# Robust Publicly Verifiable Covert Security: Limited Information Leakage and Guaranteed Correctness with Low Overhead

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Abstract. Protocols with publicly verifiable covert (PVC) security offer high efficiency and an appealing feature: a covert party may deviate from the protocol, but with a probability (e.g., 90%, referred to as the deterrence factor), the honest party can identify this deviation and expose it using a publicly verifiable certificate. These protocols are particularly suitable for practical applications involving reputation-conscious parties. However, in the cases where misbehavior goes undetected (e.g., with a probability of 10%), no security guarantee is provided for the honest party, potentially resulting in a complete loss of input privacy and output correctness.

In this paper, we tackle this critical problem by presenting a highly effective solution. We introduce and formally define an enhanced notion called robust PVC security, such that even if the misbehavior remains undetected, the malicious party can only gain an additional 1-bit of information about the honest party's input while maintaining the correctness of the output. We propose a novel approach leveraging dual execution and time-lock puzzles to design a robust PVC-secure two-party protocol with low overhead (depending on the deterrence factor). For instance, with a deterrence factor of 90%, our robust PVC-secure protocol incurs only additional  $\sim 10\%$  overhead compared to the state-of-the-art PVC-secure protocol.

Given the stronger security guarantees with low overhead, our protocol is highly suitable for practical applications of secure two-party computation.

**Keywords:** Secure two-party computation  $\cdot$  Robust publicly verifiable covert security  $\cdot$  1-bit leakage  $\cdot$  Dual execution.

## 1 Introduction

Secure two-party computation (2PC) allows two mutually distrusted parties to jointly evaluate a common function on their inputs while maintaining input privacy. Traditionally, two main security notions for 2PC, i.e., semi-honest security and malicious security, have been considered [12]. Protocols with semi-honest security could be efficient but only protect against passive attackers who strictly adhere to the prescribed protocols. Alternatively, protocols with malicious security provide a much stronger guarantee, preventing attackers from gaining any advantage through deviations from protocols. However, despite progress in the past few years, protocols with malicious security remain significantly complex and incur high overhead compared to those with semi-honest security.

The notion of covert security [4] is thereby introduced to serve as a compromise between semi-honest and malicious security. Covert security ensures that a party deviating from the protocol will be caught by the honest party with a fixed probability  $\epsilon$  (e.g.,  $\epsilon = 90\%$ ), referred to as the deterrence factor. Achieving covert security entails significantly lower overhead than malicious security [4,14,8,22]. Meanwhile, covert security provides a stronger security guarantee than semi-honest security, as it incorporates the risk of being caught, which can serve as a deterrent to potential cheaters.

Nevertheless, in certain scenarios, the deterrent effect of covert security may be insufficient. Merely catching the cheater does not enable the honest party to effectively persuade others and accuse the cheater, as the cheater can still deny their misconduct. To address this limitation, Asharov and Orlandi [2] introduced an enhanced notion called publicly verifiable covert (PVC) security. Protocols with PVC security allow the honest party to generate a publicly verifiable certificate when cheating is detected. The certificate serves as proof of cheating and can be used to convince all other parties, including external entities. The certificate can be utilized for legal proceedings or incorporated into a smart contract that automatically enforces financial penalties against the cheater. This property is particularly compelling in practice, as it is efficient<sup>4</sup> and can expose the cheater's misbehavior publicly and permanently, thereby imposing a reputational risk and providing stronger accountability measures. In recent years, PVC security has garnered substantial attention, resulting in the development of protocols for both general two-party [2,20,17] and multi-party [9,30,10,3] computation. Furthermore, PVC security model is also widely used in specific scenarios, such as financially backed protocols based on blockchain [31,11], secure computation concerning commitment based on blockchain [1], and private function evaluation [24].

While PVC security offers an effective deterrent when cheating is detected, there is a critical issue when misbehavior remains undetected (e.g., with a probability of 10%). In such cases, the honest party is left without any security guar-

 $<sup>^4</sup>$  It has been shown that a two-party PVC protocol with deterrence factor 50% incurs only 20-40% overhead compared to the state-of-the-art semi-honest protocols based on garbled circuits [17].

antees, potentially resulting in a complete loss of input privacy and output correctness. In other words, the cheater may gain complete knowledge of the honest party's input and manipulate the output. This is unacceptable in many scenarios, particularly for parties less concerned about reputation, who may be more inclined to take risks in pursuit of significant gains. An existing countermeasure to address this problem is to increase the deterrence factor to a relatively high level (e.g., 99% or 99.9%). However, it should be noted that the efficiency of protocols with PVC security is directly related to the deterrence factor, and increasing the deterrence factor comes at the cost of reduced efficiency. Worse, existing protocols with PVC security exhibit diminishing marginal benefits when increasing the deterrence factor. For instance, increasing the deterrence factor from 90% to 99% leads to a tenfold increase in protocol execution cost, and the same holds for increasing from 99% to 99.9%.

Therefore, there is still a lack of effective approaches to prevent reputationinsensitive parties from deviating from the protocol without incurring significant overhead.

#### 1.1 Our Contributions

In this paper, we present a compelling countermeasure to address the aforementioned problem. Specifically:

New security notion. We introduce an enhanced notion for PVC security named robust PVC security to capture the goal. This notion can be seen as making up for the deficiency of covert security in the other direction, focusing on reducing the benefits of malicious behavior when it goes undetected while maintaining the increased cost for cheater when caught provided by PVC security. Protocols with robust PVC security ensure that even if the misbehavior remains undetected, the malicious party can only obtain an additional 1-bit of information about the honest party's input while simultaneously preserving the correctness of the protocol's output. By significantly reducing the benefits of successful cheating, our approach goes further to effectively discourages malicious parties from cheating in the protocol.

**Protocol with low overhead.** We propose a novel approach leveraging dual execution and time-lock puzzles to design a general robust PVC-secure two-party computation protocol with low overhead (depending on the deterrence factor). For instance, when the deterrence factor is 90%, our protocol will incur only additional  $\sim 10\%$  overhead compared to the state-of-the-art PVC-secure protocol.

With its stronger security guarantees and low overhead, our protocol is highly suitable for practical applications of secure two-party computation.

## 1.2 Technical Overview

In this subsection, we commence by reviewing the *derandomization technique*, which has been employed in prior works for the design of PVC protocols. Notably,

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this technique will also serve as a key component in our protocol. Then, we briefly explain our robust PVC security notion and present the basic idea for designing protocols with robust PVC security. Finally, we discuss the main intuition behind our novel approach to achieving robust PVC security with low overhead.

**Derandomization in PVC Security** Recent general secure computation protocols with PVC security employ the *cut-and-choose* paradigm along with the derandomization technique [17,9,30,10,3], which is simpler and more efficient compared to the signed-OT technique used in earlier work [2,20].

Specifically, in the state-of-the-art PVC-secure two-party computation protocol [17] based on garbled circuits, each party pre-selects a seed for each instance. These seeds determine the randomness used in specific instances, ensuring that the execution of each instance is fully determined by the protocol description and the parties' seeds. At the start of the protocol, the evaluator, who cannot cheat in garbled circuit evaluation, commits to its own seeds and selects one instance for evaluation, leaving the remaining instances for checking. Subsequently, the evaluator, acting as the receiver, engages in classical oblivious transfer (OT) protocols with the garbler to obtain the garbler's seeds for the checking instances. Additionally, the parties sign the transcripts for each instance. Throughout the protocol execution, the evaluator uses the garbler's seeds to verify the correctness of the messages received from the garbler for the checking instances. Upon detecting a deviation from the checking instances, the evaluator combines the previously signed messages and its own seed decommitment to generate the certificate. Any other party can use the seeds to simulate the protocol execution and verify deviations. If no deviation is detected, the evaluator proceeds to evaluate the garbled circuit generated in the evaluation instance.

Importantly, in protocols with PVC security, potential cheaters are unaware of which instances are being checked, making it impossible for them to prevent honest parties from generating certificates. The deterrence factor in these protocols is determined by the number of instances. For example, in the state-of-theart PVC-secure two-party computation protocol [17],  $\lambda$  instances are involved, with  $\lambda-1$  instances checked by the evaluator and the remaining one instance used for evaluation. Hence, the deterrence factor of this protocol is  $\frac{\lambda-1}{\lambda}$ . This is the reason why existing protocols exhibit diminishing marginal benefits when increasing the deterrence factor.

Robust PVC Security In this paper, we introduce a new notion called robust PVC security. Protocols with robust PVC security aim to provide security guarantees inherited from PVC security while simultaneously limiting the benefits for cheaters when their deviations go undetected. We require that in such protocols, cheaters can obtain at most an additional 1-bit of information about the honest party's input, while ensuring the correctness of the protocol output, i.e., the output remains untampered.

The term "1-bit information" is used here because our approach leverages the idea of *dual execution*. The dual execution technique was initially introduced by

Mohassel and Franklin [26] and later formalized by Huang, Katz, and Evans [18]. This technique has found broad applications in general secure two-party computation with malicious and covert security [19,27,21,28,16] as well as private set intersection (PSI) [29].

The dual execution technique is primarily employed in garbled circuits. The idea behind dual execution is that two parties, PA and PB, execute two protocols for the same evaluation circuit and inputs. In one protocol, PA acts as the garbler, and  $P_B$  acts as the evaluator, while in the other protocol, they switch roles, i.e.,  $\mathsf{P}_\mathsf{B}$  becomes the garbler, and  $\mathsf{P}_\mathsf{A}$  becomes the evaluator. Finally, the two parties run a secure equality test protocol on the outputs of the two garbled circuits to determine the final result. If the test passes, both parties obtain the correct evaluation result; otherwise, it indicates that one party deviated from the protocol, leading to termination. By utilizing this dual execution technique, the malicious party can obtain, at most, an additional 1-bit of information about the honest party's input. The intuition is that even if the malicious party deviates from the protocol as the garbler, it cannot cheat in garbled circuit evaluation as the evaluator. Therefore, the information it can obtain from the maliciously generated garbled circuit is limited to the result of the equality test, i.e., the 1-bit information of either true or false, which may depend on the honest party's inputs.

Therefore, a straightforward approach to achieving robust PVC security is by integrating dual execution into PVC-secure protocols. Specifically, two parties  $P_A$  and  $P_B$  can execute a PVC-secure protocol, such as the one proposed in [17], to perform garbled circuit checking and obtain a final garbled circuit for evaluation. Simultaneously, these two parties switch roles and execute the protocol again to obtain another garbled circuit for evaluation. Then, each party plays the role of the evaluator and evaluates the garbled circuit they have chosen. Finally, a secure equality test protocol is employed to determine the final result. Although this approach may seem viable, we propose a superior solution in this work.

Our Novel Approach If the aforementioned approach is based on the state-of-the-art PVC-secure protocol in [17], achieving robust PVC security with a deterrence factor of  $\frac{\lambda-1}{\lambda}$  would require the protocol to generate  $2\lambda$  garbled circuits. Specifically, each party would need to generate  $2\lambda-1$  garbled circuits and evaluate one garbled circuit. This includes  $\lambda$  circuits generated as the garbler,  $\lambda-1$  garbled circuits generated for simulating garbled circuit generation in instance checking, and one garbled circuit that is not generated but needs to be evaluated. Therefore, achieving robust PVC security based on a PVC-secure protocol incurs a cost that is roughly double that of the PVC-secure protocol itself. As emphasized in [17], the cost of generating garbled circuits (unless the circuit is very small) is the efficiency bottleneck of the protocol. Therefore, this approach is not entirely satisfactory.

It happens that this cost can be significantly reduced by leveraging the special protocol framework when integrating dual execution into a PVC-secure protocol. The idea behind our novel approach stems from the following question:

Must each party generate  $\lambda$  garbled circuits as the garbler while generating  $\lambda - 1$  different garbled circuits as the evaluator for circuit checking?

Fortunately, we found that the answer is NO, and parties can combine these two circuit generation processes together. The idea of our approach is to let the two parties jointly select  $\lambda+1$  seeds in a blind fashion. Subsequently, each party randomly obtains  $\lambda$  seeds, while one seed remains hidden. When the sets of seeds obtained by the two parties differ, the intersection of their seeds is of size  $\lambda-1$ . Importantly, each party remains unaware of the seeds obtained by the other party. They can use their own  $\lambda$  seeds to generate  $\lambda$  garbled circuits and an additional dummy garbled circuit for the hidden seed. Since the parties share  $\lambda-1$  common seeds, they can now reuse the materials computed for circuit generation when playing the role of the evaluator to perform the circuit checking.

In summary, there are  $\lambda+1$  seeds, and each party obtains  $\lambda$  seeds, resulting in a seed intersection of size  $\lambda-1$ . Using their respective  $\lambda$  seeds, the parties generate  $\lambda$  garbled circuits, where  $\lambda-1$  garbled circuits (derived from seeds in the seed intersection) are identical for both parties. Each party can then reuse the materials generated from these common  $\lambda-1$  seeds to check the  $\lambda-1$  garbled circuits generated by the other party. Consequently, each party is left with one unchecked garbled circuit, which can be used for dual execution.

With this insight, to achieve robust PVC security with a deterrence factor of  $\frac{\lambda-1}{\lambda}$ , each party only needs to generate  $\lambda$  garbled circuits and evaluate one garbled circuit. Notably, the checking of  $\lambda - 1$  garbled circuits generated by the other party no longer requires garbled circuit generation. In comparison to the state-of-the-art protocol with PVC security [17], where a total of  $2\lambda - 1$ garbled circuits are generated by both parties, and one is evaluated, our approach requires only one additional garbled circuit generation and one additional garbled circuit evaluation. For instance, for the protocol in [17], achieving a deterrence factor of 90% necessitates the garbler to generate 10 garbled circuits, while the evaluator needs to perform 9 garbled circuit generations and one garbled circuit evaluation. In contrast, our approach requires each party to generate 10 garbled circuits and evaluate one garbled circuit. That is, the protocol in [17] requires 20 garbled circuit generations and evaluations, whereas our approach requires 22, and thus the additional overhead in our approach is less than 10% (given that the cost of evaluations is lower than that of generations). Furthermore, the computation of circuit checking for the protocol in [17] must be conducted after circuit generation, while this computation is already performed during the garbled circuit generation in our approach. Thus, as garbled circuit generations and evaluations for each party can be executed in parallel in our approach, the running time of our approach may outperform the PVC protocol in [17].

However, the realization of this insight is highly non-trivial. We omit intricate details and provide a brief illustration of the idea behind our approach as follows. The detailed description of our protocol can be found in Section 4.

To generate  $\lambda+1$  seeds, two parties, denoted as  $\mathsf{P}_\mathsf{A}$  and  $\mathsf{P}_\mathsf{B}$ , can each select  $\lambda+1$  seed shares  $s_i^A$  and  $s_i^B$ , respectively. Subsequently, each party engages in OT protocols with the other party in two directions. As the sender, each party inputs

their seed shares, while as the receiver, each party retrieves  $\lambda$  shares, leaving one share unretrieved. To ensure that each party retrieves all-but-one shares, we incorporate random values called *witnesses* as input in the OT protocols, similar to the approach used in [17]. If a receiving party does not retrieve a share, this party must retrieve the corresponding witness. The retrieved shares and witnesses should be provided by the receiver and verified by the sender later to continue the execution of the protocol. The seeds are then defined as  $s_i = s_i^A \oplus s_i^B$ , and each party will derive  $\lambda$  seeds. A secure equality test is performed by the two parties to ensure that the sets of their seeds are distinct, and if they are found to be identical, the two parties restart the protocol. Step 1 in Fig. 1 illustrates the scenario where 6 seeds are generated.

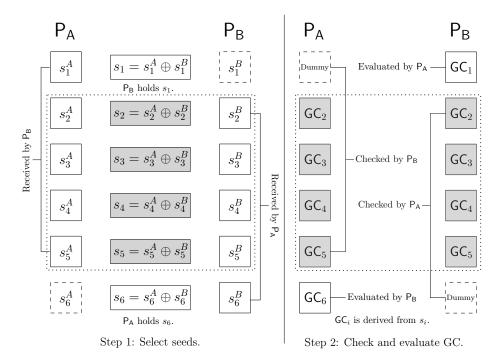


Fig. 1. Seeds generation and garbled circuit evaluation.

Then, each party can utilize the  $\lambda$  seeds they obtained to generate  $\lambda$  garbled circuits. In the case where a party does not obtain a particular seed, a dummy garbled circuit is generated in its place. The parties can exchange the commitments of their  $\lambda+1$  garbled circuits, where the randomness of each commitment is also derived from the respective seed. With  $\lambda$  seeds in hand, each party can verify the correct generation of  $\lambda-1$  garbled circuits (from the commitments) while identifying the remaining one as the dummy circuit. Finally, each party can evaluate the garbled circuit corresponding to the seed it does not obtain as

dual execution and subsequently perform a secure equality test on the outputs of the garbled circuits to determine the final result. Step 2 in Fig. 1 provides an illustrative depiction of this procedure.

One issue encountered in this approach is the potential identification of the dummy garbled circuit when receiving the commitments. More precisely, a malicious party can discern which instances are being checked by the honest party based on the dummy garbled circuit. If its maliciously generated garbled circuit is checked by the other party, the malicious party can promptly abort and refuse to sign the messages required for generating a publicly verifiable certificate. To address this issue, we must ensure that each party remains unaware of which instances are being checked until the necessary materials for certificate generation are ready.

In our approach, we leverage a verifiable time-lock puzzle scheme [10,25] to tackle this challenge. Using this scheme, the puzzle generator can efficiently create a time-lock puzzle for a message, ensuring that the message remains concealed until a specific time has passed, even against parallel adversaries. Essentially, this efficiently generated time-lock puzzle compels a solver to complete a computational task that takes no less time than the specified duration to recover the message. Moreover, once a puzzle is solved, the solver can effectively convince others that the retrieved message originates from the puzzle. In addition, we also require the option for the puzzle solver to open the puzzle at any time, serving as the commitment scheme.

By employing a verifiable time-lock puzzle scheme, each party can generate puzzles for the commitments of the garbled circuits. Therefore, both parties, unaware of the instances being checked, can generate all the necessary materials (e.g., signatures) for generating a publicly verifiable certificate. Afterwards, both parties open their puzzles, verify the garbled circuits, and continue the protocol's execution. If a party refuses to open its puzzles, the other party can solve the puzzle instead. When both parties are honest, no puzzle solving procedure is involved. In the case of detected deviation, the party solving the puzzle can still generate a publicly verifiable certificate as proof of cheating. Given that the puzzle solver can efficiently convince others that the recovered message is derived from the puzzle, the certificate verification process is also efficient. If no deviation is detected, both parties open the respective garbled circuits for evaluation and employ the dual execution approach to evaluate the garbled circuits and determine the evaluation result.

Indeed, similar to the dummy garbled circuit, there exists a potential identification of the dummy instance in the OT protocols for input-wire labels. The solution is also based on time-lock puzzles, but it is more involved (refer to Section 4 for the detailed solution). Additionally, to improve efficiency, we generate time-lock puzzle for messages in a batched fashion, allowing each party to generate only one *real* time-lock puzzle (see Section 2 and 4 for details).

## 1.3 Organization

In Section 2, we introduce the notations used in this paper and the building blocks that form the foundation of our protocol. Subsequently, in Section 3, we present the formal definition of robust PVC security. Based on this definition, in Section 4, we propose our robust PVC protocol in detail, leveraging the idea outlined in Section 1.2, and provide the security proof. Finally, we discuss the efficiency and potential enhancements of our protocol in Section 5.

## 2 Preliminaries

We denote the size of a set S as |S| and use the notation  $x \leftarrow_s S$  to represent the uniform sampling of an element x from the set S. Additionally, let  $[n] = \{1, \ldots, n\}$  for a positive integer n. For a bit string x, the ith bit of x is denoted by x[i]. The function  $\mathsf{bin}(\cdot)$  returns the bit representation of the input.

Let  $\kappa$  denote the computational security parameter, which is provided in unary format as input to all algorithms. A function f in  $\kappa$ , mapping natural numbers to [0,1], is considered negligible if  $f(\kappa) = \mathcal{O}(\kappa^{-c})$  for every constant c > 0. Conversely, a function 1 - f is deemed overwhelming if f is negligible.

Given a seed  $\in \{0,1\}^{\kappa}$ , we can use a pseudorandom function with seed as the key in the Counter (CTR) mode to derive sufficiently many pseudorandom numbers and use them as random coins for operations in protocols.

We denote a (non-interactive) commitment scheme as Com. The scheme utilizes random coins decom for commitment generation and opening. It should satisfy (computational) binding and hiding properties, while also supporting extraction and equivocation. In our protocol, we implement Com using the random oracle  $H: \{0,1\}^* \to \{0,1\}^{\kappa}$  by defining Com(m) = H(m, decom), where  $decom \leftarrow_s \{0,1\}^{\kappa}$ . We employ the collision-resistant hash function H in the protocol. Our protocol will use the signature scheme (KGen, Sig, Vf) that is existentially unforgeable under chosen-message attacks (EUF-CMA).

For an execution transcript of a two-party protocol trans =  $(m_1, m_2, m_3, ...)$ , where the parties send their messages alternately, the *transcript hash* of this execution is defined as  $\mathcal{H} = (\mathsf{H}(m_1), \mathsf{H}(m_2), \mathsf{H}(m_3), ...)$ .

Let  $\Pi_{\mathsf{OT}}$  be the protocol that securely realizes a parallel version of the OT functionality  $\mathcal{F}_{\mathsf{OT}}$  below with perfect correctness [9], such that the receiver (resp. sender) cannot "equivocate" its view by finding a random tape that produces a different output (resp. uses a different input) from the one in the real execution.

## Functionality $\mathcal{F}_{OT}$

**Private inputs:**  $P_A$  has input  $x \in \{0,1\}^{\lambda}$  and  $P_B$  has input  $\{(A_{i,0}, A_{i,1})\}_{i \in [\lambda]}$ .

Upon receiving  $x \in \{0,1\}^{\lambda}$  from  $\mathsf{P}_{\mathsf{A}}$  and  $\{(A_{i,0},A_{i,1})\}_{i\in[\lambda]}$  from  $\mathsf{P}_{\mathsf{B}}$ , send the selected message  $\{A_{i,x[i]}\}_{i\in[\lambda]}$  to  $\mathsf{P}_{\mathsf{A}}$ .

In our protocol, we will use the protocol  $\Pi_{\mathsf{Eq}}$  that securely realizes the two-party equality test [7,18] functionality  $\mathcal{F}_{\mathsf{Eq}}$  in the following.

## Functionality $\mathcal{F}_{Eq}$

**Private inputs:**  $P_A$  has input  $x \in \{0,1\}^{\kappa}$  and  $P_B$  has input  $y \in \{0,1\}^{\kappa}$ .

Upon receiving  $x \in \{0,1\}^{\kappa}$  from  $P_A$  and  $y \in \{0,1\}^{\kappa}$  from  $P_B$ , let b = true if x = y, and b = false otherwise.

- If both parties are honest, send b to both parties.
- If a party is corrupted by the adversary, send b to this corrupted party. Then
  if continue from the adversary is received, send b to the honest party.

**Garbling Scheme** Our protocol uses a circuit garbling scheme (Gb, Eval) as follows.

- The algorithm Gb takes as input the security parameter  $1^{\kappa}$  and a circuit  $\mathcal{C}$  that has  $n = n_A + n_B$  input wires and  $n_O$  output wires, and outputs inputwire labels  $\{(X_{i,0}, X_{i,1})\}_{i \in [n]}$ , a garbled circuit GC, and output-wire labels  $\{(Z_{i,0}, Z_{i,1})\}_{i \in [n_O]}$ .
- The deterministic algorithm Eval takes as input a set of input-wire labels  $\{X_i\}_{i\in[n]}$  and a garbled circuit GC. It outputs a set of output-wire labels  $\{Z_i\}_{i\in[n_O]}$ .

The correctness of the garbling scheme means that for any circuit  $\mathcal{C}$  as above and any input  $x \in \{0,1\}^n$ , we have

$$\Pr \begin{bmatrix} \forall i, Z_i = Z_{i,z[i]} \\ \land Z_i \neq Z_{i,1-z[i]} : \frac{(\{(X_{i,0}, X_{i,1})\}_{i \in [n]}, \mathsf{GC}, \{(Z_{i,0}, Z_{i,1})\}_{i \in [n_O]}) \leftarrow \mathsf{Gb}(1^\kappa, \mathcal{C})}{\{Z_i\} \leftarrow \mathsf{Eval}(\{X_{i,x[i]}, \mathsf{GC}\})} \end{bmatrix}$$

where  $z = \mathcal{C}(x)$ , except for a negligible probability. We assume that the garbling scheme satisfies the standard security definition [23,5]. We assume that there is a simulator  $\mathcal{S}_{\mathsf{Gb}}$  such that for all  $\mathcal{C}$  and x, the distribution  $\{\mathcal{S}_{\mathsf{Gb}}(1^{\kappa}, \mathcal{C}, \mathcal{C}(x))\}$  is computationally indistinguishable from

$$\left\{ \begin{pmatrix} \{X_{i,x[i]}\}_{i \in [n]}, \mathsf{GC}, \\ \{(Z_{i,0}, Z_{i,1})\}_{i \in [n_O]} \end{pmatrix} : (\{(X_{i,0}, X_{i,1})\}_{i \in [n]}, \mathsf{GC}, \{(Z_{i,0}, Z_{i,1})\}_{i \in [n_O]}) \leftarrow \mathsf{Gb}(1^\kappa, \mathcal{C}) \right\}.$$

**Verifiable Time-Lock Puzzle Scheme** We use a verifiable time-lock puzzle scheme in our protocol. We restate its definition in [10] with minor modification<sup>5</sup> as follows.

**Definition 1.** A verifiable time-lock puzzle scheme TLP consisting of algorithms (Setup, Gen, Solve, Verify, Verify') with solution space  $\mathbb{S}$  is as follows.

<sup>&</sup>lt;sup>5</sup> In particular, we include the opening  $\pi$  (e.g., randomness) as the output of Gen for later puzzle opening. We add the algorithm Verify to verify the opening of a puzzle from the puzzle generator.

- The algorithm Setup takes as input  $1^{\kappa}$  and a hardness parameter  $\tau$ , and outputs public parameters pp.
- The algorithm Gen takes as input public parameters pp and a solution  $s \in \mathbb{S}$  and then outputs a puzzle p, together with an opening  $\pi$ .
- The deterministic algorithm Solve takes as input public parameters pp and a puzzle p and then outputs a solution s and a proof  $\pi'$ .
- The deterministic algorithm Verify takes as input public parameters pp, a puzzle p, a solution s, and an opening  $\pi$  and then outputs true if the solution s is the valid solution for p. Otherwise, the algorithm outputs false.
- The deterministic algorithm Verify' takes as input public parameters pp, a puzzle p, a solution s, and a proof  $\pi'$  and then outputs true if the solution s is valid. Otherwise, the algorithm outputs false. This algorithm must run in total time polynomial in  $\kappa$  and  $\log \tau$ .

A verifiable time-lock puzzle scheme TLP should satisfy *completeness*, *correctness for opening and proof*, *soundness*, and *security*. We provide the definition of these properties and present a verifiable time-lock puzzle scheme [10,25] in the full version of this paper.

In the description of our protocol, we do not explicitly differentiate between puzzle opening and proof, as well as between the algorithms Verify and Verify'. This is because all of these components enable efficient verification of the correctness of a given solution within the protocol.

It is worth noting that we can use a time-lock puzzle scheme to generate time-lock puzzles in a batched manner. Specifically, we can generate a solution  $s \in \mathbb{S}$  and a time-lock puzzle p for s. Then, given messages  $\{m_i\}$ , we can use s as the seed to derive a sufficient number of (symmetric encryption) keys and randomness and encrypt messages  $\{m_i\}$  using keys via IND-CPA (or IND-CCA) encryption schemes with generated randomness. For simplicity, we slightly abuse notation and denote the encryption as  $\mathsf{Enc}_s(\cdot)$ . The puzzle generator can send the puzzle p and the ciphertexts of  $m_i$ 's to the puzzle receiver. Note that the ciphertexts of  $m_i$ 's can also be regarded as time-lock puzzles since the puzzle receiver learns nothing about the solution s before s is solved based on the security of the time-lock puzzle and the encryption scheme. After solving s and obtaining s, the receiver can easily derive the messages s in this approach, we refer to the solution s as the master puzzle key and the puzzle s as the master time-lock puzzle.

In our protocol, we use s as the seed to derive keys, and then use the random oracle with keys in CTR mode to generate enough pseudorandom padding to encrypt messages  $\{m_i\}$ . We can easily see that the encryption is IND-CPA-secure before s is derived from p. This scheme allows us to program the random oracle to equivocate the encrypted values in the security proof.

Remark 1. We note that given a ciphertext from the ciphertext space and a key, the decryption of the ciphertext always succeeds (although not necessarily yielding the correct result). This property is solely for the convenience of our

<sup>&</sup>lt;sup>6</sup> In this paper, we use "ciphertext" and "puzzle" interchangeably for this setting.

protocol description. It is very straightforward to modify our protocol to enable honest parties to generate publicly verifiable certificates for decryption failures and attribute blame to malicious parties responsible for generating invalid ciphertexts [25].

## 3 Definition of Robust PVC Security

Based on the discussion in Section 1.2, we define the ideal functionality  $\mathcal{F}_{\mathsf{RobustPVC}}$  for robust PVC security as follows.

### Functionality $\mathcal{F}_{\mathsf{RobustPVC}}$ with deterrence $\epsilon$

**Public inputs:** Both parties agree on a circuit C, which has  $n = n_A + n_B$  input wires and  $n_O$  output wires.

**Private inputs:**  $P_A$  has input  $x_A \in \{0,1\}^{n_A}$ , whereas the other party  $P_B$  has input  $x_B \in \{0,1\}^{n_B}$ .

Both parties send their inputs to the ideal functionality. If abort from the party corrupted by the adversary is received, send  $\perp$  to both parties and terminate.

- If an input of the form (cheat,  $\hat{\epsilon}$ ), where  $\hat{\epsilon} \geq \epsilon$ , from the party corrupted by the adversary is received:
  - With probability  $\hat{\epsilon}$ , send (corrupted) to both parties and terminate.
  - With probability  $1 \hat{\epsilon}$ , send (undetected) to the corrupted party. Then ignore any input of the form (cheat, ·) or (stupidCheat, ·).
- If an input of the form (stupidCheat,  $\hat{\epsilon}$ ) from the party corrupted by the adversary is received:
  - With probability  $\hat{\epsilon}$ , send (corrupted) to both parties and terminate.
  - With probability  $1 \hat{\epsilon}$ , send  $\perp$  to both parties and terminate.
- If input  $x_A \in \{0,1\}^{n_A}$  from  $P_A$  and  $x_B \in \{0,1\}^{n_B}$  from  $P_B$  has been received:
  - 1. If both parties are honest, give  $C(x_A, x_B)$  to them and terminate.
  - 2. If any party is corrupted, give  $C(x_A, x_B)$  to the corrupted party.
  - 3. If a boolean function g from the adversary is received and undetected has been sent, give  $g(x_A, x_B)$  to the adversary. Then if continue from the adversary is received, give cheating to the honest party if  $g(x_A, x_B) = 0$ , else give  $C(x_A, x_B)$  to the honest party.

In order to align with the security proof, we introduce slight modifications to the definition inherited from PVC security. In the ideal functionality  $\mathcal{F}_{\mathsf{RobustPVC}}$ , we permit the adversary to cheat with a probability of being caught  $\hat{\epsilon}$  that larger than or equal to the specified deterrence factor  $\epsilon$ , i.e.,  $\hat{\epsilon} \geq \epsilon$ . It is evident that this modification does not compromise security. Additionally, we allow the adversary to engage in *stupid cheating*. With stupid cheating, we do not impose any restrictions on the probability of remaining undetected. In this scenario, even if the adversary is not detected, the ideal functionality will still abort, rendering the adversary unable to gain any advantage. It is also apparent that this modification does not compromise security.

The definition of robust PVC security is given in the following.

**Definition 2.** A two-party protocol  $\Pi_{\mathsf{RobustPVC}}$  along with algorithms Blame and Judge achieves robust publicly verifiable covert (PVC) security with deterrence  $\epsilon$  if the following conditions hold.

Simulatability The protocol  $\Pi_{\mathsf{RobustPVC}}$ , where the honest party might send cert to the adversary if cheating is detected, securely realizes  $\mathcal{F}_{\mathsf{RobustPVC}}$  with deterrence  $\epsilon$ .

**Public Verifiability** If the honest party outputs corrupted (together with an output certificate cert), then the output of Judge(cert) is true, except for a negligible probability.

**Defamation Freeness** For every PPT adversary  $\mathcal{A}$  corrupting a party, if the other party is honest, the probability that  $\mathcal{A}$  generates a certificate cert\* that blames the honest party and leads to  $\mathsf{Judge}(\mathsf{cert}^*)$  outputting true is negligible.

Remark 2. In the definition above and the protocol description in Section 4, it is specified that the honest party sends the certificate to the adversary. This specification in the definition is to ensure that the adversary cannot learn any information about the honest party's input even when the certificate is provided.

Remark 3. We note that public verifiability in the definition also implies that if the honest party outputs corrupted, the malicious party cannot hinder the honest party from generating a valid certificate.

## 4 Our Robust PVC-Secure Protocol

In this section, we introduce the protocol  $\Pi_{\mathsf{RobustPVC}}$  that achieves robust PVC security defined in Section 3. This protocol is based on the idea introduced in Section 1.2.

The protocol description here employs  $\lambda$  instances instead of  $\lambda+1$  in Section 1.2 (thus with deterrence factor  $\epsilon=\frac{\lambda-2}{\lambda-1}$ ) for the sake of notation simplicity. The circuit for  $\Pi_{\mathsf{RobustPVC}}$  is denoted by  $\mathcal{C}$ , consisting of  $n=n_A+n_B$  input wires and  $n_O$  output wires. The input of  $\mathsf{P}_\mathsf{A}$  is  $x_A\in\{0,1\}^{n_A}$  while the input of  $\mathsf{P}_\mathsf{B}$  is  $x_B\in\{0,1\}^{n_B}$ .

Seed preparation. At the beginning of the protocol, each party generates three random  $\kappa$ -bit strings. For example,  $\mathsf{P}_\mathsf{A}$  generates  $\mathsf{seed}_j^A$ ,  $\mathsf{seed'}_j^A$ , and  $\mathsf{witness'}_j^A$ . Here,  $(\mathsf{seed'}_j^A, \mathsf{witness'}_j^A)$  represents  $\mathsf{P}_\mathsf{A}$ 's seed share and witness for the jth instance, as discussed in Section 1.2, and  $\mathsf{seed}_j^A$  is used to derive randomness for  $\Pi_\mathsf{OT}$  when  $\mathsf{P}_\mathsf{A}$  acts as the receiver. Each party commits to their three random strings, and the commitments will be signed by the other party later. This enables a certificate verifier to simulate the protocols execution based on these seeds/witnesses and verify the deviation of the other party, given the signature and the openings of signed commitments to these seeds/witnesses.

Next, each party executes  $\Pi_{OT}$  and retrieves all-but-one, i.e.,  $\lambda - 1$ , seed shares from the other party. For example, we assume that the index of the garbled circuit  $P_A$  will evaluate is  $\hat{\jmath}_A$ , then  $P_A$  retrieves  $\{\text{seed'}_i^B\}_{j \in [\lambda] \setminus \{\hat{\jmath}_A\}}$  and

witness' $_{j_A}^B$ . Each seed is defined as  $\operatorname{seed}'_j \leftarrow \operatorname{seed}'_j^A \oplus \operatorname{seed}'_j^B$ . Subsequently, both parties execute the equality test protocol  $\Pi_{\mathsf{Eq}}$  as mentioned in Section 1.2 to ensure they do not possess the same set of seeds. Furthermore, parties commit to their retrieved seed shares and witnesses, which should be opened and verified by the other party at a later stage.

Circuit and input preparation. After obtaining the  $\lambda-1$  seeds  $\operatorname{seed}_j$ 's, each party can generate  $\lambda-1$  garbled circuits  $\{\operatorname{GC}_j\}$  with randomness derived from  $\{\operatorname{seed}_j'\}$ . To avoid sending the whole garbled circuits, each party generates a commitment to each  $\operatorname{GC}_j$ , along with its (randomly permuted) input-wire and output-wire labels, using randomness derived from  $\operatorname{seed}_j'$ . The input-wire labels in each pair are randomly permuted to hide the semantic values of the labels when the garbled circuit is later opened for evaluation. Additionally, the garbler commits to the index of his/her input-wire labels with respect to the randomly permuted input-wire labels. This step ensures that parties cannot change the input after the instance checking. For the  $\hat{\jmath}_A$ th (resp.  $\hat{\jmath}_B$ th) instance where  $\mathsf{P}_A$  (resp.  $\mathsf{P}_B$ ) does not possess the seed, dummy materials are generated in their places. As discussed in Section 1.2, a party cannot directly send the commitments of the garbled circuits to the other party. Instead, each party uses the verifiable time-lock puzzle scheme to encrypt those commitments and sends them to the other party.

Then each party acting as the sender executes  $\Pi_{OT}$  with the other party to transmit input-wire labels. The inputs to  $\Pi_{\mathsf{OT}}$  are the input-wire labels for the other parties. For each checking instance, it is essential to ensure that each party can verify the validity of the input-wire labels provided by the other party. For example,  $P_A$  needs to verify that  $P_B$  acting as the sender in  $\Pi_{OT}$  uses the correct input-wire labels for  $P_A$ . Since  $P_A$  knows  $seed'_i$ , she knows all the correct input-wire labels. Therefore, if  $P_A$  knows the randomness used by  $P_B$  in  $\Pi_{OT}$ , she can check whether  $\mathsf{P}_\mathsf{B}$  deviates from the protocol. However, it is important to note that  $P_B$ 's randomness cannot simply be derived from  $seed'_i$  or  $seed'_i$ that are known to  $P_A$ . The reason is that, given those materials,  $P_A$  can simulate the execution of  $\Pi_{OT}$  and immediately determine which instance is the  $\hat{\jmath}_B$ th instance, i.e., the dummy instance of P<sub>B</sub>, subsequently identify the checking instances. Hence, similar to the problem mentioned in Section 1.2, we need to ensure that a party can check the instance, but until all materials for certificate generation are ready. In our protocol, we additionally introduce  $seed_{i,OT}^A$  and  $\mathsf{seed}_{j,\mathsf{OT}}^B$  to address this issue. For each instance,  $\mathsf{P}_\mathsf{A}$  randomly chooses uniform  $\kappa$ -bit string  $\operatorname{\mathsf{seed}}_{j,\mathsf{OT}}^A$  and uses the time-lock puzzle to encrypt  $\operatorname{\mathsf{seed}}_{j,\mathsf{OT}}^A$  and inputwire labels of  $P_B$ . Then in the execution of  $\Pi_{OT}$  where  $P_A$  acts as the sender, the inputs are time-lock puzzles for input-wire labels of  $P_B$ , and the randomness is derived from  $\operatorname{\mathsf{seed}}_{i,\mathsf{OT}}^A$  for  $\mathsf{P}_\mathsf{A}$ 's  $\hat{\jmath}_A$ th instance while  $\operatorname{\mathsf{seed}}_i' \oplus \operatorname{\mathsf{seed}}_{i,\mathsf{OT}}^A$  for other

Each party also acts as the receiver and executes  $\Pi_{\mathsf{OT}}$  with the other party. For example, the inputs of  $\mathsf{P}_{\mathsf{A}}$  to  $\Pi_{\mathsf{OT}}$  is  $0^{n_A}$  for checking instance and  $x_A \in [n_A]$  for the evaluation instance with index  $\hat{\jmath}_A$ . The randomness in each execution is

derived from  $\mathsf{seed}_j^A$ . With knowledge of  $\mathsf{seed}_j'$  and  $\mathsf{seed}_{j,\mathsf{OT}}^B$ ,  $\mathsf{P}_\mathsf{A}$  can later simulate the execution of  $\mathsf{P}_\mathsf{A}$  in  $\Pi_\mathsf{OT}$  and detect  $\mathsf{P}_\mathsf{B}$ 's deviations.

Publicly verifiable evidence creation. Each party proceeds to sign the messages exchanged in each instance. At this stage, all materials necessary for certificate generation are available. Since all materials related to checking deviations are encrypted using time-lock puzzles, both parties are unable to perform the instance checking at this point. Therefore, we need to set the hardness parameter of the verifiable time-lock puzzle scheme to ensure that the time-lock puzzle cannot be solved until both parties have exchanged their signatures. In our protocol, we let the hardness parameter  $\tau > 2\tau_c$ , where  $\tau_c$  is the timeout time for execution of Steps 6 and 7.

Check of instances. Upon receiving the signature of the other party, each party can open their respective time-lock puzzles, allowing the other party to perform instance checking. If the other party fails to open the puzzles, each party can solve the puzzles themselves. With the commitments of the garbled circuit generated by the other party and the seed for  $\Pi_{OT}$  (i.e., seed<sup>A</sup><sub>j,OT</sub> or/and seed<sup>B</sup><sub>j,OT</sub>), both parties can simulate the computation of the other party for their checking instances. Among these instances, one should be a dummy instance, while the remaining instances should be correct. In case a deviation by the other party is detected, the detecting party can generate the certificate based on the signed materials, the openings/proofs for the time-lock puzzles, and the decommitments for the seeds/witnesses used in  $\Pi_{OT}$ .

Circuit evaluation. Assuming the checking instances are correct, two garbled circuits remain for evaluation. First, both parties open the commitments for the seed shares and the witness they obtained at the beginning of the protocol to demonstrate their honesty. Then, they open their respective garbled circuits, input-wire labels, and the mapping of output-wire labels to each other. Both parties verify the openings provided by the other party and proceed to evaluate the garbled circuit to obtain the output-wire labels and the result. For example,  $P_A$  obtains the output-wire labels  $\{Z_{\hat{\jmath}_A,i}\}_{i\in[n_O]}$  and the result  $z_{\hat{\jmath}_A}$ , where  $\hat{\jmath}_A$  represents  $P_A$ 's index of instance for a label of  $P_A$  then sets  $P_A \leftarrow P(\bigoplus_{i=1}^{n_O}(Z_{\hat{\jmath}_A,i} \oplus Z_{\hat{\jmath}_B,i,z_{\hat{\jmath}_A}[i]}))$ , where  $\{Z_{\hat{\jmath}_B,i,b}\}_{i\in[n_O],b\in\{0,1\}}$  denotes the output-wire labels for the garbled circuit generated by  $P_A$  and evaluated by  $P_B$ . Similarly,  $P_B$  evaluates the garbled circuit, obtains the output, and computes  $P_B$ . Finally, the two parties use the equality test protocol  $P_B$  to determine the final evaluation result.

The full description of the protocol  $\Pi_{\mathsf{RobustPVC}}$  between two parties  $\mathsf{P}_\mathsf{A}$  and  $\mathsf{P}_\mathsf{B}$  is given in the following.

## ${\bf Protocol} \ {\it \Pi}_{\sf RobustPVC}$

Schemes/Protocols: The signature scheme (KGen, Sig, Vf) is EUF-CMA-secure. The verifiable time-lock puzzle scheme TLP is secure with respect to the hardness parameter  $\tau > 2\tau_c$ , where  $\tau_c$  is the timeout time for execution of Steps 6 and 7. Com is the computational binding and hiding commitment scheme, H is the collision-resistant hash function, the encryption scheme with respect to TLP is

IND-CPA-secure (see Section 2 for more information).  $\Pi_{OT}$  is a perfectly correct protocol that realizes  $\mathcal{F}_{OT}$ , and  $\Pi_{Eq}$  is an equality test protocol that realizes  $\mathcal{F}_{Eq}$ . The garbling scheme used in this protocol is secure.

**Public inputs:** Both parties agree on parameters  $\kappa$ ,  $\lambda$ , and  $\tau$ , and a circuit  $\mathcal{C}$ , which has  $n=n_A+n_B$  input wires and  $n_O$  output wires. Both parties also agree on the public information (e.g., time for communication rounds, algorithms, parameters, and unique id for the execution of this protocol).  $P_A$  and  $P_B$  know keys  $vk_B$  and  $vk_A$ , respectively, for the signature scheme.

**Private inputs:**  $\mathsf{P}_{\mathsf{A}}$  has input  $x_A \in \{0,1\}^{n_A}$  and keys  $(\mathsf{vk}_A, \mathsf{sigk}_A)$  for the signature scheme.  $\mathsf{P}_{\mathsf{B}}$  has input  $x_B \in \{0,1\}^{n_B}$  and keys  $(\mathsf{vk}_B, \mathsf{sigk}_B)$  for the signature scheme.

#### **Seed Preparation**

- 1.  $P_A$  goes through the following steps with  $P_B$ . In the meantime, they switch their roles to execute the symmetric steps, *i.e.*,  $P_A$  plays  $P_B$ 's role and  $P_B$  plays  $P_A$ 's.
  - (a)  $\mathsf{P}_\mathsf{A}$  chooses uniform  $\kappa$ -bit strings for  $\mathsf{seed}_j^A$ ,  $\mathsf{seed}_j'^A$ , and  $\mathsf{witness'}_j^A$ , and  $\mathsf{computes}\ \mathsf{c}_{\mathsf{seed}_j^A} \leftarrow \mathsf{Com}(\mathsf{seed}_j^A)$ ,  $\mathsf{c}_{\mathsf{seed}_j'_j^A} \leftarrow \mathsf{Com}(\mathsf{seed}_j'^A)$ , and  $\mathsf{c}_{\mathsf{witness'}_j^A} \leftarrow \mathsf{Com}(\mathsf{witness'}_j^A)$  for  $j \in [\lambda]$ , and sends these commitments to  $\mathsf{P}_\mathsf{B}$ .  $\mathsf{P}_\mathsf{B}$  picks  $\hat{\jmath}_B \leftarrow \mathsf{s}[\lambda]$  and sets  $b_{\hat{\jmath}_B} = 1$  and  $b_j = 0$  for  $j \neq \hat{\jmath}_B$ .
  - (b)  $\mathsf{P}_\mathsf{A}$  and  $\mathsf{P}_\mathsf{B}$  run  $\lambda$  executions of the protocol  $\Pi_\mathsf{OT}$ . In the jth execution,  $\mathsf{P}_\mathsf{A}$  uses as input  $(\mathsf{seed'}_j^A, \mathsf{witness'}_j^A)$  with randomness derived from  $\mathsf{seed}_j^A$ , while  $\mathsf{P}_\mathsf{B}$  uses as input  $b_j$  with randomness derived from his  $\mathsf{seed}_j^B$  generated in Step 1a. At the end,  $\mathsf{P}_\mathsf{B}$  has  $\{\mathsf{seed'}_j^A\}_{j\neq j_B}$  and  $\mathsf{witness'}_{j_B}^A$ . Denote the transcript of the jth execution by  $\mathsf{trans}_j^A$ .

Let  $\mathsf{CheckSet}_A = [\lambda] \setminus \{\hat{\jmath}_A\}$ ,  $\mathsf{CheckSet}_B = [\lambda] \setminus \{\hat{\jmath}_B\}$ , and  $\mathsf{ComCheckSet} = [\lambda] \setminus \{\hat{\jmath}_A, \hat{\jmath}_B\}$ .

- 2.  $\mathsf{P}_\mathsf{A}$  computes  $\mathsf{seed}_j' \leftarrow \mathsf{seed}_j'^A \oplus \mathsf{seed}_j'^B$  for all  $j \in \mathsf{CheckSet}_A$  and  $h_A \leftarrow \mathsf{H}(\bigoplus_{j \in \mathsf{CheckSet}_A} \mathsf{seed}_j')$ .  $\mathsf{P}_\mathsf{B}$  performs a similar computation to derive  $\{\mathsf{seed}_j'\}$  and  $h_B$  according to his  $\mathsf{CheckSet}_B$ .  $\mathsf{P}_\mathsf{A}$  and  $\mathsf{P}_\mathsf{B}$  use the protocol  $\mathit{\Pi}_\mathsf{Eq}$  to check whether  $h_A = h_B$ . If it does not hold, they continue the protocol execution. Otherwise, they restart the protocol.
- 3.  $P_A$  computes  $c_A \leftarrow \mathsf{Com}(\hat{\jmath}_A, \{\mathsf{seed'}_j^B\}_{j \neq \hat{\jmath}_A}, \mathsf{witness'}_{\hat{\jmath}_A}^B)$  and sends it to  $P_B$ . Similarly,  $P_B$  computes and sends  $c_B$  to  $P_A$ .

## Circuit and Input Preparation

- 4. For  $j \in \mathsf{CheckSet}_A$ ,  $\mathsf{P}_A$  follows the procedure below, where all randomness in the jth instance is derived from  $\mathsf{seed}'_j$ .
  - (a)  $\mathsf{P}_\mathsf{A}$  garbles the circuit  $\mathcal{C}$ . Denote the jth garbled circuit by  $\mathsf{GC}_j$ , the inputwire labels of  $\mathsf{P}_\mathsf{A}$  by  $\{A_{j,i,b}\}_{i\in[n_A],b\in\{0,1\}}$ , the input-wire labels of  $\mathsf{P}_\mathsf{B}$  by  $\{B_{j,i,b}\}_{i\in[n_B],b\in\{0,1\}}$ , and the output-wire labels by  $\{Z_{j,i,b}\}_{i\in[n_O],b\in\{0,1\}}$ .
  - (b)  $\mathsf{P}_\mathsf{A}$  computes her label commitments  $h_{j,i,b}^A \leftarrow \mathsf{Com}(A_{j,i,b})$  for all  $i \in [n_A]$  and  $b \in \{0,1\}$  and also  $h_{j,i,b}^B \leftarrow \mathsf{Com}(B_{j,i,b})$  for all  $i \in [n_B]$  and  $b \in \{0,1\}$ .
  - (c)  $\mathsf{P}_{\mathsf{A}}$  computes the commitment  $\mathsf{c}_{j} \leftarrow \mathsf{Com}(\mathsf{GC}_{j}, \{(h_{j,i,\alpha_{i}^{A}}^{A}, h_{j,i,\bar{\alpha}_{i}^{A}}^{A})\}_{i \in [n_{A}]}, \{(h_{j,i,\alpha_{i}^{B}}^{B}, h_{j,i,\bar{\alpha}_{i}^{B}}^{B})\}_{i \in [n_{B}]}, \{(\mathsf{H}(Z_{j,i,0}), \mathsf{H}(Z_{j,i,1}))\}_{i \in [n_{O}]}), \text{ in which each pair}$

 $(h_{j,i,0}^A, h_{j,i,1}^A)$  is randomly permuted with respect to  $\alpha_i^A \leftarrow s\{0,1\}$ , while  $(h_{j,i,0}^B, h_{j,i,1}^B)$  is also randomly permuted. Denote the index of  $h_{j,i,x_A[i]}^A$  with respect to  $x_A[i]$  in  $(h_{j,i,\alpha_i^A}^A, h_{j,i,\bar{\alpha}_i^A}^A)$  by  $\gamma_j^A[i] = \alpha_i^A \oplus x[i]$ , and thus the string of indices is denoted by  $\gamma_j^A \in \{0,1\}^{n_A}$ .

In parallel,  $P_B$  also follows this procedure as  $P_A$  for  $j \in \mathsf{CheckSet}_B$  using randomness derived from  $\mathsf{seed}'_j$ .

- Then,  $\mathsf{P}_\mathsf{A}$  lets  $\mathsf{c}_{\hat{\jmath}_A} = 0$ ,  $\gamma_{\hat{\jmath}_A}^A = 0$ , and  $B_{\hat{\jmath}_A,i,b} = 0$  for all  $i \in [n_B]$  and  $b \in \{0,1\}$ . Symmetrically,  $\mathsf{P}_\mathsf{B}$  lets  $\mathsf{c}_{\hat{\jmath}_B} = 0$ ,  $\gamma_{\hat{\jmath}_B}^B = 0$ , and  $A_{\hat{\jmath}_B,i,b} = 0$  for all  $i \in [n_A]$  and  $b \in \{0,1\}$ .
- 5.  $\mathsf{P}_\mathsf{A}$  computes and sends  $\mathsf{c}_{\gamma_j^A} \leftarrow \mathsf{Com}(\gamma_j^A)$  for  $j \in [\lambda]$  to  $\mathsf{P}_\mathsf{B}$ . Similarly,  $\mathsf{P}_\mathsf{B}$  computes and sends  $\mathsf{c}_{\gamma_j^B} \leftarrow \mathsf{Com}(\gamma_j^B)$  for  $j \in [\lambda]$  to  $\mathsf{P}_\mathsf{A}$ .
- 6. For  $j \in [\lambda]$ ,  $P_A$  chooses uniform  $\kappa$ -bit string  $\operatorname{seed}_{j,\mathsf{OT}}^A$  and a random master puzzle  $\operatorname{key} s_j^A$ , and generates a master time-lock puzzle  $\mathsf{p}_{s_j^A}$  for  $s_j^A$  with respect to the hardness parameter  $\tau$ . She also computes puzzles  $\mathsf{pc}_j \leftarrow \operatorname{Enc}_{s_j^A}(\mathsf{c}_j)$ ,  $\mathsf{p}_{\operatorname{seed}_{j,\mathsf{OT}}^A} \leftarrow \operatorname{Enc}_{s_j^A}(\operatorname{seed}_{j,\mathsf{OT}}^A)$ , and  $\mathsf{p}_{B_{j,i,b}} \leftarrow \operatorname{Enc}_{s_j^A}(B_{j,i,b})$  for  $i \in [n_B]$  and  $b \in \{0,1\}$ . Then  $\mathsf{P}_A$  sends  $\mathsf{p}_{s_j^A}$ ,  $\mathsf{pc}_j$ , and  $\mathsf{p}_{\operatorname{seed}_{j,\mathsf{OT}}^A}$  to  $\mathsf{P}_B$ . P<sub>A</sub> and  $\mathsf{P}_B$  run  $\lambda$  executions of  $H_{\mathsf{OT}}$ . In the jth execution,  $\mathsf{P}_A$  uses as input  $\{(\mathsf{p}_{B_{j,i,0}},\mathsf{p}_{B_{j,i,1}})\}_{i\in[n_B]}$ , and  $\mathsf{P}_B$  uses  $x_B \in \{0,1\}^{n_B}$  as input if  $j=\hat{\jmath}_B$  and  $\mathsf{O}^{n_B}$  otherwise. Here  $\mathsf{P}_A$  uses ( $\mathsf{seed}_j' \oplus \mathsf{seed}_{j,\mathsf{OT}}^A$ ) for  $j \neq \hat{\jmath}_A$  and  $\mathsf{seed}_{j,\mathsf{OT}}^A$  for  $j = \hat{\jmath}_A$  to derive her randomness in the jth execution, while  $\mathsf{P}_B$  uses  $\mathsf{seed}_j^B$ . Finally,  $\mathsf{P}_B$  obtains  $\{\mathsf{p}_{B_{j_B,i,x_B[i]}}\}_{i\in[n_B]}$  for the  $\hat{\jmath}_B$ th execution. Denote the transcript hash for the jth execution of  $H_{\mathsf{OT}}$  by  $\mathcal{H}_j^A$ .

Similarly,  $\mathsf{P}_\mathsf{B}$  also follows the same procedure as  $\mathsf{P}_\mathsf{A}$ , *i.e.*,  $\mathsf{P}_\mathsf{B}$  computes and sends  $\mathsf{p}_{s_j^B}$ ,  $\mathsf{p}_{\mathsf{c}_j}$ , and  $\mathsf{p}_{\mathsf{seed}_{j,\mathsf{OT}}^B}$  for  $j \in [\lambda]$  to  $\mathsf{P}_\mathsf{A}$ .  $\mathsf{P}_\mathsf{B}$  also runs  $\lambda$  executions of  $\Pi_{\mathsf{OT}}$  for input  $\{(\mathsf{p}_{A_{j,i,0}},\mathsf{p}_{A_{j,i,1}})\}_{i\in[n_A]}$  with  $\mathsf{P}_\mathsf{A}$  as above. Denote the transcript hash for the jth execution of  $\Pi_{\mathsf{OT}}$  by  $\mathcal{H}_j^B$ .

#### **Publicly Verifiable Evidence Creation**

7. For each  $j \in [\lambda]$ ,  $\mathsf{P}_\mathsf{A}$  generates a signature  $\sigma_j^A \leftarrow \mathsf{Sig}_{\mathsf{sigk}_A}(id, \mathcal{C}, j, \mathsf{c}_{\mathsf{seed}_j^B}, \mathsf{c}_{\mathsf$ 

## Check of Instances

- 8.  $P_A$  and  $P_B$  open the master time-lock puzzle of the master puzzle key to each other. If one party does not open the puzzle, the other party can also solve the puzzle to derive the master puzzle key.
- 9. For each  $j \in [\lambda]$ ,  $P_A$  decrypts  $P_B$ 's  $p_{c_j}$  and  $p_{\mathsf{seed}_{j,\mathsf{OT}}^B}$  using the master puzzle key  $s_j^B$  to obtain  $c_j$  and  $\mathsf{seed}_{j,\mathsf{OT}}^B$ .  $P_A$  also decrypts  $p_{A_{j_A,i,x_A[i]}}$  to obtain  $A_{j_A,i,x_A[i]}$ . Note that for  $j \in \mathsf{ComCheckSet}$ , honest  $P_A$  holds the same  $\mathsf{seed}_j'$  as honest  $P_B$ , and thus the same materials in Step 4.  $P_A$  follows the checking procedure

- below to check  $P_B$ 's  $\{c_j\}$  and  $\{\mathcal{H}_j^B\}$ . Once a certificate cert is generated during the check,  $P_A$  outputs corrupted, sends cert to  $P_B$ , and halts immediately.
- (a) For j ∈ CheckSet<sub>A</sub>, if there exists a c<sub>j</sub> from P<sub>B</sub> that is not equal to P<sub>A</sub>'s c<sub>j</sub> and also c<sub>j</sub> ≠ 0, P<sub>A</sub> uniformly chooses such a j and uses Blame(BadCom, j) to generate cert.
- (b) For  $j \in \mathsf{CheckSet}_A$ , if  $\mathsf{c}_j$  from  $\mathsf{P}_\mathsf{B}$  is equal to  $\mathsf{P}_\mathsf{A}$ 's  $\mathsf{c}_j$ ,  $\mathsf{P}_\mathsf{A}$  simulates  $\mathsf{P}_\mathsf{B}$ 's computation of  $\{\mathsf{p}_{A_{j,i,b}}\}_{i\in[n_A]}$  and the executions of  $\Pi_\mathsf{OT}$  in Step 6 with  $\mathsf{P}_\mathsf{B}$ 's randomness derived from  $\{\mathsf{seed}_j'\oplus\mathsf{seed}_{j,\mathsf{OT}}^B\}$  to derive the transcript hash  $\hat{\mathcal{H}}_j^B$ . If  $\hat{\mathcal{H}}_j^B \neq \mathcal{H}_j^B$ ,  $\mathsf{P}_\mathsf{A}$  uniformly chooses such a j and uses  $\mathsf{Blame}(\mathsf{BadOT},j)$  to generate cert. For  $j \in \mathsf{CheckSet}_A$ , if  $\mathsf{P}_\mathsf{B}$ 's  $\mathsf{c}_j = 0$ ,  $\mathsf{P}_\mathsf{A}$  simulates  $\mathsf{P}_\mathsf{B}$ 's computation of  $\{\mathsf{p}_{A_{j,i,b}}\}$ , where  $A_{j,i,b} = 0$ , and the executions of  $\Pi_\mathsf{OT}$  in Step 6 with  $\mathsf{P}_\mathsf{B}$ 's randomness derived from  $\mathsf{seed}_{j,\mathsf{OT}}^B$  to derive the transcript hash  $\hat{\mathcal{H}}_j^B$ . If  $\hat{\mathcal{H}}_j^B \neq \mathcal{H}_j^B$ ,  $\mathsf{P}_\mathsf{A}$  uniformly chooses such a j and uses  $\mathsf{Blame}(\mathsf{BadOT},j)$  to generate cert.
- (c) If there are more than one commitment  $c_j = 0$  for  $j \in \mathsf{CheckSet}_A$ , uniformly choose two of them and let  $J = \{j \mid c_j = 0\}$  such that |J| = 2.  $\mathsf{P}_\mathsf{A}$  uses  $\mathsf{Blame}(\mathsf{BadNum}, J)$  to generate  $\mathsf{cert}$ .
- (d) If for all  $j \in \mathsf{CheckSet}_A$ ,  $\mathsf{c}_j$  from  $\mathsf{P}_\mathsf{B}$  is equal to  $\mathsf{P}_\mathsf{A}$ 's  $\mathsf{c}_j$ ,  $\mathsf{P}_\mathsf{A}$  aborts with output  $\bot$ .

Symmetrically,  $P_B$  follows the same procedure to check instances (and generates cert if needed).

#### Circuit Evaluation

- 10.  $P_A$  opens the committed message  $(\hat{\jmath}_A, \{\text{seed}'^B_j\}_{j\neq\hat{\jmath}_A}, \text{witness}'^B_{\hat{\jmath}_A})$  inside  $c_A$  to  $P_B$ , while  $P_B$  opens  $c_B$  to  $P_A$ . If the other party does not open the commitment or the committed message is incorrect, the party aborts with output  $\bot$ .
- or the committed message is incorrect, the party aborts with output ⊥.

  11. P<sub>A</sub> sends GC<sub>ĵ<sub>B</sub></sub>, {(h<sub>i,(0)</sub><sup>A</sup>, h<sub>i,(1)</sub><sup>A</sup>) = (h<sub>ĵ<sub>B</sub>,i,α<sub>i</sub></sub><sup>A</sup>, h<sub>ĵ<sub>B</sub>,i,ᾱ<sub>i</sub></sub><sup>A</sup>)}, {(h<sub>j,i,ᾱi</sub><sup>B</sup>, h<sub>j,i,ᾱi</sub><sup>B</sup>)} (in the same permuted order as before), and {(H(Z<sub>ĵ<sub>B</sub>,i,0</sub>), H(Z<sub>ĵ<sub>B</sub>,i,0</sub>))}, together with decom<sub>cĵ<sub>B</sub></sub> to P<sub>B</sub>. If Com(GC<sub>ĵ<sub>B</sub></sub>, {(h<sub>ĵ<sub>B</sub>,i,ᾱi</sub><sup>A</sup>, h<sub>ĵ<sub>B</sub>,i,ᾱi</sub><sup>A</sup>)}, {(h<sub>j,i,ᾱi</sub><sup>B</sup>, h<sub>j,i,ᾱi</sub><sup>B</sup>)}, {H(Z<sub>ĵ<sub>B</sub>,i,b</sub>)}; decom<sub>cĵ<sub>B</sub></sub>) ≠ c<sub>ĵ<sub>B</sub></sub> for some i, P<sub>B</sub> aborts with output ⊥. Symmetrically, P<sub>B</sub> sends the corresponding materials with respect to the ĵ<sub>A</sub>th instance to P<sub>A</sub>, and P<sub>A</sub> checks the correctness of the materials.
- 12.  $\begin{aligned} &\text{P}_{\mathsf{A}} \text{ sends } \{A_{\hat{\jmath}_B,i,x_A[i]}\}_{i \in [n_A]}, \gamma_{\hat{\jmath}_B}^A, \text{ together with decommitments decom}_{\gamma_{\hat{\jmath}_B}^A} \text{ and } \\ & \{ \deg \mathsf{com}_{\hat{\jmath}_B,i,x_A[i]}^A \}_{i \in [n_A]} \text{ to } \mathsf{P}_{\mathsf{B}}. \text{ If } \mathsf{Com}(\gamma_{\hat{\jmath}_B}^A; \deg \mathsf{com}_{\gamma_{\hat{\jmath}_B}^A}) \neq \mathsf{c}_{\gamma_{\hat{\jmath}_B}^A} \text{ or } \mathsf{Com}(A_{\hat{\jmath}_B,i,x_A[i]}; \\ & \deg \mathsf{com}_{\hat{\jmath}_B,i,x_A[i]}^A) \neq h_{i,\gamma_{\hat{\jmath}_B}^A[i]}^A \text{ for some } i, \, \mathsf{P}_{\mathsf{B}} \text{ aborts with output } \bot. \end{aligned}$ 
  - Otherwise,  $\mathsf{P}_\mathsf{B}$  evaluates  $\mathsf{GC}_{\hat{\jmath}_B}$  with input-wire labels  $\{A_{\hat{\jmath}_B,i,x_A[i]}\}_{i\in[n_A]}$  and  $\{B_{\hat{\jmath}_B,i,x_B[i]}\}_{i\in[n_B]}$  to obtain the output-wire labels  $\{Z_{\hat{\jmath}_B,i}\}_{i\in[n_O]}$ .  $\mathsf{P}_\mathsf{B}$  can derive the result  $z_{\hat{\jmath}_B}$  from  $\{Z_{\hat{\jmath}_B,i}\}_{i\in[n_O]}$  and  $\{(\mathsf{H}(Z_{\hat{\jmath}_B,i,0}),\mathsf{H}(Z_{\hat{\jmath}_B,i,1}))\}_{i\in[n_O]}$ . If any of the decoded bits is  $\bot$ ,  $\mathsf{P}_\mathsf{B}$  then lets  $z_{\hat{\jmath}_B} = \bot$ .
  - Symmetrically,  $P_B$  sends the corresponding materials with respect to the  $\hat{\jmath}_A$ th instance to  $P_A$ . Then  $P_A$  checks the correctness of the materials and evaluates the  $\hat{\jmath}_A$ th garbled circuits to derive the result  $z_{\hat{\jmath}_A}$ .
- 13. If  $z_{\hat{\jmath}_A} = \perp$ ,  $\mathsf{P}_\mathsf{A}$  lets  $\beta_A$  be a random  $\kappa$ -bit value. Otherwise,  $\mathsf{P}_\mathsf{A}$  sets  $\beta_A \leftarrow \mathsf{H}(\bigoplus_{i=1}^{n_{\mathcal{O}}}(Z_{\hat{\jmath}_A,i} \oplus Z_{\hat{\jmath}_B,i,z_{\hat{\jmath}_A}[i]}))$ . Symmetrically,  $\mathsf{P}_\mathsf{B}$  computes his  $\beta_B$ . Then  $\mathsf{P}_\mathsf{A}$

and  $P_B$  use the equality test protocol  $\Pi_{Eq}$  to check whether  $\beta_A = \beta_B$ . If it holds,  $P_A$  (resp.  $P_B$ ) outputs  $z_{\hat{j}_A}$  (resp.  $z_{\hat{j}_B}$ ). Otherwise, parties abort with output cheating.

The description of the corresponding algorithm Blame that could output a publicly verifiable certificate for cheating is given in the following.

### Algorithm Blame

The party  $P_X$  runs this algorithm to obtain a certificate cert for the malicious behavior of  $P_Y$ . We first define the following notations:

- $\ \ \mathrm{Denote} \ \mathsf{msg}_j = (id,\mathsf{trans}_j^Y,\mathsf{trans}_j^X,\mathcal{H}_j^Y,\mathsf{p}_{\mathsf{s}_j^Y},\mathsf{pc}_j,\mathsf{p}_{\mathsf{seed}_{j}^Y,\mathsf{QT}},\tau,\lambda), \ \mathrm{where} \ \mathsf{pc}_j \ \mathrm{is} \ \mathrm{the}$ ciphertext from  $P_Y$ .
- Denote the proof/opening with respect to  $\mathsf{p}_{s_i^Y}$  for  $s_j^Y$  by  $\pi_j{}^a$ .
- $\text{ Denote } \mathsf{v}_{j}^{X} = (\mathsf{seed}_{j}^{X}, \mathsf{seed'}_{j}^{X}, \mathsf{witness'}_{j}^{X}) \text{ and } \mathsf{decom}_{j}^{X} = (\mathsf{decom}_{j}^{X}, \mathsf{decom'}_{j}^{X}, \mathsf{decom'}_{$

The algorithm generates a certificate cert as follows depending on the received parameters.

- $\ (\mathsf{BadCom}, j) \colon \mathsf{Output} \ \mathsf{cert} = (\mathsf{BadCom}, j, \mathsf{msg}_j, \mathsf{v}_j^X, \mathsf{decom}_j, \sigma_j^Y, s_j^Y, \pi_j).$
- $$\begin{split} &- (\mathsf{BadOT}, j) \text{: Output cert} = (\mathsf{BadOT}, j, \mathsf{msg}_j, \mathsf{v}_j^X, \mathsf{decom}_j, \sigma_j^Y, s_j^Y, \pi_j). \\ &- (\mathsf{BadNum}, J) \text{: Output cert} = (\mathsf{BadNum}, \{j, \mathsf{msg}_j, \mathsf{v}_j^X, \mathsf{decom}_j, \sigma_j^Y, s_j^Y, \pi_j\}_{j \in J}). \end{split}$$

In the following, we present the description of the algorithm Judge. The algorithm Judge could take as input a certificate cert generated by the algorithm Blame and output whether the accused party is cheating.

## Algorithm Judge

**Inputs:** A public key  $vk_Y$ , a circuit C, and a certificate cert. Depending on the types of cheating, the algorithm verifies the certificate cert as

- BadCom: Parse the remaining part as  $(j, \mathsf{msg}_j, \mathsf{v}_j^X, \mathsf{decom}_j, \sigma_j^Y, s_j^Y, \pi_j)$ . Verify the correctness of  $(s_j^Y, \pi_j)$  and output false if  $\pi_j$  is incorrect. Derive  $c_j$ from  $p_{c_j}$ . Use  $v_j^X$  and  $decom_j$  to re-construct commitments  $c_{seed_j^X}$ ,  $c_{seed_j^X}$ , and  $c_{witness',X}$ . Check the correctness of  $\sigma_j^Y$  using  $vk_Y$ , and output false if the signature is invalid. Decrypt  $p_{c_j}$  to obtain  $c_j$ . Use  $v_j^X$  to simulate the executions of  $\Pi_{\mathsf{OT}}$  (in two directions) based on  $\mathsf{trans}_j^X$  and  $\mathsf{trans}_j^Y$  and derive  $\mathsf{seed'}_j^Y$  in Step 1a. Verify the simulation of  $\Pi_{\mathsf{OT}}$  using  $\mathsf{trans}_j^X$  and  $\mathsf{trans}_j^Y$ . If they do not match, output false. Then use  $seed'_j = seed'^X_j \oplus seed'^Y_j$  to simulate Step 4 and obtain  $\hat{c}_j$ . If  $c_j \neq \hat{c}_j$  and  $c_j \neq 0$ , output true. Otherwise, output false.
- BadOT: Parse the remaining part as  $(j, \mathsf{msg}_j, \mathsf{v}_j^X, \mathsf{decom}_j, \sigma_j^Y, s_j^Y, \pi_j)$ . Verify the correctness of  $(s_j^Y, \pi_j)$ , and output false if  $\pi_j$  is incorrect. Use  $v_j^X$  and

<sup>&</sup>lt;sup>a</sup> Note that  $\pi_i$  can be provided by  $P_Y$  for puzzle opening or generated by  $P_X$  if the puzzle is solved by  $P_X$ .

 $\mathsf{decom}_j$  to re-construct commitments  $\mathsf{c}_{\mathsf{seed}_i^X}$ ,  $\mathsf{c}_{\mathsf{seed}_i^X}$ , and  $\mathsf{c}_{\mathsf{witness}_i^X}$ . Check the correctness of  $\sigma_j^Y$  using  $vk_Y$ , and output false if the signature is invalid. Decrypt  $p_{c_j}$  and  $p_{\text{seed}_{j,\text{OT}}^Y}$  to obtain  $c_j$  and  $\text{seed}_{j,\text{OT}}^Y$ .

If  $c_j = 0$ , use  $seed_{j,OT}^Y$  and the master time-lock puzzle key  $s_j^Y$  to simulate the execution of  $\Pi_{OT}$  in Step 6, and verify whether  $P_Y$  is the first one whose message hash is different from the one in  $\mathcal{H}_{j}^{Y}$ . If yes, output true. Otherwise, output false.

If  $c_j \neq 0$ , use  $v_j^X$  to simulate the executions of  $\Pi_{OT}$  (in two directions) based on  $\mathsf{trans}_j^X$  and  $\mathsf{trans}_j^Y$  and derive  $\mathsf{seed'}_j^Y$  in Step 1a. Verify the simulation of  $\Pi_{\mathsf{OT}}$  using  $\mathsf{trans}_j^X$  and  $\mathsf{trans}_j^Y$ . If they do not match, output false. Compute  $\mathsf{seed}'_j \leftarrow \mathsf{seed}'_j^X \oplus \mathsf{seed}'_j^Y$ . Then use  $\mathsf{seed}'_j$ ,  $\mathsf{seed}'_j \oplus \mathsf{seed}'_{j,\mathsf{OT}}$ , and the master time-lock puzzle key  $s_j^Y$  to simulate the executions of  $\Pi_{\mathsf{OT}}$  in Step 6, and verify whether  $P_Y$  is the first one whose message hash is different from the one in  $\mathcal{H}_{i}^{Y}$ . If yes, output true. Otherwise, output false.

BadNum: Parse the remaining part as  $\{j, \mathsf{msg}_j, \mathsf{v}_j^X, \mathsf{decom}_j, \sigma_j^Y, s_j^Y, \pi_j\}_{j \in J}$ . Verify the correctness of  $\{(s_j^Y,\pi_j)\}$  and output false if there exists a tuple  $(s_j^Y,\pi_j)$  that is incorrect. Use  $\{\mathsf{v}_j^X\}$  and  $\{\mathsf{decom}_j\}$  to re-construct commitments  $\{c_{\text{seed}_{i}^{X}}\}$ ,  $\{c_{\text{seed}_{i}^{Y}}\}$ , and  $\{c_{\text{witness}_{i}^{Y}}\}$ . Check the correctness of  $\{\sigma_{j}^{Y}\}$  using  $vk_V$ , and output false if there exists a signature that is invalid. Decrypt  $\{p_{c_i}\}$ to obtain  $\{c_j\}$ . If  $c_j = 0$  for all  $j \in J$ , output true. Otherwise, output false.

**Theorem 1.** The protocol  $\Pi_{\mathsf{RobustPVC}}$  along with algorithms  $\mathsf{Blame}$  and  $\mathsf{Judge}$  is robust publicly verifiable covert secure with deterrence  $\epsilon = 1 - \frac{1}{\lambda - 1}$ .

*Proof.* We prove the robust PVC security of  $\Pi_{\mathsf{RobustPVC}}$  by showing its simulatability, public verifiability, and defamation freeness.

Simulatability We first prove that  $\Pi_{\mathsf{RobustPVC}}$  securely realizes  $\mathcal{F}_{\mathsf{RobustPVC}}$  with deterrence  $\epsilon = 1 - \frac{1}{\lambda - 1}$ . Without loss of generality, we assume that  $P_B$  is honest and  $P_A$  is corrupted by A. Since the roles of  $P_A$  and  $P_B$  in  $\Pi_{\mathsf{RobustPVC}}$  is symmetric, the proof for the scenario where  $\mathsf{P}_\mathsf{B}$  is corrupted is similar.

For an adversary  ${\cal A}$  corrupting  $\mathsf{P}_A$  in the real world, we construct a simulator  $\mathcal{S}$  holding  $\mathsf{vk}_A$  that runs  $\mathcal{A}$  as a sub-routine with auxiliary input z and interacts with  $\mathcal{F}_{\mathsf{RobustPVC}}$  in the ideal world. The simulation procedure is presented below.

- 0. S uses KGen to generate a pair of key  $(\mathsf{vk}_B, \mathsf{sigk}_B)$  and sends  $\mathsf{vk}_B$  to  $\mathcal{A}$ .

  1. S goes through the following steps with  $\mathcal{A}$ .

  (a) S receives  $\{\mathsf{c}_{\mathsf{seed}}^A, \mathsf{c}_{\mathsf{seed}}^A, \mathsf{c}_{\mathsf{wintess}}^A\}_{j \in [\lambda]}$  from  $\mathcal{A}$ . In the meantime, S picks uniform  $\kappa\text{-bit strings } \{\mathsf{seed}_j^B, \mathsf{seed'}_j^B, \mathsf{witness'}_j^B\}_{j \in [\lambda]}, \text{ computes } \{\mathsf{c}_{\mathsf{seed}_j^B}, \mathsf{c}_{\mathsf{seed'}_j^B}, \mathsf{c}_{\mathsf{witness'}_j^B}\}_{j \in [\lambda]},$ and sends these commitments to  ${\mathcal A}$  as in the protocol.
  - (b) For all j, S playing the role of the receiver uses  $b_j=0$  to retrieve  $\operatorname{seed'}_j^A$  in  $\Pi_{\mathsf{OT}}$ with randomness derived from  $\mathsf{seed}_j^B$ .  $\mathcal S$  also plays the role of the sender and uses  $\{(\mathsf{seed'}_j^B,\mathsf{witness'}_j^B)\}_{j\in[\lambda]} \text{ as input in } \varPi_{\mathsf{OT}} \text{ with randomness derived from } \mathsf{seed}_j^B.$
- 2.  $\mathcal{S}$  computes  $\operatorname{\mathsf{seed}}_i' = \operatorname{\mathsf{seed}}_i'^A \oplus \operatorname{\mathsf{seed}}_j'^B$  for all  $j \in [\lambda]$ . Then  $\mathcal{S}$  let  $h_B^j \leftarrow \mathsf{H}(\bigoplus_{[\lambda] \setminus j} \operatorname{\mathsf{seed}}_j')$  for all  $j \in [\lambda]$ . For the execution of  $\Pi_{\mathsf{Eq}}$ ,  $\mathcal{S}$  uses the simulator  $\mathcal{S}_{\mathsf{Eq}}$ , i.e., the corresponding simulator for the protocol  $\Pi_{Eq}$ , to obtain  $h_A$ . If there exists  $h_B^j$ , such that  $h_B^j = h_A$ , Ssets GoodEq = true and picks  $\hat{\jmath}_B \leftarrow \$[\lambda]$ . If  $h_B^{\hat{\jmath}_B} = h_A$ , S returns true for  $\Pi_{Eq}$  to A and

restarts the protocol, and otherwise returns false for  $\Pi_{Eq}$  to A. If there is no  $h_B^j$ , such that  $h_B^j = h_A$ , S sets GoodEq = false and returns false for  $\Pi_{Eq}$  to A.

- $\mathcal{S}$  computes and sends dummy commitment  $c_B$  to  $\mathcal{A}$ .  $\mathcal{S}$  also receives commitment  $c_A$  from
- 4. For all  $j \in [\lambda]$ ,  $\mathcal S$  prepares garbled circuits and input materials as in Step 4 of the protocol. 5.  $\mathcal S$  computes and sends dummy commitment  $\{\mathsf c_{\gamma_j^B}\}$  to  $\mathcal A$ .  $\mathcal S$  also receives  $\{\mathsf c_{\gamma_j^A}\}$  from  $\mathcal A$ .
- 6. S generates the puzzle  $p_{s_{i}^{B}}$  for a random chosen master puzzle key  $s_{j}^{B}$  as in the protocol for  $j \in [\lambda]$ . S also generates dummy ciphertexts for his  $p_{c_j}$  and  $p_{\text{seed}_{j,\text{OT}}^B}$  for  $j \in [\lambda]$ . Then

 $\mathcal S$  sends these puzzles to  $\mathcal A$ .  $\mathcal S$  receives puzzles  $\mathsf p_{s_j^A}$ ,  $\mathsf p_{\tilde{\mathsf e}_j}$ , and  $\mathsf p_{\mathsf{seed}_{j,\mathsf{OT}}^A}$  for  $j\in[\lambda]$  from  $\mathcal A$ . Since time-lock puzzles can  $\mathcal A$  and  $\mathcal A$ 

be solved in polynomial time, S can decrypt these puzzles and derive  $s_i^A$ ,  $\hat{c}_j$ , and seed<sub>i,OT</sub>

For  $\lambda$  executions of  $\Pi_{0\mathsf{T}}$  where  $\mathcal{S}$  plays the role of the receiver,  $\mathcal{S}$  uses as input  $0^{n_B}$  and randomness derived from  $\mathsf{seed}_j^B$  and receives  $\mathcal{A}$ 's  $\{\mathsf{p}_{B_j,i,0}\}$ . Let  $\mathcal{H}_j^A$  denote the transcript hash for the jth executions.

For  $\lambda$  executions of  $\Pi_{\mathsf{OT}}$  where  $\mathcal S$  plays the role of the sender,  $\mathcal S$  first generates dummy ciphertexts  $\{\mathsf{p}_{A_j,i,b}\}$  and random  $\kappa$ -bit string  $\mathsf{seed}_j''$  for all  $j \in [\lambda]$ . Then  $\mathcal S$  executes  $\Pi_{\mathsf{OT}}$ with  $\mathcal{A}$  using  $\{(\mathbf{p}_{A_{j,i,0}},\mathbf{p}_{A_{j,i,1}})\}_{i\in[n_A]}$  as input with randomness derived from  $\mathsf{seed}_j^{\prime\prime}$ .

- 7. S generates signatures  $\{\sigma_j^B\}$  as an honest  $P_B$  and sends them to  $\mathcal{A}$ .
  - $\mathcal S$  also receives  $\{\sigma_j^A\}$  from  $\mathcal A$ . If any of the signatures are invalid,  $\mathcal S$  executes the *finishing touches* procedure as follows and sends abort to  $\mathcal F_{\mathsf{RobustPVC}}$  to terminate the execution of
  - (a) Choose  $\hat{\jmath}_B \leftarrow \$[\lambda]$  if  $\mathsf{GoodEq} = \mathsf{false}$ , and otherwise use  $\hat{\jmath}_B$  chosen in Step 2 in this simulation.
  - (b) Program the random oracle to let the decryption of  $\mathsf{p}_{\mathsf{c}_{\hat{\jmath}_B}}$  be 0, decryption of  $\mathsf{p}_{\mathsf{c}_j}$  be  $c_j$  for  $j \in [\lambda] \setminus {\hat{j}_B}$ , and decryption of  $\{p_{A_{j,i,b}}\}$  be the correct values as those in the
  - protocol for  $j \in [\lambda] \setminus \{\hat{j}_B\}$  and  $j = \hat{j}_B$ , respectively. (c) Program the random oracle: for the  $\hat{j}_B$ th instance, let the decryption of  $\mathsf{p}_{\mathsf{seed}}^B_{\hat{j}_B,\mathsf{OT}}$  be  $\operatorname{\mathsf{seed}}_{\hat{\jmath}_B,\mathsf{OT}}^B = \operatorname{\mathsf{seed}}_{\hat{\jmath}_B}''$ . For  $j \in [\lambda] \setminus \{\hat{\jmath}_B\}$ , let the decryption of  $\mathsf{p}_{\operatorname{\mathsf{seed}}_{\hat{\jmath}_D}^B}$  be the decryption  $\text{ of } \mathsf{p}_{\mathsf{seed}_{j,\mathsf{OT}}^B} \text{ be } \mathsf{seed}_{j,\mathsf{OT}}^B = \mathsf{seed}_j^{\prime\prime} \oplus \mathsf{seed}_j^{\prime}.$

Then S simulates the computation of an honest  $P_A$  playing the role of the sender in the executions of  $\Pi_{OT}$  in Step 6 of the protocol and obtain  $\hat{\mathcal{H}}_j^A$ . If  $\hat{\mathsf{c}}_j = 0$ , the simulation is based on  $seed_{j,OT}^A$  as the  $\hat{j}_A$ th instance in the protocol. If  $\hat{c}_j = c_j$ , the simulation is based on  $\mathsf{seed}_j' \oplus \mathsf{seed}_{j,\mathsf{OT}}^A$  as other instances in the protocol. Let  $J_z$  be the set of indices that  $\hat{c}_j = 0$  and  $\hat{\mathcal{H}}_i^A$  matches the simulation of  $\Pi_{OT}$  for the  $\hat{\jmath}_A$ th instance as described in the protocol. Let  $J_s$  be the set of indices that  $\hat{c}_j = c_j$  and  $\hat{\mathcal{H}}_j^A$  matches the simulation of  $\Pi_{\mathsf{OT}}$ for the checking instances.

- Hence, there are following cases (let Stupid = false and Type = $\bot$  by default): If  $|J_s| < \lambda 2$ , S executes the *finishing touches* procedure as in Step 7a-7c of the simulation, sends (cheat, 1) to  $\mathcal{F}_{RobustPVC}$ , receives corrupted, opens the puzzle as in Step 8 of the protocol, generates the certificate cert with respect to j and the inconsistent  $\hat{c}_j$  or  $\hat{\mathcal{H}}_j^A$  as in the protocol.  $\mathcal{S}$  then sends cert to  $\mathcal{A}$  as Step 9 of the
  - protocol to complete the simulation. If  $|J_z|=\lambda-2$  and  $|J_z|=2$ ,  $\mathcal S$  sets Stupid = true and sends (stupidCheat,  $\frac{\lambda-2}{\lambda}$ ) to  $\mathcal{F}_{\mathsf{RobustPVC}}$ . If  $\mathcal{F}_{\mathsf{RobustPVC}}$  returns corrupted,  $\mathcal{S}$  sets caught  $=(\frac{\lambda-2}{\lambda},\mathsf{true})$  and Type =BadNum. If  $\mathcal{F}_{\mathsf{RobustPVC}}$  returns  $\perp$ ,  $\mathcal{S}$  sets caught =  $(\frac{\lambda-2}{\lambda}, \mathsf{false})$ . Then  $\mathcal{S}$  continues the simulation.
  - If  $|J_s| = \lambda 2$ ,  $|J_z| = 1$ , and GoodEq = true, S sends (cheat,  $\frac{\lambda 2}{\lambda 1}$ ) to  $\mathcal{F}_{\mathsf{RobustPVC}}$ . If  $\mathcal{F}_{\mathsf{RobustPVC}}$  returns corrupted,  $\mathcal{S}$  sets caught  $=(\frac{\lambda-2}{\lambda-1},\mathsf{true})$  and Type according to the possible certificate with respect to the inconsistent  $\hat{c}_j$  or  $\hat{\mathcal{H}}_j^A$ . If  $\mathcal{F}_{\mathsf{RobustPVC}}$  returns undetected,  $\mathcal{S}$  sets caught =  $(\frac{\lambda-2}{\lambda-1}, \text{false})$ . Then  $\mathcal{S}$  continues the simulation.
  - If  $|J_s| = \lambda 2$ ,  $|J_z| = 1$ , and GoodEq = false, S sends (cheat,  $\frac{\lambda 1}{\lambda}$ ) to  $\mathcal{F}_{\mathsf{RobustPVC}}$ . If  $\mathcal{F}_{\mathsf{RobustPVC}}$  returns corrupted,  $\mathcal{S}$  sets caught =  $(\frac{\lambda-1}{\lambda},\mathsf{true})$  and Type according to the possible certificate with respect to the inconsistent  $\hat{c}_j$  or  $\hat{\mathcal{H}}_j^A$ . If  $\mathcal{F}_{\mathsf{RobustPVC}}$  returns undetected,  $\mathcal{S}$  sets caught =  $(\frac{\lambda-1}{\lambda}, \mathsf{false})$ . Then  $\mathcal{S}$  continues the simulation.

- If  $|J_s|=\lambda-2$  and  $|J_z|=0$ ,  $\mathcal S$  executes the finishing touches procedure as in Step 7a-7c, sends (cheat, 1) to  $\mathcal{F}_{\text{RobustPVC}}$ , receives corrupted, opens the puzzle as in Step 8 of the protocol, generates the certificate cert with respect to j and the inconsistent  $\hat{c}_j$ or  $\hat{\mathcal{H}}_i^A$  as in the protocol, and sends  $\mathsf{cert}$  to  $\mathcal{A}$  as in Step 9 of the protocol to complete the simulation.
- If  $|J_s| = \lambda 1$ ,  $|J_z| = 1$ , and GoodEq = true, S sets caught =  $\perp$ . Then S continues the simulation.
- If  $|J_s| = \lambda 1$ ,  $|J_z| = 1$ , and GoodEq = false, then S tosses a coin, which with probability  $\frac{1}{\lambda}$  outputs false and  $\frac{\lambda-1}{\lambda}$  outputs true. If the output is false, then S executes the *finishing touches* procedure as follows, opens his puzzle, and sends abort to  $\mathcal{F}_{\mathsf{RobustPVC}}$  to terminate the execution of the protocol.
  - (a) Let  $\hat{\jmath}_B$  be the element in  $J_z$ .
  - (b) Program the random oracle to let the decryption of  $\mathsf{p}_{\mathsf{c}_{\hat{\jmath}_B}}$  be 0, decryption of  $p_{c_j}$  be  $c_j$  for  $j \in [\lambda] \setminus \{\hat{j}_B\}$ , and decryption of  $\{p_{A_{j,i,b}}\}$  be the correct values as
  - those in the protocol for  $j \in [\lambda] \setminus \{\hat{\jmath}_B\}$  and  $j = \hat{\jmath}_B$ , respectively. (c) Program the random oracle: Let the decryption of  $\mathsf{p}_{\mathsf{seed}_{\hat{\jmath}_B}^B,\mathsf{OT}}$  be  $\mathsf{seed}_{\hat{\jmath}_B,\mathsf{OT}}^B$  be  $\mathsf{seed}_{\hat{\jmath}_B,\mathsf{OT}}^B = \mathsf{seed}_{\hat{\jmath}_B,\mathsf{OT}}^B$ . For  $j \in [\lambda] \setminus \{\hat{\jmath}_B\}$ , let the decryption of  $\mathsf{p}_{\mathsf{seed}_{\hat{\jmath}_b,\mathsf{OT}}^B}$  be  $\mathsf{seed}_{j,\mathsf{OT}}^B = \mathsf{seed}_{j}^{B} \in \mathsf{Seed}_{j,\mathsf{OT}}^B = \mathsf{seed}_{j,\mathsf{OT}}^{B} = \mathsf{seed}_{j$
  - If the output is true, then S sets caught  $=\perp$  and continues the simulation.
- If  $|J_s|=\lambda-1$  and  $|J_z|=0$ ,  $\mathcal S$  sets Stupid = true and then sends the message (stupidCheat,  $\frac{\lambda-1}{\lambda}$ ) to  $\mathcal F_{\mathsf{RobustPVC}}$ . If  $\mathcal F_{\mathsf{RobustPVC}}$  returns corrupted,  $\mathcal S$  executes the finishing touches by picking  $\hat \jmath_B \leftarrow \mathbb s J_s$ ,

programming the random oracle to let the decryption of  $\mathsf{p}_{\mathsf{c}_{\hat{j}_B}}$  be 0, decryption of  $\mathsf{p}_{\mathsf{c}_j}$ be  $c_j$  for  $j \in [\lambda] \setminus {\hat{j}_B}$ , and decryption of  $\{p_{A_{j,i,b}}\}$  be the correct values as those in the protocol for  $j \in [\lambda] \setminus \{\hat{j}_B\}$  and  $j = \hat{j}_B$ , respectively. S also programs the random

oracle: for the  $\hat{j}_B$ th instance, let the decryption of  $\mathsf{p}_{\mathsf{seed}_{j,0}^B,\mathsf{OT}}$  be  $\mathsf{seed}_{jB}^B,\mathsf{OT} = \mathsf{seed}_{jB}^{\prime\prime}$ . For  $j \in [\lambda] \setminus \{\hat{j}_B\}$ , let the decryption of  $\mathsf{p}_{\mathsf{seed}_{j,0}^B,\mathsf{OT}} = \mathsf{seed}_{j,0}^{\prime\prime} = \mathsf$ Step 9 of the protocol to complete the simulation.

If  $\mathcal{F}_{\mathsf{RobustPVC}}$  returns  $\perp$ ,  $\mathcal{S}$  executes the finishing touches by picking  $\hat{\jmath}_B \leftarrow \$[\lambda] \setminus J_s$  and programming the random oracle following the same procedure as  $\mathcal{F}_{\mathsf{RobustPVC}}$  returns corrupted. Then S opens his puzzle as in Step 8 of the protocol, and simulates the abortion of the honest  $P_B$  to terminate the simulation.

If  $|J_s|=\lambda$ , S executes the finishing touches procedure as in Step 7a-7c in this simulation, opens his puzzle, and sends abort to  $\mathcal{F}_{\mathsf{RobustPVC}}$  to terminate the execution of the protocol.

Rewind A and run steps 1'-7' below until<sup>a</sup>  $|J_s'|=|J_s|,\ |J_z'|=|J_z|,\ \mathsf{caught}'=\mathsf{caught},\ \mathsf{GoodEq}'=\mathsf{GoodEq},\ \mathsf{Stupid}'=\mathsf{Stupid},\ \mathsf{and}\ \mathsf{Type}'=\mathsf{Type}.$ 

- 1'. S goes through the following steps with A.
  - S goes through the following steps with A.
    (a) S receives the commitments {c<sub>seed</sub><sub>j</sub> A, c<sub>seed'</sub><sub>j</sub> A, c<sub>witness'</sub><sub>j</sub> A}<sub>j∈[λ]</sub> from A. In the meantime, S playing the role of P<sub>B</sub> randomly chooses ĵ<sub>B</sub> ← s[λ] and then picks uniform κ-bit strings {seed<sup>B</sup><sub>j</sub>, seed'<sup>B</sup><sub>j</sub>, witness'<sup>B</sup><sub>j</sub>}<sub>j∈[λ]</sub>. S then computes c<sub>seed</sub><sub>j</sub> B, c<sub>seed'</sub><sub>j</sub> B, and c<sub>witness'</sub> B<sub>j</sub> for j ∈ [λ]\{ĵ<sub>B</sub>} as in the protocol and let c<sub>seed</sub><sub>j</sub> C, c<sub>seed'</sub> B, and c<sub>witness'</sub> B be dummy commitments. Finally, S sends these commitments to A as in the protocol.
    (b) For all j ∈ [λ]\{ĵ<sub>B</sub>}, S playing the role of the receiver uses b<sub>j</sub> = 0 to retrieve {seed'<sub>j</sub> A}<sub>j∈[λ]\{ĵ<sub>B</sub>}</sub> with randomness derived from {seed<sup>B</sup><sub>j</sub>}. For the ĵ<sub>B</sub>th instance, S rups the simulator Sor for the protocol Hor, and extracts (seed'<sup>A</sup><sub>j</sub> witness'<sup>A</sup><sub>j</sub>).
  - S runs the simulator  $S_{\mathsf{OT}}$  for the protocol  $\Pi_{\mathsf{OT}}$ , and extracts  $(\mathsf{seed'}_{\hat{\jmath}_B}^A, \mathsf{witness'}_{\hat{\jmath}_B}^A)$ . S also plays the role of the sender and uses  $\{(seed_j^B, witness_j^B)\}_{j \in [\lambda]}$  as input with randomness derived from  $\mathsf{seed}_{\,i}^B$
- 2'. S computes  $\operatorname{seed}_j' = \operatorname{seed}_j'^A \oplus \operatorname{seed}_j'^B$  for all  $j \in [\lambda]$ . Then S let  $h_B^j \leftarrow \operatorname{H}(\bigoplus_{[\lambda] \setminus j} \operatorname{seed}_j')$  for all  $j \in [\lambda]$ . S uses the simulator  $\mathcal{S}_{\mathsf{Eq}}$  for  $\Pi_{\mathsf{Eq}}$  to obtain  $h_A$ . If there exists  $h_B^j$ , such that  $h_B^j = h_A$ , S sets GoodEq' = true. Then if  $h_B^{\hat{\jmath}B} = h_A$ , S returns true for  $\Pi_{Eq}$  to A and restart the protocol, and otherwise returns false for  $\Pi_{Eq}$  to  $\mathcal{A}$ . If there is no  $h_B^j = h_A$ ,  $\mathcal{S}$ sets  $\mathsf{GoodEq}' = \mathsf{false}$  and returns  $\mathsf{false}$  for  $\Pi_{\mathsf{Eq}}$  to  $\mathcal{A}.$

- 3'. S computes and sends commitment  $c_B$  to A. S also receives commitment  $c_A$  from A. S extracts  $(\hat{\jmath}_A, \{\mathsf{seed'}_j^B\}_{j \neq \hat{\jmath}_A}, \mathsf{witness'}_{\hat{\jmath}_A}^B)$  from  $c_A$ . If this extracted message is correct, store  $\hat{\jmath}_A$ . Otherwise, let  $\hat{\jmath}_A = \bot$ .

  4'. For all  $j \in [\lambda]$ , S prepares garbled circuits and input materials as in Step 4 of the protocol.

  5'. S computes and sends dummy  $\{c_{\gamma_j^B}\}$  to A. S also receives  $\{c_{\gamma_j^A}\}$  from A.

- 6'.  $\mathcal{S}$  generates puzzles  $\mathbf{p}_{s_i^B}$  for a random chosen master puzzle key  $s_j^B$  and ciphertexts  $\mathsf{p}_{\mathsf{seed}}^B_{j,\mathsf{OT}}$  for  $j \in [\lambda]$  as in the protocol.  $\mathcal S$  generates ciphertexts  $\mathsf{p}_{\mathsf{c}_j}$  for computed  $\mathsf{c}_j$  for  $j \in [\lambda] \setminus \{\hat{\jmath}_B\}$  and let the ciphertext  $\mathsf{p}_{\mathsf{c}_{\hat{\jmath}_B}}$  encrypt 0. Then  $\mathcal S$  sends these puzzles to  $\mathcal A$ .  $\mathcal S$  receives puzzles  $\mathsf{p}_{s_j^A}$ ,  $\mathsf{p}_{\hat{\mathsf{c}}_j}$ , and  $\mathsf{p}_{\mathsf{seed}_{j,\mathsf{OT}}^A}$  for  $j \in [\lambda]$  from  $\mathcal A$ . Since time-lock puzzles can be solved in polynomial time, S can decrypt these puzzles and derive  $s_j^A$ ,  $\hat{c}_j$ , and  $seed_{j,OT}^A$

for  $j \in [\lambda]$ . For all  $j \neq \hat{\jmath}_B$ ,  $\mathcal{S}$  playing the role of the receiver runs  $\Pi_{\mathsf{OT}}$  with  $\mathcal{A}$ , using input  $0^{n_B}$  and randomness derived from  $\mathsf{seed}_j^B$ . In this way,  $\mathcal{S}$  receives  $\mathcal{A}$ 's  $\{\mathsf{p}_{B_{j,i},0}\}$ . In the  $\hat{\jmath}_B$ th execution of  $\Pi_{\mathsf{OT}}$ ,  $\mathcal S$  playing the role of the receiver uses the simulator  $\mathcal S_{\mathsf{OT}}$  for  $\Pi_{\mathsf{OT}}$  to extract  $\{\mathsf p_{B_{\hat{J}_B,i,b}}\}_{i\in[n_B],b\in\{0,1\}}$ .  $\mathcal S$  can decrypt  $\{\mathsf p_{B_{\hat{J}_B,i,b}}\}_{i\in[n_B],b\in\{0,1\}}$  and obtain  $\{B_{\hat{\jmath}_B,i,b}\}_{i\in[n_B],b\in\{0,1\}}$ 

If  $\hat{\jmath}_A = \bot$ ,  $\mathcal{S}$  first generates ciphertexts for  $\{\mathsf{p}_{A_j,i,b}\}$  for  $j \in [\lambda]$  as in the protocol. Then,  $\mathcal{S}$  playing the role of the sender executes  $\Pi_{\mathsf{OT}}$  with  $\mathcal{A}$  using  $\{(\mathsf{p}_{A_j,i,0},\mathsf{p}_{A_j,i,1})\}_{i\in[n_A]}$  as input with randomness derived from  $\mathsf{seed}_j' \oplus \mathsf{seed}_{j,\mathsf{OT}}^B$  or  $\mathsf{seed}_{j,\mathsf{OT}}^B$  as in the protocol. If  $\hat{\jmath}_A \neq \bot$ ,  $\mathcal{S}$  generates ciphertexts for  $\{\mathsf{p}_{A_j,i,b}\}$  for  $j \in [\lambda] \setminus \{\hat{\jmath}_A\}$  as in the protocol. For  $[\lambda] \setminus \{\hat{\jmath}_A\}$ ,  $\mathcal{S} \text{ playing the role of the sender executes } \varPi_{\mathsf{OT}} \text{ with } \mathcal{A} \text{ using } \{(\mathsf{p}_{A_j,i,0},\mathsf{p}_{A_j,i,1})\}_{i \in [n_A]} \text{ as } (\mathsf{p}_{A_j,i,0},\mathsf{p}_{A_j,i,1})\}_{i \in [n_A]} \text{ as } (\mathsf{p}_{A_j,i,0},\mathsf{p}_{A_j,i,1})\}_{i \in [n_A]} \text{ as } (\mathsf{p}_{A_j,i,0},\mathsf{p}_{A_j,i,1})\}_{i \in [n_A]} \text{ as } (\mathsf{p}_{A_j,i,0},\mathsf{p}_{A_j,i,1})$ input with randomness derived from  $\operatorname{seed}'_j \oplus \operatorname{seed}^B_{j,\mathsf{OT}}$  or  $\operatorname{seed}^B_{j,\mathsf{OT}}$  as in the protocol. For  $j = \hat{j}_A$ ,  $\mathcal{S}$  runs the simulator  $\mathcal{S}_{\mathsf{OT}}$  for  $\mathcal{H}_{\mathsf{OT}}$  to extract the input  $x_A$  and returns dummy eighborhoots  $(x_A, y_A)$  and  $(x_A, y_A)$  are  $(x_A, y_A)$ .

ciphertexts  $\{p_{A_{\hat{j}_A,i}}\}$  to  $\mathcal{A}$ . 7'.  $\mathcal{S}$  generates  $\{\sigma_j^B\}$  as an honest  $\mathsf{P}_\mathsf{B}$  in the protocol and sends them to  $\mathcal{A}$ .  $\mathcal{S}$  also receives  $\{\sigma_j^A\}$  from  $\mathcal{A}$ . If any of the signatures are invalid, then return to Step 1'. Then  $\mathcal{S}$  simulates the computation of an honest  $\mathsf{P}_\mathsf{A}$  playing the role of the sender in the executions of  $\Pi_\mathsf{OT}$  in Step 6 of the protocol and obtain  $\hat{\mathcal{H}}_j^A$ . If  $\hat{\mathsf{c}}_j = 0$ , the simulation is based on seed<sub>j,OT</sub> as the  $\hat{j}_A$ th instance in the protocol. If  $\hat{c}_j = c_j$ , the simulation is based on  $\mathsf{seed}_j' \oplus \mathsf{seed}_{j,\mathsf{OT}}^A$  as other instances in the protocol. Let  $J_z'$  be the set of indices that  $\hat{c}_j = 0$  and  $\hat{\mathcal{H}}_j^A$  matches the simulation of  $\Pi_{\mathsf{OT}}$  for the  $\hat{\jmath}_A$ th instance as described in the protocol. Let  $J'_s$  be the set of indices that  $\hat{\mathsf{c}}_j = \mathsf{c}_j$  and  $\hat{\mathcal{H}}^A_j$  matches the simulation of  $\Pi_{\mathsf{OT}}$ for the checking instances.

- for the checking instances. Hence, there are following cases (let Stupid' = false and Type' =  $\bot$  by default): If  $|J_s'| < \lambda 2$ , then return to Step 1'.

   If  $|J_s'| = \lambda 2$  and  $|J_z'| = 2$ , S sets Stupid' = true. If  $\hat{\jmath}_B \in J_s'$ , S sets caught' =  $(\frac{\lambda 2}{\lambda}, \text{true})$  and Type' = BadNum. Otherwise, S sets caught' =  $(\frac{\lambda 2}{\lambda}, \text{false})$ .

   When  $|J_s'| = \lambda 2$ ,  $|J_z'| = 1$ , and GoodEq' = true, if  $\hat{\jmath}_B \in J_s'$ , S sets caught' =  $(\frac{\lambda 2}{\lambda 1}, \text{true})$  and Type' according to the possible certificate with respect to the inconsistent  $\hat{c}_j$  or  $\hat{\mathcal{H}}_j^A$ . Otherwise,  $\mathcal{S}$  sets caught' =  $(\frac{\lambda-2}{\lambda-1}, \text{false})$ .
  - When  $|J'_s| = \lambda 2$ ,  $|J'_z| = 1$ , and GoodEq' = false, if  $\hat{\jmath}_B \in J'_s$  or  $\hat{\jmath}_B \in J'_z$ ,  $\mathcal{S}$  sets  $\mathsf{caught}' = (\frac{\lambda - 1}{\lambda}, \mathsf{true})$  and  $\mathsf{Type}'$  according to the possible certificate with respect to the inconsistent  $\hat{c}_j$  or  $\hat{\mathcal{H}}_j^A$ . Otherwise,  $\mathcal{S}$  sets caught' =  $(\frac{\lambda-1}{\lambda}, \mathsf{false})$ .

  - The intensistent  $C_j$  of  $H_j$ . Otherwise, S sets Caught' =  $(\frac{1}{\lambda}, \text{false})$ .

    If  $|J_s'| = \lambda 2$  and  $|J_z'| = 0$ , then return to Step 1'.

    If  $|J_s'| = \lambda 1$ ,  $|J_z'| = 1$ , and  $\mathsf{GoodEq'} = \mathsf{false}$ , if  $\hat{\jmath} \in J_s$ , then S sets caught' =  $\bot$ .

    Otherwise, return to Step 1'.

    If  $|J_s'| = \lambda 1$  and  $|J_z'| = 0$ , then return to Step 1'.

    If  $|J_s'| = \lambda$ , then return to Step 1'.
- 8. If  $\hat{\jmath}_A \neq \perp$ , S sends  $x_A$  to  $\mathcal{F}_{\mathsf{RobustPVC}}$  and receives the output z. Then S regenerates the garbled circuit via

$$(\{A_{\hat{j}_A,i}\}, \{B_{\hat{j}_A,i}\}, \mathsf{GC}_{\hat{j}_A}, \{Z_{\hat{j}_A,i,b}\}) \leftarrow \mathcal{S}_{\mathsf{Gb}}(1^{\kappa}, \mathcal{C}, z)$$

and recomputes the materials of the  $\hat{\jmath}_A$ th instance in Step 4b and 4c of the protocol. Since this garbled circuit is simulated,  $\mathcal{S}$  uses/programs dummy commitments/values in case of need, e.g., for  $\gamma_{j_A}^B$ . S also uses the random oracle to program the opening of  $c_{j_A}$  and  $\{p_{A_{j_A,i}}\}$  with respect to the simulated garbled circuit. Then S opens his puzzle to  $\mathcal{A}$  as in the protocol.  $\mathcal{A}$  may also open her puzzle.

- 9. If  $\mathsf{caught}' = (\cdot, \mathsf{true})$ ,  $\mathcal S$  generates the corresponding  $\mathsf{cert}$  and sends it to  $\mathcal A$  to complete the simulation.
- $\mathcal S$  sends the opening for  $c_B$  to  $\mathcal A$  as in the protocol.  $\mathcal S$  also receives the opening for  $c_A$  from  $\mathcal A$ . If  $\mathsf{Stupid}' = \mathsf{true}$ ,  $\mathcal S$  simulates the abortion of the honest party to complete the simulation. If the opening  $(\hat j_A, \{\mathsf{seed}'^B_j\}_{j\neq\hat j_A}, \mathsf{witness}'^B_{\hat j_A})$  is not correct,  $\mathcal S$  sends abort to  $\mathcal{F}_{\mathsf{RobustPVC}}$  and simulates the abortion of the honest party to complete the simulation.
- 11.  $\mathcal{S}$  sends the simulated garbled circuit  $\mathsf{GC}_{\hat{\jmath}_A}$ , together with corresponding label hash values, to  $\mathcal{A}$ .  $\mathcal{S}$  also receives the garbled circuit  $\mathsf{GC}_{\hat{\jmath}_B}$  and related materials from  $\mathcal{A}$ . If they are invalid,  $\mathcal{S}$  sends abort to  $\mathcal{F}_{\mathsf{RobustPVC}}$  and simulates the abortion of the honest party to complete the simulation.
- 12. S sends the simulated labels,  $\gamma_{\hat{j}_A}^B$ , and corresponding decommitments to A. S also receives the labels,  $\gamma_{\hat{\jmath}_B}^A$ , and corresponding decommitments. If the received materials are invalid,  $\mathcal{S}$  sends abort to  $\mathcal{F}_{\mathsf{RobustPVC}}$  and simulates the abortion of the honest party to complete the
- 13. S uses the simulator  $S_{\mathsf{Eq}}$  for  $\Pi_{\mathsf{Eq}}$  to obtain  $\beta_A$  from A. Then S defines the boolean function g as follows
  - (a) On input  $x_B \in \{0,1\}^{n_B}$ , select the corresponding input labels for  $x_B$  in the label tuples  $\{(B_{\hat{j}_B,i,0},B_{\hat{j}_B,i,1})\}_{i\in[n_B]}$ .
  - (b) Evaluate the garbled circuit  $GC_{j_B}$  with the input-wire labels  $\{A_{j_B,i,x_A[i]}\}_{i\in[n_A]}$  and  $\{B_{j_B,i,x_B[i]}\}_{i\in[n_B]}$  as in the protocol to obtain  $\{Z_{j_B,i}\}_{i\in[n_O]}$  and  $z_{j_B}$ . In particular, if some error occurs in the evaluation of garbled circuit, some hard-coded random values provided by S are used for  $\{Z_{\hat{j}_B,i}\}_{i\in[n_O]}$  and  $z_{\hat{j}_B}$ .
  - (c) Compute  $\beta_B \leftarrow \mathsf{H}(\bigoplus_{i=1}^{n_O}(Z_{\hat{\jmath}_A,i,z_{\hat{\jmath}_B}[i]} \oplus Z_{\hat{\jmath}_B,i,z_{\hat{\jmath}_B}[i]}))$ . (d) If  $\beta_A = \beta_B$ , return true. Otherwise, return false.

The probability of the state o

Now it remains to show that the joint distribution of the view of A simulated by  ${\mathcal S}$  and the output of  ${\mathsf P}_{\mathsf B}$  in the ideal world is computationally indistinguishable from the joint distribution of the view of A and the output of  $P_B$  in the real world. We provide the detailed proof in the full version of this paper.

Public Verifiability We argue that whenever an honest party  $P_X$  outputs the message corrupted, this party should also be capable of producing a valid certificate for the malicious party  $P_Y$  corrupted by the adversary. This implies that once the honest party detects the adversary's cheating behavior, the adversary cannot prevent the honest party from generating the certificate.

Note that in Step 7, without receiving a valid signature, the honest party will not continue the execution of the protocol. Alternatively, if the honest party does receive valid signatures, though this party still cannot obtain the solutions for the time-lock puzzles/ciphertexts at this time, it is guaranteed that the adversary has signed the time-lock puzzles/ciphertexts. Meanwhile, the adversary still cannot access the solution for the time-lock puzzles and remains unaware of the indices of the instances chosen by  $P_X$ . Therefore, the adversary cannot base her decision to continue or abort on these indices.

When the adversary gains knowledge of the indices of instances chosen by  $P_X$ to verify, the honest party has already gathered sufficient evidence to attribute

<sup>&</sup>lt;sup>a</sup> We could use standard techniques [13,15] to ensure that  $\mathcal{S}$  runs in expected polynomial time.

blame to the adversary. The honest party can locally solve the adversary's puzzles to obtain  $s_j^Y$ ,  $\mathbf{c}_j$ , and  $\mathsf{seed}_{j,\mathsf{OT}}^Y$  sent by the adversary. These messages, combined with the committed seeds and witness, as well as  $\mathsf{trans}_j^X$  and  $\mathsf{trans}_j^Y$ , provide enough information for anyone to simulate the execution of the checked instance and obtain  $\hat{\mathbf{c}}_j$  and  $\hat{\mathcal{H}}_j^Y$ . Anyone can conduct the same verification on  $\hat{\mathbf{c}}_j$  and  $\hat{\mathcal{H}}_j^Y$  as  $\mathsf{P}_X$  to determine if malicious  $\mathsf{P}_Y$  deviated from the protocol execution. Since  $\mathsf{P}_X$ 's signature is provided, the non-repudiation property is ensured.

Defamation Freeness Assuming an honest party  $P_X$  is accused by the adversary corrupting  $P_Y$  with a valid certificate, it implies that the adversary will provide valid signature(s) of  $P_X$  for the message(s)

$$(\mathcal{C}, j, \mathsf{c}_{\mathsf{seed}_j^Y}, \mathsf{c}_{\mathsf{seed}_j^{'Y}}, \mathsf{c}_{\mathsf{witness}_j^{'Y}}, \mathsf{trans}_j^X, \mathsf{trans}_j^Y, \mathcal{H}_j^X, \mathsf{p}_{s_j^X}, \mathsf{pc}_j, \mathsf{p}_{\mathsf{seed}_{j,\mathsf{OT}}^X}, \tau, \lambda) \,.$$

Since  $\mathsf{P}_X$  is honest, she only signs the puzzles  $\mathsf{p}_{s_j^X}$ ,  $\mathsf{p}_{\mathsf{c}_j}$ , and  $\mathsf{p}_{\mathsf{seed}_{j,\mathsf{OT}}^X}$  she has generated. These puzzles can be decrypted to derive  $s_j^X$ ,  $\mathsf{c}_j$ , and  $\mathsf{seed}_{j,\mathsf{OT}}^X$ . According to the soundness of the verifiable time-lock puzzle scheme, the adversary cannot provide openings/proofs for solutions different from  $s_j^X$ ,  $\mathsf{c}_j$ , and  $\mathsf{seed}_{j,\mathsf{OT}}^X$ .

First, we consider the certificate with type BadCom. In this setting, the adversary aims to demonstrate that  $c_j$  does not match the commitment generated from the  $\operatorname{seed}_j'$  (and  $c_j \neq 0$ , which is obvious). Due to the binding property, the adversary can only provide the valid committed values  $\operatorname{seed}_j^Y$ ,  $\operatorname{seed}_j'^Y$ , and witness' $_j^Y$  inside  $\mathsf{c}_{\operatorname{seed}_j^Y}$ ,  $\mathsf{c}_{\operatorname{seed}_j'^Y}$ , and  $\mathsf{c}_{\operatorname{witness}_j'^Y}$ . A certificate verifier will recompute  $\operatorname{seed}_j'^X$  from  $\operatorname{trans}_j^X$  with randomness derived from  $\operatorname{seed}_j'^X$ . On the one hand, since  $\operatorname{seed}_j'^X$  is the output of a perfectly correct OT protocol, given the signed transcript of  $\Pi_{\mathrm{OT}}$ , there is exactly one valid output for  $\mathsf{P}_Y$  that is consistent with  $\operatorname{trans}_j^X$ , regardless of  $\mathsf{P}_Y$ 's randomness and inputs. On the other hand, if the committed values  $\operatorname{seed}_j'^Y$  and witness' $_j^Y$  are not the inputs of  $\mathsf{P}_Y$  playing the role of the sender in the perfectly correct protocol  $\Pi_{\mathrm{OT}}$ , these committed values do not match the signed transcript of  $\Pi_{\mathrm{OT}}$ . Therefore,  $\operatorname{seed}_j' = \operatorname{seed}_j'^A \oplus \operatorname{seed}_j'^B$  should be the same as the one derived by the honest  $\mathsf{P}_X$ . Consequently, simulation for the computation conducted by  $\mathsf{P}_X$  always leads to the same  $c_j$ , and the algorithm Judge will not output true (except for a negligible probability).

Then we consider the certificate with type BadOT. Similarly, we know that the adversary cannot forge  $\operatorname{seed}_j' = \operatorname{seed'}_j^A \oplus \operatorname{seed'}_j^B$ ,  $\operatorname{seed}_{j,\mathsf{OT}}^X$ , and  $s_j^X$ , and a certificate verifier should derive the same  $\{(\mathsf{p}_{Y_{j,i,0}},\mathsf{p}_{Y_{j,i,1}})\}$  and  $\operatorname{seed'}_j \oplus \operatorname{seed}_{j,\mathsf{OT}}^X$ . Hence, given the signed  $\mathcal{H}_j^X$ , the algorithm Judge will not output true except for a negligible probability (when a collision of the hash function is found).

Finally, for the certificate with type BadNum, we know that the adversary cannot forge  $c_j$ . Hence, the honest  $P_X$  should always have exactly one  $c_j = 0$ . Therefore, the algorithm Judge will not output true (except for a negligible probability).

Therefore, the protocol  $\Pi_{\mathsf{RobustPVC}}$  along with algorithms Blame and Judge is robust publicly verifiable secure with deterrence  $\epsilon = 1 - \frac{1}{\lambda - 1}$ .

## 5 Discussion

In this section, we discuss the performance and possible enhancement of our protocol  $\Pi_{\mathsf{RobustPVC}}$ .

## 5.1 Comparison

The protocol  $\Pi_{\mathsf{RobustPVC}}$  is building upon the state-of-the-art secure two-party computation protocol with PVC security [17]. As discussed in Section 1.2, our protocol incurs low additional overhead. We can easily observe that, compared to the protocol in [17], our protocol only requires an additional garbled circuit generation and an additional garbled circuit evaluation (see Table 1). Interestingly, as the deterrence factor increases, the additional overhead for garbled circuit generation/evaluation in our protocol compared to the protocol in [17] decreases. As emphasized in [17], the cost of generating garbled circuits (unless the circuit is very small) is the efficiency bottleneck of their protocol, making the number of garbled circuit generations in our protocol highly desirable.

**Table 1.** Number of garbled circuit generation and evaluation needed to achieve different deterrence factor  $\epsilon$ , along with the additional overhead of our  $\Pi_{\mathsf{RobustPVC}}$  compared to the protocol in [17]. Since evaluations should be faster than generations, the additional cost is actually overestimated.

$\epsilon$	PVC-secure protocol [17]			Our protocol $\Pi_{RobustPVC}$			Additional
	PA	P <sub>B</sub>	Total	PA	P <sub>B</sub>	Total	overhead
80%	5 + 0 = 5			5 + 1 = 6	5 + 1 = 6	12	20%
87.5%	8 + 0 = 8	7 + 1 = 8	16	8 + 1 = 9	8 + 1 = 9	18	12.5%
90%	10 + 0 = 10	9 + 1 = 10	20	10 + 1 = 11	10 + 1 = 11	22	10%
95%	20 + 0 = 20	19 + 1 = 20	40	20 + 1 = 21	20 + 1 = 21	42	5%

In the following, we argue that each phase of our protocol incurs low additional overhead compared to the protocol in [17].

Seed Preparation It is easy to verify that the expected number of executions for this phase is  $2 - \epsilon$ , where  $\epsilon$  is the deterrence factor. For  $\epsilon = 90\%$ , the expected number of executions is only 1.1. For  $\epsilon = 95\%$ , the expected number is reduced to only 1.05. Additionally, the secure equality test can be completed very quickly [18,7]. Therefore, the overhead of this phase is low.

Circuit and Input Preparation In our protocol, two parties can perform garbled circuit generation in parallel during this phase. For the same deterrence factor, the number of garbled circuits generated in [17] is the same as in  $\Pi_{\mathsf{RobustPVC}}$  (for each party). Therefore, the running time for garbled circuit generation is approximately the same as that of the protocol in [17]. We also note that time-lock puzzle generation is efficient. Indeed, for *all* instances, a single master puzzle key (inside a *real* time-lock puzzle) is sufficient. Hence, the overhead of this phase is low.

Publicly Verifiable Evidence Creation This phase is almost identical to the protocol in [17].

Check of Instances If both parties are honest and the master time-lock puzzle is correctly opened, the computation performed by both parties (in parallel) mainly involves the simulation of  $\Pi_{\text{OT}}$ , which incurs a similar running time as the protocol in [17]. Moreover, compared to the protocol in [17], no simulation of garbled circuit generation is needed. Therefore, our protocol may outperform the protocol in [17] in this phase.

Circuit Evaluation In this phase, both parties can evaluate the garbled circuit in parallel. Hence, the running time required for garbled circuit evaluation is almost the same as that of the protocol in [17]. Additionally, secure equality tests can be completed quickly. Therefore, the overhead of this phase is low.

The communication cost primarily encompasses the execution of OT protocols and the transmission of garbled circuits (including input-wire labels) for evaluation. Consequently, the one-way communication is nearly identical to that in [17], and the two-way communication is twice of that in [17]. Therefore, there is no additional communication overhead in duplex networks compared to [17].

Based on the implementation presented in [17], as an example, when  $\epsilon = 87.5\%$ , *i.e.*, the number of garbled circuit is 8, the execution time of their PVC-secure protocol for an SHA-256 circuit is 71.31 ms in LAN and 2436 ms in WAN. In comparison, the corresponding semi-honest protocol takes 38.04 ms in LAN and 1080ms in WAN, while the maliciously secure protocol takes 611.7 ms in LAN and 17300 ms in WAN. Given that the performance of our protocol is similar to that of the protocol in [17], it is evident that our  $\Pi_{\mathsf{RobustPVC}}$  achieves comparable performance to the semi-honest protocol while significantly outperforming the maliciously secure protocol.

## 5.2 Size of Certificate

In  $\Pi_{\mathsf{RobustPVC}}$ , we have chosen not to include the circuit description  $\mathcal C$  in the certificate. Instead, we make the assumption that the circuit description is commonly known. This practice aligns with the convention followed in PVC-secure protocols [17,9,10,30,3]. Alternatively, one could opt to include the circuit description  $\mathcal C$  in the certificate. It is worth noting that the description of  $\mathcal C$  can be significantly shorter than the full circuit, such as representing it in high-level code or utilizing an ID number from a widely used "reference circuits" database.

Due to the exclusion of the circuit description in the certificate, the size of publicly verifiable certificates generated in the  $\Pi_{\mathsf{RobustPVC}}$  protocol remains constant.

## 5.3 Potential Enhancements

In our protocol  $\Pi_{\mathsf{RobustPVC}}$ , we do not aim to prevent an attacker from learning the evaluation result  $\mathcal{C}(x_A, x_B)$  even when the honest party outputs cheating at the end of the protocol. This occurs when the attacker generates a malicious

garbled circuit but not being caught (with probability  $1-\epsilon$ ) or when the attacker causes an abortion in the final equality test protocol.

We note this issue is not the focus of our protocol. In fact, it is well known that two-party computation cannot guarantee fairness in general [6]. But there are still some countermeasures that can be readily incorporated into our protocols.

For instance, one approach is to introduce an additional circuit that processes the output-wire labels before they are used in the equality test, effectively concealing the semantic values associated with the garbled circuit's output. Another technique, known as *progressive revelation*, allows for a gradual release of the evaluation result bit-by-bit, preventing the attacker from obtaining the complete input while leaving the honest party with nothing. For more detailed information on these countermeasures, we refer interested readers to the work [18].

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