1x_{13} + x_{18}x_{25} + y_{99}{}^1x_{47} + x_{65}x_{84} + y_{16}{}^1y_{99}{}^1x_{100} + x_{98} \end{aligned}$

 $\begin{aligned} & x_{134} = x_6 + x_{13} + x_{44} + x_{76} + x_{87} + x_{102} \\ & y_{133}{}^1 = x_6 + y_5{}^1 + y_{31}{}^1 + y_{61}{}^1 + y_{96}{}^1 + y_{101}{}^1 + y_8{}^1y_{72}{}^1 + y_{16}{}^1y_{18}{}^1 + \\ & y_{22}{}^1y_{23}{}^1 + y_{32}{}^1y_{64}{}^1 + y_{45}{}^1y_{53}{}^1 + y_{66}{}^1y_{70}{}^1 + y_{73}{}^1y_{89}{}^1 \\ & o_5{}^1 = y_7{}^1 + y_{20}{}^1 + y_{41}{}^1 + y_{50}{}^1 + y_{69}{}^1 + y_{78}{}^1 + y_{94}{}^1 + y_{17}{}^1x_{14} + x_{19}x_{26} + y_{100}{}^1x_{48} + \\ & x_{66}x_{85} + y_{17}{}^1y_{100}{}^1x_{101} + x_{99} \end{aligned}$

Equations of Grain-128 with two phase-shifts

The internal state after initialisation phase of NFSR is represented as $(y_1^2, y_2^2, ..., y_{128}^2)$ and the output keystream is represented by $(o_1^2, o_2^2, ..., o_n^2)$.

 $\begin{aligned} x_{129} &= x_1 + x_8 + x_{39} + x_{71} + x_{82} + x_{97} \\ x_{130} &= x_2 + x_9 + x_{40} + x_{72} + x_{83} + x_{98} \\ x_{131} &= x_3 + x_{10} + x_{41} + x_{73} + x_{84} + x_{99} \end{aligned}$

 $y_{129}{}^2 = x_3 + y_1{}^2 + y_{27}{}^2 + y_{57}{}^2 + y_{92}{}^2 + y_{97}{}^2 + y_4{}^2y_{68}{}^2 + y_{12}{}^2y_{14}{}^2 + y_{18}{}^2y_{19}{}^2 + y_{28}{}^2y_{60}{}^2 + y_{41}{}^2y_{49}{}^2 + y_{62}{}^2y_{66}{}^2 + y_{69}{}^2y_{85}{}^2 \\ o_1^2 = y_3{}^2 + y_{16}{}^2 + y_{37}{}^2 + y_{46}{}^2 + y_{65}{}^2 + y_{74}{}^2 + y_{90}{}^2 + y_{13}{}^2x_9 + x_{14}x_{21} + y_{96}{}^2x_{43} + x_{61}x_{80} + y_{13}{}^2y_{96}{}^2x_{96} + x_{94}$

 $\begin{aligned} x_{132} &= x_4 + x_{11} + x_{42} + x_{74} + x_{85} + x_{100} \\ y_{130}{}^2 &= x_4 + y_2{}^2 + y_{28}{}^2 + y_{58}{}^2 + y_{93}{}^2 + y_{98}{}^2 + y_5{}^2 y_{69}{}^2 + y_{13}{}^2 y_{15}{}^2 + \\ y_{19}{}^2 y_{20}{}^2 + y_{29}{}^2 y_{61}{}^2 + y_{42}{}^2 y_{50}{}^2 + y_{63}{}^2 y_{67}{}^2 + y_{70}{}^2 y_{86}{}^2 \\ o_2{}^2 &= y_4{}^2 + y_{17}{}^2 + y_{38}{}^2 + y_{47}{}^2 + y_{66}{}^2 + y_{75}{}^2 + y_{91}{}^2 + y_{14}{}^2 x_{12} + x_{17}x_{24} + y_{97}{}^2 x_{46} + \\ x_{64}x_{83} + y_{14}{}^2 y_{97}{}^2 x_{99} + x_{97} \end{aligned}$

$$\begin{aligned} x_{133} &= x_5 + x_{12} + x_{43} + x_{75} + x_{86} + x_{101} \\ y_{131}{}^2 &= x_5 + y_3{}^2 + y_{29}{}^2 + y_{59}{}^2 + y_{94}{}^2 + y_{99}{}^2 + y_{6}{}^2 y_{70}{}^2 + y_{14}{}^2 y_{16}{}^2 + \\ y_{20}{}^2 y_{21}{}^2 + y_{30}{}^2 y_{62}{}^2 + y_{43}{}^2 y_{51}{}^2 + y_{64}{}^2 y_{68}{}^2 + y_{71}{}^2 y_{87}{}^2 \\ o_3{}^2 &= y_5{}^2 + y_{18}{}^2 + y_{39}{}^2 + y_{48}{}^2 + y_{67}{}^2 + y_{76}{}^2 + y_{92}{}^2 + y_{15}{}^2 x_{13} + x_{18}x_{25} + y_{98}{}^2 x_{47} + \\ x_{65}x_{84} + y_{15}{}^2 y_{98}{}^2 x_{100} + x_{98} \end{aligned}$$

$$\begin{aligned} x_{134} &= x_6 + x_{13} + x_{44} + x_{76} + x_{87} + x_{102} \\ y_{132}{}^2 &= x_6 + y_4{}^2 + y_{30}{}^2 + y_{60}{}^2 + y_{95}{}^2 + y_{100}{}^2 + y_7{}^2y_{71}{}^2 + y_{15}{}^2y_{17}{}^2 + \\ y_{21}{}^2y_{22}{}^2 + y_{31}{}^2y_{63}{}^2 + y_{44}{}^2y_{52}{}^2 + y_{65}{}^2y_{69}{}^2 + y_{72}{}^2y_{88}{}^2 \\ o_4{}^2 &= y_6{}^2 + y_{19}{}^2 + y_{40}{}^2 + y_{49}{}^2 + y_{68}{}^2 + y_{77}{}^2 + y_{93}{}^2 + y_{16}{}^2x_{14} + x_{19}x_{26} + y_{99}{}^2x_{48} + \\ x_{66}x_{85} + y_{16}{}^2y_{99}{}^2x_{101} + x_{99} \end{aligned}$$

$$\begin{aligned} x_{135} &= x_7 + x_{14} + x_{45} + x_{77} + x_{88} + x_{103} \\ y_{133}{}^2 &= x_7 + y_5{}^2 + y_{31}{}^2 + y_{61}{}^2 + y_{96}{}^2 + y_{101}{}^2 + y_8{}^2y_{72}{}^2 + y_{16}{}^2y_{18}{}^2 + \\ y_{22}{}^2y_{23}{}^2 + y_{32}{}^2y_{64}{}^2 + y_{45}{}^2y_{53}{}^2 + y_{66}{}^2y_{70}{}^2 + y_{73}{}^2y_{89}{}^2 \\ o_5{}^2 &= y_7{}^2 + y_{20}{}^2 + y_{41}{}^2 + y_{50}{}^2 + y_{69}{}^2 + y_{78}{}^2 + y_{94}{}^2 + y_{17}{}^2x_{15} + x_{20}x_{27} + y_{100}{}^2x_{49} + \\ x_{67}x_{86} + y_{17}{}^2y_{100}{}^2x_{102} + x_{100} \end{aligned}$$